

# Package: zmctp (via r-universe)

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**Type** Package

**Title** Zero-Modified Complex 'Tri-Parametric' Pearson Distribution for Overdispersed Count Data

**Version** 0.1.2

**Description** Implements zero-modified versions of the Complex 'Tri-Parametric' Pearson distribution for overdispersed count data. The package addresses limitations of existing implementations when the parameter  $b$  approaches zero. It provides distribution functions, maximum likelihood estimation, and diagnostic tools for modeling count data with excess zeros. The methodology is based on 'Rodriguez-Avi' and coauthors (2003) <[doi:10.1007/s00362-002-0134-7](https://doi.org/10.1007/s00362-002-0134-7)>.

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**Suggests** testthat (>= 3.0.0), knitr, rmarkdown, spelling

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**URL** <https://github.com/roladoja/zmctp>

**BugReports** <https://github.com/roladoja/zmctp/issues>

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|               |                                                                        |
|---------------|------------------------------------------------------------------------|
| zmctp-package | <i>zmctp: Zero-Modified Complex Triparametric Pearson Distribution</i> |
|---------------|------------------------------------------------------------------------|

---

**Description**

The zmctp package extends the Complex Triparametric Pearson (CTP) distribution with zero-modified versions for handling overdispersed count data, particularly when the parameter  $b$  approaches zero.

**Details**

Main functions:

- [dctp](#), [pctp](#), [qctp](#), [rctp](#) - CTP distribution functions
- [dzictp](#), [pzip](#), [qzip](#), [rzip](#) - Zero-Modified CTP distribution functions
- [ctp.fit](#) - Fit CTP model
- [zip](#) - Fit Zero-Modified CTP model

**Author(s)**

**Maintainer:** Rasheedat Oladoja <roladoja@ttu.edu> ([ORCID](#))

**See Also**

Useful links:

- <https://github.com/roladoja/zmctp>
- Report bugs at <https://github.com/roladoja/zmctp/issues>

---

 ctp.fit

---

*Maximum Likelihood Estimation for the CTP Distribution*


---

**Description**

Fits the Complex Triparametric Pearson (CTP) distribution to count data using maximum likelihood estimation.

**Usage**

```
ctp.fit(
  x,
  a_start = NULL,
  b_start = NULL,
  gama_start = NULL,
  method = "L-BFGS-B",
  penalty = 1e+10
)
```

**Arguments**

|            |                                                                      |
|------------|----------------------------------------------------------------------|
| x          | Numeric vector of nonnegative counts.                                |
| a_start    | Optional starting value for parameter a.                             |
| b_start    | Optional starting value for parameter b.                             |
| gama_start | Optional starting value for parameter gamma.                         |
| method     | Optimization method (default: "L-BFGS-B").                           |
| penalty    | numeric penalty added for numerical stability when $b \rightarrow 0$ |

**Value**

An object of class "ctpfir" containing:

|           |                            |
|-----------|----------------------------|
| estimates | Named vector of MLEs       |
| se        | Standard errors            |
| vcov      | Variance-covariance matrix |

|               |                                                |
|---------------|------------------------------------------------|
| logLik        | Log-likelihood                                 |
| AIC           | Akaike Information Criterion                   |
| BIC           | Bayesian Information Criterion                 |
| pearson_chisq | Pearson's chi-squared statistic                |
| wald_chisq    | Wald's chi-squared statistic                   |
| fitted_freq   | Data frame of observed vs expected frequencies |
| data          | Original data                                  |
| converged     | Convergence status                             |

### Examples

```
set.seed(123)

x <- rctp(30, a = 1, b = 0.5, gama = 5)
fit <- ctp.fit(x)
print(fit)
plot(fit)
```

---

dctp

---

*Probability Mass Function of the CTP Distribution*


---

### Description

Evaluates the probability mass function of the Complex TriParametric Pearson (CTP) distribution for nonnegative integer values.

The pmf is

$$p(x) = p(0) \frac{(a + ib)_x (a - ib)_x}{(\gamma)_x x!}, \quad x = 0, 1, \dots$$

and satisfies the recurrence

$$\frac{p(x+1)}{p(x)} = \frac{(a+x)^2 + b^2}{(\gamma+x)(x+1)}.$$

### Usage

```
dctp(x, a, b, gama, log = FALSE)
```

### Arguments

|      |                                              |
|------|----------------------------------------------|
| x    | Vector of nonnegative integers.              |
| a    | Parameter a.                                 |
| b    | Parameter b (must satisfy $b \geq 0$ ).      |
| gama | Parameter gamma.                             |
| log  | Logical; if TRUE, returns log-probabilities. |

**Value**

A numeric vector of probabilities.

**Examples**

```
dctp(0:5, a = 1, b = 0.5, gama = 6)
```

---

dzictp

---

*Probability Mass Function of the ZM-CTP Distribution*


---

**Description**

The Zero-Modified CTP (ZM-CTP) distribution modifies the zero probability of the baseline CTP distribution.

**Usage**

```
dzictp(x, a, b, gama, omega, log = FALSE)
```

**Arguments**

|       |                                                      |
|-------|------------------------------------------------------|
| x     | Vector of nonnegative integers.                      |
| a     | Parameter a.                                         |
| b     | Parameter b.                                         |
| gama  | Parameter gamma.                                     |
| omega | Zero-modification parameter, with $0 < \omega < 1$ . |
| log   | Logical; if TRUE, returns log-probabilities.         |

**Value**

Numeric vector of probabilities.

**Examples**

```
dzictp(0:5, a = 1, b = 0.5, gama = 6, omega = 0.3)
```

---

|          |                                                    |
|----------|----------------------------------------------------|
| mean_ctp | <i>Theoretical moments of the CTP distribution</i> |
|----------|----------------------------------------------------|

---

### Description

Theoretical moments of the CTP distribution

### Usage

```
mean_ctp(a, b, gama)
```

```
var_ctp(a, b, gama)
```

```
skew_ctp(a, b, gama)
```

### Arguments

a, b, gama            CTP parameters.

### Details

These functions do not validate that the parameter constraints required for a given moment to exist are satisfied (e.g.  $\text{gama} > 2*a+2$  for the variance,  $\text{gama} > 2*a+3$  for the skewness). Outside these regions the returned value may be Inf, NaN, or negative; see [dctp](#) for the corresponding existence warnings applied at the density level. See [mode\\_ctp](#) for the mode, including its tie-case handling.

### Examples

```
mean_ctp(a = 1, b = 0.5, gama = 6)
var_ctp(a = 1, b = 0.5, gama = 6)
skew_ctp(a = 1, b = 0.5, gama = 6)
```

---

|            |                                                                |
|------------|----------------------------------------------------------------|
| mean_zictp | <i>Theoretical moments and mode of the ZI-CTP distribution</i> |
|------------|----------------------------------------------------------------|

---

### Description

Theoretical moments and mode of the ZI-CTP distribution

### Usage

```
mean_zictp(a, b, gama, omega)
```

```
var_zictp(a, b, gama, omega)
```

```
skew_zictp(a, b, gama, omega)
```

**Arguments**

|            |                           |
|------------|---------------------------|
| a, b, gama | CTP parameters.           |
| omega      | Zero-inflation parameter. |

**Details**

These functions do not validate that the parameter constraints required for a given moment to exist are satisfied (e.g.  $\text{gama} > 2*a+2$  for the variance,  $\text{gama} > 2*a+3$  for the skewness), the same caveat documented in [mean\\_ctp](#).

**Examples**

```
# Quick illustration (fast, runs during R CMD check)
mean_zictp(a = 1, b = 0.5, gama = 6, omega = 0.3)
var_zictp(a = 1, b = 0.5, gama = 6, omega = 0.3)
skew_ctp(a = 1, b = 0.5, gama = 6)
skew_zictp(a = 1, b = 0.5, gama = 6, omega = 0.3)
mode_zictp(a = 1, b = 0.5, gama = 6, omega = 0.3)

# Empirical check against simulated data (slower, skipped on CRAN checks)
set.seed(2026)
x <- rzictp(50000, a = 1, b = 0.5, gama = 6, omega = 0.3)
skew_zictp(1, 0.5, 6, 0.3)           # theoretical
mean((x - mean(x))^3) / sd(x)^3     # empirical
```

---

|          |                                     |
|----------|-------------------------------------|
| mode_ctp | <i>Mode of the CTP distribution</i> |
|----------|-------------------------------------|

---

**Description**

Mode of the CTP distribution

**Usage**

```
mode_ctp(a, b, gama)
```

**Arguments**

|      |                            |
|------|----------------------------|
| a    | alpha parameter            |
| b    | b parameter ( $b \geq 0$ ) |
| gama | gamma parameter            |

**Value**

the mode (a single integer), or, in the exact tie case, a numeric vector of length 2 giving both consecutive modes

---

|            |                                        |
|------------|----------------------------------------|
| mode_zictp | <i>Mode of the ZI-CTP distribution</i> |
|------------|----------------------------------------|

---

**Description**

Mode of the ZI-CTP distribution

**Usage**

```
mode_zictp(a, b, gama, omega)
```

**Arguments**

|       |                          |
|-------|--------------------------|
| a     | alpha parameter          |
| b     | b parameter (b >= 0)     |
| gama  | gamma parameter          |
| omega | zero-inflation parameter |

**Value**

the mode (a single integer)

---

|      |                                                                 |
|------|-----------------------------------------------------------------|
| pctp | <i>Cumulative Distribution Function of the CTP Distribution</i> |
|------|-----------------------------------------------------------------|

---

**Description**

Cumulative Distribution Function of the CTP Distribution

**Usage**

```
pctp(q, a, b, gama, lower.tail = TRUE, log.p = FALSE)
```

**Arguments**

|            |                                                                            |
|------------|----------------------------------------------------------------------------|
| q          | Vector of quantiles.                                                       |
| a          | Parameter a.                                                               |
| b          | Parameter b.                                                               |
| gama       | Parameter gamma.                                                           |
| lower.tail | Logical; if TRUE, probabilities are $P(X \leq q)$ , otherwise $P(X > q)$ . |
| log.p      | Logical; if TRUE, probabilities are given on the log scale.                |

**Value**

Numeric vector of cumulative probabilities.

**Examples**

```
pctp(0:5, a = 1, b = 0.5, gama = 6)
```

---

|             |                                       |
|-------------|---------------------------------------|
| plot.ctpfit | <i>Plot method for ctpfit objects</i> |
|-------------|---------------------------------------|

---

**Description**

Plot method for ctpfit objects

**Usage**

```
## S3 method for class 'ctpfit'
plot(x, type = c("frequency", "cdf", "qq"), ...)
```

**Arguments**

|      |                                           |
|------|-------------------------------------------|
| x    | A ctpfit object                           |
| type | Type of plot: "frequency", "cdf", or "qq" |
| ...  | Additional graphical parameters           |

**Value**

No return value. Called for its side effect of producing a plot.

---

|               |                                         |
|---------------|-----------------------------------------|
| plot.zictpfit | <i>Plot method for zictpfit objects</i> |
|---------------|-----------------------------------------|

---

**Description**

Creates diagnostic plots for Zero-Modified CTP distribution fits, including frequency comparisons, CDF plots, and Q-Q plots.

**Usage**

```
## S3 method for class 'zictpfit'
plot(x, type = c("frequency", "cdf", "qq"), ...)
```

**Arguments**

|      |                                           |
|------|-------------------------------------------|
| x    | A zictpfit object from zictp.fit()        |
| type | Type of plot: "frequency", "cdf", or "qq" |
| ...  | Additional graphical parameters           |

**Value**

No return value. Called for its side effect of producing a plot.

---

|              |                                        |
|--------------|----------------------------------------|
| print.ctpfit | <i>Print method for ctpfit objects</i> |
|--------------|----------------------------------------|

---

**Description**

Print method for ctpfit objects

**Usage**

```
## S3 method for class 'ctpfit'  
print(x, ...)
```

**Arguments**

|     |                                |
|-----|--------------------------------|
| x   | A ctpfit object                |
| ... | Additional arguments (ignored) |

**Value**

Invisibly returns the original fitted model object. The function is called for its side effect of printing a model summary.

---

|                |                                          |
|----------------|------------------------------------------|
| print.zictpfit | <i>Print method for zictpfit objects</i> |
|----------------|------------------------------------------|

---

**Description**

Print method for zictpfit objects

**Usage**

```
## S3 method for class 'zictpfit'  
print(x, ...)
```

**Arguments**

|     |                                |
|-----|--------------------------------|
| x   | A zictpfit object              |
| ... | Additional arguments (ignored) |

**Value**

Invisibly returns the original fitted model object. The function is called for its side effect of printing a model summary.

---

pzictp

---

*Cumulative Distribution Function of the ZM-CTP Distribution*


---

**Description**

Cumulative Distribution Function of the ZM-CTP Distribution

**Usage**

```
pzictp(q, a, b, gama, omega, lower.tail = TRUE, log.p = FALSE)
```

**Arguments**

|            |                              |
|------------|------------------------------|
| q          | Vector of quantiles.         |
| a          | Parameter a.                 |
| b          | Parameter b.                 |
| gama       | Parameter gamma.             |
| omega      | Zero-modification parameter. |
| lower.tail | Logical.                     |
| log.p      | Logical.                     |

**Value**

Numeric vector of cumulative probabilities.

**Examples**

```
pzictp(0:5, a = 1, b = 0.5, gama = 6, omega = 0.3)
```

---

qctp

*Quantile Function of the CTP Distribution*


---

**Description**

Quantile Function of the CTP Distribution

**Usage**

```
qctp(p, a, b, gama, lower.tail = TRUE, log.p = FALSE, max_q = 1000)
```

**Arguments**

|            |                          |
|------------|--------------------------|
| p          | Vector of probabilities. |
| a          | Parameter a.             |
| b          | Parameter b.             |
| gama       | Parameter gamma.         |
| lower.tail | Logical.                 |
| log.p      | Logical.                 |
| max_q      | Maximum x to search.     |

**Value**

Numeric vector of quantiles.

**Examples**

```
qctp(c(0.25, 0.5, 0.75), a = 1, b = 0.5, gama = 6)
```

---

qzictp

*Quantile Function of the ZM-CTP Distribution*


---

**Description**

Quantile Function of the ZM-CTP Distribution

**Usage**

```
qzictp(p, a, b, gama, omega, lower.tail = TRUE, log.p = FALSE, max_q = 1000)
```

**Arguments**

|            |                              |
|------------|------------------------------|
| p          | Vector of probabilities.     |
| a          | Parameter a.                 |
| b          | Parameter b.                 |
| gama       | Parameter gamma.             |
| omega      | Zero-modification parameter. |
| lower.tail | Logical.                     |
| log.p      | Logical.                     |
| max_q      | Maximum x to search.         |

**Value**

Numeric vector of quantiles.

**Examples**

```
qzictp(c(0.25, 0.5, 0.75), a = 1, b = 0.5, gama = 6, omega = 0.3)
```

---

rctp

*Random Generation from the CTP Distribution*


---

**Description**

Random Generation from the CTP Distribution

**Usage**

```
rctp(n, a, b, gama)
```

**Arguments**

|      |                         |
|------|-------------------------|
| n    | Number of observations. |
| a    | Parameter a.            |
| b    | Parameter b.            |
| gama | Parameter gamma.        |

**Value**

Integer vector of random draws.

**Examples**

```
set.seed(123)
rctp(10, a = 1, b = 0.5, gama = 6)
```

---

 rzictp

*Random Generation from the ZM-CTP Distribution*


---

**Description**

Random Generation from the ZM-CTP Distribution

**Usage**

```
rzictp(n, a, b, gama, omega)
```

**Arguments**

|       |                              |
|-------|------------------------------|
| n     | Number of observations.      |
| a     | Parameter a.                 |
| b     | Parameter b.                 |
| gama  | Parameter gamma.             |
| omega | Zero-modification parameter. |

**Value**

Integer vector of random draws.

**Examples**

```
set.seed(123)
rzictp(10, a = 1, b = 0.5, gama = 6, omega = 0.3)
```

---

 summary.ctpfit

*Summary method for ctpfit objects*


---

**Description**

Summary method for ctpfit objects

**Usage**

```
## S3 method for class 'ctpfit'
summary(object, ...)
```

**Arguments**

|        |                                |
|--------|--------------------------------|
| object | A ctpfit object                |
| ...    | Additional arguments (ignored) |

**Value**

Invisibly returns the original fitted model object. The function is called for its side effects, producing a formatted summary of parameter estimates, moments, and goodness-of-fit diagnostics.

---

|                   |                                             |
|-------------------|---------------------------------------------|
| summary.zictpfitt | <i>Summary method for zictpfitt objects</i> |
|-------------------|---------------------------------------------|

---

**Description**

Summary method for zictpfitt objects

**Usage**

```
## S3 method for class 'zictpfitt'
summary(object, ...)
```

**Arguments**

|        |                                |
|--------|--------------------------------|
| object | A zictpfitt object             |
| ...    | Additional arguments (ignored) |

**Value**

Invisibly returns the original fitted model object. The function is called for its side effects, producing a formatted summary of parameter estimates, moments, and goodness-of-fit diagnostics.

---

|           |                                                                             |
|-----------|-----------------------------------------------------------------------------|
| zictp.fit | <i>Maximum Likelihood Estimation for the Zero-Modified CTP Distribution</i> |
|-----------|-----------------------------------------------------------------------------|

---

**Description**

Fits the Zero-Modified Complex TriParametric Pearson (ZM-CTP) distribution to count data using maximum likelihood estimation.

A logit reparameterization is used for omega to ensure  $0 < \omega < 1$ , and a log reparameterization is used for gamma so that  $\gamma = 2^a + 2 + \exp(\eta)$ , which guarantees variance existence throughout optimization.

**Usage**

```
zictp.fit(
  x,
  a_start = NULL,
  b_start = NULL,
  gama_start = NULL,
  omega_start = NULL,
  method = "BFGS"
)
```

**Arguments**

|                          |                                                                      |
|--------------------------|----------------------------------------------------------------------|
| <code>x</code>           | Numeric vector of nonnegative counts.                                |
| <code>a_start</code>     | Optional starting value for parameter <code>a</code> .               |
| <code>b_start</code>     | Optional starting value for parameter <code>b</code> .               |
| <code>gama_start</code>  | Optional starting value for parameter <code>gamma</code> .           |
| <code>omega_start</code> | Optional starting value for <code>omega</code> ( $0 < \omega < 1$ ). |
| <code>method</code>      | Optimization method (default: "BFGS").                               |

**Value**

An object of class `"zictpfit"`.

**Examples**

```
set.seed(123)
x <- rzictp(30, a = 1, b = 0.5, gama = 5, omega = 0.3)
fit <- zictp.fit(x)
fit$estimates
```

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