# Package: plaqr (via r-universe)

October 8, 2024

Title Partially Linear Additive Quantile Regression

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**Description** Estimation, prediction, thresholding, transformation, and plotting for partially linear additive quantile regression.

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bic

BIC for the Partially Linear Additive Quantile Regression Model

# **Description**

Returns the BIC for the partially linear additive quantile regression model from Lee, Noh, and Park (2014).

## Usage

```
bic(fit, ...)
```

# **Arguments**

```
fit a "plaqr" object obtained from a call to plaqr
... additional parameters which will be ignored
```

#### Value

BIC value

# Author(s)

Adam Maidman

## References

Lee, E. R., Noh, H., and Park, B. U. (2014). Model selection via bayesian information criterion for quantile regression models. Journal of the American Statistical Association 109, 216-229.

```
data(simData)
ss <- vector("list", 2)
ss[[2]]$degree <- 3
fit1 <- plaqr(y~., nonlinVars=~z1+z2, data=simData, splinesettings=ss)
ss[[2]]$degree <- 4
fit2 <- plaqr(y~., nonlinVars=~z1+z2, data=simData, splinesettings=ss)
ss[[2]]$degree <- 5
fit3 <- plaqr(y~., nonlinVars=~z1+z2, data=simData, splinesettings=ss)
bic(fit1)
bic(fit2)
bic(fit3)</pre>
```

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nonlinEffect

Nonlinear Effects Plots

## **Description**

Returns an object of class "plaqreffect" which represents the effect plot(s) of the nonlinear term(s) of a "plaqr" object from the plaqr function. A "plaqreffect" object should be plotted using the plot function.

## Usage

```
nonlinEffect(fit, select=NULL, renames=NULL)
```

## **Arguments**

fit a "plaqr" object.

select a character vector with entries matching nonlinear terms in fit.

renames a character vector with length equal to the number of nonlinear terms in select

(if select is NULL, the length must be equal to the number of nonlinear terms in fit). The first entry renames the first nonlinear term for plotting purposes, and so on. Note that select can reorder the nonlinear terms (see the examples).

# Value

A returned "plaqreffect" object to be used with the "plot" function. Each nonlinear term is associated with a list containing information for plotting. See the examples for accessing the list.

## Author(s)

Adam Maidman

```
data(simData)
fit <- plaqr(y~.,~z1+z2,data=simData)

eff1 <- nonlinEffect(fit)
eff1
plot(eff1)

eff2 <- nonlinEffect(fit, select=c("z1","z2"), renames=c("Length", "Height"))
eff2
plot(eff2)

eff3 <- nonlinEffect(fit, select=c("z2","z1"), renames=c("Height", "Length"))
eff3
eff3$z1
eff3$z2</pre>
```

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```
plot(eff3)
par(mfrow=c(1,2))
plot(eff3)
```

plagr

Partially Linear Additive Quantile Regression

## **Description**

Returns an object of class "plaqr" and "rq" that represents a quantile regression fit. A nonlinear term z is transformed using bs(z) before fitting the model. The formula of the model (as it appears in R) becomes  $y^{-}x1 + x2 + bs(z1) + bs(z2)$  where bs(z1) is a B-spline.

## Usage

#### **Arguments**

formula	a formula object	, with the response	on the left of a ~ c	perator, and the linear
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terms, separated by + operators, on the right. Any terms on the right of the  $\sim$  operator that also appear in nonlinVars will be included in the model as spline

terms, not linear terms.

nonlinVars a one-sided formula object, with a ~ operator to the left of the nonlinear terms

seperated by + operators. A term appearing in both formula and nonlinVars will be treated as a nonlinear term. If nonlinVars is not NULL, then an intercept will automatically be included in the model (despite a -1 or 0 term included in

formula).

tau the quantile to be estimated, this is a number strictly between 0 and 1 (for now).

data a data frame in which to interpret the variables named in the formula, or in the

subset and the weights argument. If this is missing, then the variables in the formula should be on the search list. This may also be a single number to handle

some special cases – see below for details.

subset an optional vector specifying a subset of observations to be used in the fitting

process.

weights vector of observation weights; if supplied, the algorithm fits to minimize the sum

of the weights multiplied into the absolute residuals. The length of weights must be the same as the number of observations. The weights must be nonnegative and it is strongly recommended that they be strictly positive, since zero weights

are ambiguous.

na.action a function to filter missing data. This is applied to the model.frame after any

subset argument has been used. The default (with na.fail) is to create an error if any missing values are found. A possible alternative is na.omit, which deletes

observations that contain one or more missing values.

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model if TRUE then the model frame is returned. This is essential if one wants to call

summary subsequently.

method the algorithmic method used to compute the fit. There are several options: The

default method is the modified version of the Barrodale and Roberts algorithm for  $l_1$ -regression, used by l1fit in S, and is described in detail in Koenker and d'Orey(1987, 1994), default = "br". This is quite efficient for problems up to several thousand observations, and may be used to compute the full quantile regression process. It also implements a scheme for computing confidence intervals for the estimated parameters, based on inversion of a rank test described in Koenker(1994). For larger problems it is advantagous to use the Frisch–Newton interior point method "fn". And very large problems one can use the Frisch–Newton approach after preprocessing "pfn". Both of the latter methods are described in detail in Portnoy and Koenker(1997). There is a fifth option "fnc" that enables the user to specify linear inequality constraints on the fitted coefficients; in this case one needs to specify the matrix R and the vector r representing the constraints in the form  $Rb \geq r$ . See the examples. Finally, there are two penalized methods: "lasso" and "scad" that implement the lasso penalty and Fan and Li's smoothly clipped absolute deviation penalty, respectively. These

methods should probably be regarded as experimental.

contrasts a list giving contrasts for some or all of the factors default = NULL appearing in

the model formula. The elements of the list should have the same name as the variable and should be either a contrast matrix (specifically, any full-rank matrix with as many rows as there are levels in the factor), or else a function to compute

such a matrix given the number of levels.

splinesettings a list of length equal to the number of nonlinear effects containing arguments to

pass to the bs function for each term. Each element of the list is either NULL or a list with named elements correpsonding to the arguments in bs. If not NULL, the first element of splinesettings corresponds to the first nonlinear effect and so on.

additional arguments for the fitting routines (see the rq function in the 'quantreg'

package).

#### Value

Returns the following:

coefficients Coefficients from the fitted model

x optionally the model matrix, if x=TRUE.

y optionally the response, if y=TRUE.

residuals the residuals from the fit.

dual the vector dual variables from the fit.

fitted.values fitted values from the fit.

formula the formula that was used in the rq function.

rho the value of the objective function at the solution.

model optionally the model frame, if model=TRUE

linear the linear terms used in the model fit.

nonlinear the nonlinear terms used in the model fit.

z the values of the nonlinear terms.

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## Author(s)

Adam Maidman

#### References

Hastie, T. J. (1992) Generalized additive models. Chapter 7 of Statistical Models in S eds J. M. Chambers and T. J. Hastie, Wadsworth & Brooks/Cole.

Koenker, R. W. (2005). Quantile Regression, Cambridge U. Press.

Sherwood, B. and Wang, L. (2016). Partially linear additive quantile regression in ultra-high dimension. The Annals of Statistics 44, 288-317.

Maidman, A., Wang, L. (2017). New Semiparametric Method for Predicting High-Cost Patients. Preprint.

# **Examples**

```
data(simData)
ss <- vector("list", 2)
ss[[2]]$degree <- 5
ss[[2]]$Boundary.knots <- c(-1, 1)
plaqr(y~., nonlinVars=~z1+z2, data=simData)
#same as plaqr(formula= y~x1+x2+x3, nonlinVars=~z1+z2, data=simData)
plaqr(y~0, nonlinVars=~z1+z2, data=simData, splinesettings=ss) #no linear terms in the model
plaqr(y~., data=simData) #all linear terms</pre>
```

plot.plaqreffect Nonlinear Effect Plot for a Partially Linear Additive Quantile Regression Model

# Description

Makes nonlinear effect plots for the nonlinear effects in a fit returned from the nonlinEffect function. Note: you cannot use this function to plot a "plaqr" object.

## Usage

```
## S3 method for class 'plaqreffect'
plot(x, select=NULL, rug = TRUE, jit = TRUE, titles = NULL, pages = 0, type="1", ...)
```

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# **Arguments**

x	a plaqreffect object returned from nonlinEffect.
select	vector of indices of nonlinear terms in x to be plotted, by default all.
rug	if TRUE, a rugplot for the x-coordinate is plotted.
jit	if TRUE, the x-values of the rug plot are jittered.
titles	$title(s) \ as \ vector \ of \ character \ strings, \ by \ default \ titles \ are \ chosen \ for \ each \ plot \ as \\ "Effect \ of \ CovariateName \ (tau=tau)".$
pages	number of pages desired for the plots.
type	the type of plot that should be drawn.
	additional arguments for the plotting algorithm.

# Author(s)

Adam Maidman

# **Examples**

```
data(simData)
fit <- plaqr(y~.,~z1+z2,data=simData)
eff <- nonlinEffect(fit, select=c("z1","z2"), renames=c("Length", "Height"))
eff

plot(eff)
plot(eff, select=1, col="red")
plot(eff, select=c(2,1), titles=c("Effect Z1","Effect Z2"))
plot(eff, select=1, col="red", lwd=4)

par(mfrow=c(1,2))
plot(eff)</pre>
```

predictInt

Prediction Inteval for Quantile Regression

# Description

Predicts future values using the median and finds a prediction interval for future values using an upper and lower quantile. The lower quantile is (1-level)/2 and the upper quantile is .5 + level/2.

# Usage

```
predictInt(fit, level=.95, newdata=NULL, ...)
```

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# **Arguments**

fit a fitted model of class "plaqr" or "rq" to be used for prediction.

level the prediction level required. The lower quantile is (1-level)/2 and the upper

quantile is .5 + level/2.

newdata an optional data frame in which to look for variables with which to predict. If

omitted, the fitted values are used.

... additional argument(s) for methods.

#### Value

a matrix with columns giving the predicted median and lower and upper prediction bounds.

# Author(s)

Adam Maidman

# **Examples**

```
data(simData)
fit <- plaqr(y~.,~z1+z2,data=simData)
predictInt(fit, level=.95)</pre>
```

print.plagreffect

Print a plagreffect object

# **Description**

Print an object generated by nonlinEffect.

# Usage

```
## S3 method for class 'plaqreffect' print(x, ...)
```

# **Arguments**

x an object returned from nonlinEffect.

... optional arguments.

# Author(s)

Adam Maidman

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print.thresh

Print a thresh Object

# Description

Print an object generated by threshold.

# Usage

```
## S3 method for class 'thresh'
print(x,...)
```

# **Arguments**

x an object returned from threshold.

... optional arguments.

## Author(s)

Adam Maidman

simData

Simulated Data

# Description

A simulated data set to illustrate the functions in this package.

```
set.seed(4)
x1 <- rbinom(100, 1,.5)
x2 <- rnorm(100)
x3 <- rnorm(100)
z1 <- runif(100, 0, 1)
z2 <- runif(100, -1, 1)
y <- 3*x1 +1.5*x2 + 2*x3 + 5*sin(2*pi*z1) + 5*z2^3 + rnorm(100)
simData <- data.frame(y,x1,x2,x3,z1,z2)</pre>
```

# Usage

```
data(simData)
```

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#### **Format**

A data frame with 100 observations on the following 6 variables.

y response: expenditure

**x1** male/female (a linear term)

x2 distance north/south from center (a linear term)

x3 distance east/west from center (a linear term)

**z1** income/(max income) (a nonlinear term)

**z2** spending habits on a -1 to 1 scale (frugal to lavish) (a nonlinear term)

threshold

Classifying a Numerical Response Using a Threshold

#### **Description**

Classification of a numerical response into a "high" class and "low" class using a threshold. This function can be used with any model that has a numerical outcome and allows for prediction using the predict function.

## Usage

```
threshold(fit, t, newdata=NULL, ...)
```

# Arguments

fit any model with a numerical response.

t the desired threshold value. All values above t will be labeled "1" and all values

below t will be labeled "0".

newdata an optional data frame in which to look for variables with which to predict. If

omitted, no prediction is done.

... additional argument(s) for methods in the predict function.

#### Value

pred.class if newdata is not NULL, then pred.class is a vector of predicted classes for

newdata. If newdata is NULL, then pred.class is NULL.

t the threshold.

train.class a vector of the predicted classes of the data used in fit.

true.class a vector of the true classes of the data used in fit.

train.error a scalar equal to the mean(train.class!= true.class).

true.high the number of observations in class"1" using the data used in fit.

true.low the number of observations in class "1" using the data used in fit.

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false.high the number of observations truly in class "0", but predicted to be in class "1"

using the data used in fit.

false.low the number of observations truly in class "1", but predicted to be in class "1"

using the data used in fit.

call the call of fit.

formula the formula used in fit.

#### Author(s)

Adam Maidman

# **Examples**

```
data(simData)
fit <- plaqr(y~.,~z1+z2,data=simData)
testdata <- .5*simData[4,2:6]
trh <- threshold(fit, t=9, newdata=testdata)
trh$pred.class
trh</pre>
```

transform\_plaqr

Transformation for Partially Linear Additive Quantile Regression

## **Description**

Returns the estimated transformation parameter for the one-parameter symmetric transformation (Geraci and Jones, 2015). Confidence intervals for the transformation parameter can also be created using the bootstrap. The response variable must be strictly positive; a constant can be added to the variable to ensure that all values are positive.

# Usage

## **Arguments**

formula a formula object, with the response on the left of a ~ operator, and the linear

terms, separated by + operators, on the right. Any terms on the right of the  $\sim$  operator that also appear in nonlinVars will be included in the model as spline

terms, not linear terms.

nonlinVars a one-sided formula object, with a ~ operator to the left of the nonlinear terms

seperated by + operators. A term appearing in both formula and nonlinVars will be treated as a nonlinear term. If nonlinVars is not NULL, then an intercept will automatically be included in the model (despite a -1 or 0 term included in

formula).

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tau the quantile to be estimated, this is a number strictly between 0 and 1 (for now).

data a data.frame in which to interpret the variables named in the formula, or in the subset and the weights argument. If this is missing, then the variables in the formula should be on the search list. This may also be a single number to handle

some special cases – see below for details.

lambda a real-valued sequence of possible transformation parameters. 0 corresponds to the log transformation and 1 corresponds to the identity. The transformation is symmetric so a negative transformation parameter is redundant and can be avoided. See Geraci and Jones (2015) for more information on the one-

parameter, symmetric transformation.

confint a confint confidence interval for the transformation parameter will be created if confint is a number between 0 and 1 (otherwise automatically creates 95% CI). Otherwise, no confidence interval will be created. The bootstrap is used to

create the confidence interval.

the number of bootstrap replications for the confidence interval. If no confidence

interval is being created, this argument is ignored.

subset an optional vector specifying a subset of observations to be used in the fitting

process.

vector of observation weights; if supplied, the algorithm fits to minimize the sum of the weights multiplied into the absolute residuals. The length of weights must be the same as the number of observations. The weights must be nonnegative and it is strongly recommended that they be strictly positive, since zero weights

are ambiguous.

a function to filter missing data. This is applied to the model.frame after any subset argument has been used. The default (with na.fail) is to create an error if any missing values are found. A possible alternative is na. omit, which deletes

observations that contain one or more missing values.

the algorithmic method used to compute the fit. There are several options: The default method is the modified version of the Barrodale and Roberts algorithm for  $l_1$ -regression, used by 11fit in S, and is described in detail in Koenker and

d'Orey(1987, 1994), default = "br". This is quite efficient for problems up to several thousand observations, and may be used to compute the full quantile regression process. It also implements a scheme for computing confidence intervals for the estimated parameters, based on inversion of a rank test described in Koenker(1994). For larger problems it is advantagous to use the Frisch–Newton interior point method "fn". And very large problems one can use the Frisch-Newton approach after preprocessing "pfn". Both of the latter methods are described in detail in Portnoy and Koenker (1997). There is a fifth option "fnc" that enables the user to specify linear inequality constraints on the fitted coefficients; in this case one needs to specify the matrix R and the vector r representing the constraints in the form  $Rb \geq r$ . See the examples. Finally, there are two penalized methods: "lasso" and "scad" that implement the lasso penalty and

Fan and Li's smoothly clipped absolute deviation penalty, respectively. These methods should probably be regarded as experimental.

a list giving contrasts for some or all of the factors default = NULL appearing in the model formula. The elements of the list should have the same name as the

В

weights

na.action

method

contrasts

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> variable and should be either a contrast matrix (specifically, any full-rank matrix with as many rows as there are levels in the factor), or else a function to compute such a matrix given the number of levels.

splinesettings a list of length equal to the number of nonlinear effects containing arguments to pass to the bs function for each term. Each element of the list is either NULL or a list with named elements correpsonding to the arguments in bs. If not NULL, the first element of splinesettings corresponds to the first nonlinear effect and so on.

#### Value

# Returns the following:

parameter	The transformation parameter
Υ	The values of the transformed response
confint	If a confidence interval is created, this is the confidence interval for the transformation parameter. Otherwise, NULL.
U	If a confidence interval is created, a B by n matrix containing the indices used in each bootstrap sample. Otherwise, NULL.
P	If a confidence interval is created, a B length vector containing the transformation parameter estimated in each bootstrap sample. Otherwise, NULL.

## Author(s)

Adam Maidman

## References

Geraci, M. and Jones, M. (2015). Improved transformation-based quantile regression. Canadian Journal of Statistics 43, 118-132.

Maidman, A., Wang, L. (2017). New Semiparametric Method for Predicting High-Cost Patients. Preprint.

```
data(simData)
simData$Y <- exp(simData$y)</pre>
transform_plaqr(Y~x1+x2+x3, nonlinVars=~z1+z2, data=simData)
transform_plaqr(Y~x1+x2+x3, nonlinVars=~z1+z2, confint=.95, data=simData)
```

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Transformation of the Response Variable

## **Description**

Transform the response variable using the one-paremter, symmetric transformation of Geraci and Jones (2015).

## Usage

```
trans_parameter(x, parameter, inverse=FALSE)
```

## **Arguments**

x a vector of values to be transformed (the response variable)

parameter a real-valued transformation parameter. 0 corresponds to the log transforma-

tion and 1 corresponds to the identity. See Geraci and Jones (2015) for more

information on the one-parameter, symmetric transformation.

inverse If TRUE, the inverse transformation is done to transform the variable back to

the original scale. If FALSE, the standard transformation is computed.

#### Value

Returns a vector of the transformed (or back-transformed) variable.

## Author(s)

Adam Maidman

## References

Geraci, M. and Jones, M. (2015). Improved transformation-based quantile regression. Canadian Journal of Statistics 43, 118-132.

Maidman, A., Wang, L. (2017). New Semiparametric Method for Predicting High-Cost Patients. Preprint.

```
data(simData)
simData$Y <- exp(simData$y)

tparam <- transform_plaqr(Y~x1+x2+x3, nonlinVars=~z1+z2, data=simData)
simData$newy <- trans_parameter(simData$Y, tparam$parameter)

fit <- plaqr(newy~x1+x2+x3, nonlinVars=~z1+z2, data=simData)
trans_parameter( predictInt(fit), tparam$parameter, inverse=TRUE)</pre>
```

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