# Package: singleRcapture (via r-universe)

February 13, 2025

Type Package

Version 0.2.3

Title Single-Source Capture-Recapture Models

Description Implementation of single-source capture-recapture methods for population size estimation using zero-truncated, zero-one truncated and zero-truncated one-inflated Poisson, Geometric and Negative Binomial regression as well as Zelterman's and Chao's regression. Package includes point and interval

```
estimators for the population size with variances estimated
     using analytical or bootstrap method. Details can be found in:
     van der Heijden et all. (2003) <doi:10.1191/1471082X03st057oa>,
     Böhning and van der Heijden (2019) <doi:10.1214/18-AOAS1232>,
     Böhning et al. (2020) Capture-Recapture Methods for the Social
     and Medical Sciences or Böhning and Friedl (2021)
     <doi:10.1007/s10260-021-00556-8>.
License MIT + file LICENSE
Encoding UTF-8
LazyData yes
RdMacros mathjaxr
BuildManual TRUE
VignetteBuilder knitr
Depends R (>= 3.5.0)
RoxygenNote 7.3.2
URL https://github.com/ncn-foreigners/singleRcapture
BugReports https://github.com/ncn-foreigners/singleRcapture/issues
Imports stats, lamW, mathjaxr, sandwich, doParallel, foreach, parallel
Suggests rmarkdown, knitr, tinytest, covr, VGAM, lmtest
NeedsCompilation no
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```

2 carcassubmission

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Config/pak/sysreqs make

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# Description

Data on British animal farms submissions to AHVLA. British farms are able to submit samples to AHVLA if cause of death for an animal cannot be determined and private veterinary surgeon decides to submit them, unless there is notifiable disease suspected then such a submission is not required.

This data set contains information about such farms. Only submissions that are included in this data frame are submissions of carcasses i.e. submissions of blood samples etc. are excluded.

### Usage

```
data("carcassubmission")
```

#### **Format**

Data frame with 1,858 rows and 4 columns.

TOTAL\_SUB Number of submissions of animal carcasses.

log\_size Numerical value equal to logarithm of size of farm.

log\_distance Numerical value equal to logarithm of distance to nearest AHVLA center.

C\_TYPE Factor describing type of activity on farm that animals are used for. Either Dairy or Beef

#### References

This data set and its description was provided in publication: Böhning, D., Vidal Diez, A., Lerdsuwansri, R., Viwatwongkasem, C., and Arnold, M. (2013). "A generalization of Chao's estimator for covariate information". *Biometrics*, 69(4), 1033-1042. doi:10.1111/biom.12082

chao

Family functions in singleRcapture package

# Description

Package singleRcapture utilizes various family type functions that specify variable parts of population size estimation, regression, diagnostics and other necessary information that depends on the model. These functions are used as model argument in estimatePopsize function.

### Usage

```
chao(lambdaLink = "loghalf", ...)

Hurdleztgeom(
  lambdaLink = c("log", "neglog"),
  piLink = c("logit", "cloglog", "probit"),
  ...
)

Hurdleztnegbin(
  nSim = 1000,
  epsSim = 1e-08,
  eimStep = 6,
  lambdaLink = c("log", "neglog"),
  alphaLink = c("logit", "cloglog", "probit"),
  ...
)
```

```
Hurdleztpoisson(
  lambdaLink = c("log", "neglog"),
  piLink = c("logit", "cloglog", "probit"),
)
oiztgeom(
  lambdaLink = c("log", "neglog"),
 omegaLink = c("logit", "cloglog", "probit"),
)
oiztnegbin(
  nSim = 1000,
  epsSim = 1e-08,
  eimStep = 6,
  lambdaLink = c("log", "neglog"),
  alphaLink = c("log", "neglog"),
  omegaLink = c("logit", "cloglog", "probit"),
)
oiztpoisson(
  lambdaLink = c("log", "neglog"),
 omegaLink = c("logit", "cloglog", "probit"),
)
zelterman(lambdaLink = "loghalf", ...)
zotgeom(lambdaLink = c("log", "neglog"), ...)
zotnegbin(
  nSim = 1000,
  epsSim = 1e-08,
  eimStep = 6,
  lambdaLink = c("log", "neglog"),
  alphaLink = c("log", "neglog"),
)
zotpoisson(lambdaLink = c("log", "neglog"), ...)
ztHurdlegeom(
  lambdaLink = c("log", "neglog"),
  piLink = c("logit", "cloglog", "probit"),
  . . .
```

```
ztHurdlenegbin(
  nSim = 1000,
  epsSim = 1e-08,
  eimStep = 6,
  lambdaLink = c("log", "neglog"),
  alphaLink = c("log", "neglog"),
  piLink = c("logit", "cloglog", "probit"),
)
ztHurdlepoisson(
  lambdaLink = c("log", "neglog"),
  piLink = c("logit", "cloglog", "probit"),
)
ztgeom(lambdaLink = c("log", "neglog"), ...)
ztnegbin(
  nSim = 1000,
  epsSim = 1e-08,
  eimStep = 6,
  lambdaLink = c("log", "neglog"),
  alphaLink = c("log", "neglog"),
)
ztoigeom(
  lambdaLink = c("log", "neglog"),
omegaLink = c("logit", "cloglog", "probit"),
)
ztoinegbin(
  nSim = 1000,
  epsSim = 1e-08,
  eimStep = 6,
  lambdaLink = c("log", "neglog"),
  alphaLink = c("log", "neglog"),
  omegaLink = c("logit", "cloglog", "probit"),
)
ztoipoisson(
  lambdaLink = c("log", "neglog"),
  omegaLink = c("logit", "cloglog", "probit"),
```

```
...
)
ztpoisson(lambdaLink = c("log", "neglog"), ...)
```

#### **Arguments**

lambdaLink a link for Poisson parameter, "log" by default except for zelterman's and chao's

models where only  $\ln\left(\frac{x}{2}\right)$  is possible.

... Additional arguments, not used for now.

piLink a link for probability parameter, "logit" by default

nSim, epsSim if working weights cannot be computed analytically these arguments specify

maximum number of simulations allowed and precision level for finding them

numerically respectively.

eimStep a non negative integer describing how many values should be used at each step

of approximation of information matrixes when no analytic solution is available (e.g. "ztnegbin"), default varies depending on a function. Higher value usually means faster convergence but may potentially cause issues with convergence.

alphaLink a link for dispersion parameter, "log" by default omegaLink a link for inflation parameter, "logit" by default

#### **Details**

Most of these functions are based on some "base" distribution with support  $\mathbb{N}_0 = \mathbb{N} \cup \{0\}$  that describe distribution of Y before truncation. Currently they include:

$$\mathbb{P}(Y=y|\lambda,\alpha) = \left\{ \begin{array}{cc} \frac{\lambda^y e^{-\lambda}}{y!} & \text{Poisson distribution} \\ \frac{\Gamma(y+\alpha^{-1})}{\Gamma(\alpha^{-1})y!} \left(\frac{\alpha^{-1}}{\alpha^{-1}+\lambda}\right)^{\alpha^{-1}} \left(\frac{\lambda}{\alpha^{-1}+\lambda}\right)^y & \text{negative binomial distribution} \\ \frac{\lambda^y}{(1+\lambda)^{y+1}} & \text{geometric distribution} \end{array} \right.$$

where  $\lambda$  is the Poisson parameter and  $\alpha$  is the dispersion parameter. Geometric distribution is a special case of negative binomial distribution when  $\alpha=1$  it is included because negative binomial distribution is quite troublesome numerical regression in fitting. It is important to know that PMF of negative binomial distribution approaches the PMF of Poisson distribution when  $\alpha \to 0^+$ .

Note in literature on single source capture recapture models the dispersion parameter which introduces greater variability in negative binomial distribution compared to Poisson distribution is generally interpreted as explaining the *unobserved* heterogeneity i.e. presence of important unobserved independent variables. All these methods for estimating population size are tied to Poisson processes hence we use  $\lambda$  as parameter symbol instead of  $\mu$  to emphasize this connection. Also will not be hard to see that **all** estimators derived from modifying the "base" distribution are unbiased if assumptions made by respective models are not violated.

The zero-truncated models corresponding to "base" distributions are characterized by relation:

$$\mathbb{P}(Y=y|Y>0) = \left\{ \begin{array}{cc} \frac{\mathbb{P}(Y=y)}{1-\mathbb{P}(Y=0)} & \text{when } y \neq 0 \\ 0 & \text{when } y=0 \end{array} \right.$$

which allows us to estimate parameter values using only observed part of population. These models lead to the following estimates, respectively:

$$\hat{N} = \sum_{k=1}^{N_{obs}} \frac{1}{1 - \exp(-\lambda_k)}$$
 For Poisson distribution 
$$\hat{N} = \sum_{k=1}^{N_{obs}} \frac{1}{1 - (1 + \alpha_k \lambda_k)^{-\alpha_k^{-1}}}$$
 For negative binomial distribution 
$$\hat{N} = \sum_{k=1}^{N_{obs}} \frac{1 + \lambda_k}{\lambda_k}$$
 For geometric distribution

One common way in which assumptions of zero-truncated models are violated is presence of **one-inflation** the presence of which is somewhat similar in single source capture-recapture models to zero-inflation in usual count data analysis. There are two ways in which one-inflation may be understood, they relate to whether  $\mathbb{P}(Y=0)$  is modified by inflation. The first approach is inflate  $(\omega$  parameter) zero-truncated distribution as:

$$\mathbb{P}_{new}(Y=y|Y>0) = \left\{ \begin{array}{ll} \omega + (1-\omega)\mathbb{P}_{old}(Y=1|Y>0) & \text{when: } y=1 \\ (1-\omega)\mathbb{P}_{old}(Y=y|Y>0) & \text{when: } y\neq 1 \end{array} \right.$$

which corresponds to:

$$\mathbb{P}_{new}(Y=y) = \begin{cases} \mathbb{P}_{old}(Y=0) & \text{when: } y=0 \\ \omega(1-\mathbb{P}(Y=0)) + (1-\omega)\mathbb{P}_{old}(Y=1) & \text{when: } y=1 \\ (1-\omega)\mathbb{P}_{old}(Y=y) & \text{when: } y>1 \end{cases}$$

before zero-truncation. Models that utilize this approach are commonly referred to as *zero-truncated one-inflated models*. Another way of accommodating one-inflation in SSCR is by putting inflation parameter on base distribution as:

$$\mathbb{P}_{new}(Y=y) = \left\{ \begin{array}{ll} \omega + (1-\omega)\mathbb{P}_{old}(Y=1) & \text{when: } y=1 \\ (1-\omega)\mathbb{P}_{old}(Y=y) & \text{when: } y \neq 1 \end{array} \right.$$

which then becomes:

$$\mathbb{P}_{new}(Y=y|Y>0) = \left\{ \begin{array}{cc} \frac{\omega}{1-(1-\omega)\mathbb{P}_{old}(Y=0)} + \frac{(1-\omega)}{1-(1-\omega)\mathbb{P}_{old}(Y=0)} \mathbb{P}_{old}(Y=1) & \text{when: } y=1 \\ \frac{(1-\omega)}{1-(1-\omega)\mathbb{P}_{old}(Y=0)} \mathbb{P}_{old}(Y=y) & \text{when: } y>1 \end{array} \right.$$

after truncation. It was shown by Böhning in 2022 paper that these approaches are equivalent in terms of maximizing likelihoods if we do not put formula on  $\omega$ . They can however lead to different population size estimates.

For zero-truncated one-inflated models the formula for population size estimate  $\hat{N}$  does not change since  $\mathbb{P}(y=0)$  remains the same but estimation of parameters changes all calculations.

For one-inflated zero-truncated models population size estimates are expressed, respectively by:

$$\hat{N} = \sum_{k=1}^{N_{obs}} \frac{1}{1 - (1 - \omega_k) \exp(-\lambda_k)}$$
 For base Poisson distribution 
$$\hat{N} = \sum_{k=1}^{N_{obs}} \frac{1}{1 - (1 - \omega_k)(1 + \alpha_k \lambda_k)^{-\alpha_k^{-1}}}$$
 For base negative binomial distribution 
$$\hat{N} = \sum_{k=1}^{N_{obs}} \frac{1 + \lambda_k}{\lambda_k + \omega_k}$$
 For base geometric distribution

**Zero-one-truncated** models ignore one counts instead of accommodating one-inflation by utilizing the identity

$$\ell_{\text{ztoi}} = \boldsymbol{f}_1 \ln \frac{\boldsymbol{f}_1}{N_{obs}} + (N_{obs} - \boldsymbol{f}_1) \ln \left(1 - \frac{\boldsymbol{f}_1}{N_{obs}}\right) + \ell_{\text{zot}}$$

where  $\ell_{zot}$  is the log likelihood of zero-one-truncated distribution characterized by probability mass function:

$$\mathbb{P}(Y=y|Y>1) = \left\{ \begin{array}{ll} \frac{\mathbb{P}(Y=y)}{1-\mathbb{P}(Y=0)-\mathbb{P}(Y=1)} & \text{when } y>1 \\ 0 & \text{when } y \in \{0,1\} \end{array} \right.$$

where  $\mathbb{P}(Y)$  is the probability mass function of the "base" distribution. The identity above justifies use of zero-one-truncated, unfortunately it was only proven for intercept only models, however numerical simulations seem to indicate that even if the theorem cannot be extended for (non trivial) regression population size estimation is still possible.

For zero-one-truncated models population size estimates are expressed by:

$$\hat{N} = \boldsymbol{f}_1 + \sum_{k=1}^{N_{obs}} \frac{1 - \lambda_k \exp(-\lambda_k)}{1 - \exp(-\lambda_k) - \lambda_k \exp(-\lambda_k)}$$
 For base Poisson distribution 
$$\hat{N} = \boldsymbol{f}_1 + \sum_{k=1}^{N_{obs}} \frac{1 - \lambda_k (1 + \alpha_k \lambda_k)^{-1 - \alpha_k^{-1}}}{1 - (1 + \alpha_k \lambda_k)^{-\alpha_k^{-1}} - \lambda_k (1 + \alpha_k \lambda_k)^{-1 - \alpha_k^{-1}}}$$
 For base negative binomial distribution 
$$\hat{N} = \boldsymbol{f}_1 + \sum_{k=1}^{N_{obs}} \frac{\lambda_k^2 + \lambda_k + 1}{\lambda_k^2}$$
 For base geometric distribution

Pseudo hurdle models are experimental and not yet described in literature.

Lastly there are **chao** and **zelterman** models which are based on logistic regression on the dummy variable

$$Z = \begin{cases} 0 & \text{if } Y = 1\\ 1 & \text{if } Y = 2 \end{cases}$$

based on the equation:

$$\operatorname{logit}(p_k) = \ln\left(\frac{\lambda_k}{2}\right) = \boldsymbol{\beta}\mathbf{x}_k = \eta_k$$

where  $\lambda_k$  is the Poisson parameter.

The *zelterman* estimator of population size is expressed as:

$$\hat{N} = \sum_{k=1}^{N_{obs}} 1 - \exp\left(-\lambda_k\right)$$

and chao estimator has the form:

$$\hat{N} = N_{obs} + \sum_{k=1}^{f_1 + f_2} \frac{1}{\lambda_k + \frac{\lambda_k^2}{2}}$$

#### Value

A object of class family containing objects:

- makeMinusLogLike A factory function for creating the following functions:  $\ell(\beta)$ ,  $\frac{\partial \ell}{\partial \beta}$ ,  $\frac{\partial^2 \ell}{\partial \beta^T \partial \beta}$  functions from the y vector and the  $X_{vlm}$  matrix (or just X if applied to model with single linear predictor)which has the deriv argument with possible values in c(0, 1, 2) that determine which derivative to return; the default value is 0, which represents the minus log-likelihood.
- links A list with link functions.
- mu.eta, variance Functions of linear predictors that return expected value and variance. The type argument with 2 possible values ("trunc" and "nontrunc") that specifies whether to return  $\mathbb{E}(Y|Y>0)$ ,  $\mathrm{var}(Y|Y>0)$  or  $\mathbb{E}(Y)$ ,  $\mathrm{var}(Y)$  respectively; the deriv argument with values in  $\mathrm{c}(0,1,2)$  is used for indicating the derivative with respect to the linear predictors, which is used for providing standard errors in the predict method.
- family A string that specifies name of the model.
- valideta, validmu For now it only returns TRUE. In the near future, it will be used to check whether applied linear predictors are valid (i.e. are transformed into some elements of the parameter space subjected to the inverse link function).
- funcZ, Wfun Functions that create pseudo residuals and working weights used in IRLS algorithm.
- devResids A function that given the linear predictors prior weights vector and response vector returns deviance residuals. Not all family functions have these functions implemented yet.
- pointEst, popVar Functions that given prior weights linear predictors and in the latter case also estimate of  $cov(\hat{\beta})$  and  $X_{vlm}$  matrix return point estimate for population size and analytic estimation of its variance. There is a additional boolean parameter contr in the former function that if set to true returns contribution of each unit.
- etaNames Names of linear predictors.
- densityFunction A function that given linear predictors returns value of PMF at values x. Additional argument type specifies whether to return  $\mathbb{P}(Y|Y>0)$  or  $\mathbb{P}(Y)$ .
- simulate A function that generates values of a dependent vector given linear predictors.
- getStart An expression for generating starting points.

#### Author(s)

Piotr Chlebicki, Maciej Beręsewicz

#### See Also

estimatePopsize()

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```
confint.singleRStaticCountData
```

Confidence intervals for model parameters

# **Description**

A function that computes studentized confidence intervals for model coefficients.

# Usage

```
## S3 method for class 'singleRStaticCountData'
confint(object, parm, level = 0.95, ...)
```

# **Arguments**

object of singleRStaticCountData class.

parm names of parameters for which confidence intervals are to be computed, if miss-

ing all parameters will be considered.

level confidence level for intervals.

... currently does nothing.

#### Value

An object with named columns that include upper and lower limit of confidence intervals.

controlMethod

Control parameters for regression

# **Description**

controlMethod constructs a list with all necessary control parameters for regression fitting in estimatePopsizeFit and estimatePopsize.

### Usage

```
controlMethod(
  epsilon = 1e-08,
  maxiter = 1000,
  verbose = 0,
  printEveryN = 1L,
  coefStart = NULL,
  etaStart = NULL,
  optimMethod = "Nelder-Mead",
  silent = FALSE,
  optimPass = FALSE,
```

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```
stepsize = 1,
  checkDiagWeights = TRUE,
  weightsEpsilon = 1e-08,
  momentumFactor = 0,
  saveIRLSlogs = FALSE,
  momentumActivation = 5,
   criterion = c("coef", "abstol", "reltol")
```

# Arguments

epsilon a tolerance level for fitting algorithms by default 1e-8.

maxiter a maximum number of iterations.

verbose a numeric value indicating whether to trace steps of fitting algorithm for IRLS fitting method different values of verbose give the following information:

- 1 Returns information on the number of current iteration and current loglikelihood.
- 2 Returns information on vector of regression parameters at current iteration (and all of the above).
- 3 Returns information on reduction of log-likelihood at current iteration (and all of the above).
- 4 Returns information on value of log-likelihood function gradient at current iteration (and all of the above).
- 5 Returns information on convergence criterion and values that are taken into account when considering convergence (and all of the above).

if optim method was chosen verbose will be passed to stats::optim() as trace.

printEveryN

an integer value indicating how often to print information specified in verbose, by default set to 1.

coefStart, etaStart

initial parameters for regression coefficients or linear predictors if NULL. For IRLS fitting only etaStart is needed so if coefStart is provided it will be converted to etaStart, for optim fitting coefStart is necessary and argument etaStart will be ignored.

optimMethod

a method of stats::optim() used "Nelder-Mead" is the default.

silent

a logical value, indicating whether warnings in IRLS method should be suppressed.

optimPass

an optional list of parameters passed to stats::optim(..., control = optimPass) if FALSE then list of control parameters will be inferred from other parameters.

stepsize

only for IRLS, scaling of updates to beta vector lower value means slower convergence but more accuracy by default 1. In general if fitting algorithm fails lowering this value tends to be most effective at correcting it.

checkDiagWeights

a logical value indicating whether to check if diagonal elements of working weights matrixes in IRLS are sufficiently positive so that these matrixes are positive defined. By default TRUE.

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weightsEpsilon a small number to ensure positive definedness of weights matrixes. Only matters if checkDiagWeights is set to TRUE. By default 1e-8.

momentumFactor an experimental parameter in IRLS only allowing for taking previous step into account at current step, i.e instead of updating regression parameters as:

$$\beta_{(a)} = \beta_{(a-1)} + \text{stepsize} \cdot \text{step}_{(a)}$$

the update will be made as:

output object, by default FALSE.

$$\boldsymbol{\beta}_{(a)} = \boldsymbol{\beta}_{(a-1)} + \operatorname{stepsize} \cdot (\operatorname{step}_{(a)} + \operatorname{momentum} \cdot \operatorname{step}_{(a-1)})$$

saveIRLSlogs a logical value indicating if information specified in verbose should be saved to

momentumActivation

the value of log-likelihood reduction bellow which momentum will apply.

criterion a criterion used to determine convergence in IRLS, multiple values may be provided. By default c("coef", "abstol").

# Value

List with selected parameters, it is also possible to call list directly.

#### Author(s)

Piotr Chlebicki, Maciej Beręsewicz

# See Also

estimatePopsize() estimatePopsizeFit() controlModel() controlPopVar()

controlModel

Control parameters specific to some models

### **Description**

controlModel constructs a list with all necessary control parameters in estimatePopsize that are either specific to selected model or do not fit anywhere else.

Specifying additional formulas should be done by using only right hand side of the formula also for now all variables from additional formulas should also be included in the "main" formula.

# Usage

```
controlModel(
  weightsAsCounts = FALSE,
  omegaFormula = ~1,
  alphaFormula = ~1,
  piFormula = ~1
```

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# **Arguments**

weightsAsCounts

a boolean value indicating whether to treat weights argument as number of occurrences for each row in the data and adjust necessary methods and functionalities, like adjustments in bootstrap or decreasing weights in dfbeta instead or deleting rows from data, to accommodate this form of model specification.

omegaFormula a formula for inflation parameter in one inflated zero truncated and zero trun-

cated one inflated models.

alphaFormula a formula for dispersion parameter in negative binomial based models.

piFormula a formula for probability parameter in pseudo hurdle zero truncated and zero

truncated pseudo hurdle models.

### Value

A list with selected parameters, it is also possible to call list directly.

### Author(s)

Piotr Chlebicki, Maciej Beresewicz

### See Also

```
estimatePopsize() controlMethod() controlPopVar() singleRmodels()
```

controlPopVar

Control parameters for population size estimation

### **Description**

Creating control parameters for population size estimation and respective standard error and variance estimation.

# Usage

```
controlPopVar(
   alpha = 0.05,
   bootType = c("parametric", "semiparametric", "nonparametric"),
   B = 500,
   confType = c("percentilic", "normal", "basic"),
   keepbootStat = TRUE,
   traceBootstrapSize = FALSE,
   bootstrapVisualTrace = FALSE,
   fittingMethod = c("optim", "IRLS"),
   bootstrapFitcontrol = NULL,
   sd = c("sqrtVar", "normalMVUE"),
   covType = c("observedInform", "Fisher"),
   cores = 1L
)
```

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#### **Arguments**

alpha a significance level, 0.05 used by default.

bootType the bootstrap type to be used. Default is "parametric", other possible values

are: "semiparametric" and "nonparametric".

B a number of bootstrap samples to be performed (default 500).

confType a type of confidence interval for bootstrap confidence interval, "percentile"

by default. Other possibilities: "studentized" and "basic".

keepbootStat a boolean value indicating whether to keep a vector of statistics produced by

bootstrap.

traceBootstrapSize

a boolean value indicating whether to print size of bootstrapped sample after

truncation for semi- and fully parametric bootstraps.

bootstrapVisualTrace

a boolean value indicating whether to plot bootstrap statistics in real time if

cores = 1 if cores > 1 it instead indicates whether to make progress bar.

fittingMethod a method used for fitting models from bootstrap samples.

 $bootstrap {\tt Fit} control$ 

control parameters for each regression works exactly like controlMethod but

for fitting models from bootstrap samples.

sd a character indicating how to compute standard deviation of population size es-

timator either as:

 $\hat{\sigma} = \sqrt{\hat{\text{var}}(\hat{N})}$ 

for sqrt (which is slightly biased if  $\hat{N}$  has a normal distribution) or for normal MVUE as the unbiased minimal variance estimator for normal distribution:

$$\hat{\sigma} = \sqrt{\hat{\text{var}}(\hat{N})} \frac{\Gamma\left(\frac{N_{obs}-1}{2}\right)}{\Gamma\left(\frac{N_{obs}}{2}\right)} \sqrt{\frac{N_{obs}}{2}}$$

where the ration involving gamma functions is computed by log gamma func-

tion.

covType a type of covariance matrix for regression parameters by default observed infor-

mation matrix.

cores for bootstrap only, a number of processor cores to be used, any number greater

than 1 activates code designed with doParallel, foreach and parallel packages. Note that for now using parallel computing makes tracing impossible so traceBootstrapSize and bootstrapVisualTrace parameters are ignored in

this case.

#### Value

A list with selected parameters, it is also possible to call list directly.

# Author(s)

Piotr Chlebicki, Maciej Beręsewicz

#### See Also

```
estimatePopsize() controlModel() controlMethod()
```

estfun.singleRStaticCountData

Heteroscedasticity-consistent covariance matrix estimation for singleRStaticCountData class

# Description

S3 method for vcovHC to handle singleRStaticCountData class objects. Works exactly like vcovHC.default the only difference being that this method handles vector generalised linear models. Updating the covariance matrix in variance/standard error estimation for population size estimator can be done via redoPopEstimation()

#### Usage

```
## S3 method for class 'singleRStaticCountData'
estfun(x, ...)

## S3 method for class 'singleRStaticCountData'
bread(x, ...)

## S3 method for class 'singleRStaticCountData'
vcovHC(
    x,
    type = c("HC3", "const", "HC", "HC0", "HC1", "HC2", "HC4", "HC4m", "HC5"),
    omega = NULL,
    sandwich = TRUE,
    ...
)
```

# **Arguments**

x a fitted singleRStaticCountData class object.

... for vcovHC additional optional arguments passed to the following functions:

- estfun for empirical estimating functions.
- hatvalues for diagonal elements of projection matrix.
- sandwich only if sandwich argument in function call was set to TRUE.
- vcov when calling bread internally.

type

a character string specifying the estimation type, same as in sandwich::vcovHC.default. HC3 is the default value.

omega

a vector or a function depending on the arguments residuals (i.e. the derivative of log-likelihood with respect to each linear predictor), diaghat (the diagonal of the corresponding hat matrix) and df (the residual degrees of freedom), same as in sandwich::vcovHC.default.

sandwich

logical. Should the sandwich estimator be computed? If set to FALSE only the meat matrix is returned. Same as in sandwich::vcovHC()

# Value

Variance-covariance matrix estimation corrected for heteroscedasticity of regression errors

### Author(s)

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#### See Also

```
sandwich::vcovHC() redoPopEstimation()
```

# **Examples**

```
set.seed(1)
N <- 10000
gender <- rbinom(N, 1, 0.2)</pre>
eta <- -1 + 0.5*gender
counts <- rpois(N, lambda = exp(eta))</pre>
df <- data.frame(gender, eta, counts)</pre>
df2 <- subset(df, counts > 0)
mod1 <- estimatePopsize(</pre>
  formula = counts ~ 1 + gender,
  data = df2,
  model = "ztpoisson",
 method = "optim",
  popVar = "analytic"
)
require(sandwich)
HC <- sandwich::vcovHC(mod1, type = "HC4")</pre>
Fisher <- vcov(mod1, "Fisher") # variance covariance matrix obtained from
#Fisher (expected) information matrix
HC
Fisher
# usual results
summary(mod1)
# updated results
summary(mod1, cov = HC,
popSizeEst = redoPopEstimation(mod1, cov = HC))
# estimating equations
mod1_sims <- sandwich::estfun(mod1)</pre>
head(mod1_sims)
# bread method
all(vcov(mod1, "Fisher") * nrow(df2) == sandwich::bread(mod1, type = "Fisher"))
```

estimatePopsize

Single-source capture-recapture models

### Description

estimatePopsize first fits appropriate (v)glm model and then estimates full (observed and unobserved) population size. In this types of models it is assumed that the response vector (i.e. the dependent variable) corresponds to the number of times a given unit was observed in the source. Population size is then usually estimated by Horvitz-Thompson type estimator:

$$\hat{N} = \sum_{k=1}^{N} \frac{I_k}{\mathbb{P}(Y_k > 0)} = \sum_{k=1}^{N_{obs}} \frac{1}{1 - \mathbb{P}(Y_k = 0)}$$

where  $I_k = I_{Y_k>0}$  are indicator variables, with value 1 if kth unit was observed at least once and 0 otherwise.

# Usage

```
estimatePopsize(formula, ...)
## Default S3 method:
estimatePopsize(
  formula,
  model = c("ztpoisson", "ztnegbin", "ztgeom", "zotpoisson", "ztoipoisson",
  "oiztpoisson", "ztHurdlepoisson", "Hurdleztpoisson", "zotnegbin", "ztoinegbin",
  "oiztnegbin", "ztHurdlenegbin", "Hurdleztnegbin", "zotgeom", "ztoigeom", "oiztgeom",
    "ztHurdlegeom", "ztHurdlegeom", "zelterman", "chao"),
  weights = NULL,
  subset = NULL,
  naAction = NULL,
 method = c("optim", "IRLS"),
  popVar = c("analytic", "bootstrap", "noEst"),
  controlMethod = NULL,
  controlModel = NULL,
  controlPopVar = NULL,
 modelFrame = TRUE,
  x = FALSE,
  y = TRUE,
  contrasts = NULL,
  ratioReg = FALSE,
 offset,
)
```

# Arguments

| formula          | a formula for the model to be fitted, only applied to the "main" linear predictor. Only single response models are available.   |
|------------------|---|
|                  | additional optional arguments passed to other methods eg. estimatePopsizeFit.   |
| data             | a data frame or object coercible to data.frame class containing data for the regression and population size estimation.   |
| model            | a model for regression and population estimate full description in singleRmodels().   |
| weights          | an optional object of prior weights used in fitting the model. Can be used to specify number of occurrences of rows in data see controlModel()  |
| subset           | a logical vector indicating which observations should be used in regression and population size estimation. It will be evaluated on data argument provided on call.   |
| naAction         | Not yet implemented.  |
| method           | a method for fitting values currently supported: iteratively reweighted least squares (IRLS) and maximum likelihood (optim).  |
| popVar           | a method of constructing confidence interval and estimating the standard error either analytic or bootstrap. Bootstrap confidence interval type may be specified in controlPopVar. There is also the third possible value of noEst which skips the population size estimate all together. |
| controlMethod    | a list indicating parameters to use in fitting the model may be constructed with singleRcapture::controlMethod function. More information included in controlMethod().  |
| controlModel     | a list indicating additional formulas for regression (like formula for inflation parameter/dispersion parameter) may be constructed with singleRcapture::controlModel function. More information will eventually be included in controlModel().   |
| controlPopVar    | a list indicating parameters to use in estimating variance of population size estimation may be constructed with singleRcapture::controlPopVar function.  More information included in controlPopVar().   |
| modelFrame, x, y | logical values indicating whether to return model matrix, dependent vector and model matrix as a part of output.  |
| contrasts        | not yet implemented.  |
| ratioReg         | Not yet implemented   |
| offset           | a matrix of offset values with the number of columns matching the number of distribution parameters providing offset values to each of linear predictors.   |

# **Details**

The generalized linear model is characterized by equation

$$\eta = X\beta$$

where  $\boldsymbol{X}$  is the (lm) model matrix. The vector generalized linear model is similarly characterized by equations

$$\boldsymbol{\eta}_k = \boldsymbol{X}_k \boldsymbol{\beta}_k$$

where  $X_k$  is a (lm) model matrix constructed from appropriate formula (specified in controlModel parameter).

The  $\eta$  is then a vector constructed as:

$$oldsymbol{\eta} = egin{pmatrix} oldsymbol{\eta}_1 \ oldsymbol{\eta}_2 \ \ldots \ oldsymbol{\eta}_p \end{pmatrix}^T$$

and in cases of models in our package the (vlm) model matrix is constructed as a block matrix:

$$oldsymbol{X}_{vlm} = egin{pmatrix} oldsymbol{X}_1 & oldsymbol{0} & \ldots & oldsymbol{0} \ oldsymbol{0} & oldsymbol{X}_2 & \ldots & oldsymbol{0} \ dots & dots & \ddots & dots \ oldsymbol{0} & oldsymbol{0} & \ldots & oldsymbol{X}_p \end{pmatrix}$$

this differs from convention in VGAM package (if we only consider our special cases of vglm models) but this is just a convention and does not affect the model, this convention is taken because it makes fitting with IRLS (explanation of algorithm in estimatePopsizeFit()) algorithm easier. (If constraints matrixes in vglm match the ones we implicitly use the vglm model matrix differs with respect to order of kronecker multiplication of X and constraints.) In this package we use observed likelihood to fit regression models.

As mentioned above usually the population size estimation is done via:

$$\hat{N} = \sum_{k=1}^{N} \frac{I_k}{\mathbb{P}(Y_k > 0)} = \sum_{k=1}^{N_{obs}} \frac{1}{1 - \mathbb{P}(Y_k = 0)}$$

where  $I_k = I_{Y_k>0}$  are indicator variables, with value 1 if kth unit was observed at least once and 0 otherwise. The  $\mathbb{P}(Y_k>0)$  are estimated by maximum likelihood.

The following assumptions are usually present when using the method of estimation described above:

- The specified regression model is correct. This entails linear relationship between independent variables and dependent ones and dependent variable being generated by appropriate distribution.
- 2. No unobserved heterogeneity. If this assumption is broken there are some possible (admittedly imperfect) workarounds see details in singleRmodels().
- 3. The population size is constant in relevant time frame.
- 4. Depending on confidence interval construction (asymptotic) normality of  $\hat{N}$  statistic is assumed.

There are two ways of estimating variance of estimate  $\hat{N}$ , the first being "analytic" usually done by application of law of total variance to  $\hat{N}$ :

$$\operatorname{var}(\hat{N}) = \mathbb{E}\left(\operatorname{var}\left(\hat{N}|I_1,\ldots,I_n\right)\right) + \operatorname{var}\left(\mathbb{E}(\hat{N}|I_1,\ldots,I_n)\right)$$

and then by  $\delta$  method to  $\hat{N}|I_1, \dots I_N$ :

$$\mathbb{E}\left(\operatorname{var}\left(\hat{N}|I_1,\ldots,I_n\right)\right) = \left.\left(\frac{\partial(N|I_1,\ldots,I_N)}{\partial\boldsymbol{\beta}}\right)^T\operatorname{cov}\left(\boldsymbol{\beta}\right)\left(\frac{\partial(N|I_1,\ldots,I_N)}{\partial\boldsymbol{\beta}}\right)\right|_{\boldsymbol{\beta}=\hat{\boldsymbol{\beta}}}$$

and the var  $\left(\mathbb{E}(\hat{N}|I_1,\ldots,I_n)\right)$  term may be derived analytically (if we assume independence of observations) since  $\hat{N}|I_1,\ldots,I_n$  is just a constant.

In general this gives us:

$$\operatorname{var}\left(\mathbb{E}(\hat{N}|I_{1},\ldots,I_{n})\right) = \operatorname{var}\left(\sum_{k=1}^{N} \frac{I_{k}}{\mathbb{P}(Y_{k}>0)}\right)$$

$$= \sum_{k=1}^{N} \operatorname{var}\left(\frac{I_{k}}{\mathbb{P}(Y_{k}>0)}\right)$$

$$= \sum_{k=1}^{N} \frac{1}{\mathbb{P}(Y_{k}>0)^{2}} \operatorname{var}(I_{k})$$

$$= \sum_{k=1}^{N} \frac{1}{\mathbb{P}(Y_{k}>0)^{2}} \mathbb{P}(Y_{k}>0)(1 - \mathbb{P}(Y_{k}>0))$$

$$= \sum_{k=1}^{N} \frac{1}{\mathbb{P}(Y_{k}>0)}(1 - \mathbb{P}(Y_{k}>0))$$

$$\approx \sum_{k=1}^{N} \frac{I_{k}}{\mathbb{P}(Y_{k}>0)^{2}}(1 - \mathbb{P}(Y_{k}>0))$$

$$= \sum_{k=1}^{N_{obs}} \frac{1 - \mathbb{P}(Y_{k}>0)}{\mathbb{P}(Y_{k}>0)^{2}}$$

Where the approximation on 6th line appears because in 5th line we sum over all units, that includes unobserved units, since  $I_k$  are independent and  $I_k \sim b(\mathbb{P}(Y_k > 0))$  the 6th line is an unbiased estimator of the 5th line.

The other method for estimating variance is "bootstrap", but since  $N_{obs} = \sum_{k=1}^{N} I_k$  is also a random variable bootstrap will not be as simple as just drawing  $N_{obs}$  units from data with replacement and just computing  $\hat{N}$ .

Method described above is referred to in literature as "nonparametric" bootstrap (see controlPopVar()), due to ignoring variability in observed sample size it is likely to underestimate variance.

A more sophisticated bootstrap procedure may be described as follows:

1. Compute the probability distribution as:

$$rac{\hat{m{f}}_0}{\hat{N}},rac{m{f}_1}{\hat{N}},\ldots,rac{m{f}_{\max y}}{\hat{N}}$$

where  $f_n$  denotes observed marginal frequency of units being observed exactly n times.

2. Draw  $\hat{N}$  units from the distribution above (if  $\hat{N}$  is not an integer than draw  $\lfloor \hat{N} \rfloor + b(\hat{N} - \lfloor \hat{N} \rfloor)$ ), where  $|\cdot|$  is the floor function.

- 3. Truncated units with y = 0.
- 4. If there are covariates draw them from original data with replacement from uniform distribution. For example if unit drawn to new data has y=2 choose one of covariate vectors from original data that was associated with unit for which was observed 2 times.
- 5. Regress  $y_{new}$  on  $X_{vlmnew}$  and obtain  $\hat{\beta}_{new}$ , with starting point  $\hat{\beta}$  to make it slightly faster, use them to compute  $\hat{N}_{new}$ .
- 6. Repeat 2-5 unit there are at least B statistics are obtained.
- 7. Compute confidence intervals based on alpha and confType specified in controlPopVar().

To do step 1 in procedure above it is convenient to first draw binary vector of length  $\lfloor \hat{N} \rfloor + b(\hat{N} - \lfloor \hat{N} \rfloor)$  with probability  $1 - \frac{\hat{f}_0}{\hat{N}}$ , sum elements in that vector to determine the sample size and then draw sample of this size uniformly from the data.

This procedure is known in literature as "semiparametric" bootstrap it is necessary to assume that the have a correct estimate  $\hat{N}$  in order to use this type of bootstrap.

Lastly there is "paramteric" bootstrap where we assume that the probabilistic model used to obtain  $\hat{N}$  is correct the bootstrap procedure may then be described as:

- 1. Draw  $\lfloor \hat{N} \rfloor + b(\hat{N} \lfloor \hat{N} \rfloor)$  covariate information vectors with replacement from data according to probability distribution that is proportional to:  $N_k$ , where  $N_k$  is the contribution of kth unit i.e.  $\frac{1}{\mathbb{P}(Y_k > 0)}$ .
- 2. Determine  $\eta$  matrix using estimate  $\beta$ .
- 3. Generate y (dependent variable) vector using  $\eta$  and probability mass function associated with chosen model.
- 4. Truncated units with y = 0 and construct  $y_{new}$  and  $X_{vlmnew}$ .
- 5. Regress  $y_{new}$  on  $X_{vlmnew}$  and obtain  $\hat{\beta}_{new}$  use them to compute  $\hat{N}_{new}$ .
- 6. Repeat 1-5 unit there are at least B statistics are obtained.
- 7. Compute confidence intervals based on alpha and confType specified in controlPopVar()

It is also worth noting that in the "analytic" method estimatePopsize only uses "standard" covariance matrix estimation. It is possible that improper covariance matrix estimate is the only part of estimation that has its assumptions violated. In such cases post-hoc procedures are implemented in this package to address this issue.

Lastly confidence intervals for  $\hat{N}$  are computed (in analytic case) either by assuming that it follows a normal distribution or that variable  $\ln(N-\hat{N})$  follows a normal distribution.

These estimates may be found using either summary.singleRStaticCountData method or popSizeEst.singleRStaticCountData method or popSizeEst.singleRStaticCou

#### Value

Returns an object of class c("singleRStaticCountData", "singleR", "glm", "lm") with type list containing:

- y Vector of dependent variable if specified at function call.
- X Model matrix if specified at function call.
- formula A list with formula provided on call and additional formulas specified in controlModel.
- call Call matching original input.
- coefficients A vector of fitted coefficients of regression.
- control A list of control parameters for controlMethod and controlModel, controlPopVar is included in populationSize.
- model Model which estimation of population size and regression was built, object of class family.
- deviance Deviance for the model.
- priorWeights Prior weight provided on call.
- weights If IRLS method of estimation was chosen weights returned by IRLS, otherwise same as priorWeights.
- residuals Vector of raw residuals.
- logL Logarithm likelihood obtained at final iteration.
- iter Numbers of iterations performed in fitting or if stats::optim was used number of call to loglikelihood function.
- dfResiduals Residual degrees of freedom.
- dfNull Null degrees of freedom.
- fittValues Data frame of fitted values for both mu (the expected value) and lambda (Poisson parameter).
- populationSize A list containing information of population size estimate.
- modelFrame Model frame if specified at call.
- linearPredictors Vector of fitted linear predictors.
- sizeObserved Number of observations in original model frame.
- terms terms attribute of model frame used.
- contrasts contrasts specified in function call.
- naAction naAction used.
- which list indicating which observations were used in regression/population size estimation.
- fittingLog log of fitting information for "IRLS" fitting if specified in controlMethod.

# Author(s)

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#### References

General single source capture recapture literature:

Zelterman, Daniel (1988). 'Robust estimation in truncated discrete distributions with application to capture-recapture experiments'. In: Journal of statistical planning and inference 18.2, pp. 225–237.

Heijden, Peter GM van der et al. (2003). 'Point and interval estimation of the population size using the truncated Poisson regression model'. In: Statistical Modelling 3.4, pp. 305–322. doi: 10.1191/1471082X03st057oa.

Cruyff, Maarten J. L. F. and Peter G. M. van der Heijden (2008). 'Point and Interval Estimation of the Population Size Using a Zero-Truncated Negative Binomial Regression Model'. In: Biometrical Journal 50.6, pp. 1035–1050. doi: 10.1002/bimj.200810455

Böhning, Dankmar and Peter G. M. van der Heijden (2009). 'A covariate adjustment for zero-truncated approaches to estimating the size of hidden and elusive populations'. In: The Annals of Applied Statistics 3.2, pp. 595–610. doi: 10.1214/08-AOAS214.

Böhning, Dankmar, Alberto Vidal-Diez et al. (2013). 'A Generalization of Chao's Estimator for Covariate Information'. In: Biometrics 69.4, pp. 1033–1042. doi: 10.1111/biom.12082

Böhning, Dankmar and Peter G. M. van der Heijden (2019). 'The identity of the zero-truncated, one-inflated likelihood and the zero-one-truncated likelihood for general count densities with an application to drink-driving in Britain'. In: The Annals of Applied Statistics 13.2, pp. 1198–1211. doi: 10.1214/18-AOAS1232.

Navaratna WC, Del Rio Vilas VJ, Böhning D. Extending Zelterman's approach for robust estimation of population size to zero-truncated clustered Data. Biom J. 2008 Aug;50(4):584-96. doi: 10.1002/bimj.200710441.

Böhning D. On the equivalence of one-inflated zero-truncated and zero-truncated one-inflated count data likelihoods. Biom J. 2022 Aug 15. doi: 10.1002/bimj.202100343.

Böhning, D., Friedl, H. Population size estimation based upon zero-truncated, one-inflated and sparse count data. Stat Methods Appl 30, 1197–1217 (2021). doi: 10.1007/s10260-021-00556-8 Bootstrap:

Zwane, PGM EN and Van der Heijden, Implementing the parametric bootstrap in capture-recapture models with continuous covariates 2003 Statistics & probability letters 65.2 pp 121-125

Norris, James L and Pollock, Kenneth H Including model uncertainty in estimating variances in multiple capture studies 1996 in Environmental and Ecological Statistics 3.3 pp 235-244

Vector generalized linear models:

Yee, T. W. (2015). Vector Generalized Linear and Additive Models: With an Implementation in R. New York, USA: Springer. ISBN 978-1-4939-2817-0.

# See Also

stats::glm() - For more information on generalized linear models.
stats::optim() - For more information on optim function used in

stats::optim() - For more information on optim function used in optim method of fitting regression.

controlMethod() - For control parameters related to regression.

controlPopVar() – For control parameters related to population size estimation.

controlModel() - For control parameters related to model specification.

estimatePopsizeFit() - For more information on fitting procedure in esitmate\_popsize.

popSizeEst() redoPopEstimation() - For extracting population size estimation results are applying post-hoc procedures.

summary.singleRStaticCountData() – For summarizing important information about the model and population size estimation results.

marginalFreq() – For information on marginal frequencies and comparison between observed and fitted quantities.

VGAM::vglm() – For more information on vector generalized linear models.

singleRmodels() - For description of various models.

# **Examples**

```
# Model from 2003 publication
# Point and interval estimation of the
# population size using the truncated Poisson regression mode
# Heijden, Peter GM van der et al. (2003)
model <- estimatePopsize(</pre>
   formula = capture ~ gender + age + nation,
   data = netherlandsimmigrant,
   model = ztpoisson
)
summary(model)
# Graphical presentation of model fit
plot(model, "rootogram")
# Statistical test
# see documentation for summary.singleRmargin
summary(marginalFreq(model), df = 1, "group")
# We currently support 2 methods of numerical fitting
# (generalized) IRLS algorithm and via stats::optim
# the latter one is faster when fitting negative binomial models
# (and only then) due to IRLS having to numerically compute
# (expected) information matrixes, optim is also less reliable when
# using alphaFormula argument in controlModel
modelNegBin <- estimatePopsize(</pre>
    formula = TOTAL_SUB ~ .,
    data = farmsubmission,
    model = ztnegbin,
    method = "optim"
)
summary(modelNegBin)
summary(marginalFreq(modelNegBin))
# More advanced call that specifies additional formula and shows
# in depth information about fitting procedure
pseudoHurdleModel <- estimatePopsize(</pre>
    formula = capture ~ nation + age,
    data = netherlandsimmigrant,
   model = Hurdleztgeom,
    method = "IRLS",
    controlMethod = controlMethod(verbose = 5),
    controlModel = controlModel(piFormula = ~ gender)
summary(pseudoHurdleModel)
```

```
# Assessing model fit
plot(pseudoHurdleModel, "rootogram")
summary(marginalFreq(pseudoHurdleModel), "group", df = 1)
# A advanced input with additional information for fitting procedure and
# additional formula specification and different link for inflation parameter.
Model <- estimatePopsize(</pre>
formula = TOTAL_SUB ~ .,
data = farmsubmission,
model = oiztgeom(omegaLink = "cloglog"),
method = "IRLS",
 controlMethod = controlMethod(
  stepsize = .85,
  momentumFactor = 1.2,
  epsilon = 1e-10,
  silent = TRUE
),
controlModel = controlModel(omegaFormula = ~ C_TYPE + log_size)
summary(marginalFreq(Model), df = 18 - length(Model$coefficients))
summary(Model)
```

estimatePopsizeFit

Regression fitting in single-source capture-recapture models

# Description

estimatePopsizeFit does for estimatePopsize what glm.fit does for glm. It is internally called in estimatePopsize. Since estimatePopsize does much more than just regression fitting estimatePopsizeFit is much faster.

### Usage

```
estimatePopsizeFit(
  y,
  X,
  family,
  control,
  method,
  priorWeights,
  coefStart,
  etaStart,
  offset,
  ...
)
```

#### **Arguments**

y vector of dependent variables.X model matrix, the vglm one.

family same as model in estimatePopsize.

control control parameters created in controlModel.

method method of estimation same as in estimatePopsize.

priorWeights vector of prior weights its the same argument as weights in estimatePopsize.

etaStart, coefStart

initial value of regression parameters or linear predictors.

offset passed from by default passed from estimatePopsize().

... arguments to pass to other methods.

# **Details**

If method argument was set to "optim" the stats::optim function will be used to fit regression with analytically computed gradient and (minus) log likelihood functions as gr and fn arguments. Unfortunately optim does not allow for hessian to be specified. More information about how to modify optim fitting is included in controlMethod().

If method argument was set to "IRLS" the iteratively reweighted least squares. The algorithm is well know in generalised linear models. Thomas W. Yee later extended this algorithm to vector generalised linear models and in more general terms it can roughly be described as (this is Yee's description after changing some conventions):

- 1. Initialize with:
  - converged <- FALSE
  - iter <- 1
  - *β* <- start
  - $W \leftarrow$  prior
  - ℓ <- ℓ(β)</li>
- 2. If converged or iter > Maxiter move to step 7.
- 3. Store values from previous algorithm step:
  - $W_{-} \leftarrow W$
  - ℓ\_ <- ℓ</li>
  - β\_ <- β</li>

and assign values at current step:

- $\eta \leftarrow X_{vlm}\beta$
- $\bullet \ \ Z_i \mathrel{<\!\!\!\!-} \ \eta_i + \tfrac{\partial \ell_i}{\partial \eta_i} \mathbb{E} \left( \tfrac{\partial^2 \ell_i}{\partial \eta_i^T \partial \eta_i} \right)^{-1}$
- $\boldsymbol{W}_{ij} \leftarrow \mathbb{E}\left(\frac{\partial^2 \ell}{\partial \boldsymbol{\eta}_j^T \partial \boldsymbol{\eta}_i}\right)$

where  $\ell_i$  is the ith component of log likelihood function,  $\eta_i$  is the vector of linear predictors associated with ith row and  $\mathbb{E}\left(\frac{\partial^2 \ell_i}{\partial \eta_i^T \partial \eta_i}\right)$  corresponds to weights associated with ith row and

 $m{W}$  is a block matrix, made of diagonal matrixes  $\mathbb{E}\left(rac{\partial^2 \ell}{\partial m{\eta}_I^T \partial m{\eta}_i}
ight)$ 

4. Regress Z on  $X_{vlm}$  to obtain  $\beta$  as:

$$oldsymbol{eta} = \left(oldsymbol{X}_{vlm}^T oldsymbol{W} oldsymbol{X}_{vlm}
ight)^{-1} oldsymbol{X}_{vlm}^T oldsymbol{W} oldsymbol{Z}$$

- 5. Assign:
  - converged <-  $\ell(\beta) \ell_- < \varepsilon \cdot \ell_-$  or  $||\beta \beta_-||_{\infty} < \varepsilon$
  - iter <- iter + 1

where  $\varepsilon$  is the relative tolerance level, by default 1e-8.

- 6. Return to step 2.
- 7. Return  $\beta$ , W, iter.

In this package we use different conventions for  $X_{vlm}$  matrix hence slight differences are present in algorithm description but results are identical.

#### Value

List with regression parameters, working weights (if IRLS fitting method) was chosen and number of iterations taken.

### Author(s)

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#### References

Yee, T. W. (2015). Vector Generalized Linear and Additive Models: With an Implementation in R. New York, USA: Springer. ISBN 978-1-4939-2817-0.

#### See Also

```
stats::glm() estimatePopsize() controlMethod() stats::optim()
```

### **Examples**

```
summary(farmsubmission)

# construct vglm model matrix
X <- matrix(data = 0, nrow = 2 * NROW(farmsubmission), ncol = 7)
X[1:NROW(farmsubmission), 1:4] <- model.matrix(
~ 1 + log_size + log_distance + C_TYPE,
farmsubmission
)

X[-(1:NROW(farmsubmission)), 5:7] <- X[1:NROW(farmsubmission), c(1, 3, 4)]

# this attribute tells the function which elements of the design matrix
# correspond to which linear predictor
attr(X, "hwm") <- c(4, 3)</pre>
```

```
# get starting points
start <- glm.fit(</pre>
y = farmsubmission$TOTAL_SUB,
x = X[1:NROW(farmsubmission), 1:4],
family = poisson()
)$coefficients
res <- estimatePopsizeFit(</pre>
y = farmsubmission$TOTAL_SUB,
X = X,
method = "IRLS",
priorWeights = 1,
family = ztoigeom(),
control = controlMethod(verbose = 5),
coefStart = c(start, 0, 0, 0),
etaStart = matrix(X %*% c(start, 0, 0, 0), ncol = 2),
offset = cbind(rep(0, NROW(farmsubmission)), rep(0, NROW(farmsubmission)))
)
# extract results
# regression coefficient vector
res$beta
# check likelihood
11 <- ztoigeom()$makeMinusLogLike(y = farmsubmission$TOTAL_SUB, X = X)</pre>
-ll(res$beta)
# number of iterations
res$iter
# working weights
head(res$weights)
# Compare with optim call
res2 <- estimatePopsizeFit(</pre>
  y = farmsubmission$TOTAL_SUB,
  X = X,
  method = "optim",
  priorWeights = 1,
  family = ztoigeom(),
  coefStart = c(start, 0, 0, 0),
  control = controlMethod(verbose = 1, silent = TRUE),
  offset = cbind(rep(0, NROW(farmsubmission)), rep(0, NROW(farmsubmission)))
)
# extract results
# regression coefficient vector
res2$beta
```

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```
# check likelihood
-ll(res2$beta)

# number of calls to log lik function
# since optim does not return the number of
# iterations
res2$iter

# optim does not calculated working weights
head(res2$weights)
```

farmsubmission

The British farm submissions data

# **Description**

Data on British animal farms submissions to AHVLA. British farms are able to submit samples to AHVLA if cause of death for an animal cannot be determined and private veterinary surgeon decides to submit them, unless there is notifiable disease suspected then such a submission is not required.

This data set contains information about such farms. All submissions from farms are included in this data frame not only carcasses but also blood samples etc.

# Usage

```
data("farmsubmission")
```

# Format

Data frame with 12,036 rows and 4 columns.

TOTAL\_SUB Number of submissions of animal material.

log\_size Numerical value equal to logarithm of size of farm.

log\_distance Numerical value equal to logarithm of distance to nearest AHVLA center.

C\_TYPE Factor describing type of activity on farm that animals are used for. Either Dairy or Beef

# References

This data set and its description was provided in publication: Böhning, D., Vidal Diez, A., Lerdsuwansri, R., Viwatwongkasem, C., and Arnold, M. (2013). "A generalization of Chao's estimator for covariate information". *Biometrics*, 69(4), 1033-1042. doi:10.1111/biom.12082

30 marginalFreq

marginalFreq

Observed and fitted marginal frequencies

# **Description**

A function that given a fitted singleR class object computed marginal frequencies by as sum of probability density functions for each unit in data at each point i.e. kth element of marginal frequency table is given by  $\sum_{j=1}^{N_{obs}} \mathbb{P}(Y_j = k | \eta_j)$ . For k=0 only (if specified at call) they are computed as  $\hat{N} - N_{obs}$  because  $f_0$  is assumed to the unobserved part of the studied population.

These frequencies are useful in diagnostics for count data regression, such as assessment of fit.

# Usage

```
marginalFreq(
  object,
  includeones = TRUE,
  includezeros = TRUE,
  onecount = NULL,
  range,
  ...
)
```

### **Arguments**

object of singleR class.

includeones logical value indicating whether to include the estimated number of zero counts. includezeros logical value indicating whether to include one counts in the zero-one truncated

models.

one count a numeric value indicating number of one counts if null trount from object

will be assumed to be a number one counts.

range optional argument specifying range of selected Y values.

... currently does nothing.

### Value

A list with observed name of the fitted model family degrees of freedom and observed and fitted marginal frequencies.

# Author(s)

Piotr Chlebicki

#### See Also

```
estimatePopsize() - where example of usage is provided
```

netherlandsimmigrant 31

netherlandsimmigrant Immigration data in the Netherlands

# **Description**

This data set contains information about immigrants in four cities (Amsterdam, Rotterdam, The Hague and Utrecht) in Netherlands that have been staying in the country illegally in 1995 and have appeared in police records that year.

### Usage

data("netherlandsimmigrant")

#### **Format**

Data frame with 1,880 rows and 5 columns.

capture Number of times a person has been captured by police.

gender Factor describing gender of the apprehended person.

age Factor describing age of apprehended person. Either bellow or above 40 years old.

reason Factor describing reason for being apprehended by police either illegal stay in Netherlands or other reasons.

nation Factor with nation of origin of the captured person. There are 6 levels of this variable:

"American and Australia", "Asia", "North Africa", "Rest of Africa", "Surinam", "Turkey".

#### References

This data set and its description was provided in publication: van Der Heijden, P. G., Bustami, R., Cruyff, M. J., Engbersen, G., and Van Houwelingen, H. C. (2003). Point and interval estimation of the population size using the truncated Poisson regression model. *Statistical Modelling*, 3(4), 305-322. doi:10.1191/1471082X03st057oa

plot.singleRStaticCountData

Diagnostic plots for regression and population size estimation

# **Description**

Simple diagnostic plots for singleRStaticCountData class objects.

# Usage

```
## $3 method for class 'singleRStaticCountData'
plot(
    x,
    plotType = c("qq", "marginal", "fitresid", "bootHist", "rootogram", "dfpopContr",
        "dfpopBox", "scaleLoc", "cooks", "hatplot", "strata"),
    confIntStrata = c("normal", "logNormal"),
    histKernels = TRUE,
    dfpop,
    ...
)
```

# **Arguments**

Х

object of singleRStaticCountData class.

plotType

character parameter (default "qq") specifying type of plot to be made. The following list presents and briefly explains possible type of plots:

- qq The quantile-quantile plot for pearson residuals (or standardized pearson residuals if these are available for the model) i.e. empirical quantiles from residuals are plotted against theoretical quantiles from standard distribution
- marginal A plot made by matplot with fitted and observed marginal frequencies with labels.
- fitresid Plot of fitted linear predictors against (standardized) pearson residuals.
- bootHist Simple histogram for statistics obtained from bootstrapping (if one was performed and the statistics were saved).
- rootogram Rootogram, for full explanation see: Kleiber and Zeileis Visualizing Count Data Regressions Using Rootograms (2016), in short it is a barplot where height is the square root of observed marginal frequencies adjusted by difference between square root of observed and fitted marginal frequencies connected by line representing fitted marginal frequencies. The less of a difference there is between the 0 line and beginning of a bar the more accurate fitt was produced by the model.
- dfpopContr Plot of dfpopsize against unit contribution. On the plot is
  y = x line i.e. what deletion effect would be if removing the unit from the
  model didn't effect regression coefficients. The further away the observation is from this line the more influential it is.
- dfpopBox Boxplot of dfpopsize for getting the general idea about the distribution of the "influence" of each unit on population size estimate.
- scaleLoc The scale location plot i.e. square root of absolute values of (standardized) pearson residuals against linear predictors for each column of linear predictors.
- cooks Plot of cooks distance for detecting influential observations.
- hatplot Plot of hat values for each linear predictor for detecting influential observations.

• strata – Plot of confidence intervals and point estimates for strata provided in . . . argument

confIntStrata

confidence interval type to use for strata plot. Currently supported values are "normal" and "logNormal".

histKernels

logical value indicating whether to add density lines to histogram.

dfpop

TODO

... a

additional optional arguments passed to the following functions:

- For plotType = "bootHist"
  - graphics::hist with x, main, xlab, ylab parameters fixed.
- For plotType = "rootogram"
  - graphics::barplot with height, offset, ylab, xlab, ylim parameters fixed.
  - graphics::lines-withx,y,pch, type, lwd, col parameters fixed.
- For plotType = "dfpopContr"
  - dfpopsize with model, observedPop parameters fixed.
  - plot.default with x, y, xlab, main parameters fixed.
- For plotType = "dfpopBox"
  - dfpopsize with model, observedPop parameters fixed.
  - graphics::boxplot with x, ylab, main parameters fixed.
- For plotType = "scaleLoc"
  - plot.default with x, y, xlab, ylab, main, sub parameters fixed.
- For plotType = "fitresid"
  - plot.default with x, y, xlab, ylab, main, sub parameters fixed.
- For plotType = "cooks"
  - plot.default with x, xlab, ylab, main parameters fixed.
- For plotType = "hatplot"
  - hatvalues.singleRStaticCountData
  - plot.default with x, xlab, ylab, main parameters fixed.
- For plotType = "strata"
  - stratifyPopsize.singleRStaticCountData

### Value

No return value only the plot being made.

#### Author(s)

Piotr Chlebicki

# See Also

estimatePopsize() dfpopsize() marginalFreq() stats::plot.lm() stats::cooks.distance()
hatvalues.singleRStaticCountData()

popSizeEst

Extract population size estimation results

### **Description**

An extractor function with singleRStaticCountData method for extracting important information regarding pop size estimate.

# Usage

```
popSizeEst(object, ...)
## S3 method for class 'singleRStaticCountData'
popSizeEst(object, ...)
```

# **Arguments**

object object with population size estimates.
... additional optional arguments, currently not used in singleRStaticCountData

class method.

### Value

An object of class popSizeEstResults containing population size estimation results.

```
predict.singleRStaticCountData
```

Predict method for singleRStaticCountData class

# **Description**

A method for predict function, works analogous to predict.glm but gives the possibility to get standard errors of mean/distribution parameters and directly get pop size estimates for new data.

# Usage

```
## S3 method for class 'singleRStaticCountData'
predict(
  object,
  newdata,
  type = c("response", "link", "mean", "popSize", "contr"),
  se.fit = FALSE,
  na.action = NULL,
  weights,
  cov,
  ...
)
```

#### **Arguments**

object an object of singleRStaticCountData class.

newdata an optional data. frame containing new data.

type the type of prediction required, possible values are:

- "response" For matrix containing estimated distributions parameters.
- "link" For matrix of linear predictors.
- "mean" For fitted values of both Y and Y|Y>0.
- "contr" For inverse probability weights (here named for observation contribution to population size estimate).
- "popSize" For population size estimation. Note this results in a call to redoPopEstimation and it is usually better to call this function directly.

by default set to "response".

se.fit a logical value indicating whether standard errors should be computed. Only

matters for type in "response", "mean", "link".

na.action does nothing yet.

weights optional vector of weights for type in "contr", "popSize".

cov optional matrix or function or character specifying either a covariance matrix or

a function to compute that covariance matrix. By default vcov.singleRStaticCountData

can be set to e.g. vcovHC.

... arguments passed to other functions, for now this only affects vcov.singleRStaticCountData

method and cov function.

### Details

Standard errors are computed with assumption of regression coefficients being asymptotically normally distributed, if this assumption holds then each of linear predictors i.e. each row of  $\eta = X_{vlm}\beta$  is asymptotically normally distributed and their variances are expressed by well known formula. The mean  $\mu$  and distribution parameters are then differentiable functions of asymptotically normally distributed variables and therefore their variances can be computed using (multivariate) delta method.

# Value

Depending on type argument if one of "response", "link", "mean" a matrix with fitted values and possibly standard errors if se.fit argument was set to TRUE, if type was set to "contr" a vector with inverses of probabilities, finally for "popSize" an object of class popSizeEstResults with its own methods containing population size estimation results.

# See Also

redoPopEstimation() stats::summary.glm() estimatePopsize()

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redoPopEstimation

Updating population size estimation results

### **Description**

A function that applies all post-hoc procedures that were taken (such as heteroscedastic consistent covariance matrix estimation or bias reduction) to population size estimation and standard error estimation.

# Usage

```
redoPopEstimation(object, newdata, ...)
## S3 method for class 'singleRStaticCountData'
redoPopEstimation(
  object,
  newdata,
  cov,
  weights,
  coef,
  control,
  popVar,
  offset,
  weightsAsCounts,
  ...
)
```

# **Arguments**

object object for which update of population size estimation results will be done.

newdata optional data. frame with new data for pop size estimation.

... additional optional arguments, currently not used in singleRStaticCountData

class method.

cov an updated covariance matrix estimate.

weights optional vector of weights to use in population size estimation.

coef optional vector of coefficients of regression on which to base population size

estimation. If missing it is set to coef(object).

control similar to controlPopVar in estimatePopsize(). If missing set to controls

provided on call to object.

popVar similar to popVar in estimatePopsize(). If missing set to "analytic".

offset offset argument for new data

weightsAsCounts

for singleRStaticCountData method used to specify whether weights should be treated as number of occurrences for rows in data

# **Details**

Any non specified arguments will be inferred from the object

#### Value

An object of class popSizeEstResults containing updated population size estimation results.

# **Examples**

```
# Create simple model
Model <- estimatePopsize(</pre>
  formula = capture ~ nation + gender,
  data = netherlandsimmigrant,
  model = ztpoisson,
  method = "IRLS"
)
# Apply heteroscedasticity consistent covariance matrix estimation
require(sandwich)
cov <- vcovHC(Model, type = "HC3")</pre>
summary(Model, cov = cov,
popSizeEst = redoPopEstimation(Model, cov = cov))
# Compare to results with usual covariance matrix estimation
summary(Model)
## get confidence interval with larger significance level
redoPopEstimation(Model, control = controlPopVar(alpha = .000001))
```

regDiagSingleR

Regression diagnostics in singleRcapture

# Description

List of some regression diagnostics implemented for singleRStaticCountData class. Functions that either require no changes from glm class or are not relevant to context of singleRcapture are omitted.

# Usage

```
dfpopsize(model, ...)
## S3 method for class 'singleRStaticCountData'
dfpopsize(model, dfbeta = NULL, ...)
## S3 method for class 'singleRStaticCountData'
dfbeta(model, maxitNew = 1, trace = FALSE, cores = 1, ...)
## S3 method for class 'singleRStaticCountData'
hatvalues(model, ...)
```

```
## S3 method for class 'singleRStaticCountData'
residuals(
   object,
   type = c("pearson", "pearsonSTD", "response", "working", "deviance", "all"),
   ...
)

## S3 method for class 'singleRStaticCountData'
cooks.distance(model, ...)

## S3 method for class 'singleRStaticCountData'
sigma(object, ...)

## S3 method for class 'singleRStaticCountData'
influence(model, do.coef = FALSE, ...)

## S3 method for class 'singleRStaticCountData'
rstudent(model, ...)

## S3 method for class 'singleRStaticCountData'
rstudent(model, ...)
```

# **Arguments**

| model, object | an object of singleRStaticCountData class.  |
|---------------|---|
|               | arguments passed to other methods. Notably dfpopsize.singleRStaticCountData calls dfbeta.singleRStaticCountData if no dfbeta argument was provided and controlMethod is called in dfbeta method.  |
| dfbeta        | if dfbeta was already obtained it is possible to pass them into function so that they need not be computed for the second time.   |
| maxitNew      | the maximal number of iterations for regressions with starting points $\hat{\beta}$ on data specified at call for model after the removal of k'th row. By default 1.  |
| trace         | a logical value specifying whether to tracking results when cores > 1 it will result in a progress bar being created.   |
| cores         | a number of processor cores to be used, any number greater than 1 activates code designed with doParallel, foreach and parallel packages. Note that for now using parallel computing makes tracing impossible so trace parameter is ignored in this case. |
| type          | a type of residual to return.   |
| do.coef       | logical indicating if dfbeta computation for influence should be done. FALSE by default.  |

## **Details**

dfpopsize and dfbeta are closely related. dfbeta fits a regression after removing a specific row from the data and returns the difference between regression coefficients estimated on full data set

and data set obtained after deletion of that row, and repeats procedure once for every unit present in the data.dfpopsize does the same for population size estimation utilizing coefficients computed by dfbeta.

cooks.distance is implemented (for now) only for models with a single linear predictor and works exactly like the method for glm class.

sigma computes the standard errors of predicted means. Returns a matrix with two columns first for truncated mean and the other for the non-truncated mean.

residuals.singleRStaticCountData (can be abbreviated to resid) works like residuals.glm with the exception that:

- "pearson" returns non standardized residuals.
- "pearsonSTD" is currently defined only for single predictors models but will be extended to all models in a near future, but for families with more than one distribution parameter it will be a multivariate residual.
- "response" returns both residuals computed with truncated and non truncated fitted value.
- "working" is possibly multivariate if more than one linear predictor is present.
- "deviance" is not yet defined for all families in singleRmodels() e.g. negative binomial based methods.
- "all" returns all available residual types.

hatvalues.singleRStaticCountData is method for singleRStaticCountData class for extracting diagonal elements of projection matrix.

Since singleRcapture supports not only regular glm's but also vglm's the hatvalues returns a matrix with number of columns corresponding to number of linear predictors in a model, where kth column corresponds to elements of the diagonal of projection matrix associated with kth linear predictor. For glm's

$$oldsymbol{W}^{rac{1}{2}}oldsymbol{X}\left(oldsymbol{X}^Toldsymbol{W}oldsymbol{X}
ight)^{-1}oldsymbol{X}^Toldsymbol{W}^{rac{1}{2}}$$

where:  $m{W} = \mathbb{E}\left(\mathrm{Diag}\left(\frac{\partial^2 \ell}{\partial {\pmb{\eta}}^T \partial {\pmb{\eta}}}\right)\right)$  and  $m{X}$  is a model (lm) matrix. For vglm's present in the package it is instead:

$$oldsymbol{X}_{vlm} \left(oldsymbol{X}_{vlm}^T oldsymbol{W} oldsymbol{X}_{vlm}
ight)^{-1} oldsymbol{X}_{vlm}^T oldsymbol{W}$$

where:

$$oldsymbol{W} = \mathbb{E} egin{bmatrix} \operatorname{Diag} \left( rac{\partial^2 \ell}{\partial \eta_1^T \partial \eta_1} 
ight) & \operatorname{Diag} \left( rac{\partial^2 \ell}{\partial \eta_1^T \partial \eta_2} 
ight) & \ldots & \operatorname{Diag} \left( rac{\partial^2 \ell}{\partial \eta_1^T \partial \eta_p} 
ight) \\ \operatorname{Diag} \left( rac{\partial^2 \ell}{\partial \eta_2^T \partial \eta_1} 
ight) & \operatorname{Diag} \left( rac{\partial^2 \ell}{\partial \eta_2^T \partial \eta_2} 
ight) & \ldots & \operatorname{Diag} \left( rac{\partial^2 \ell}{\partial \eta_2^T \partial \eta_p} 
ight) \\ dots & dots & \ddots & dots \\ \operatorname{Diag} \left( rac{\partial^2 \ell}{\partial \eta_2^T \partial \eta_1} 
ight) & \operatorname{Diag} \left( rac{\partial^2 \ell}{\partial \eta_2^T \partial \eta_2} 
ight) & \ldots & \operatorname{Diag} \left( rac{\partial^2 \ell}{\partial \eta_2^T \partial \eta_p} 
ight) \\ \end{pmatrix}$$

is a block matrix constructed by taking the expected value from diagonal matrixes corresponding to second derivatives with respect to each linear predictor (and mixed derivatives) and  $\boldsymbol{X}_{vlm}$  is a model (vlm) matrix constructed using specifications in controlModel and call to estimatePopsize.

influence works like glm counterpart computing the most important influence measures.

#### Value

• For hatvalues – A matrix with n rows and p columns where n is a number of observations in the data and p is number of regression parameters.

- For dfpopsize A vector for which k'th element corresponds to the difference between point estimate of population size estimation on full data set and point estimate of population size estimation after the removal of k'th unit from the data set.
- For dfbeta A matrix with n rows and p observations where p is a number of units in data and p is the number of regression parameters. K'th row of this matrix corresponds to  $\hat{\beta} \hat{\beta}_{-k}$  where  $\hat{\beta}_{-k}$  is a vector of estimates for regression parameters after the removal of k'th row from the data.
- cooks.distance A matrix with a single columns with values of cooks distance for every unit in model.matrix
- residuals.singleRStaticCountData A data.frame with chosen residuals.

## Author(s)

Piotr Chlebicki, Maciej Beręsewicz

#### See Also

```
estimatePopsize() stats::hatvalues() controlMethod() stats::dfbeta() stats::cooks.distance()
```

# **Examples**

```
# For singleRStaticCountData class
# Get simple model
Model <- estimatePopsize(</pre>
 formula = capture ~ nation + age + gender,
 data = netherlandsimmigrant,
 model = ztpoisson,
 method = "IRLS"
)
# Get dfbeta
dfb <- dfbeta(Model)</pre>
# The dfpopsize results are obtained via (It is also possible to not provide
# dfbeta then they will be computed manually):
res <- dfpopsize(Model, dfbeta = dfb)</pre>
summary(res)
plot(res)
# see vaious types of residuals:
head(resid(Model, "all"))
```

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| simulate | Generating data in singleRcapture |  |
|----------|-----------------------------------|--|
|          |                                   |  |

# **Description**

An S3 method for stats::simulate to handle singleRStaticCountData and singleRfamily classes.

# **Usage**

```
## S3 method for class 'singleRStaticCountData'
simulate(object, nsim = 1, seed = NULL, ...)

## S3 method for class 'singleRfamily'
simulate(object, nsim, seed = NULL, eta, truncated = FALSE, ...)
```

# **Arguments**

object an object representing a fitted model. a numeric scalar specifying: nsim • number of response vectors to simulate in simulate.singleRStaticCountData, defaults to 1L. • number of units to draw in simulate.singleRfamily, defaults to NROW(eta). an object specifying if and how the random number generator should be initialseed ized ('seeded'). additional optional arguments. . . . a matrix of linear predictors eta logical value indicating whether to sample from truncated or full distribution. truncated

# Value

a data. frame with n rows and nsim columns.

# Author(s)

Maciej Beręsewicz, Piotr Chlebicki

# See Also

```
stats::simulate() estimatePopsize()
```

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# **Examples**

```
N <- 10000
###gender <- rbinom(N, 1, 0.2)
gender \leftarrow rep(0:1, c(8042, 1958))
eta <--1 + 0.5*gender
counts <- simulate(ztpoisson(), eta = cbind(eta), seed = 1)</pre>
df <- data.frame(gender, eta, counts)</pre>
df2 <- subset(df, counts > 0)
### check coverage with summary
mod1 <- estimatePopsize(</pre>
                = counts ~ 1 + gender,
  formula
  data
                = df2,
  model
                = ztpoisson,
  controlMethod = list(silent = TRUE)
)
mod1_sims <- simulate(mod1, nsim=10, seed = 1)</pre>
colMeans(mod1_sims)
mean(df2$counts)
```

stratifyPopsize

Estimate size of sub-populations

# **Description**

A function that estimates sizes of specific sub populations based on a capture-recapture model for the whole population.

# Usage

```
stratifyPopsize(object, strata, alpha, ...)
## S3 method for class 'singleRStaticCountData'
stratifyPopsize(object, strata, alpha, cov = NULL, ...)
```

# **Arguments**

object

an object on which the population size estimates should be based in singleRcapture package this is a fitter singleRStaticCountData class object.

strata

a specification of sub populations given by one of:

- formula a formula to be applied to model.frame extracted from the object.
- Logical vector with number of entries equal to number of rows in the dataset.
- A (named) list where each element is a logical vector, names of the list will be used to specify names variable in returned object.
- Vector of names of explanatory variables. For singleRStaticCountData method for this function this specification of strata parameter will result in every level of explanatory variable having its own sub population for each variable specified.

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• If no value was provided the singleRStaticCountData method for this function will itself create sub populations based on levels of factor variables in model.frame.

alpha significance level for confidence intervals – Either a single numeric value or a vector of length equal to number of sub populations specified in strata. If

missing it is set to .05 in singleRStaticCountData method.

a vector of arguments to be passed to other functions. For singleRStaticCountData method for this functions arguments in . . . are passed to either cov if argument

provided was a function or vcov if cov argument was missing at call.

for singleRStaticCountData method an estimate of variance-covariance matrix for estimate of regression parameters. It is possible to pass a function such as for example sandwich::vcovHC which will be called as: foo(object, ...)

and a user may specify additional arguments of a function in . . . argument. If not provided an estimate for covariance matrix will be set by calling appropriate

vcov method.

#### **Details**

cov

In single source capture-recapture models the most frequently used estimate for population size is Horvitz-Thompson type estimate:

$$\hat{N} = \sum_{k=1}^{N} \frac{I_k}{\mathbb{P}(Y_k > 0)} = \sum_{k=1}^{N_{obs}} \frac{1}{1 - \mathbb{P}(Y_k = 0)}$$

where  $I_k = I_{Y_k>0}$  are indicator variables, with value 1 if kth unit was observed at least once and 0 otherwise and the inverse probabilistic weights weights for units observed in the data  $\frac{1}{\mathbb{P}(Y_k>0)}$  are estimated using fitted linear predictors.

The estimates for different sub populations are made by changing the  $I_k = I_{Y_k>0}$  indicator variables to refer not to the population as a whole but to the sub populations that are being considered i.e. by changing values from 1 to 0 if kth unit is not a member of sub population that is being considered at the moment.

The estimation of variance for these estimates and estimation of variance for estimate of population size for the whole population follow the same relation as the one described above.

# Value

A data. frame object with row names being the names of specified sub populations either provided or inferred.

#### See Also

vcov.singleRStaticCountData() estimatePopsize()

summary.singleRmargin Statistical tests of goodness of fit

# **Description**

Performs two statistical test on observed and fitted marginal frequencies. For G test the test statistic is computed as:

$$G = 2\sum_{k} O_k \ln \left(\frac{O_k}{E_k}\right)$$

and for  $\chi^2$  the test statistic is computed as:

$$\chi^2 = \sum_k \frac{\left(O_k - E_k\right)^2}{E_k}$$

where  $O_k$ ,  $E_k$  denoted observed and fitted frequencies respectively. Both of these statistics converge to  $\chi^2$  distribution asymptotically with the same degrees of freedom.

The convergence of  $G, \chi^2$  statistics to  $\chi^2$  distribution may be violated if expected counts in cells are too low, say < 5, so it is customary to either censor or omit these cells.

# Usage

```
## S3 method for class 'singleRmargin'
summary(object, df, drop15 = c("drop", "group", "no"), ...)
```

## **Arguments**

object of singleRmargin class.

df degrees of freedom if not provided the function will try and manually but it is not always possible.

drop15 a character indicating treatment of cells with frequencies < 5 either grouping them, dropping or leaving them as is. Defaults to drop.

... currently does nothing.

# Value

A chi squared test and G test for comparison between fitted and observed marginal frequencies.

# Examples

```
# Create a simple model
Model <- estimatePopsize(
  formula = capture ~ .,
  data = netherlandsimmigrant,
  model = ztpoisson,
  method = "IRLS"</pre>
```

```
)
plot(Model, "rootogram")
# We see a considerable lack of fit
summary(marginalFreq(Model), df = 1, drop15 = "group")
```

summary.singleRStaticCountData

Summary statistics for model of singleRStaticCountData class

#### **Description**

A summary method for singleRStaticCountData class

# Usage

```
## S3 method for class 'singleRStaticCountData'
summary(
   object,
   test = c("t", "z"),
   resType = "pearson",
   correlation = FALSE,
   confint = FALSE,
   cov,
   popSizeEst,
   ...
)
```

# Arguments

| object | object of singleRStaticCountData class.   |
|--------|---|
| 00)000 | object of shighertstatic countrata class. |

test type of test for significance of parameters "t" for t-test and "z" for normal

approximation of students t distribution, by default "z" is used if there are more

than 30 degrees of freedom and "t" is used in other cases.

resType type of residuals to summarize any value that is allowed in residuals.singleRStaticCountData

except for "all" is allowed. By default pearson residuals are used.

correlation logical value indicating whether correlation matrix should be computed from

covariance matrix by default FALSE.

confint logical value indicating whether confidence intervals for regression parameters

should be constructed. By default FALSE.

cov covariance matrix corresponding to regression parameters. It is possible to give

cov argument as a function of object. If not specified it will be constructed using vcov.singleRStaticCountData method. (i.e using Cramer-Rao lower

bound)

popSizeEst a popSizeEstResults class object. If not specified population size estimation

results will be drawn from object. If any post-hoc procedures, such as sand-wich covariance matrix estimation or bias reduction, were taken it is possible to include them in population size estimation results by calling redoPopEstimation.

... additional optional arguments passed to the following functions:

- vcov.singleRStaticCountData if no cov argument was provided.
- cov if cov parameter specified at call was a function.
- confint.singleRStaticCountData if confint parameter was set to TRUE at function call. In particular it is possible to set confidence level in . . . .

#### **Details**

Works analogically to summary.glm but includes population size estimation results. If any additional statistics, such as confidence intervals for coefficients or coefficient correlation, are specified they will be printed.

# Value

An object of summarysingleRStaticCountData class containing:

- call A call which created object.
- coefficients A dataframe with estimated regression coefficients and their summary statistics such as standard error Wald test statistic and p value for Wald test.
- residuals A vector of residuals of type specified at call.
- aic Akaike's information criterion.
- bic Bayesian (Schwarz's) information criterion.
- iter Number of iterations taken in fitting regression.
- logL Logarithm of likelihood function evaluated at coefficients.
- deviance Residual deviance.
- populationSize Object with population size estimation results.
- dfResidual Residual degrees of freedom.
- sizeObserved Size of observed population.
- correlation Correlation matrix if correlation parameter was set to TRUE
- test Type of statistical test performed.
- model Family class object specified in call for object.
- skew If bootstrap sample was saved contains estimate of skewness.

#### See Also

```
redoPopEstimation() stats::summary.glm()
```

```
vcov.singleRStaticCountData
```

Obtain covariance matrix estimation

# **Description**

A vcov method for singleRStaticCountData class.

# Usage

```
## S3 method for class 'singleRStaticCountData'
vcov(object, type = c("Fisher", "observedInform"), ...)
```

# **Arguments**

object of singleRStaticCountData class.

type of estimate for covariance matrix for now either expected (Fisher) informa-

tion matrix or observed information matrix.

... additional arguments for method functions

#### **Details**

Returns a estimated covariance matrix for model coefficients calculated from analytic hessian or Fisher information matrix usually utilizing asymptotic effectiveness of maximum likelihood estimates. Covariance type is taken from control parameter that have been provided on call that created object if arguments type was not specified.

#### Value

A covariance matrix for fitted coefficients, rows and columns of which correspond to parameters returned by coef method.

# See Also

```
vcovHC.singleRStaticCountData() sandwich::sandwich()
```

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