

Package: pgdraw (via r-universe)

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Type Package

Title Generate Random Samples from the Polya-Gamma Distribution

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Description Generates random samples from the Polya-Gamma distribution using an implementation of the algorithm described in J. Windle's PhD thesis (2013) <<https://repositories.lib.utexas.edu/bitstream/handle/2152/21842/WINDLE-DISSERTATION-2013.pdf>>. The underlying implementation is in C.

License GPL (>= 3)

Imports Rcpp (>= 0.12.16)

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pgdraw-package

The pgdraw package

Description

This package contains a function to generate random samples from the Polya-Gamma distribution using an implementation of the algorithm described in J. Windle's PhD thesis. A frequent application of this distribution is in Bayesian analysis of logistic regression models.

Details

The underlying implementation is in C.

For usage, see the examples in `pgdraw` and `pgdraw.moments`.

Note

To cite this package please reference:

Makalic, E. & Schmidt, D. F. High-Dimensional Bayesian Regularised Regression with the BayesReg Package arXiv:1611.06649 [stat.CO], 2016 <https://arxiv.org/pdf/1611.06649.pdf>

A MATLAB-compatible implementation of the sampler in this package can be obtained from:

http://dschmidt.org/?page_id=189

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References

Jesse Bennett Windle Forecasting High-Dimensional, Time-Varying Variance-Covariance Matrices with High-Frequency Data and Sampling Polya-Gamma Random Variates for Posterior Distributions Derived from Logistic Likelihoods PhD Thesis, 2013

Bayesian Inference for Logistic Models Using Polya-Gamma Latent Variables Nicholas G. Polson, James G. Scott and Jesse Windle Journal of the American Statistical Association Vol. 108, No. 504, pp. 1339–1349, 2013

Chung, Y.: Simulation of truncated gamma variables Korean Journal of Computational & Applied Mathematics, 1998, 5, 601-610

See Also

`pgdraw`, `pgdraw.moments`

pgdraw	<i>Generate random samples from the Polya-Gamma distribution, PG(b,c)</i>
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Description

Generate random samples from the Polya-Gamma distribution

Usage

```
pgdraw(b, c)
```

Arguments

- | | |
|---|--|
| b | Either a single integer scalar, or a vector of integers, corresponding to the 'b' parameter for the PG(b,c) distribution. If b is a scalar, then the same value is paired with every value in c; if b is a vector then it must be of the same length as the c parameter. |
| c | A vector of real numbers corresponding to the 'c' parameter for the PG(b,c) distribution. |

Value

A vector of samples from the Polya-Gamma distribution, one for each entry of c

Details

This code generates random variates from the Polya-Gamma distribution with desired 'b' and 'c' parameters. The underlying code is written in C and is an implementation of the algorithm described in J. Windle's PhD thesis.

The main application of the Polya-Gamma distribution is in Bayesian analysis as it allows for a data augmentation (via a scale mixture of normals) approach for representation of the logistic regression likelihood (see Example 2 below).

Note

To cite this package please reference:

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References

Jesse Bennett Windle Forecasting High-Dimensional, Time-Varying Variance-Covariance Matrices with High-Frequency Data and Sampling Polya-Gamma Random Variates for Posterior Distributions Derived from Logistic Likelihoods, PhD Thesis, 2013

Bayesian Inference for Logistic Models Using Polya-Gamma Latent Variables Nicholas G. Polson, James G. Scott and Jesse Windle, Journal of the American Statistical Association Vol. 108, No. 504, pp. 1339–1349, 2013

Chung, Y.: Simulation of truncated gamma variables, Korean Journal of Computational & Applied Mathematics, 1998, 5, 601-610

See Also

[pgdraw.moments](#)

Examples

```
# -----
# Example 1: Simulated vs exact moments
u = matrix(1,1e6,1)
x = pgdraw(1,0.5*u)
mean(x)
var(x)
pgdraw.moments(1,0.5)

x = pgdraw(2,2*u)
mean(x)
var(x)
pgdraw.moments(2,2)

# -----
# Example 2: Simple logistic regression
# Sample from the following Bayesian hierarchy:
#  $y_i \sim \text{Be}(1/(1+\exp(-b)))$ 
#  $b \sim \text{uniform on R (improper)}$ 
#
# which is equivalent to
#  $y_i - 1/2 \sim N(b, 1/\omega_{2_i})$ 
#  $\omega_{2_i} \sim \text{PG}(1,0)$ 
#  $b \sim \text{uniform on R}$ 
#
sample_simple_logreg <- function(y, nsamples)
{
  n = length(y)
  omega2 = matrix(1,n,1) # Polya-Gamma latent variables
  beta = matrix(0,nsamples,1)

  for (i in 1:nsamples)
  {
    # Sample 'beta'
    s = sum(omega2)
```

```
m = sum(y-1/2)/s
beta[i] = rnorm(1, m, sqrt(1/s))
# Sample P-G L.Vs
omega2 = pgdraw(1, matrix(1,n,1)*beta[i])
}
return(beta)
}

# 3 heads, 7 tails; ML estimate of p = 3/10 = 0.3
y = c(1,1,1,0,0,0,0,0,0,0)

# Sample
b = sample_simple_logreg(y, 1e4)
hist(x=b)

# one way of estimating of 'p' from posterior samples
1/(1+exp(-mean(b)))
```

pgdraw.moments	<i>Compute exact first and second moments for the Polya-Gamma distribution, PG(b, c)</i>
----------------	--

Description

Compute exact first and second moments for the Polya-Gamma distribution

Usage

```
pgdraw.moments(b, c)
```

Arguments

b	The 'b' parameter of the Polya-Gamma distribution.
c	The 'c' parameter of the Polya-Gamma distribution.

Value

A list containing the mean and variance.

Details

This code computes the exact mean and variance of the Polya-Gamma distribution for the specified parameters.

References

Jesse Bennett Windle Forecasting High-Dimensional, Time-Varying Variance-Covariance Matrices with High-Frequency Data and Sampling Polya-Gamma Random Variates for Posterior Distributions Derived from Logistic Likelihoods PhD Thesis, 2013

Bayesian Inference for Logistic Models Using Polya-Gamma Latent Variables Nicholas G. Polson, James G. Scott and Jesse Windle Journal of the American Statistical Association Vol. 108, No. 504, pp. 1339–1349, 2013

See Also

[pgdraw](#)

Examples

```
# -----  
# Example: Simulated vs exact moments  
  
u = matrix(1,1e6,1)  
x = pgdraw(1,0.5*u)  
mean(x)  
var(x)  
pgdraw.moments(1,0.5)  
  
x = pgdraw(2,2*u)  
mean(x)  
var(x)  
pgdraw.moments(2,2)
```

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