Package: probout (via r-universe)

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Title Unsupervised Multivariate Outlier Probabilities for Large Datasets

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Suggests mvtnorm, GDAdata, knitr, rmarkdown

VignetteBuilder knitr

Description Estimates unsupervised outlier probabilities for multivariate numeric data with many observations from a nonparametric outlier statistic.

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```
allProb
```

Description

Outlier probabilities for all of the data, obtained by assigning to each observation the probability of the its associated leader partition.

Usage

allProb(leaderInstance, partprob)

Arguments

leaderInstance	A single component from a call to leader, giving leader algorithm results for
	one value of the partitioning radius.
partprob	A vector of probabilities for each partition in leaderInstance.

Value

A vector of probabilities for each observation in the data underlying leaderInstance. Each observation inherits the probability of its associated partition.

See Also

leader, partProb

Examples

```
set.seed(0)
lead <- leader(faithful)
nlead <- length(lead[[1]]$partitions)
# repeat multiple times to account for randomness
ntimes <- 100
probs <- matrix( NA, nlead, ntimes)
for (i in 1:ntimes) {
    probs[,i] <- partProb( simData(lead[[1]]), method = "distance")
}
# median probability for each partition
partprobs <- apply( probs, 1, median)
quantile(partprobs)
# plot leaders with outlier probability > .95
plot( faithful[,1], faithful[,2], pch = 16, cex = .5,
    main = "red : instances with outlier probability > .95")
```

leader

```
allprobs <- allProb( lead[[1]], partprobs)
out <- allprobs > .95
points( faithful[out,1], faithful[out,2], pch = 8, cex = 1, col = "red")
```

leader

Leader Algorithm for Data Partitioning

Description

Partitions the data according to Hartigan's leader algorithm, and provides ranges, centroids, and variances for the partitions.

Usage

leader(data, radius = NULL, scale = T)

Arguments

data	A numeric vector or matrix of observations. If a matrix, rows correspond to observations and columns correspond to variables.
radius	A vector of values for the partitioning radius. Wilkinson's default radius is used if radius is left unspecified (see function LWradius).
scale	A logical variable indicating whether or not the data should be mapped to the unit hypercube. The default is to scale the data. Values of the radius will not be scaled; they should be specifed relative to the unit hypercube unless $scale = F$.

Details

Given a partitioning radius r, the leader algorithm makes one pass through the data, designating an observation as a new leader if it is not within r of an existing leader, and otherwise assigning it to the partition associated with the nearest existing leader. The set of leaders typically depends on the order of the data observations.

If radius = 0, then all of the data observations are leaders, and only radius and leaders are returned as output components.

This implementation does a completely new nearest-neighbor search for each observation and for each radius. A more efficient approach would be to maintain, for each radius, a data structure (such as a kd-tree) allowing fast nearest-neighbor search. These data structures could then be updated to account for new observations. Currently, there doesn't seem to be a way to do this in R.

Value

A list with one component for each value of radius, each having the following sub-components:

radius The value of the radius associated with the partitioning.

partitions A list with one component for each partition, giving the indexes (as observations in the data) of the members of the partition. The first index is that of the associated *leader* (sometimes called *exemplar*).

leaders	The indexes of the leaders for each partition.
centroids	The centroids for each partition, as a matrix with rows corresponding to the partitions and columns corresponding to variables if multidimensional. These will be the data if radius $== 0$.
variances	The variances for each partition, as a matrix with rows corresponding to the partitions and columns corresponding to variables if multidimensional.
ranges	A list with two components: min and max giving the minimum and maximum values for each variable for each partition. These range components are given as a matrix with rows corresponding to the partitions and columns corresponding to variables if multidimensional.
maxdist	A vector with one value for each partition, giving the largest distance from each leader to any member of its partition.

References

J. A. Hartigan, Clustering Algorithms, Wiley, 1975.

L. Wilkinson, Visualizing Outliers, Technical Report, University of Illinois at Chicago, 2016. https://www.cs.uic.edu/~wilkinson/Publications/outliers.pdf

See Also

LWradius

Examples

```
radius.default <- LWradius(nrow(faithful),ncol(faithful))
lead <- leader(faithful, radius = c(0,radius.default))
# number of partitions for each radius
sapply(lead, function(x) length(x$partitions))
# plot the leaders for the non-zero radius
plot(faithful[,1], faithful[,2],
        main = "blue indicates leaders (default radius)",
        pch = 16, cex = .5)
ldrs <- lead[[2]]$leaders
points(faithful[ldrs,1], faithful[ldrs,2],
```

pch = 8, col = "dodgerblue", cex = .5)

logdens

Log Density for Gaussian Mixture Model

Description

Computes the log density for observations in a univariate or multivariate Gaussian mixture model with spherical or diagonal (co)variance that varies across components.

logdens

Usage

logdens(x, simData, shrink = 1)

Arguments

x	A numeric vector or matrix for which the log density is to be computed.
simData	Observations from a call to simData, which includes the partition centroids and variance information for the underlying simulation model.
shrink	Shrinkage parameter for the mixture model variance. To be consistent with the shrinkage as described in partProb, the variance is scaled by the <i>square</i> of shrink. The default value is shrink = 1, so that no shrinkage is applied to the variance.

Details

If either radius = 0, or simData returns only centroids (nsim = 0), then no density estimate is attempted.

Value

A vector giving the log density of x in the model as specified by simData, with optional shrinkage applied to the variance.

References

G. Celeux and G. Govaert, Gaussian Parsimonious Mixture Models, Pattern Recognition, 1995.

G. J. McLachlan and D. Peel, Finite Mixture Models, Wiley, 2000.

C. Fraley and A. E. Raftery, Model-based clustering, discriminant analysis and density estimation, *Journal of the American Statistical Association*, 2002.

See Also

partProb

Examples

```
lead <- leader(faithful)
sim <- simData( lead)</pre>
```

logdens(faithful, sim)

LWradius

Description

Wilkinson's default leader-partitioning radius.

Usage

LWradius(n, p)

Arguments

n	The number of observations (rows) in the data.
р	The number of variables (columns) in the data; p = 1 if univariate.

Value

Wilkinson's default leader partitioning radius 0.1/(log(n)^(1/p)).

References

L. Wilkinson (2016), Visualizing Outliers, Technical Report, University of Illinois at Chicago, https://www.cs.uic.edu/~wilkinson/Publications/outliers.pdf.

See Also

leader

Examples

```
x1 <- rnorm(10000)
LWradius(length(x1),1)</pre>
```

LWradius(nrow(faithful),ncol(faithful))

OutlierStatistic Nonparametric Outlier Statistic

Description

Robust nonparametric outlier statistic for univariate or multivariate data.

Usage

```
OutlierStatistic( x, nproj=1000, prior=NULL, seed=NULL)
```

OutlierStatistic

Arguments

х	A numeric vector or matrix for which the outlier statistic is to be determined.
nproj	If x is multivariate, the number of random projections to be used in computing the statistic.
prior	If x is multivariate, a prior estimate of the statistic for each observation in x, to be used as a base line for maximization relative to new random projections.
seed	An optional integer argument to set.seed for reproducible simulations. By default the current seed will be used. Reproducibility can also be achieved by calling set.seed before calling OutlierStatistic.

Value

A vector giving the maximum value of the outlier statistic for each observation over all projections.

References

W. A. Stahel, *Breakdown of Covariance Estimators*, doctoral thesis, Fachgruppe Fur Statistik, Eidgenossische Technische Hochshule (ETH), 1981.

D. L. Donoho, *Breakdown Properties of Multivariate Location Estimators*, doctoral thesis, Department of Statistics, Harvard University, 1982.

Note

Note that partition probabilities are computed from an exponential distribution fit to the outlier statistic, rather than from the empirical distribution of the outlier statistic.

See Also

partProb

Examples

```
stat <- OutlierStatistic(faithful)
q.99 <- quantile(stat,.99)
out <- stat > q.99
plot( faithful[,1], faithful[,2],
    main="red : .99 quantile for outlier statistic", cex=.5)
points( faithful[out,1], faithful[out,2],
    pch = 4, col = "red", lwd = 1, cex = .5)
require(mvtnorm)
```

```
set.seed(0)
Sigma <- crossprod(matrix(rnorm(2*2),2,2))
x <- rmvt( 10000, sigma = Sigma, df = 2)
stat <- OutlierStatistic(x)
q.95 <- quantile(stat,.95)</pre>
```

```
hist(x, main = "gray : .95 quantile for outlier statistic", col = "black")
abline( v = x[stat > q.95], col = "gray")
hist(x, col = "black", add = TRUE)
```

```
partProb
```

Partition outlier probabilities

Description

Assigns outlier probabilities to the partitions by fitting an exponential distribution to a nonparametric outlier statistic for simulated data or partition centroids.

Usage

Arguments

simData		Observations from a call to simData, which includes the partition centroids and (optionally) simulated data as well.	
method		One of the following options:	
"intrinsic" "distance" "logdensity" "distdens" "density"	: : : :	outlier statistic applied to simulation data (centroids if no simulation) outlier statistic applied to distances between NN partitions outlier statistic applied to differences in log density between NN partitions outlier statistic applied to a matrix consisting of the "distance" and "logdensity" values outlier statistic applied to smallest/largest ratios of density between NN partitions	
		The default is to use the "intrinsic" method.	
shrink		Shrinkage parameter for outlier detection data. The offsets from simData are scaled by this factor before adding them to the partition centroids as data for outlier detection. The default value is shrink = 1, so that no shrinkage is applied to simulation offsets.	
nproj		If the data is multivariate or method = "distdens", the number of random pro- jections to be used to obtain the outlier statistic.	
seed		An optional integer argument to set.seed for reproducible outlier statistics. By default the current seed will be used. Reproducibility can also be achieved by calling set.seed before calling partProb.	

Details

"logdensity" is generally prefered over "density", because negative values that are large in magniude of the logarithm of the density will not be numerically distinguishable as density values.

simData

Value

A vector of probabilities for each partition, obtained by fitting an exponential distribution to the outlier statistic.

References

C. Fraley, Estimating Outlier Probabilities for Large Datasets, 2017.

See Also

simData,OutlierStatistic,allProb

Examples

```
set.seed(0)
lead <- leader(faithful)</pre>
nlead <- length(lead[[1]]$partitions)</pre>
# repeat multiple times to account for randomness
ntimes <- 100
probs <- matrix( NA, nlead, ntimes)</pre>
for (i in 1:ntimes) {
   probs[,i] <- partProb( simData(lead[[1]]), method = "distance")</pre>
}
# median probability for each partition
partprobs <- apply( probs, 1, median)</pre>
quantile(probs)
# plot leaders with outlier probability > .95
plot( faithful[,1], faithful[,2], pch = 16, cex = .5,
       main = "red : leaders with outlier probability > .95")
out <- partprobs > .95
1 <- lead[[1]]$leaders</pre>
points( faithful[l[out],1], faithful[l[out],2], pch = 8, cex = 1, col = "red")
```

simData

Simulates observations for outlier determination.

Description

Simulates observations from a mixture model based on information on partitions from the leader function.

Usage

```
simData( leaderInstance, nsim=NULL, model=c("diagonal","spherical"), seed=NULL)
```

Arguments

leaderInstance	A single component from a call to leader, giving Leader Algorithm results for one value of the partitioning radius.
nsim	The number of observations to be simulated. Only the radius and centroids are returned of nsim = 0 or leaderInstance\$radius == 0) — no observations are simulated. Default: min(# observations,max(# partitions, 1000)).
model	For multivariate data, a vector of character strings indicating the type of Gaussian mixture model covariance to be used in generating the simulated observations (see details). For univariate data, the observations are generated from a model in which the variances may vary across components.
seed	An optional integer argument to set.seed for reproducible simulations. By default the current seed will be used. Reproducibility can also be achieved by calling set.seed before calling simData.

Details

The following models are available for multivariate data:

"spherical"	:	spherical, varying volume
"diagonal"	:	diagonal, varying volume and shape

An ellipsoidal model is also possible, but has not yet been implemented. If nsim = 0 or leaderInstance\$radius == 0, no observations are simulated, and only the radius and partition centroids are returned.

Value

A list with the following components:

radius	The value of the radius associated with leaderInstance.
location	The vector or matrix of centroids of the partitions. If a matrix, rows correspond to the partitions and columns to the variables.
index	A vector of integer values giving the index of the partition associated with each simulated observation.
offset	A vector of numeric values giving offset for the simulated observations from their associated centroids.
weight	A vector of numeric values between 0 and 1 giving the proportion of data observations in each partition.
scale	The scale (variance) of the mixture components in a univariate or spherical model. Set to 1 for each component in the diagonal model.
shape	A matrix giving the variances of the mixture component in a diagonal model. The rows correspond to the dimensions of the data, while the columns corre- spond to the mixture components (partitions).

simData

References

C. Fraley, Estimating Outlier Probabilities for Large Datasets, 2017.

See Also

leader, partProb

Examples

```
radius.default <- LWradius(nrow(faithful),ncol(faithful))
lead <- leader(faithful, radius = c(0,radius.default))
# (simulated) data for outlier statistic (no simulation for radius = 0)</pre>
```

components of simData output
lapply(sim, names)

sim <- lapply(lead, simData)</pre>

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