Package: sda (via r-universe)

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Description Provides an efficient framework for high-dimensional linear and diagonal discriminant analysis with variable selection. The classifier is trained using James-Stein-type shrinkage estimators and predictor variables are ranked using correlation-adjusted t-scores (CAT scores). Variable selection error is controlled using false non-discovery rates or higher criticism.
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Description

This package performs linear discriminant analysis (LDA) and diagonal discriminant analysis (DDA) with variable selection using correlation-adjusted t (CAT) scores.

The classifier is trained using James-Stein-type shrinkage estimators. Variable selection is based on ranking predictors by CAT scores (LDA) or t-scores (DDA). A cutoff is chosen by false non-discovery rate (FNDR) or higher criticism (HC) thresholding.

This approach is particularly suited for high-dimensional classification with correlation among predictors. For details see Zuber and Strimmer (2009) and Ahdesm\"aki and Strimmer (2010).

Typically the functions in this package are applied in three steps:

- Step 1:feature selection with sda.ranking,
- Step 2:training the classifier with sda, and
- Step 3:classification using predict.sda.

The accompanying web site (see below) provides example R scripts to illustrate the functionality of this package.

Author(s)

Miika Ahdesm\"aki, Verena Zuber and Korbinian Strimmer (https://strimmerlab.github.io/)

References

Ahdesm\"aki, A., and K. Strimmer. 2010. Feature selection in omics prediction problems using cat scores and false non-discovery rate control. Ann. Appl. Stat. 4: 503-519. <DOI:10.1214/09-AOAS277>

Zuber, V., and K. Strimmer. 2009. Gene ranking and biomarker discovery under correlation. Bioinformatics 25: 2700-2707. <DOI:10.1093/bioinformatics/btp460>

See website: https://strimmerlab.github.io/software/sda/

See Also

catscore, sda.ranking, sda, predict.sda.

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Description

catscore computes CAT scores (correlation-adjusted t-scores) between the group centroids and the pooled mean.

Usage

catscore(Xtrain, L, lambda, lambda.var, lambda.freqs, diagonal=FALSE, verbose=TRUE)

Arguments

Xtrain	A matrix containing the training data set. Note that the rows correspond to observations and the columns to variables.
L	A factor with the class labels of the training samples.
lambda	Shrinkage intensity for the correlation matrix. If not specified it is estimated from the data. lambda=0 implies no shrinkage and lambda=1 complete shrinkage.
lambda.var	Shrinkage intensity for the variances. If not specified it is estimated from the data. lambda.var=0 implies no shrinkage and lambda.var=1 complete shrinkage.
lambda.freqs	Shrinkage intensity for the frequencies. If not specified it is estimated from the data. lambda.freqs=0 implies no shrinkage (i.e. empirical frequencies) and lambda.freqs=1 complete shrinkage (i.e. uniform frequencies).
diagonal	for diagonal=FALSE (the default) CAT scores are computed; otherwise with diagonal=TRUE t-scores.
verbose	Print out some info while computing.

Details

CAT scores generalize conventional t-scores to account for correlation among predictors (Zuber and Strimmer 2009). If there is no correlation then CAR scores reduce to t-scores. The squared CAR scores provide a decomposition of Hotelling's T^2 statistic.

CAT scores for two classes are described in Zuber and Strimmer (2009), for the multi-class case see Ahdesm\"aki and Strimmer (2010).

The scale factors for t-scores and CAT-scores are computed from the estimated frequencies (for empirical scale factors set lambda.freqs=0).

Value

catscore returns a matrix containing the cat score (or t-score) between each group centroid and the pooled mean for each feature.

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Author(s)

Verena Zuber, Miika Ahdesm\"aki and Korbinian Strimmer (https://strimmerlab.github.io).

References

Ahdesm\"aki, A., and K. Strimmer. 2010. Feature selection in omics prediction problems using cat scores and false non-discovery rate control. Ann. Appl. Stat. 4: 503-519. <DOI:10.1214/09-AOAS277>

Zuber, V., and K. Strimmer. 2009. Gene ranking and biomarker discovery under correlation. Bioinformatics 25: 2700-2707. <DOI:10.1093/bioinformatics/btp460>

See Also

```
sda.ranking, carscore,.
```

```
# load sda library
library("sda")
##################
# training data #
#################
# prostate cancer set
data(singh2002)
# training data
Xtrain = singh2002$x
Ytrain = singh2002$y
dim(Xtrain)
# shrinkage t-score (DDA setting - no correlation) #
tstat = catscore(Xtrain, Ytrain, diagonal=TRUE)
dim(tstat)
tstat[1:10,]
# shrinkage CAT score (LDA setting - with correlation) #
cat = catscore(Xtrain, Ytrain, diagonal=FALSE)
dim(cat)
cat[1:10,]
```

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centroids Group Centroids and (Pooled) Variances
--

Description

centroids computes group centroids, the pooled mean and pooled variance, and optionally the group specific variances.

Usage

```
centroids(x, L, lambda.var, lambda.freqs, var.groups=FALSE,
  centered.data=FALSE, verbose=TRUE)
```

Arguments

X	A matrix containing the data set. Note that the rows are sample observations and the columns are variables.
L	A factor with the group labels.
lambda.var	Shrinkage intensity for the variances. If not specified it is estimated from the data, see details below. lambda.var=0 implies no shrinkage and lambda.var=1 complete shrinkage.
lambda.freqs	Shrinkage intensity for the frequencies. If not specified it is estimated from the data. lambda.freqs=0 implies no shrinkage (i.e. empirical frequencies) and lambda.freqs=1 complete shrinkage (i.e. uniform frequencies).
var.groups	Estimate group-specific variances.

centered.data Return column-centered data matrix.

verbose Provide some messages while computing.

Details

As estimator of the variance we employ var.shrink as described in Opgen-Rhein and Strimmer (2007). For the estimates of frequencies we rely on freqs.shrink as described in Hausser and Strimmer (2009). Note that the pooled mean is computed using the estimated frequencies.

Value

centroids returns a list with the following components:

samples a vector containing the samples sizes in each group,

freqs a vector containing the estimated frequency in each group,

means the group means and the pooled mean,

variances the group-specific and the pooled variances, and

centered.data a matrix containing the centered data.

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Author(s)

```
Korbinian Strimmer (https://strimmerlab.github.io).
```

See Also

```
var.shrink, powcor.shrink.
```

Examples

```
# load sda library
library("sda")
## prepare data set
data(iris) # good old iris data
X = as.matrix(iris[,1:4])
Y = iris[,5]
## estimate centroids and empirical pooled variances
centroids(X, Y, lambda.var=0)
## also compute group-specific variances
centroids(X, Y, var.groups=TRUE, lambda.var=0)
## use shrinkage estimator for the variances
centroids(X, Y, var.groups=TRUE)
## return centered data
xc = centroids(X, Y, centered.data=TRUE)$centered.data
apply(xc, 2, mean)
## useful, e.g., to compute the inverse pooled correlation matrix
powcor.shrink(xc, alpha=-1)
```

khan2001

Childhood Cancer Study of Khan et al. (2001)

Description

Gene expression data (2308 genes for 88 samples) from the microarray study of Khan et al. (2001).

Usage

```
data(khan2001)
```

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Format

khan2001\$x is a 88 x 2308 matrix containing the expression levels. Note that rows correspond to samples, and columns to genes. The row names are the original image IDs, and the column names the original probe labels.

khan2001\$y is a factor containing the diagnosis for each sample ("BL", "EWS", "NB", "non-SRBCT", "RMS").

khan2001\$descr provides some annotation for each gene.

Details

This data set contains measurements of the gene expression of 2308 genes for 88 observations: 29 cases of Ewing sarcoma (EWS), 11 cases of Burkitt lymphoma (BL), 18 cases of neuroblastoma (NB), 25 cases of rhabdomyosarcoma (RMS), and 5 other (non-SRBCT) samples.

Source

The data are described in Khan et al. (2001). Note that the values in khan.data\$x are logarithmized (using natural log) for normalization.

References

Khan et al. 2001. Classification and diagnostic prediction of cancers using gene expression profiling and artificial neural networks. Nature Medicine 7:673–679.

```
# load sda library
library("sda")
# load full Khan et al (2001) data set
data(khan2001)
dim(khan2001$x) # 88 2308
hist(khan2001$x)
khan2001$y # 5 levels
# data set containing the SRBCT samples
get.srbct = function()
{
  data(khan2001)
  idx = which( khan2001$y == "non-SRBCT" )
  x = khan2001$x[-idx,]
  y = factor(khan2001$y[-idx])
  descr = khan2001$descr[-idx]
  list(x=x, y=y, descr=descr)
}
srbct = get.srbct()
dim(srbct$x) # 83 2308
hist(srbct$x)
```

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```
srbct$y # 4 levels
```

predict.sda

Shrinkage Discriminant Analysis 3: Prediction Step

Description

predict.sda performs class prediction.

Usage

```
## S3 method for class 'sda'
predict(object, Xtest, verbose=TRUE, ...)
```

Arguments

object An sda fit object obtained from the function sda.

Xtest A matrix containing the test data set. Note that the rows correspond to observa-

tions and the columns to variables.

verbose Report shrinkage intensities (sda) and number of used features (predict.sda).

... Additional arguments for generic predict.

Value

predict.sda predicts class probabilities for each test sample and returns a list with two components:

class a factor with the most probable class assignment for each test sample, and

posterior a matrix containing the respective class posterior probabilities.

Author(s)

Miiika Ahdesm\"aki and Korbinian Strimmer (https://strimmerlab.github.io).

See Also

```
sda, sda.ranking.
```

```
# see the examples at the "sda" help page
```

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sda	Shrinkage Discriminant Analysis 2: Training Step
sda	Shrinkage Discriminant Analysis 2: Training Step

Description

sda trains a LDA or DDA classifier using James-Stein-type shrinkage estimation.

Usage

```
sda(Xtrain, L, lambda, lambda.var, lambda.freqs, diagonal=FALSE, verbose=TRUE)
```

Arguments

Xtrain	A matrix containing the training data set. Note that the rows correspond to observations and the columns to variables.
L	A factor with the class labels of the training samples.
lambda	Shrinkage intensity for the correlation matrix. If not specified it is estimated from the data. lambda=0 implies no shrinkage and lambda=1 complete shrinkage.
lambda.var	Shrinkage intensity for the variances. If not specified it is estimated from the data. lambda.var=0 implies no shrinkage and lambda.var=1 complete shrinkage.
lambda.freqs	Shrinkage intensity for the frequencies. If not specified it is estimated from the data. lambda.freqs=0 implies no shrinkage (i.e. empirical frequencies) and lambda.freqs=1 complete shrinkage (i.e. uniform frequencies).
diagonal	Chooses between LDA (default, diagonal=FALSE) and DDA (diagonal=TRUE).
verbose	Print out some info while computing.

Details

In order to train the LDA or DDA classifier, three separate shrinkage estimators are employed:

- class frequencies: the estimator freqs.shrink from Hausser and Strimmer (2008),
- variances: the estimator var. shrink from Opgen-Rhein and Strimmer (2007),
- correlations: the estimator cor. shrink from Sch\"afer and Strimmer (2005).

Note that the three corresponding regularization parameters are obtained analytically without resorting to computer intensive resampling.

Value

sda trains the classifier and returns an sda object with the following components needed for the subsequent prediction:

regularization a vector containing the three estimated shrinkage intensities,

freqs the estimated class frequencies,

alpha vector containing the intercepts used for prediction, beta matrix containing the coefficients used for prediction. 10 sda

Author(s)

Miika Ahdesm\"aki and Korbinian Strimmer (https://strimmerlab.github.io).

References

Ahdesm\"aki, A., and K. Strimmer. 2010. Feature selection in omics prediction problems using cat scores and false non-discovery rate control. Ann. Appl. Stat. 4: 503-519. <DOI:10.1214/09-AOAS277>

See Also

predict.sda, sda.ranking, freqs.shrink, var.shrink, invcor.shrink.

```
# load sda library
library("sda")
# training and test data #
###############################
# data set containing the SRBCT samples
get.srbct = function()
 data(khan2001)
 idx = which( khan2001$y == "non-SRBCT" )
 x = khan2001$x[-idx,]
 y = factor(khan2001$y[-idx])
 descr = khan2001$descr[-idx]
 list(x=x, y=y, descr=descr)
srbct = get.srbct()
# training data
Xtrain = srbct$x[1:63,]
Ytrain = srbct$y[1:63]
Xtest = srbct$x[64:83,]
Ytest = srbct y[64:83]
# classification with correlation (shrinkage LDA) #
sda.fit = sda(Xtrain, Ytrain)
ynew = predict(sda.fit, Xtest)$class # using all 2308 features
sum(ynew != Ytest)
# classification with diagonal covariance (shrinkage DDA) #
```

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sda.ranking

Shrinkage Discriminant Analysis 1: Predictor Ranking

Description

sda.ranking determines a ranking of predictors by computing CAT scores (correlation-adjusted t-scores) between the group centroids and the pooled mean.

plot.sda.ranking provides a graphical visualization of the top ranking features.

Usage

```
sda.ranking(Xtrain, L, lambda, lambda.var, lambda.freqs,
  ranking.score=c("entropy", "avg", "max"),
  diagonal=FALSE, fdr=TRUE, plot.fdr=FALSE, verbose=TRUE)
## S3 method for class 'sda.ranking'
plot(x, top=40, arrow.col="blue", zeroaxis.col="red",
    ylab="Features", main, ...)
```

Arguments

Xtrain A matrix containing the training data set. Note that the rows correspond to

observations and the columns to variables.

L A factor with the class labels of the training samples.

lambda Shrinkage intensity for the correlation matrix. If not specified it is estimated

from the data. lambda=0 implies no shrinkage and lambda=1 complete shrink-

age.

lambda.var Shrinkage intensity for the variances. If not specified it is estimated from the

data. lambda.var=0 implies no shrinkage and lambda.var=1 complete shrink-

age.

lambda.freqs Shrinkage intensity for the frequencies. If not specified it is estimated from the

data. lambda.freqs=0 implies no shrinkage (i.e. empirical frequencies) and

lambda.freqs=1 complete shrinkage (i.e. uniform frequencies).

diagonal Chooses between LDA (default, diagonal=FALSE) and DDA (diagonal=TRUE).

ranking.score how to compute the summary score for each variable from the CAT scores of all

classes - see Details.

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fdr compute FDR values and HC scores for each feature.

plot.fdr Show plot with estimated FDR values. verbose Print out some info while computing.

x An "sda.ranking" object – this is produced by the sda.ranking() function.

top The number of top-ranking features shown in the plot (default: 40).

arrow.col Color of the arrows in the plot (default is "blue"). zeroaxis.col Color for the center zero axis (default is "red").

ylab Label written next to feature list (default is "Features").

main Main title (if missing, "The", top, "Top Ranking Features" is used).

... Other options passed on to generic plot().

Details

For each predictor variable and centroid a shrinkage CAT scores of the mean versus the pooled mean is computed. If there are only two classes the CAT score vs. the pooled mean reduces to the CAT score between the two group means. Moreover, in the diagonal case (LDA) the (shrinkage) CAT score reduces to the (shrinkage) t-score.

The overall ranking of a feature is determine by computing a summary score from the CAT scores. This is controlled by the option ranking. score. The default setting (ranking.score="entropy") uses mutual information between the response and the respective predictors (ranking.score) for ranking. This is equivalent to a weighted sum of squared CAT scores across the classes. Another possibility is to employ the average of the squared CAT scores for ranking (as suggested in Ahdesm\"aki and Strimmer 2010) by setting ranking.score="avg". A third option is to use the maximum of the squared CAT scores across groups (similarly as in the PAM algorithm) via setting ranking.score="max". Note that in the case of two classes all three options are equivalent and lead to identical scores. Thus, the choice of ranking.score is important only in the multi-class setting. In the two-class case the features are simply ranked according to the (shrinkage) squared CAT-scores (or t-scores, if there is no correlation among predictors).

The current default approach is to use ranking by mutual information (i.e. relative entropy between full model vs. model without predictor) and to use shrinkage estimators of frequencies. In order to reproduce exactly the ranking computed by previous versions (1.1.0 to 1.3.0) of the sda package set the options ranking.score="avg" and lambda.freqs=0.

Calling sda.ranking is step 1 in a classification analysis with the sda package. Steps 2 and 3 are sda and predict.sda

See Zuber and Strimmer (2009) for CAT scores in general, and Ahdesm\"aki and Strimmer (2010) for details on multi-class CAT scores. For shrinkage t scores see Opgen-Rhein and Strimmer (2007).

Value

sda.ranking returns a matrix with the following columns:

idx original feature number

score sum of the squared CAT scores across groups - this determines the overall rank-

ing of a feature

cat for each group and feature the cat score of the centroid versus the pooled mean

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If fdr=TRUE then additionally local false discovery rate (FDR) values as well as higher criticism (HC) scores are computed for each feature (using fdrtool).

Author(s)

Miika Ahdesm\"aki, Verena Zuber, Sebastian Gibb, and Korbinian Strimmer (https://strimmerlab.github.io).

References

Ahdesm\"aki, A., and K. Strimmer. 2010. Feature selection in omics prediction problems using cat scores and false non-discovery rate control. Ann. Appl. Stat. 4: 503-519. <DOI:10.1214/09-AOAS277>

Opgen-Rhein, R., and K. Strimmer. 2007. Accurate ranking of differentially expressed genes by a distribution-free shrinkage approach. Statist. Appl. Genet. Mol. Biol. 6:9. <DOI:10.2202/1544-6115.1252>

Zuber, V., and K. Strimmer. 2009. Gene ranking and biomarker discovery under correlation. Bioinformatics 25: 2700-2707. <DOI:10.1093/bioinformatics/btp460>

See Also

```
catscore, sda, predict.sda.
```

```
# load sda library
library("sda")
##################
# training data #
##############################
# prostate cancer set
data(singh2002)
# training data
Xtrain = singh2002$x
Ytrain = singh2002$y
# feature ranking (diagonal covariance) #
# ranking using t-scores (DDA)
ranking.DDA = sda.ranking(Xtrain, Ytrain, diagonal=TRUE)
ranking.DDA[1:10,]
# plot t-scores for the top 40 genes
plot(ranking.DDA, top=40)
# number of features with local FDR < 0.8
```

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```
# (i.e. features useful for prediction)
sum(ranking.DDA[,"lfdr"] < 0.8)</pre>
\# number of features with local FDR < 0.2
# (i.e. significant non-null features)
sum(ranking.DDA[,"lfdr"] < 0.2)</pre>
# optimal feature set according to HC score
plot(ranking.DDA[,"HC"], type="1")
which.max( ranking.DDA[1:1000,"HC"] )
# feature ranking (full covariance) #
# ranking using CAT-scores (LDA)
ranking.LDA = sda.ranking(Xtrain, Ytrain, diagonal=FALSE)
ranking.LDA[1:10,]
# plot t-scores for the top 40 genes
plot(ranking.LDA, top=40)
\# number of features with local FDR < 0.8
# (i.e. features useful for prediction)
sum(ranking.LDA[,"lfdr"] < 0.8)</pre>
# number of features with local FDR < 0.2
# (i.e. significant non-null features)
sum(ranking.LDA[,"lfdr"] < 0.2)</pre>
# optimal feature set according to HC score
plot(ranking.LDA[,"HC"], type="l")
which.max( ranking.LDA[1:1000,"HC"] )
```

singh2002

Prostate Cancer Study of Singh et al. (2002)

Description

Gene expression data (6033 genes for 102 samples) from the microarray study of Singh et al. (2002).

Usage

data(singh2002)

singh2002

Format

singh2002\$x is a 102 x 6033 matrix containing the expression levels. The rows contain the samples and the columns the genes.

singh2002\$y is a factor containing the diagnosis for each sample ("cancer" or "healthy").

Details

This data set contains measurements of the gene expression of 6033 genes for 102 observations: 52 prostate cancer patients and 50 healty men.

Source

The data are described in Singh et al. (2001) and are provided in exactly the form as used by Efron (2008).

References

D. Singh et al. 2002. Gene expression correlates of clinical prostate cancer behavior. Cancer Cell 1:203–209.

Efron, B. 2008. Empirical Bayes estimates for large-scale prediction problems. Technical Report, Standford University.

```
# load sda library
library("sda")

# load Singh et al (2001) data set
data(singh2002)
dim(singh2002$x) # 102 6033
hist(singh2002$x)
singh2002$y # 2 levels
```

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