

# Package: pense (via r-universe)

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**Type** Package

**Title** Penalized Elastic Net S/MM-Estimator of Regression

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<https://github.com/dakep/pense-rpkg>

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**Description** Robust penalized (adaptive) elastic net S and M estimators for linear regression. The methods are proposed in Cohen Freue, G. V., Kepplinger, D., Salibián-Barrera, M., and Smucler, E. (2019) <<https://projecteuclid.org/euclid.aoas/1574910036>>. The package implements the extensions and algorithms described in Kepplinger, D. (2020) <[doi:10.14288/1.0392915](https://doi.org/10.14288/1.0392915)>.

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**License** MIT + file LICENSE

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cd\_algorithm\_options    *Coordinate Descent (CD) Algorithm to Compute Penalized Elastic Net S-estimates*

---

### Description

Set options for the CD algorithm to compute adaptive EN S-estimates.

### Usage

```
cd_algorithm_options(  
  max_it = 1000,  
  reset_it = 8,  
  linesearch_steps = 4,  
  linesearch_mult = 0.5  
)
```

### Arguments

`max_it`            maximum number of iterations.

`reset_it`        number of iterations after which the residuals are re-computed from scratch, to prevent numerical drifts from incremental updates.

`linesearch_steps`            maximum number of steps used for line search.

`linesearch_mult`            multiplier to adjust the step size in the line search.

### Value

options for the CD algorithm to compute (adaptive) PENSE estimates.

### See Also

`mm_algorithm_options` to optimize the non-convex PENSE objective function via a sequence of convex problems.

---

 coef.pense\_cvfit      *Extract Coefficient Estimates*


---

### Description

Extract coefficients from an adaptive PENSE (or LS-EN) regularization path with hyper-parameters chosen by cross-validation.

### Usage

```
## S3 method for class 'pense_cvfit'
coef(
  object,
  alpha = NULL,
  lambda = "min",
  se_mult = 1,
  sparse = NULL,
  standardized = FALSE,
  exact = deprecated(),
  correction = deprecated(),
  ...
)
```

### Arguments

object	PENSE with cross-validated hyper-parameters to extract coefficients from.
alpha	Either a single number or NULL (default). If given, only fits with the given alpha value are considered. If lambda is a numeric value and object was fit with multiple <i>alpha</i> values and no value is provided, the first value in object\$alpha is used with a warning.
lambda	either a string specifying which penalty level to use ("min", "se", "{m}-se") or a single numeric value of the penalty parameter. See details.
se_mult	If lambda = "se", the multiple of standard errors to tolerate.
sparse	should coefficients be returned as sparse or dense vectors? Defaults to the sparsity setting of the given object. Can also be set to sparse = 'matrix', in which case a sparse matrix is returned instead of a sparse vector.
standardized	return the standardized coefficients.
exact, correction	defunct.
...	currently not used.

### Value

either a numeric vector or a sparse vector of type `dsparseVector` of size  $p + 1$ , depending on the sparse argument. Note: prior to version 2.0.0 sparse coefficients were returned as sparse matrix of type `dgCMatrix`. To get a sparse matrix as in previous versions, use sparse = 'matrix'.

### Hyper-parameters

If `lambda = "{m}-se"` and `object` contains fitted estimates for every penalization level in the sequence, use the fit the most parsimonious model with prediction performance statistically indistinguishable from the best model. This is determined to be the model with prediction performance within  $m * cv\_se$  from the best model. If `lambda = "se"`, the multiplier  $m$  is taken from `se_mult`.

By default all *alpha* hyper-parameters available in the fitted object are considered. This can be overridden by supplying one or multiple values in parameter `alpha`. For example, if `lambda = "1-se"` and `alpha` contains two values, the "1-SE" rule is applied individually for each `alpha` value, and the fit with the better prediction error is considered.

In case `lambda` is a number and `object` was fit for several *alpha* hyper-parameters, `alpha` must also be given, or the first value in `object$alpha` is used with a warning.

### See Also

Other functions for extracting components: [coef.pense\\_fit\(\)](#), [predict.pense\\_cvfit\(\)](#), [predict.pense\\_fit\(\)](#), [residuals.pense\\_cvfit\(\)](#), [residuals.pense\\_fit\(\)](#)

### Examples

```
# Compute the PENSE regularization path for Freeny's revenue data
# (see ?freeny)
data(freeny)
x <- as.matrix(freeny[, 2:5])

regpath <- pense(x, freeny$y, alpha = 0.5)
plot(regpath)

# Extract the coefficients at a certain penalization level
coef(regpath, lambda = regpath$lambda[[1]][[40]])

# What penalization level leads to good prediction performance?
set.seed(123)
cv_results <- pense_cv(x, freeny$y, alpha = 0.5,
                      cv_repl = 2, cv_k = 4)
plot(cv_results, se_mult = 1)

# Extract the coefficients at the penalization level with
# smallest prediction error ...
coef(cv_results)
# ... or at the penalization level with prediction error
# statistically indistinguishable from the minimum.
coef(cv_results, lambda = '1-se')
```

**Description**

Extract coefficients from an adaptive PENSE (or LS-EN) regularization path fitted by [pense\(\)](#) or [elnet\(\)](#).

**Usage**

```
## S3 method for class 'pense_fit'
coef(
  object,
  lambda,
  alpha = NULL,
  sparse = NULL,
  standardized = FALSE,
  exact = deprecated(),
  correction = deprecated(),
  ...
)
```

**Arguments**

object	PENSE regularization path to extract coefficients from.
lambda	a single number for the penalty level.
alpha	Either a single number or NULL (default). If given, only fits with the given alpha value are considered. If object was fit with multiple alpha values, and no value is provided, the first value in object\$alpha is used with a warning.
sparse	should coefficients be returned as sparse or dense vectors? Defaults to the sparsity setting in object. Can also be set to sparse = 'matrix', in which case a sparse matrix is returned instead of a sparse vector.
standardized	return the standardized coefficients.
exact, correction	defunct.
...	currently not used.

**Value**

either a numeric vector or a sparse vector of type [dsparseVector](#) of size  $p + 1$ , depending on the sparse argument. Note: prior to version 2.0.0 sparse coefficients were returned as sparse matrix of type *dgCMatrix*. To get a sparse matrix as in previous versions, use sparse = 'matrix'.

**See Also**

[coef.pense\\_cvfit\(\)](#) for extracting coefficients from a PENSE fit with hyper-parameters chosen by cross-validation

Other functions for extracting components: [coef.pense\\_cvfit\(\)](#), [predict.pense\\_cvfit\(\)](#), [predict.pense\\_fit\(\)](#), [residuals.pense\\_cvfit\(\)](#), [residuals.pense\\_fit\(\)](#)

**Examples**

```

# Compute the PENSE regularization path for Freeny's revenue data
# (see ?freeny)
data(freeny)
x <- as.matrix(freeny[, 2:5])

regpath <- pense(x, freeny$y, alpha = 0.5)
plot(regpath)

# Extract the coefficients at a certain penalization level
coef(regpath, lambda = regpath$lambda[[1]][[40]])

# What penalization level leads to good prediction performance?
set.seed(123)
cv_results <- pense_cv(x, freeny$y, alpha = 0.5,
                      cv_repl = 2, cv_k = 4)
plot(cv_results, se_mult = 1)

# Extract the coefficients at the penalization level with
# smallest prediction error ...
coef(cv_results)
# ... or at the penalization level with prediction error
# statistically indistinguishable from the minimum.
coef(cv_results, lambda = '1-se')
```

---

consistency\_const      *Get the Constant for Consistency for the M-Scale*

---

**Description**

Get the Constant for Consistency for the M-Scale

**Usage**

```
consistency_const(delta, rho)
```

**Arguments**

delta	desired breakdown point (between 0 and 0.5)
rho	the name of the chosen $\rho$ function.

**Value**

consistency constant

**See Also**

Other miscellaneous functions: [rho\\_function\(\)](#)

---

deprecated\_en\_options *Deprecated*

---

## Description

### [Deprecated]

Options for computing EN estimates.

## Usage

```
en_options_aug_lars(use_gram = c("auto", "yes", "no"), eps = 1e-12)
```

```
en_options_dal(
  maxit = 100,
  eps = 1e-08,
  eta_mult = 2,
  eta_start_numerator = 0.01,
  eta_start,
  preconditioner = c("approx", "none", "diagonal"),
  verbosity = 0
)
```

## Arguments

use_gram	<b>ignored.</b> Should the Gram matrix be pre-computed.
eps	<b>ignored.</b> Numeric tolerance for convergence.
maxit	maximum number of iterations allowed.
eta_mult	multiplier to increase eta at each iteration.
eta_start_numerator	if eta_start is missing, it is defined by eta_start = eta_start_numerator / lambda.
eta_start	<b>ignored.</b> The start value for eta.
preconditioner	<b>ignored.</b> Preconditioner for the numerical solver. If none, a standard solver will be used, otherwise the faster preconditioned conjugate gradient is used.
verbosity	<b>ignored.</b>

## Functions

- en\_options\_aug\_lars(): Superseded by [en\\_lars\\_options\(\)](#).
- en\_options\_dal(): Superseded by [en\\_dal\\_options\(\)](#)

## Warning

Do not use these functions in new code. They may be removed from future versions of the package.



**See Also**

Other deprecated functions: [enpy\(\)](#), [initest\\_options\(\)](#), [mstep\\_options\(\)](#), [pense\\_options\(\)](#), [pensem\(\)](#)

---

 elnet

---

*Compute the Least Squares (Adaptive) Elastic Net Regularization Path*


---

**Description**

Compute least squares EN estimates for linear regression with optional observation weights and penalty loadings.

**Usage**

```
elnet(
  x,
  y,
  alpha,
  nlambda = 100,
  lambda_min_ratio,
  lambda,
  penalty_loadings,
  weights,
  intercept = TRUE,
  en_algorithm_opts,
  sparse = FALSE,
  eps = 1e-06,
  standardize = TRUE,
  correction = deprecated(),
  xtest = deprecated(),
  options = deprecated()
)
```

**Arguments**

<code>x</code>	n by p matrix of numeric predictors.
<code>y</code>	vector of response values of length n. For binary classification, y should be a factor with 2 levels.
<code>alpha</code>	elastic net penalty mixing parameter with $0 \leq \alpha \leq 1$ . <code>alpha = 1</code> is the LASSO penalty, and <code>alpha = 0</code> the Ridge penalty. Can be a vector of several values, but <code>alpha = 0</code> cannot be mixed with other values.
<code>nlambda</code>	number of penalization levels.
<code>lambda_min_ratio</code>	Smallest value of the penalization level as a fraction of the largest level (i.e., the smallest value for which all coefficients are zero). The default depends on

	the sample size relative to the number of variables and alpha. If more observations than variables are available, the default is $1e-3 * \alpha$ , otherwise $1e-2 * \alpha$ .
lambda	optional user-supplied sequence of penalization levels. If given and not NULL, nlambda and lambda_min_ratio are ignored.
penalty_loadings	a vector of positive penalty loadings (a.k.a. weights) for different penalization of each coefficient.
weights	a vector of positive observation weights.
intercept	include an intercept in the model.
en_algorithm_opts	options for the EN algorithm. See <a href="#">en_algorithm_options</a> for details.
sparse	use sparse coefficient vectors.
eps	numerical tolerance.
standardize	standardize variables to have unit variance. Coefficients are always returned in original scale.
correction	defunct. Correction for EN estimates is not supported anymore.
xtest	defunct.
options	deprecated. Use en_algorithm_opts instead.

### Details

The elastic net estimator for the linear regression model solves the optimization problem

$$\operatorname{argmin}_{\mu, \beta} (1/2n) \sum_i w_i (y_i - \mu - x_i' \beta)^2 + \lambda \sum_j 0.5(1 - \alpha) \beta_j^2 + \alpha l_j |\beta_j|$$

with observation weights  $w_i$  and penalty loadings  $l_j$ .

### Value

a list-like object with the following items

alpha the sequence of alpha parameters.

lambda a list of sequences of penalization levels, one per alpha parameter.

estimates a list of estimates. Each estimate contains the following information:

intercept intercept estimate.

beta beta (slope) estimate.

lambda penalization level at which the estimate is computed.

alpha *alpha* hyper-parameter at which the estimate is computed.

statuscode if  $> 0$  the algorithm experienced issues when computing the estimate.

status optional status message from the algorithm.

call the original call.

**See Also**

[pense\(\)](#) for an S-estimate of regression with elastic net penalty.

[coef.pense\\_fit\(\)](#) for extracting coefficient estimates.

[plot.pense\\_fit\(\)](#) for plotting the regularization path.

Other functions for computing non-robust estimates: [elnet\\_cv\(\)](#)

**Examples**

```
# Compute the LS-EN regularization path for Freeny's revenue data
# (see ?freeny)
data(freeny)
x <- as.matrix(freeny[, 2:5])

regpath <- elnet(x, freeny$y, alpha = c(0.5, 0.75))
plot(regpath)
plot(regpath, alpha = 0.75)

# Extract the coefficients at a certain penalization level
coef(regpath, lambda = regpath$lambda[[1]][[5]],
      alpha = 0.75)

# What penalization level leads to good prediction performance?
set.seed(123)
cv_results <- elnet_cv(x, freeny$y, alpha = c(0.5, 0.75),
                      cv_repl = 10, cv_k = 4,
                      cv_measure = "tau")
plot(cv_results, se_mult = 1.5)
plot(cv_results, se_mult = 1.5, what = "coef.path")

# Extract the coefficients at the penalization level with
# smallest prediction error ...
summary(cv_results)
coef(cv_results)
# ... or at the penalization level with prediction error
# statistically indistinguishable from the minimum.
summary(cv_results, lambda = "1.5-se")
coef(cv_results, lambda = "1.5-se")
```

**Description**

Perform (repeated) K-fold cross-validation for [elnet\(\)](#).

**Usage**

```

elnet_cv(
  x,
  y,
  lambda,
  cv_k,
  cv_repl = 1,
  cv_metric = c("rmspe", "tau_size", "mape", "auroc"),
  fit_all = TRUE,
  cl = NULL,
  ncores = deprecated(),
  ...
)

```

**Arguments**

<code>x</code>	n by p matrix of numeric predictors.
<code>y</code>	vector of response values of length n. For binary classification, y should be a factor with 2 levels.
<code>lambda</code>	optional user-supplied sequence of penalization levels. If given and not NULL, <code>nlambda</code> and <code>lambda_min_ratio</code> are ignored.
<code>cv_k</code>	number of folds per cross-validation.
<code>cv_repl</code>	number of cross-validation replications.
<code>cv_metric</code>	either a string specifying the performance metric to use, or a function to evaluate prediction errors in a single CV replication. If a function, the number of arguments define the data the function receives. If the function takes a single argument, it is called with a single numeric vector of prediction errors. If the function takes two or more arguments, it is called with the predicted values as first argument and the true values as second argument. The function must always return a single numeric value quantifying the prediction performance. The order of the given values corresponds to the order in the input data.
<code>fit_all</code>	If TRUE, fit the model for all penalization levels. Can also be any combination of "min" and "{x}-se", in which case only models at the penalization level with smallest average CV accuracy, or within {x} standard errors, respectively. Setting <code>fit_all</code> to FALSE is equivalent to "min". Applies to all alpha value.
<code>cl</code>	a <a href="#">parallel</a> cluster. Can only be used in combination with <code>ncores = 1</code> .
<code>ncores</code>	deprecated and not used anymore.
<code>...</code>	Arguments passed on to <a href="#">elnet</a>
	<code>alpha</code> elastic net penalty mixing parameter with $0 \leq \alpha \leq 1$ . <code>alpha = 1</code> is the LASSO penalty, and <code>alpha = 0</code> the Ridge penalty. Can be a vector of several values, but <code>alpha = 0</code> cannot be mixed with other values.
	<code>nlambda</code> number of penalization levels.
	<code>lambda_min_ratio</code> Smallest value of the penalization level as a fraction of the largest level (i.e., the smallest value for which all coefficients are zero). The default depends on the sample size relative to the number of variables and

alpha. If more observations than variables are available, the default is  $1e-3 * \alpha$ , otherwise  $1e-2 * \alpha$ .

penalty\_loadings a vector of positive penalty loadings (a.k.a. weights) for different penalization of each coefficient.

standardize standardize variables to have unit variance. Coefficients are always returned in original scale.

weights a vector of positive observation weights.

intercept include an intercept in the model.

sparse use sparse coefficient vectors.

en\_algorithm\_opts options for the EN algorithm. See [en\\_algorithm\\_options](#) for details.

eps numerical tolerance.

xtest defunct.

options deprecated. Use en\_algorithm\_opts instead.

correction defunct. Correction for EN estimates is not supported anymore.

## Details

The built-in CV metrics are

"tau\_size"  $\tau$ -size of the prediction error, computed by [tau\\_size\(\)](#) (default).

"mape" Median absolute prediction error.

"rmspe" Root mean squared prediction error.

"auroc" Area under the receiver operator characteristic curve (actually 1 - AUROC). Only sensible for binary responses.

## Value

a list-like object with the same components as returned by [elnet\(\)](#), plus the following:

cvres data frame of average cross-validated performance.

## See Also

[elnet\(\)](#) for computing the LS-EN regularization path without cross-validation.

[pense\\_cv\(\)](#) for cross-validation of S-estimates of regression with elastic net penalty.

[coef.pense\\_cvfit\(\)](#) for extracting coefficient estimates.

[plot.pense\\_cvfit\(\)](#) for plotting the CV performance or the regularization path.

Other functions for computing non-robust estimates: [elnet\(\)](#)

## Examples

```
# Compute the LS-EN regularization path for Freeny's revenue data
# (see ?freeny)
data(freeny)
x <- as.matrix(freeny[, 2:5])
```

```

regpath <- elnet(x, freeny$y, alpha = c(0.5, 0.75))
plot(regpath)
plot(regpath, alpha = 0.75)

# Extract the coefficients at a certain penalization level
coef(regpath, lambda = regpath$lambda[[1]][[5]],
      alpha = 0.75)

# What penalization level leads to good prediction performance?
set.seed(123)
cv_results <- elnet_cv(x, freeny$y, alpha = c(0.5, 0.75),
                      cv_repl = 10, cv_k = 4,
                      cv_measure = "tau")
plot(cv_results, se_mult = 1.5)
plot(cv_results, se_mult = 1.5, what = "coef.path")

# Extract the coefficients at the penalization level with
# smallest prediction error ...
summary(cv_results)
coef(cv_results)
# ... or at the penalization level with prediction error
# statistically indistinguishable from the minimum.
summary(cv_results, lambda = "1.5-se")
coef(cv_results, lambda = "1.5-se")

```

---

enpy

*Deprecated*


---

## Description

### [Deprecated]

Compute initial estimates for EN S-estimates using ENPY. Superseded by [enpy\\_initial\\_estimates\(\)](#).

## Usage

```
enpy(x, y, alpha, lambda, delta, cc, options, en_options)
```

## Arguments

x	data matrix with predictors.
y	response vector.
alpha, lambda	EN penalty parameters (NOT adjusted for the number of observations in x).
delta	desired breakdown point of the resulting estimator.
cc	tuning constant for the S-estimator. Default is to chosen based on the breakdown point delta. Should never have to be changed.
options	<b>ignored.</b> Additional options for the initial estimator.
en_options	<b>ignored.</b> Additional options for the EN algorithm.

**Value**

coeff	A numeric matrix with one initial coefficient per column
objF	A vector of values of the objective function for the respective coefficient

**Warning**

Do not use this function in new code. It may be removed from future versions of the package.

**See Also**

Other deprecated functions: [deprecated\\_en\\_options](#), [initest\\_options\(\)](#), [mstep\\_options\(\)](#), [pense\\_options\(\)](#), [pensem\(\)](#)

---

enpy\_initial\_estimates

*ENPY Initial Estimates for EN S-Estimators*


---

**Description**

Compute initial estimates for the EN S-estimator using the EN-PY procedure.

**Usage**

```
enpy_initial_estimates(
  x,
  y,
  alpha,
  lambda,
  bdp = 0.25,
  cc,
  intercept = TRUE,
  penalty_loadings,
  enpy_opts = enpy_options(),
  mscale_opts = mscale_algorithm_options(),
  eps = 1e-06,
  sparse = FALSE,
  ncores = 1L
)
```

**Arguments**

x	n by p matrix of numeric predictors.
y	vector of response values of length n.
alpha	elastic net penalty mixing parameter with $0 \leq \alpha \leq 1$ . alpha = 1 is the LASSO penalty, and alpha = 0 the Ridge penalty. Can be a vector of several values, but alpha = 0 cannot be mixed with other values.

lambda	a vector of positive values of penalization levels.
bdp	desired breakdown point of the estimator, between 0.05 and 0.5. The actual breakdown point may be slightly larger/smaller to avoid instabilities of the S-loss.
cc	cutoff value for the bisquare rho function. By default, chosen to yield a consistent estimate for the Normal distribution.
intercept	include an intercept in the model.
penalty_loadings	a vector of positive penalty loadings (a.k.a. weights) for different penalization of each coefficient. Only allowed for alpha > 0.
enpy_opts	options for the EN-PY algorithm, created with the <a href="#">enpy_options()</a> function.
m-scale_opts	options for the M-scale estimation. See <a href="#">mscale_algorithm_options()</a> for details.
eps	numerical tolerance.
sparse	use sparse coefficient vectors.
ncores	number of CPU cores to use in parallel. By default, only one CPU core is used. Not supported on all platforms, in which case a warning is given.

### Details

If these manually computed initial estimates are intended as starting points for [pense\(\)](#), they are by default *shared* for all penalization levels. To restrict the use of the initial estimates to the penalty level they were computed for, use `as_starting_point(..., specific = TRUE)`. See [as\\_starting\\_point\(\)](#) for details.

### References

Cohen Freue, G.V.; Kepplinger, D.; Salibián-Barrera, M.; Smucler, E. Robust elastic net estimators for variable selection and identification of proteomic biomarkers. *Ann. Appl. Stat.* **13** (2019), no. 4, 2065–2090 [doi:10.1214/19AOAS1269](https://doi.org/10.1214/19AOAS1269)

### See Also

Other functions for initial estimates: [prinsens\(\)](#), [starting\\_point\(\)](#)

---

enpy\_options

*Options for the ENPY Algorithm*


---

### Description

Additional control options for the elastic net Peña-Yohai procedure.



**Usage**

```

enpy_options(
  max_it = 10,
  keep_psc_proportion = 0.5,
  en_algorithm_opts,
  keep_residuals_measure = c("threshold", "proportion"),
  keep_residuals_proportion = 0.5,
  keep_residuals_threshold = 2,
  retain_best_factor = 2,
  retain_max = 500
)

```

**Arguments**

`max_it` maximum number of EN-PY iterations.

`keep_psc_proportion` how many observations should to keep based on the Principal Sensitivity Components.

`en_algorithm_opts` options for the LS-EN algorithm. See [en\\_algorithm\\_options](#) for details.

`keep_residuals_measure` how to determine what observations to keep, based on their residuals. If `proportion`, a fixed number of observations is kept. If `threshold`, only observations with residuals below the threshold are kept.

`keep_residuals_proportion` proportion of observations to kept based on their residuals.

`keep_residuals_threshold` only observations with (standardized) residuals less than this threshold are kept.

`retain_best_factor` only keep candidates that are within this factor of the best candidate. If  $\leq 1$ , only keep candidates from the last iteration.

`retain_max` maximum number of candidates, i.e., only the best `retain_max` candidates are retained.

**Details**

The EN-PY procedure for computing initial estimates iteratively cleans the data of observations with possibly outlying residual or high leverage. Least-squares elastic net (LS-EN) estimates are computed on the possibly clean subsets. At each iteration, the Principal Sensitivity Components are computed to remove observations with potentially high leverage. Among all the LS-EN estimates, the estimate with smallest M-scale of the residuals is selected. Observations with largest residual for the selected estimate are removed and the next iteration is started.

**Value**

options for the ENPY algorithm.

---

en\_admm\_options      *Use the ADMM Elastic Net Algorithm*

---

### Description

Use the ADMM Elastic Net Algorithm

### Usage

```
en_admm_options(max_it = 1000, step_size, acceleration = 1)
```

### Arguments

max\_it            maximum number of iterations.  
step\_size        step size for the algorithm.  
acceleration    acceleration factor for linearized ADMM.

### Value

options for the ADMM EN algorithm.

### See Also

Other EN algorithms: [en\\_cd\\_options\(\)](#), [en\\_dal\\_options\(\)](#), [en\\_lars\\_options\(\)](#)

---

en\_algorithm\_options    *Control the Algorithm to Compute (Weighted) Least-Squares Elastic Net Estimates*

---

### Description

The package supports different algorithms to compute the EN estimate for weighted LS loss functions. Each algorithm has certain characteristics that make it useful for some problems. To select a specific algorithm and adjust the options, use any of the `en_***_options` functions.

### Details

- [en\\_lars\\_options\(\)](#): Use the tuning-free LARS algorithm. This computes *exact* (up to numerical errors) solutions to the EN-LS problem. It is not iterative and therefore can not benefit from approximate solutions, but in turn guarantees that a solution will be found.
- [en\\_cd\\_options\(\)](#): Use an iterative coordinate descent algorithm which needs  $O(np)$  operations per iteration and converges sub-linearly.
- [en\\_admm\\_options\(\)](#): Use an iterative ADMM-type algorithm which needs  $O(np)$  operations per iteration and converges sub-linearly.
- [en\\_dal\\_options\(\)](#): Use the iterative Dual Augmented Lagrangian (DAL) method. DAL needs  $O(n^3p^2)$  operations per iteration, but converges exponentially.

---

en_cd_options	<i>Use Coordinate Descent to Solve Elastic Net Problems</i>
---------------	---

---

**Description**

Use Coordinate Descent to Solve Elastic Net Problems

**Usage**

```
en_cd_options(max_it = 1000, reset_it = 8)
```

**Arguments**

max_it	maximum number of iterations.
reset_it	number of iterations after which the residuals are re-computed from scratch, to prevent numerical drifts from incremental updates.

**See Also**

Other EN algorithms: [en\\_admm\\_options\(\)](#), [en\\_dal\\_options\(\)](#), [en\\_lars\\_options\(\)](#)

---

en_dal_options	<i>Use the DAL Elastic Net Algorithm</i>
----------------	--

---

**Description**

Use the DAL Elastic Net Algorithm

**Usage**

```
en_dal_options(  
  max_it = 100,  
  max_inner_it = 100,  
  eta_multiplier = 2,  
  eta_start_conservative = 0.01,  
  eta_start_aggressive = 1,  
  lambda_relchange_aggressive = 0.25  
)
```

**Arguments**

max_it	maximum number of (outer) iterations.
max_inner_it	maximum number of (inner) iterations in each outer iteration.
eta_multiplier	multiplier for the barrier parameter. In each iteration, the barrier must be more restrictive (i.e., the multiplier must be $> 1$ ).
eta_start_conservative	conservative initial barrier parameter. This is used if the previous penalty is undefined or too far away.
eta_start_aggressive	aggressive initial barrier parameter. This is used if the previous penalty is close.
lambda_relchange_aggressive	how close must the lambda parameter from the previous penalty term be to use an aggressive initial barrier parameter (i.e., what constitutes "too far").

**Value**

options for the DAL EN algorithm.

**See Also**

Other EN algorithms: [en\\_admm\\_options\(\)](#), [en\\_cd\\_options\(\)](#), [en\\_lars\\_options\(\)](#)

---

en\_lars\_options      *Use the LARS Elastic Net Algorithm*

---

**Description**

Use the LARS Elastic Net Algorithm

**Usage**

```
en_lars_options()
```

**See Also**

Other EN algorithms: [en\\_admm\\_options\(\)](#), [en\\_cd\\_options\(\)](#), [en\\_dal\\_options\(\)](#)

---

initest\_options      *Deprecated*

---

## Description

### [Deprecated]

Options for computing initial estimates via ENPY. Superseded by [enpy\\_options\(\)](#).

## Usage

```
initest_options(
  keep_solutions = 5,
  psc_method = c("exact", "rr"),
  maxit = 10,
  maxit_pense_refinement = 5,
  eps = 1e-06,
  psc_keep = 0.5,
  resid_keep_method = c("proportion", "threshold"),
  resid_keep_prop = 0.6,
  resid_keep_thresh = 2,
  mscale_eps = 1e-08,
  mscale_maxit = 200
)
```

## Arguments

`keep_solutions` how many initial estimates should be kept to perform full PENSE iterations?

`psc_method` The method to use for computing the principal sensitivity components. See details for the possible choices.

`maxit` maximum number of refinement iterations.

`maxit_pense_refinement`  
**ignored.** Maximum number of PENSE iterations to refine initial estimator.

`eps` **ignored.** Numeric tolerance for convergence.

`psc_keep` proportion of observations to keep based on the PSC scores.

`resid_keep_method`  
How to clean the data based on large residuals. If "proportion", observations with the smallest `resid_keep_prop` residuals will be retained. If "threshold", all observations with scaled residuals smaller than the threshold `resid_keep_thresh` will be retained.

`resid_keep_prop, resid_keep_thresh`  
proportion or threshold for observations to keep based on their residual.

`mscale_eps, mscale_maxit`  
**ignored.** Maximum number of iterations and numeric tolerance for the M-scale.

**Warning**

Do not use this function in new code. It may be removed from future versions of the package.

**See Also**

Other deprecated functions: [deprecated\\_en\\_options](#), [enpy\(\)](#), [mstep\\_options\(\)](#), [pense\\_options\(\)](#), [pensem\(\)](#)

---

 mloc

---

*Compute the M-estimate of Location*


---

**Description**

Compute the M-estimate of location using an auxiliary estimate of the scale.

**Usage**

```
mloc(x, scale, rho, cc, opts = mscale_algorithm_options())
```

**Arguments**

x	numeric values. Missing values are verbosely ignored.
scale	scale of the x values. If omitted, uses the <a href="#">mad()</a> .
rho	the $\rho$ function to use. See <a href="#">rho_function()</a> for available functions.
cc	value of the tuning constant for the chosen $\rho$ function. By default, chosen to achieve 95% efficiency under the Normal distribution.
opts	a list of options for the M-estimating algorithm, see <a href="#">mscale_algorithm_options()</a> for details.

**Value**

a single numeric value, the M-estimate of location.

**See Also**

Other functions to compute robust estimates of location and scale: [mlocscale\(\)](#), [mscale\(\)](#), [tau\\_size\(\)](#)

---

mlocscale	<i>Compute the M-estimate of Location and Scale</i>
-----------	---

---

### Description

Simultaneous estimation of the location and scale by means of M-estimates.

### Usage

```
mlocscale(  
  x,  
  bdp = 0.25,  
  scale_cc = consistency_const(bdp, "bisquare"),  
  location_rho,  
  location_cc,  
  opts = mscale_algorithm_options()  
)
```

### Arguments

x	numeric values. Missing values are verbosely ignored.
bdp	desired breakdown point (between 0 and 0.5).
scale_cc	cutoff value for the bisquare $\rho$ function for computing the scale estimate. By default, chosen to yield a consistent estimate for normally distributed values.
location_rho, location_cc	$\rho$ function and cutoff value for computing the location estimate. See <a href="#">rho_function()</a> for a list of available $\rho$ functions.
opts	a list of options for the M-estimating equation, see <a href="#">mscale_algorithm_options()</a> for details.

### Value

a vector with 2 elements, the M-estimate of location and the M-scale estimate.

### See Also

Other functions to compute robust estimates of location and scale: [mloc\(\)](#), [mscale\(\)](#), [tau\\_size\(\)](#)

---

mm\_algorithm\_options *MM-Algorithm to Compute Penalized Elastic Net S- and M-Estimates*

---

### Description

Additional options for the MM algorithm to compute EN S- and M-estimates.

### Usage

```
mm_algorithm_options(
  max_it = 500,
  tightening = c("adaptive", "exponential", "none"),
  tightening_steps = 2,
  en_algorithm_opts
)
```

### Arguments

`max_it` maximum number of iterations.

`tightening` how to make inner iterations more precise as the algorithm approaches a local minimum.

`tightening_steps` for *adaptive* tightening strategy, how often to tighten until the desired tolerance is attained.

`en_algorithm_opts` options for the inner LS-EN algorithm. See [en\\_algorithm\\_options](#) for details.

### Value

options for the MM algorithm.

### See Also

`cd_algorithm_options` for a direct optimization of the non-convex PENSE loss.

---

mscale *Compute the M-Scale of Centered Values*

---

### Description

Compute the M-scale without centering the values.



**Usage**

```

mscale(
  x,
  bdp = 0.25,
  cc = consistency_const(bdp, "bisquare"),
  opts = mscale_algorithm_options(),
  delta = deprecated(),
  rho = deprecated(),
  eps = deprecated(),
  maxit = deprecated()
)

```

**Arguments**

<code>x</code>	numeric values. Missing values are verbosely ignored.
<code>bdp</code>	desired breakdown point (between 0 and 0.5).
<code>cc</code>	cutoff value for the bisquare rho function. By default, chosen to yield a consistent estimate for the Normal distribution.
<code>opts</code>	a list of options for the M-scale estimation algorithm, see <a href="#">mscale_algorithm_options()</a> for details.
<code>delta</code>	deprecated. Use <code>bdp</code> instead.
<code>rho, eps, maxit</code>	deprecated. Instead set control options for the algorithm with the <code>opts</code> arguments.

**Value**

the M-estimate of scale.

**See Also**

Other functions to compute robust estimates of location and scale: [mloc\(\)](#), [mlocscale\(\)](#), [tau\\_size\(\)](#)

---

mscale\_algorithm\_options

*Options for the M-scale Estimation Algorithm*

---

**Description**

Options for the M-scale Estimation Algorithm

**Usage**

```
mscale_algorithm_options(max_it = 200, eps = 1e-08)
```

**Arguments**

max_it	maximum number of iterations.
eps	numerical tolerance to check for convergence.

**Value**

options for the M-scale estimation algorithm.

---

mstep_options	<i>Deprecated</i>
---------------	-------------------

---

**Description****[Deprecated]**

Additional options for computing penalized EN MM-estimates. Superseded by `mm_algorithm_options()` and options supplied directly to `pensem_cv()`.

**Usage**

```
mstep_options(
  cc = 3.44,
  maxit = 1000,
  eps = 1e-06,
  adjust_bdp = FALSE,
  verbosity = 0,
  en_correction = TRUE
)
```

**Arguments**

cc	<b>ignored.</b> Tuning constant for the M-estimator.
maxit	maximum number of iterations allowed.
eps	<b>ignored.</b> Numeric tolerance for convergence.
adjust_bdp	<b>ignored.</b> Should the breakdown point be adjusted based on the effective degrees of freedom?
verbosity	<b>ignored.</b> Verbosity of the algorithm.
en_correction	<b>ignored.</b> Should the corrected EN estimator be used to choose the optimal lambda with CV. If TRUE, as by default, the estimator is "bias corrected".

**Warning**

Do not use this function in new code. It may be removed from future versions of the package.

**See Also**

Other deprecated functions: `deprecated_en_options`, `enpy()`, `initest_options()`, `pense_options()`, `pensem()`

---

pense

*Compute (Adaptive) Elastic Net S-Estimates of Regression*

---

### Description

Compute elastic net S-estimates (PENSE estimates) along a grid of penalization levels with optional penalty loadings for adaptive elastic net.

### Usage

```
pense(  
  x,  
  y,  
  alpha,  
  nlambda = 50,  
  nlambda_ncpy = 10,  
  lambda,  
  lambda_min_ratio,  
  ncpy_lambda,  
  penalty_loadings,  
  intercept = TRUE,  
  bdp = 0.25,  
  cc,  
  add_zero_based = TRUE,  
  ncpy_specific = FALSE,  
  other_starts,  
  carry_forward = TRUE,  
  eps = 1e-06,  
  explore_solutions = 10,  
  explore_tol = 0.1,  
  explore_it = 5,  
  max_solutions = 1,  
  comparison_tol = sqrt(eps),  
  sparse = FALSE,  
  ncores = 1,  
  standardize = TRUE,  
  algorithm_opts = mm_algorithm_options(),  
  mscale_opts = mscale_algorithm_options(),  
  ncpy_opts = ncpy_options(),  
  cv_k = deprecated(),  
  cv_objective = deprecated(),  
  ...  
)
```

### Arguments

x                    n by p matrix of numeric predictors.

<code>y</code>	vector of response values of length $n$ . For binary classification, <code>y</code> should be a factor with 2 levels.
<code>alpha</code>	elastic net penalty mixing parameter with $0 \leq \alpha \leq 1$ . <code>alpha = 1</code> is the LASSO penalty, and <code>alpha = 0</code> the Ridge penalty. Can be a vector of several values, but <code>alpha = 0</code> cannot be mixed with other values.
<code>nlambda</code>	number of penalization levels.
<code>nlambda_ency</code>	number of penalization levels where the EN-PY initial estimate is computed.
<code>lambda</code>	optional user-supplied sequence of penalization levels. If given and not NULL, <code>nlambda</code> and <code>lambda_min_ratio</code> are ignored.
<code>lambda_min_ratio</code>	Smallest value of the penalization level as a fraction of the largest level (i.e., the smallest value for which all coefficients are zero). The default depends on the sample size relative to the number of variables and <code>alpha</code> . If more observations than variables are available, the default is $1e-3 * \alpha$ , otherwise $1e-2 * \alpha$ .
<code>ency_lambda</code>	optional user-supplied sequence of penalization levels at which EN-PY initial estimates are computed. If given and not NULL, <code>nlambda_ency</code> is ignored.
<code>penalty_loadings</code>	a vector of positive penalty loadings (a.k.a. weights) for different penalization of each coefficient. Only allowed for <code>alpha &gt; 0</code> .
<code>intercept</code>	include an intercept in the model.
<code>bdp</code>	desired breakdown point of the estimator, between 0.05 and 0.5. The actual breakdown point may be slightly larger/smaller to avoid instabilities of the S-loss.
<code>cc</code>	tuning constant for the S-estimator. Default is chosen based on the breakdown point <code>bdp</code> . This affects the estimated coefficients only if <code>standardize=TRUE</code> . Otherwise only the estimated scale of the residuals would be affected.
<code>add_zero_based</code>	also consider the 0-based regularization path. See details for a description.
<code>ency_specific</code>	use the EN-PY initial estimates only at the penalization level they are computed for. See details for a description.
<code>other_starts</code>	a list of other starting points, created by <code>starting_point()</code> . If the output of <code>ency_initial_estimates()</code> is given, the starting points will be <i>shared</i> among all penalization levels. Note that if a the starting point is <i>specific</i> to a penalization level, this penalization level is added to the grid of penalization levels (either the manually specified grid in <code>lambda</code> or the automatically generated grid of size <code>nlambda</code> ). If <code>standardize = TRUE</code> , the starting points are also scaled.
<code>carry_forward</code>	carry the best solutions forward to the next penalty level.
<code>eps</code>	numerical tolerance.
<code>explore_solutions</code>	number of solutions to compute up to the desired precision <code>eps</code> .
<code>explore_tol, explore_it</code>	numerical tolerance and maximum number of iterations for exploring possible solutions. The tolerance should be (much) looser than <code>eps</code> to be useful, and the number of iterations should also be much smaller than the maximum number of iterations given via <code>algorithm_opts</code> .

<code>max_solutions</code>	only retain up to <code>max_solutions</code> unique solutions per penalization level.
<code>comparison_tol</code>	numeric tolerance to determine if two solutions are equal. The comparison is first done on the absolute difference in the value of the objective function at the solution. If this is less than <code>comparison_tol</code> , two solutions are deemed equal. If the squared difference of the intercepts is less than <code>comparison_tol</code> and the squared $L_2$ norm of the difference vector is less than <code>comparison_tol</code> .
<code>sparse</code>	use sparse coefficient vectors.
<code>ncores</code>	number of CPU cores to use in parallel. By default, only one CPU core is used. Not supported on all platforms, in which case a warning is given.
<code>standardize</code>	logical flag to standardize the $x$ variables prior to fitting the PENSE estimates. Coefficients are always returned on the original scale. This can fail for variables with a large proportion of a single value (e.g., zero-inflated data). In this case, either compute with <code>standardize = FALSE</code> or standardize the data manually.
<code>algorithm_opts</code>	options for the MM algorithm to compute the estimates. See <a href="#">mm_algorithm_options()</a> for details.
<code>m-scale_opts</code>	options for the M-scale estimation. See <a href="#">mscale_algorithm_options()</a> for details.
<code>enpy_opts</code>	options for the ENPY initial estimates, created with the <a href="#">enpy_options()</a> function. See <a href="#">enpy_initial_estimates()</a> for details.
<code>cv_k, cv_objective</code>	deprecated and ignored. See <a href="#">pense_cv()</a> for estimating prediction performance via cross-validation.
<code>...</code>	ignored. See the section on deprecated parameters below.

## Value

a list-like object with the following items

`alpha` the sequence of alpha parameters.

`lambda` a list of sequences of penalization levels, one per alpha parameter.

`estimates` a list of estimates. Each estimate contains the following information:

`intercept` intercept estimate.

`beta` beta (slope) estimate.

`lambda` penalization level at which the estimate is computed.

`alpha` *alpha* hyper-parameter at which the estimate is computed.

`bdp` chosen breakdown-point.

`objf_value` value of the objective function at the solution.

`statuscode` if  $> 0$  the algorithm experienced issues when computing the estimate.

`status` optional status message from the algorithm.

`bdp` the actual breakdown point used.

`call` the original call.

### Strategies for Using Starting Points

The function supports several different strategies to compute, and use the provided starting points for optimizing the PENSE objective function.

Starting points are computed internally but can also be supplied via `other_starts`. By default, starting points are computed internally by the EN-PY procedure for penalization levels supplied in `enpy_lambda` (or the automatically generated grid of length `nlambda_enpy`). By default, starting points computed by the EN-PY procedure are *shared* for all penalization levels in `lambda` (or the automatically generated grid of length `nlambda`). If the starting points should be *specific* to the penalization level the starting points' penalization level, set the `enpy_specific` argument to TRUE.

In addition to EN-PY initial estimates, the algorithm can also use the "0-based" strategy if `add_zero_based = TRUE` (by default). Here, the 0-vector is used to start the optimization at the largest penalization level in `lambda`. At subsequent penalization levels, the solution at the previous penalization level is also used as starting point.

At every penalization level, all starting points are explored using the loose numerical tolerance `explore_tol`. Only the best `explore_solutions` are computed to the stringent numerical tolerance `eps`. Finally, only the best `max_solutions` are retained and carried forward as starting points for the subsequent penalization level.

### Deprecated Arguments

Starting with version 2.0.0, cross-validation is performed by separate function `pense_cv()`. Arguments related cross-validation cause an error when supplied to `pense()`. Furthermore, the following arguments are deprecated as of version 2.0.0: `initial`, `warm_reset`, `cl`, `options`, `init_options`, `en_options`. If `pense()` is called with any of these arguments, warnings detail how to replace them.

### See Also

`pense_cv()` for selecting hyper-parameters via cross-validation.

`coef.pense_fit()` for extracting coefficient estimates.

`plot.pense_fit()` for plotting the regularization path.

Other functions to compute robust estimates: `regmest()`

### Examples

```
# Compute the PENSE regularization path for Freeny's revenue data
# (see ?freeny)
data(freeny)
x <- as.matrix(freeny[, 2:5])

regpath <- pense(x, freeny$y, alpha = 0.5)
plot(regpath)

# Extract the coefficients at a certain penalization level
coef(regpath, lambda = regpath$lambda[[1]][[40]])

# What penalization level leads to good prediction performance?
set.seed(123)
```

```

cv_results <- pense_cv(x, freeny$y, alpha = 0.5,
                      cv_repl = 2, cv_k = 4)
plot(cv_results, se_mult = 1)

# Extract the coefficients at the penalization level with
# smallest prediction error ...
coef(cv_results)
# ... or at the penalization level with prediction error
# statistically indistinguishable from the minimum.
coef(cv_results, lambda = '1-se')

```

---

pensem	<i>Deprecated Alias of pensem_cv</i>
--------	--------------------------------------

---

### Description

pensem() is a deprecated alias for [pensem\\_cv\(\)](#).

### Usage

```
pensem(x, ...)
```

### Arguments

x                    either a numeric matrix of predictor values, or a cross-validated PENSE fit from [pense\\_cv\(\)](#).

...                    ignored. See the section on deprecated parameters below.

### See Also

Other deprecated functions: [deprecated\\_en\\_options](#), [enpy\(\)](#), [initest\\_options\(\)](#), [mstep\\_options\(\)](#), [pense\\_options\(\)](#)

---

pensem_cv	<i>Compute Penalized Elastic Net M-Estimates from PENSE</i>
-----------	---

---

### Description

This is a convenience wrapper around [pense\\_cv\(\)](#) and [regmest\\_cv\(\)](#), for the common use-case of computing a highly-robust S-estimate followed by a more efficient M-estimate using the scale of the residuals from the S-estimate.

**Usage**

```
pensem_cv(x, ...)  
  
## Default S3 method:  
pensem_cv(  
  x,  
  y,  
  alpha = 0.5,  
  nlambda = 50,  
  lambda_min_ratio,  
  lambda_m,  
  lambda_s,  
  standardize = TRUE,  
  penalty_loadings,  
  intercept = TRUE,  
  bdp = 0.25,  
  ncores = 1,  
  sparse = FALSE,  
  eps = 1e-06,  
  cc = 4.7,  
  cv_k = 5,  
  cv_repl = 1,  
  cl = NULL,  
  cv_metric = c("tau_size", "mape", "rmspe"),  
  add_zero_based = TRUE,  
  explore_solutions = 10,  
  explore_tol = 0.1,  
  explore_it = 5,  
  max_solutions = 10,  
  fit_all = TRUE,  
  comparison_tol = sqrt(eps),  
  algorithm_opts = mm_algorithm_options(),  
  mscale_opts = mscale_algorithm_options(),  
  nlambda_emy = 10,  
  emy_opts = emy_options(),  
  ...  
)  
  
## S3 method for class 'pense_cvfit'  
pensem_cv(  
  x,  
  scale,  
  alpha,  
  nlambda = 50,  
  lambda_min_ratio,  
  lambda_m,  
  standardize = TRUE,  
  penalty_loadings,
```



```

intercept = TRUE,
bdp = 0.25,
ncores = 1,
sparse = FALSE,
eps = 1e-06,
cc = 4.7,
cv_k = 5,
cv_repl = 1,
cl = NULL,
cv_metric = c("tau_size", "mape", "rmspe"),
add_zero_based = TRUE,
explore_solutions = 10,
explore_tol = 0.1,
explore_it = 5,
max_solutions = 10,
fit_all = TRUE,
comparison_tol = sqrt(eps),
algorithm_opts = mm_algorithm_options(),
mscale_opts = mscale_algorithm_options(),
x_train,
y_train,
...
)

```

### Arguments

x	either a numeric matrix of predictor values, or a cross-validated PENSE fit from <a href="#">pense_cv()</a> .
...	ignored. See the section on deprecated parameters below.
y	vector of response values of length n. For binary classification, y should be a factor with 2 levels.
alpha	elastic net penalty mixing parameter with $0 \leq \alpha \leq 1$ . alpha = 1 is the LASSO penalty, and alpha = 0 the Ridge penalty. Can be a vector of several values, but alpha = 0 cannot be mixed with other values.
nlambda	number of penalization levels.
lambda_min_ratio	Smallest value of the penalization level as a fraction of the largest level (i.e., the smallest value for which all coefficients are zero). The default depends on the sample size relative to the number of variables and alpha. If more observations than variables are available, the default is $1e-3 * \alpha$ , otherwise $1e-2 * \alpha$ .
lambda_m, lambda_s	optional user-supplied sequence of penalization levels for the S- and M-estimates. If given and not NULL, nlambda and lambda_min_ratio are ignored for the respective estimate (S and/or M).
standardize	logical flag to standardize the x variables prior to fitting the PENSE estimates. Coefficients are always returned on the original scale. This can fail for variables

with a large proportion of a single value (e.g., zero-inflated data). In this case, either compute with `standardize = FALSE` or standardize the data manually.

<code>penalty_loadings</code>	a vector of positive penalty loadings (a.k.a. weights) for different penalization of each coefficient. Only allowed for $\alpha > 0$ .
<code>intercept</code>	include an intercept in the model.
<code>bdp</code>	desired breakdown point of the estimator, between 0.05 and 0.5. The actual breakdown point may be slightly larger/smaller to avoid instabilities of the S-loss.
<code>ncores</code>	number of CPU cores to use in parallel. By default, only one CPU core is used. Not supported on all platforms, in which case a warning is given.
<code>sparse</code>	use sparse coefficient vectors.
<code>eps</code>	numerical tolerance.
<code>cc</code>	cutoff constant for Tukey's bisquare $\rho$ function in the M-estimation objective function.
<code>cv_k</code>	number of folds per cross-validation.
<code>cv_repl</code>	number of cross-validation replications.
<code>cl</code>	a <a href="#">parallel</a> cluster. Can only be used in combination with <code>ncores = 1</code> .
<code>cv_metric</code>	either a string specifying the performance metric to use, or a function to evaluate prediction errors in a single CV replication. If a function, the number of arguments define the data the function receives. If the function takes a single argument, it is called with a single numeric vector of prediction errors. If the function takes two or more arguments, it is called with the predicted values as first argument and the true values as second argument. The function must always return a single numeric value quantifying the prediction performance. The order of the given values corresponds to the order in the input data.
<code>add_zero_based</code>	also consider the 0-based regularization path. See details for a description.
<code>explore_solutions</code>	number of solutions to compute up to the desired precision <code>eps</code> .
<code>explore_tol, explore_it</code>	numerical tolerance and maximum number of iterations for exploring possible solutions. The tolerance should be (much) looser than <code>eps</code> to be useful, and the number of iterations should also be much smaller than the maximum number of iterations given via <code>algorithm_opts</code> .
<code>max_solutions</code>	only retain up to <code>max_solutions</code> unique solutions per penalization level.
<code>fit_all</code>	If TRUE, fit the model for all penalization levels. Can also be any combination of "min" and "{x}-se", in which case only models at the penalization level with smallest average CV accuracy, or within {x} standard errors, respectively. Setting <code>fit_all</code> to FALSE is equivalent to "min". Applies to all alpha value.
<code>comparison_tol</code>	numeric tolerance to determine if two solutions are equal. The comparison is first done on the absolute difference in the value of the objective function at the solution. If this is less than <code>comparison_tol</code> , two solutions are deemed equal if the squared difference of the intercepts is less than <code>comparison_tol</code> and the squared $L_2$ norm of the difference vector is less than <code>comparison_tol</code> .

algorithm_opts	options for the MM algorithm to compute the estimates. See <a href="#">mm_algorithm_options()</a> for details.
mscale_opts	options for the M-scale estimation. See <a href="#">mscale_algorithm_options()</a> for details.
nlambda_ency	number of penalization levels where the EN-PY initial estimate is computed.
ency_opts	options for the ENPY initial estimates, created with the <a href="#">ency_options()</a> function. See <a href="#">ency_initial_estimates()</a> for details.
scale	initial scale estimate to use in the M-estimation. By default the S-scale from the PENSE fit is used.
x_train, y_train	override arguments x and y as provided in the call to <a href="#">pense_cv()</a> . This is useful if the arguments in the <a href="#">pense_cv()</a> call are not available in the current environment.

### Details

The built-in CV metrics are

"tau\_size"  $\tau$ -size of the prediction error, computed by [tau\\_size\(\)](#) (default).

"mape" Median absolute prediction error.

"rmspe" Root mean squared prediction error.

"auroc" Area under the receiver operator characteristic curve (actually 1 - AUROC). Only sensible for binary responses.

### Value

an object of cross-validated regularized M-estimates as returned from [regmest\\_cv\(\)](#).

### See Also

[pense\\_cv\(\)](#) to compute the starting S-estimate.

Other functions to compute robust estimates with CV: [pense\\_cv\(\)](#), [regmest\\_cv\(\)](#)

### Description

Perform (repeated) K-fold cross-validation for [pense\(\)](#).

[adapense\\_cv\(\)](#) is a convenience wrapper to compute adaptive PENSE estimates.

**Usage**

```
pense_cv(
  x,
  y,
  standardize = TRUE,
  lambda,
  cv_k,
  cv_repl = 1,
  cv_metric = c("tau_size", "mape", "rmspe", "auroc"),
  fit_all = TRUE,
  fold_starts = c("full", "enpy", "both"),
  cl = NULL,
  ...
)
```

```
adapense_cv(x, y, alpha, alpha_preliminary = 0, exponent = 1, ...)
```

**Arguments**

<code>x</code>	<code>n</code> by <code>p</code> matrix of numeric predictors.
<code>y</code>	vector of response values of length <code>n</code> . For binary classification, <code>y</code> should be a factor with 2 levels.
<code>standardize</code>	whether to standardize the <code>x</code> variables prior to fitting the PENSE estimates. Can also be set to <code>"cv_only"</code> , in which case the input data is not standardized, but the training data in the CV folds is scaled to match the scaling of the input data. Coefficients are always returned on the original scale. This can fail for variables with a large proportion of a single value (e.g., zero-inflated data). In this case, either compute with <code>standardize = FALSE</code> or standardize the data manually.
<code>lambda</code>	optional user-supplied sequence of penalization levels. If given and not <code>NULL</code> , <code>nlambda</code> and <code>lambda_min_ratio</code> are ignored.
<code>cv_k</code>	number of folds per cross-validation.
<code>cv_repl</code>	number of cross-validation replications.
<code>cv_metric</code>	either a string specifying the performance metric to use, or a function to evaluate prediction errors in a single CV replication. If a function, the number of arguments define the data the function receives. If the function takes a single argument, it is called with a single numeric vector of prediction errors. If the function takes two or more arguments, it is called with the predicted values as first argument and the true values as second argument. The function must always return a single numeric value quantifying the prediction performance. The order of the given values corresponds to the order in the input data.
<code>fit_all</code>	If <code>TRUE</code> , fit the model for all penalization levels. Can also be any combination of <code>"min"</code> and <code>"{x}-se"</code> , in which case only models at the penalization level with smallest average CV accuracy, or within <code>{x}</code> standard errors, respectively. Setting <code>fit_all</code> to <code>FALSE</code> is equivalent to <code>"min"</code> . Applies to all alpha value.
<code>fold_starts</code>	how to determine starting values in the cross-validation folds. If <code>"full"</code> (default), use the best solution from the fit to the full data as starting value. This

implies `fit_all=TRUE`. If "enpy" compute separate ENPY initial estimates in each fold. The option "both" uses both. These starts are in addition to the starts provided in `other_starts`.

`cl` a [parallel](#) cluster. Can only be used in combination with `ncores = 1`.

`...` Arguments passed on to [pense](#)

`nlambda` number of penalization levels.

`lambda_min_ratio` Smallest value of the penalization level as a fraction of the largest level (i.e., the smallest value for which all coefficients are zero). The default depends on the sample size relative to the number of variables and `alpha`. If more observations than variables are available, the default is  $1e-3 * \alpha$ , otherwise  $1e-2 * \alpha$ .

`nlambda_enpy` number of penalization levels where the EN-PY initial estimate is computed.

`penalty_loadings` a vector of positive penalty loadings (a.k.a. weights) for different penalization of each coefficient. Only allowed for `alpha > 0`.

`enpy_lambda` optional user-supplied sequence of penalization levels at which EN-PY initial estimates are computed. If given and not `NULL`, `nlambda_enpy` is ignored.

`other_starts` a list of other starting points, created by [starting\\_point\(\)](#). If the output of [enpy\\_initial\\_estimates\(\)](#) is given, the starting points will be *shared* among all penalization levels. Note that if a the starting point is *specific* to a penalization level, this penalization level is added to the grid of penalization levels (either the manually specified grid in `lambda` or the automatically generated grid of size `nlambda`). If `standardize = TRUE`, the starting points are also scaled.

`intercept` include an intercept in the model.

`bdp` desired breakdown point of the estimator, between 0.05 and 0.5. The actual breakdown point may be slightly larger/smaller to avoid instabilities of the S-loss.

`cc` tuning constant for the S-estimator. Default is chosen based on the breakdown point `bdp`. This affects the estimated coefficients only if `standardize=TRUE`. Otherwise only the estimated scale of the residuals would be affected.

`eps` numerical tolerance.

`explore_solutions` number of solutions to compute up to the desired precision `eps`.

`explore_tol, explore_it` numerical tolerance and maximum number of iterations for exploring possible solutions. The tolerance should be (much) looser than `eps` to be useful, and the number of iterations should also be much smaller than the maximum number of iterations given via `algorithm_opts`.

`max_solutions` only retain up to `max_solutions` unique solutions per penalization level.

`comparison_tol` numeric tolerance to determine if two solutions are equal. The comparison is first done on the absolute difference in the value of the objective function at the solution. If this is less than `comparison_tol`, two solutions are deemed equal if the squared difference of the intercepts is less than `comparison_tol` and the squared  $L_2$  norm of the difference vector is less than `comparison_tol`.

<code>add_zero_based</code>	also consider the 0-based regularization path. See details for a description.
<code>enpy_specific</code>	use the EN-PY initial estimates only at the penalization level they are computed for. See details for a description.
<code>carry_forward</code>	carry the best solutions forward to the next penalty level.
<code>sparse</code>	use sparse coefficient vectors.
<code>ncores</code>	number of CPU cores to use in parallel. By default, only one CPU core is used. Not supported on all platforms, in which case a warning is given.
<code>algorithm_opts</code>	options for the MM algorithm to compute the estimates. See <code>mm_algorithm_options()</code> for details.
<code>mscale_opts</code>	options for the M-scale estimation. See <code>mscale_algorithm_options()</code> for details.
<code>enpy_opts</code>	options for the ENPY initial estimates, created with the <code>enpy_options()</code> function. See <code>enpy_initial_estimates()</code> for details.
<code>cv_k, cv_objective</code>	deprecated and ignored. See <code>pense_cv()</code> for estimating prediction performance via cross-validation.
<code>alpha</code>	elastic net penalty mixing parameter with $0 \leq \alpha \leq 1$ . <code>alpha = 1</code> is the LASSO penalty, and <code>alpha = 0</code> the Ridge penalty. Can be a vector of several values, but <code>alpha = 0</code> cannot be mixed with other values.
<code>alpha_preliminary</code>	alpha parameter for the preliminary estimate.
<code>exponent</code>	the exponent for computing the penalty loadings based on the preliminary estimate.

## Details

The built-in CV metrics are

"tau\_size"  $\tau$ -size of the prediction error, computed by `tau_size()` (default).

"mape" Median absolute prediction error.

"rmspe" Root mean squared prediction error.

"auroc" Area under the receiver operator characteristic curve (actually 1 - AUROC). Only sensible for binary responses.

`adapense_cv()` is a convenience wrapper which performs 3 steps:

1. compute preliminary estimates via `pense_cv(..., alpha = alpha_preliminary)`,
2. computes the penalty loadings from the estimate `beta` with best prediction performance by `adapense_loadings = 1 / abs(beta)^exponent`, and
3. compute the adaptive PENSE estimates via `pense_cv(..., penalty_loadings = adapense_loadings)`.

## Value

a list-like object with the same components as returned by `pense()`, plus the following:

`cvres` data frame of average cross-validated performance.

a list-like object as returned by `pense_cv()` plus the following

- preliminary the CV results for the preliminary estimate.
- exponent exponent used to compute the penalty loadings.
- penalty\_loadings penalty loadings used for the adaptive PENSE estimate.

### See Also

`pense()` for computing regularized S-estimates without cross-validation.  
`coef.pense_cvfit()` for extracting coefficient estimates.  
`plot.pense_cvfit()` for plotting the CV performance or the regularization path.  
Other functions to compute robust estimates with CV: `pensem_cv()`, `regmest_cv()`  
Other functions to compute robust estimates with CV: `pensem_cv()`, `regmest_cv()`

### Examples

```
# Compute the adaptive PENSE regularization path for Freeny's
# revenue data (see ?freeny)
data(freeny)
x <- as.matrix(freeny[, 2:5])

## Either use the convenience function directly ...
set.seed(123)
ada_convenience <- adapense_cv(x, freeny$y, alpha = 0.5,
                              cv_repl = 2, cv_k = 4)

## ... or compute the steps manually:
# Step 1: Compute preliminary estimates with CV
set.seed(123)
preliminary_estimate <- pense_cv(x, freeny$y, alpha = 0,
                                 cv_repl = 2, cv_k = 4)
plot(preliminary_estimate, se_mult = 1)

# Step 2: Use the coefficients with best prediction performance
# to define the penalty loadings:
prelim_coefs <- coef(preliminary_estimate, lambda = 'min')
pen_loadings <- 1 / abs(prelim_coefs[-1])

# Step 3: Compute the adaptive PENSE estimates and estimate
# their prediction performance.
set.seed(123)
ada_manual <- pense_cv(x, freeny$y, alpha = 0.5,
                      cv_repl = 2, cv_k = 4,
                      penalty_loadings = pen_loadings)

# Visualize the prediction performance and coefficient path of
# the adaptive PENSE estimates (manual vs. automatic)
def.par <- par(no.readonly = TRUE)
layout(matrix(1:4, ncol = 2, byrow = TRUE))
plot(ada_convenience$preliminary)
```

```
plot(preliminary_estimate)
plot(ada_convenience)
plot(ada_manual)
par(def.par)
```

---

pense\_options                      *Deprecated*

---

## Description

### [Deprecated]

Additional options for computing penalized EN S-estimates. Superseded by [mm\\_algorithm\\_options\(\)](#) and options supplied directly to [pense\(\)](#).

## Usage

```
pense_options(
  delta = 0.25,
  maxit = 1000,
  eps = 1e-06,
  mscale_eps = 1e-08,
  mscale_maxit = 200,
  verbosity = 0,
  cc = NULL,
  en_correction = TRUE
)
```

## Arguments

delta	desired breakdown point of the resulting estimator.
maxit	maximum number of iterations allowed.
eps	numeric tolerance for convergence.
mscale_eps, mscale_maxit	maximum number of iterations and numeric tolerance for the M-scale.
verbosity	<b>ignored.</b> Verbosity of the algorithm.
cc	<b>ignored.</b> Tuning constant for the S-estimator. Default is to chosen based on the breakdown point delta. Should never have to be changed.
en_correction	<b>ignored.</b> Should the corrected EN estimator be used to choose the optimal lambda with CV. If TRUE, as by default, the estimator is "bias corrected".

## Warning

Do not use this function in new code. It may be removed from future versions of the package.

## See Also

Other deprecated functions: [deprecated\\_en\\_options](#), [enpy\(\)](#), [initest\\_options\(\)](#), [mstep\\_options\(\)](#), [pensem\(\)](#)



---

plot.pense\_cvfit      *Plot Method for Penalized Estimates With Cross-Validation*

---

### Description

Plot the cross-validation performance or the coefficient path for fitted penalized elastic net S- or LS-estimates of regression.

### Usage

```
## S3 method for class 'pense_cvfit'
plot(x, what = c("cv", "coef.path"), alpha = NULL, se_mult = 1, ...)
```

### Arguments

x	fitted estimates with cross-validation information.
what	plot either the CV performance or the coefficient path.
alpha	If what = "cv", only CV performance for fits with matching alpha are plotted. In case alpha is missing or NULL, all fits in x are plotted. If what = "coef.path", plot the coefficient path for the fit with the given hyper-parameter value or, in case alpha is missing, for the first value in x\$alpha.
se_mult	if plotting CV performance, multiplier of the estimated SE.
...	currently ignored.

### See Also

Other functions for plotting and printing: [plot.pense\\_fit\(\)](#), [prediction\\_performance\(\)](#), [summary.pense\\_cvfit\(\)](#)

### Examples

```
# Compute the PENSE regularization path for Freeny's revenue data
# (see ?freeny)
data(freeny)
x <- as.matrix(freeny[, 2:5])

regpath <- pense(x, freeny$y, alpha = 0.5)
plot(regpath)

# Extract the coefficients at a certain penalization level
coef(regpath, lambda = regpath$lambda[[1]][[40]])

# What penalization level leads to good prediction performance?
set.seed(123)
cv_results <- pense_cv(x, freeny$y, alpha = 0.5,
                      cv_repl = 2, cv_k = 4)
plot(cv_results, se_mult = 1)

# Extract the coefficients at the penalization level with
```

```
# smallest prediction error ...
coef(cv_results)
# ... or at the penalization level with prediction error
# statistically indistinguishable from the minimum.
coef(cv_results, lambda = '1-se')
```

---

plot.pense\_fit                    *Plot Method for Penalized Estimates*

---

### Description

Plot the coefficient path for fitted penalized elastic net S- or LS-estimates of regression.

### Usage

```
## S3 method for class 'pense_fit'
plot(x, alpha, ...)
```

### Arguments

x	fitted estimates.
alpha	Plot the coefficient path for the fit with the given hyper-parameter value. If missing or NULL, the first value in x\$alpha is used.
...	currently ignored.

### See Also

Other functions for plotting and printing: [plot.pense\\_cvfit\(\)](#), [prediction\\_performance\(\)](#), [summary.pense\\_cvfit\(\)](#)

### Examples

```
# Compute the PENSE regularization path for Freeny's revenue data
# (see ?freeny)
data(freeny)
x <- as.matrix(freeny[, 2:5])

regpath <- pense(x, freeny$y, alpha = 0.5)
plot(regpath)

# Extract the coefficients at a certain penalization level
coef(regpath, lambda = regpath$lambda[[1]][[40]])

# What penalization level leads to good prediction performance?
set.seed(123)
cv_results <- pense_cv(x, freeny$y, alpha = 0.5,
                      cv_repl = 2, cv_k = 4)
plot(cv_results, se_mult = 1)
```

```

# Extract the coefficients at the penalization level with
# smallest prediction error ...
coef(cv_results)
# ... or at the penalization level with prediction error
# statistically indistinguishable from the minimum.
coef(cv_results, lambda = '1-se')

```

---

predict.pense\_cvfit     *Predict Method for PENSE Fits*

---

### Description

Predict response values using a PENSE (or LS-EN) regularization path with hyper-parameters chosen by cross-validation.

### Usage

```

## S3 method for class 'pense_cvfit'
predict(
  object,
  newdata,
  alpha = NULL,
  lambda = "min",
  se_mult = 1,
  exact = deprecated(),
  correction = deprecated(),
  ...
)

```

### Arguments

object	PENSE with cross-validated hyper-parameters to extract coefficients from.
newdata	an optional matrix of new predictor values. If missing, the fitted values are computed.
alpha	Either a single number or NULL (default). If given, only fits with the given alpha value are considered. If lambda is a numeric value and object was fit with multiple <i>alpha</i> values and no value is provided, the first value in object\$alpha is used with a warning.
lambda	either a string specifying which penalty level to use ("min", "se", "{m}-se") or a single numeric value of the penalty parameter. See details.
se_mult	If lambda = "se", the multiple of standard errors to tolerate.
exact	deprecated. Always gives a warning if lambda is not part of the fitted sequence and coefficients are interpolated.
correction	defunct.
...	currently not used.

**Value**

a numeric vector of residuals for the given penalization level.

**Hyper-parameters**

If `lambda = "{m}-se"` and `object` contains fitted estimates for every penalization level in the sequence, use the fit the most parsimonious model with prediction performance statistically indistinguishable from the best model. This is determined to be the model with prediction performance within  $m * cv\_se$  from the best model. If `lambda = "se"`, the multiplier  $m$  is taken from `se_mult`.

By default all *alpha* hyper-parameters available in the fitted object are considered. This can be overridden by supplying one or multiple values in parameter `alpha`. For example, if `lambda = "1-se"` and `alpha` contains two values, the "1-SE" rule is applied individually for each `alpha` value, and the fit with the better prediction error is considered.

In case `lambda` is a number and `object` was fit for several *alpha* hyper-parameters, `alpha` must also be given, or the first value in `object$alpha` is used with a warning.

**See Also**

Other functions for extracting components: [coef.pense\\_cvfit\(\)](#), [coef.pense\\_fit\(\)](#), [predict.pense\\_fit\(\)](#), [residuals.pense\\_cvfit\(\)](#), [residuals.pense\\_fit\(\)](#)

**Examples**

```
# Compute the LS-EN regularization path for Freeny's revenue data
# (see ?freeny)
data(freeny)
x <- as.matrix(freeny[, 2:5])

regpath <- elnet(x, freeny$y, alpha = 0.75)

# Predict the response using a specific penalization level
predict(regpath, newdata = freeny[1:5, 2:5],
        lambda = regpath$lambda[[1]][[10]])

# Extract the residuals at a certain penalization level
residuals(regpath, lambda = regpath$lambda[[1]][[5]])

# Select penalization level via cross-validation
set.seed(123)
cv_results <- elnet_cv(x, freeny$y, alpha = 0.5,
                      cv_repl = 10, cv_k = 4)

# Predict the response using the "best" penalization level
predict(cv_results, newdata = freeny[1:5, 2:5])

# Extract the residuals at the "best" penalization level
residuals(cv_results)
# Extract the residuals at a more parsimonious penalization level
residuals(cv_results, lambda = "1.5-se")
```

---

predict.pense\_fit      *Predict Method for PENSE Fits*

---

### Description

Predict response values using a PENSE (or LS-EN) regularization path fitted by [pense\(\)](#), [regmest\(\)](#) or [elnet\(\)](#).

### Usage

```
## S3 method for class 'pense_fit'
predict(
  object,
  newdata,
  alpha = NULL,
  lambda,
  exact = deprecated(),
  correction = deprecated(),
  ...
)
```

### Arguments

object	PENSE regularization path to extract residuals from.
newdata	an optional matrix of new predictor values. If missing, the fitted values are computed.
alpha	Either a single number or NULL (default). If given, only fits with the given alpha value are considered. If object was fit with multiple alpha values, and no value is provided, the first value in object\$alpha is used with a warning.
lambda	a single number for the penalty level.
exact	defunct Always gives a warning if lambda is not part of the fitted sequence and coefficients need to be interpolated.
correction	defunct.
...	currently not used.

### Value

a numeric vector of residuals for the given penalization level.

### See Also

Other functions for extracting components: [coef.pense\\_cvfit\(\)](#), [coef.pense\\_fit\(\)](#), [predict.pense\\_cvfit\(\)](#), [residuals.pense\\_cvfit\(\)](#), [residuals.pense\\_fit\(\)](#)

**Examples**

```

# Compute the LS-EN regularization path for Freeny's revenue data
# (see ?freeny)
data(freeny)
x <- as.matrix(freeny[, 2:5])

regpath <- elnet(x, freeny$y, alpha = 0.75)

# Predict the response using a specific penalization level
predict(regpath, newdata = freeny[1:5, 2:5],
        lambda = regpath$lambda[[1]][[10]])

# Extract the residuals at a certain penalization level
residuals(regpath, lambda = regpath$lambda[[1]][[5]])

# Select penalization level via cross-validation
set.seed(123)
cv_results <- elnet_cv(x, freeny$y, alpha = 0.5,
                      cv_repl = 10, cv_k = 4)

# Predict the response using the "best" penalization level
predict(cv_results, newdata = freeny[1:5, 2:5])

# Extract the residuals at the "best" penalization level
residuals(cv_results)
# Extract the residuals at a more parsimonious penalization level
residuals(cv_results, lambda = "1.5-se")

```

---

prediction\_performance

*Prediction Performance of Adaptive PENSE Fits*

---

**Description**

Extract the prediction performance of one or more (adaptive) PENSE fits.

**Usage**

```

prediction_performance(..., alpha = NULL, lambda = "min", se_mult = 1)

## S3 method for class 'pense_pred_perf'
print(x, ...)

```

**Arguments**

... one or more (adaptive) PENSE fits with cross-validation information.

alpha Either a numeric vector or NULL (default). If given, only fits with the given alpha value are considered. If lambda is a numeric value and object was fit with multiple alpha values, the parameter alpha must not be missing.

lambda	either a string specifying which penalty level to use ("min", "se", "{x}-se") or a single numeric value of the penalty parameter. See details.
se_mult	If lambda = "se", the multiple of standard errors to tolerate.
x	an object with information on prediction performance created with <code>prediction_performance()</code> .

### Details

If lambda = "se" and the cross-validation was performed with multiple replications, use the penalty level with prediction performance within `se_mult` of the best prediction performance.

### Value

a data frame with details about the prediction performance of the given PENSE fits. The data frame has a custom print method summarizing the prediction performances.

### See Also

[summary.pense\\_cvfit\(\)](#) for a summary of the fitted model.

Other functions for plotting and printing: [plot.pense\\_cvfit\(\)](#), [plot.pense\\_fit\(\)](#), [summary.pense\\_cvfit\(\)](#)

---

prinsens	<i>Principal Sensitivity Components</i>
----------	---

---

### Description

Compute Principal Sensitivity Components for Elastic Net Regression

### Usage

```
prinsens(
  x,
  y,
  alpha,
  lambda,
  intercept = TRUE,
  penalty_loadings,
  en_algorithm_opts,
  eps = 1e-06,
  sparse = FALSE,
  ncores = 1L,
  method = deprecated()
)
```

**Arguments**

x	n by p matrix of numeric predictors.
y	vector of response values of length n.
alpha	elastic net penalty mixing parameter with $0 \leq \alpha \leq 1$ . alpha = 1 is the LASSO penalty, and alpha = 0 the Ridge penalty. Can be a vector of several values, but alpha = 0 cannot be mixed with other values.
lambda	optional user-supplied sequence of penalization levels. If given and not NULL, nlambda and lambda_min_ratio are ignored.
intercept	include an intercept in the model.
penalty_loadings	a vector of positive penalty loadings (a.k.a. weights) for different penalization of each coefficient. Only allowed for alpha > 0.
en_algorithm_opts	options for the LS-EN algorithm. See <a href="#">en_algorithm_options</a> for details.
eps	numerical tolerance.
sparse	use sparse coefficient vectors.
ncores	number of CPU cores to use in parallel. By default, only one CPU core is used. Not supported on all platforms, in which case a warning is given.
method	defunct. PSCs are always computed for EN estimates. For the PY procedure for unpenalized estimation use package <a href="#">pyinit</a> .

**Value**

a list of principal sensitivity components, one per element in lambda. Each PSC is itself a list with items lambda, alpha, and pscs.

**References**

Cohen Freue, G.V.; Kepplinger, D.; Salibián-Barrera, M.; Smucler, E. Robust elastic net estimators for variable selection and identification of proteomic biomarkers. *Ann. Appl. Stat.* **13** (2019), no. 4, 2065–2090 [doi:10.1214/19AOAS1269](#)

Pena, D., and Yohai, V.J. A Fast Procedure for Outlier Diagnostics in Large Regression Problems. *J. Amer. Statist. Assoc.* **94** (1999). no. 446, 434–445. [doi:10.2307/2670164](#)

**See Also**

Other functions for initial estimates: [enpy\\_initial\\_estimates\(\)](#), [starting\\_point\(\)](#)



regmest

*Compute (Adaptive) Elastic Net M-Estimates of Regression***Description**

Compute elastic net M-estimates along a grid of penalization levels with optional penalty loadings for adaptive elastic net.

**Usage**

```
regmest(
  x,
  y,
  alpha,
  nlambda = 50,
  lambda,
  lambda_min_ratio,
  scale,
  starting_points,
  penalty_loadings,
  intercept = TRUE,
  cc = 4.7,
  eps = 1e-06,
  explore_solutions = 10,
  explore_tol = 0.1,
  max_solutions = 10,
  comparison_tol = sqrt(eps),
  sparse = FALSE,
  ncores = 1,
  standardize = TRUE,
  algorithm_opts = mm_algorithm_options(),
  add_zero_based = TRUE,
  mscale_bdp = 0.25,
  mscale_opts = mscale_algorithm_options()
)
```

**Arguments**

<code>x</code>	n by p matrix of numeric predictors.
<code>y</code>	vector of response values of length n. For binary classification, y should be a factor with 2 levels.
<code>alpha</code>	elastic net penalty mixing parameter with $0 \leq \alpha \leq 1$ . <code>alpha = 1</code> is the LASSO penalty, and <code>alpha = 0</code> the Ridge penalty.
<code>nlambda</code>	number of penalization levels.
<code>lambda</code>	optional user-supplied sequence of penalization levels. If given and not NULL, <code>nlambda</code> and <code>lambda_min_ratio</code> are ignored.

<code>lambda_min_ratio</code>	Smallest value of the penalization level as a fraction of the largest level (i.e., the smallest value for which all coefficients are zero). The default depends on the sample size relative to the number of variables and $\alpha$ . If more observations than variables are available, the default is $1e-3 * \alpha$ , otherwise $1e-2 * \alpha$ .
<code>scale</code>	fixed scale of the residuals.
<code>starting_points</code>	a list of starting points, created by <code>starting_point()</code> . The starting points are shared among all penalization levels.
<code>penalty_loadings</code>	a vector of positive penalty loadings (a.k.a. weights) for different penalization of each coefficient. Only allowed for $\alpha > 0$ .
<code>intercept</code>	include an intercept in the model.
<code>cc</code>	cutoff constant for Tukey's bisquare $\rho$ function.
<code>eps</code>	numerical tolerance.
<code>explore_solutions</code>	number of solutions to compute up to the desired precision <code>eps</code> .
<code>explore_tol</code>	numerical tolerance for exploring possible solutions. Should be (much) looser than <code>eps</code> to be useful.
<code>max_solutions</code>	only retain up to <code>max_solutions</code> unique solutions per penalization level.
<code>comparison_tol</code>	numeric tolerance to determine if two solutions are equal. The comparison is first done on the absolute difference in the value of the objective function at the solution. If this is less than <code>comparison_tol</code> , two solutions are deemed equal if the squared difference of the intercepts is less than <code>comparison_tol</code> and the squared $L_2$ norm of the difference vector is less than <code>comparison_tol</code> .
<code>sparse</code>	use sparse coefficient vectors.
<code>ncores</code>	number of CPU cores to use in parallel. By default, only one CPU core is used. Not supported on all platforms, in which case a warning is given.
<code>standardize</code>	logical flag to standardize the $x$ variables prior to fitting the M-estimates. Coefficients are always returned on the original scale. This can fail for variables with a large proportion of a single value (e.g., zero-inflated data). In this case, either compute with <code>standardize = FALSE</code> or standardize the data manually.
<code>algorithm_opts</code>	options for the MM algorithm to compute estimates. See <code>mm_algorithm_options()</code> for details.
<code>add_zero_based</code>	also consider the 0-based regularization path in addition to the given starting points.
<code>m-scale_bdp, m-scale_opts</code>	options for the M-scale estimate used to standardize the predictors (if <code>standardize = TRUE</code> ).

**Value**

a list-like object with the following items

**alpha** the sequence of alpha parameters.  
**lambda** a list of sequences of penalization levels, one per alpha parameter.  
**scale** the used scale of the residuals.  
**estimates** a list of estimates. Each estimate contains the following information:
 

- intercept** intercept estimate.
- beta** beta (slope) estimate.
- lambda** penalization level at which the estimate is computed.
- alpha** *alpha* hyper-parameter at which the estimate is computed.
- objf\_value** value of the objective function at the solution.
- statuscode** if  $> 0$  the algorithm experienced issues when computing the estimate.
- status** optional status message from the algorithm.

**call** the original call.

### See Also

[regmest\\_cv\(\)](#) for selecting hyper-parameters via cross-validation.  
[coef.pense\\_fit\(\)](#) for extracting coefficient estimates.  
[plot.pense\\_fit\(\)](#) for plotting the regularization path.  
 Other functions to compute robust estimates: [pense\(\)](#)

---

 regmest\_cv

*Cross-validation for (Adaptive) Elastic Net M-Estimates*


---

### Description

Perform (repeated) K-fold cross-validation for [regmest\(\)](#).  
[adamest\\_cv\(\)](#) is a convenience wrapper to compute adaptive elastic-net M-estimates.

### Usage

```

regmest_cv(
  x,
  y,
  standardize = TRUE,
  lambda,
  cv_k,
  cv_repl = 1,
  cv_metric = c("tau_size", "mape", "rmspe", "auroc"),
  fit_all = TRUE,
  cl = NULL,
  ...
)

adamest_cv(x, y, alpha, alpha_preliminary = 0, exponent = 1, ...)
  
```

**Arguments**

<code>x</code>	<code>n</code> by <code>p</code> matrix of numeric predictors.
<code>y</code>	vector of response values of length <code>n</code> . For binary classification, <code>y</code> should be a factor with 2 levels.
<code>standardize</code>	whether to standardize the <code>x</code> variables prior to fitting the PENSE estimates. Can also be set to "cv_only", in which case the input data is not standardized, but the training data in the CV folds is scaled to match the scaling of the input data. Coefficients are always returned on the original scale. This can fail for variables with a large proportion of a single value (e.g., zero-inflated data). In this case, either compute with <code>standardize = FALSE</code> or standardize the data manually.
<code>lambda</code>	optional user-supplied sequence of penalization levels. If given and not NULL, <code>nlambda</code> and <code>lambda_min_ratio</code> are ignored.
<code>cv_k</code>	number of folds per cross-validation.
<code>cv_repl</code>	number of cross-validation replications.
<code>cv_metric</code>	either a string specifying the performance metric to use, or a function to evaluate prediction errors in a single CV replication. If a function, the number of arguments define the data the function receives. If the function takes a single argument, it is called with a single numeric vector of prediction errors. If the function takes two or more arguments, it is called with the predicted values as first argument and the true values as second argument. The function must always return a single numeric value quantifying the prediction performance. The order of the given values corresponds to the order in the input data.
<code>fit_all</code>	If TRUE, fit the model for all penalization levels. Can also be any combination of "min" and "{x}-se", in which case only models at the penalization level with smallest average CV accuracy, or within {x} standard errors, respectively. Setting <code>fit_all</code> to FALSE is equivalent to "min". Applies to all alpha value.
<code>cl</code>	a <a href="#">parallel</a> cluster. Can only be used in combination with <code>ncores = 1</code> .
<code>...</code>	Arguments passed on to <a href="#">regmest</a>
<code>scale</code>	fixed scale of the residuals.
<code>nlambda</code>	number of penalization levels.
<code>lambda_min_ratio</code>	Smallest value of the penalization level as a fraction of the largest level (i.e., the smallest value for which all coefficients are zero). The default depends on the sample size relative to the number of variables and alpha. If more observations than variables are available, the default is $1e-3 * \alpha$ , otherwise $1e-2 * \alpha$ .
<code>penalty_loadings</code>	a vector of positive penalty loadings (a.k.a. weights) for different penalization of each coefficient. Only allowed for <code>alpha &gt; 0</code> .
<code>starting_points</code>	a list of starting points, created by <a href="#">starting_point()</a> . The starting points are shared among all penalization levels.
<code>intercept</code>	include an intercept in the model.
<code>add_zero_based</code>	also consider the 0-based regularization path in addition to the given starting points.
<code>cc</code>	cutoff constant for Tukey's bisquare $\rho$ function.
<code>eps</code>	numerical tolerance.

	<p><code>explore_solutions</code> number of solutions to compute up to the desired precision <code>eps</code>.</p> <p><code>explore_tol</code> numerical tolerance for exploring possible solutions. Should be (much) looser than <code>eps</code> to be useful.</p> <p><code>max_solutions</code> only retain up to <code>max_solutions</code> unique solutions per penalization level.</p> <p><code>comparison_tol</code> numeric tolerance to determine if two solutions are equal. The comparison is first done on the absolute difference in the value of the objective function at the solution. If this is less than <code>comparison_tol</code>, two solutions are deemed equal if the squared difference of the intercepts is less than <code>comparison_tol</code> and the squared <math>L_2</math> norm of the difference vector is less than <code>comparison_tol</code>.</p> <p><code>sparse</code> use sparse coefficient vectors.</p> <p><code>ncores</code> number of CPU cores to use in parallel. By default, only one CPU core is used. Not supported on all platforms, in which case a warning is given.</p> <p><code>algorithm_opts</code> options for the MM algorithm to compute estimates. See <a href="#">mm_algorithm_options()</a> for details.</p> <p><code>m-scale_bdp, m-scale_opts</code> options for the M-scale estimate used to standardize the predictors (if <code>standardize = TRUE</code>).</p>
<code>alpha</code>	elastic net penalty mixing parameter with $0 \leq \alpha \leq 1$ . <code>alpha = 1</code> is the LASSO penalty, and <code>alpha = 0</code> the Ridge penalty.
<code>alpha_preliminary</code>	alpha parameter for the preliminary estimate.
<code>exponent</code>	the exponent for computing the penalty loadings based on the preliminary estimate.

## Details

The built-in CV metrics are

"tau\_size"  $\tau$ -size of the prediction error, computed by [tau\\_size\(\)](#) (default).

"mape" Median absolute prediction error.

"rmspe" Root mean squared prediction error.

"auoc" Area under the receiver operator characteristic curve (actually 1 - AUROC). Only sensible for binary responses.

`adamest_cv()` is a convenience wrapper which performs 3 steps:

1. compute preliminary estimates via `regmest_cv(..., alpha = alpha_preliminary)`,
2. computes the penalty loadings from the estimate `beta` with best prediction performance by `adamest_loadings = 1 / abs(beta)^exponent`, and
3. compute the adaptive PENSE estimates via `regmest_cv(..., penalty_loadings = adamest_loadings)`.



```

# Visualize the prediction performance and coefficient path of
# the adaptive PENSE estimates (manual vs. automatic)
def.par <- par(no.readonly = TRUE)
layout(matrix(1:4, ncol = 2, byrow = TRUE))
plot(ada_convenience$preliminary)
plot(preliminary_estimate)
plot(ada_convenience)
plot(ada_manual)
par(def.par)

```

---

residuals.pense\_cvfit *Extract Residuals*

---

### Description

Extract residuals from a PENSE (or LS-EN) regularization path with hyper-parameters chosen by cross-validation.

### Usage

```

## S3 method for class 'pense_cvfit'
residuals(
  object,
  alpha = NULL,
  lambda = "min",
  se_mult = 1,
  exact = deprecated(),
  correction = deprecated(),
  ...
)

```

### Arguments

object	PENSE with cross-validated hyper-parameters to extract coefficients from.
alpha	Either a single number or NULL (default). If given, only fits with the given alpha value are considered. If lambda is a numeric value and object was fit with multiple <i>alpha</i> values and no value is provided, the first value in object\$alpha is used with a warning.
lambda	either a string specifying which penalty level to use ("min", "se", "{m}-se") or a single numeric value of the penalty parameter. See details.
se_mult	If lambda = "se", the multiple of standard errors to tolerate.
exact	deprecated. Always gives a warning if lambda is not part of the fitted sequence and coefficients are interpolated.
correction	defunct.
...	currently not used.

**Value**

a numeric vector of residuals for the given penalization level.

**Hyper-parameters**

If `lambda = "{m}-se"` and `object` contains fitted estimates for every penalization level in the sequence, use the fit the most parsimonious model with prediction performance statistically indistinguishable from the best model. This is determined to be the model with prediction performance within  $m * cv\_se$  from the best model. If `lambda = "se"`, the multiplier  $m$  is taken from `se_mult`.

By default all *alpha* hyper-parameters available in the fitted object are considered. This can be overridden by supplying one or multiple values in parameter `alpha`. For example, if `lambda = "1-se"` and `alpha` contains two values, the "1-SE" rule is applied individually for each `alpha` value, and the fit with the better prediction error is considered.

In case `lambda` is a number and `object` was fit for several *alpha* hyper-parameters, `alpha` must also be given, or the first value in `object$alpha` is used with a warning.

**See Also**

Other functions for extracting components: [coef.pense\\_cvfit\(\)](#), [coef.pense\\_fit\(\)](#), [predict.pense\\_cvfit\(\)](#), [predict.pense\\_fit\(\)](#), [residuals.pense\\_fit\(\)](#)

**Examples**

```
# Compute the LS-EN regularization path for Freeny's revenue data
# (see ?freeny)
data(freeny)
x <- as.matrix(freeny[, 2:5])

regpath <- elnet(x, freeny$y, alpha = 0.75)

# Predict the response using a specific penalization level
predict(regpath, newdata = freeny[1:5, 2:5],
        lambda = regpath$lambda[[1]][[10]])

# Extract the residuals at a certain penalization level
residuals(regpath, lambda = regpath$lambda[[1]][[5]])

# Select penalization level via cross-validation
set.seed(123)
cv_results <- elnet_cv(x, freeny$y, alpha = 0.5,
                      cv_repl = 10, cv_k = 4)

# Predict the response using the "best" penalization level
predict(cv_results, newdata = freeny[1:5, 2:5])

# Extract the residuals at the "best" penalization level
residuals(cv_results)
# Extract the residuals at a more parsimonious penalization level
residuals(cv_results, lambda = "1.5-se")
```



---

residuals.pense\_fit *Extract Residuals*

---

## Description

Extract residuals from a PENSE (or LS-EN) regularization path fitted by [pense\(\)](#), [regmest\(\)](#) or [elnet\(\)](#).

## Usage

```
## S3 method for class 'pense_fit'  
residuals(  
  object,  
  alpha = NULL,  
  lambda,  
  exact = deprecated(),  
  correction = deprecated(),  
  ...  
)
```

## Arguments

object	PENSE regularization path to extract residuals from.
alpha	Either a single number or NULL (default). If given, only fits with the given alpha value are considered. If object was fit with multiple alpha values, and no value is provided, the first value in object\$alpha is used with a warning.
lambda	a single number for the penalty level.
exact	defunct Always gives a warning if lambda is not part of the fitted sequence and coefficients need to be interpolated.
correction	defunct.
...	currently not used.

## Value

a numeric vector of residuals for the given penalization level.

## See Also

Other functions for extracting components: [coef.pense\\_cvfit\(\)](#), [coef.pense\\_fit\(\)](#), [predict.pense\\_cvfit\(\)](#), [predict.pense\\_fit\(\)](#), [residuals.pense\\_cvfit\(\)](#)

**Examples**

```

# Compute the LS-EN regularization path for Freeny's revenue data
# (see ?freeny)
data(freeny)
x <- as.matrix(freeny[, 2:5])

regpath <- elnet(x, freeny$y, alpha = 0.75)

# Predict the response using a specific penalization level
predict(regpath, newdata = freeny[1:5, 2:5],
        lambda = regpath$lambda[[1]][[10]])

# Extract the residuals at a certain penalization level
residuals(regpath, lambda = regpath$lambda[[1]][[5]])

# Select penalization level via cross-validation
set.seed(123)
cv_results <- elnet_cv(x, freeny$y, alpha = 0.5,
                      cv_repl = 10, cv_k = 4)

# Predict the response using the "best" penalization level
predict(cv_results, newdata = freeny[1:5, 2:5])

# Extract the residuals at the "best" penalization level
residuals(cv_results)
# Extract the residuals at a more parsimonious penalization level
residuals(cv_results, lambda = "1.5-se")

```

rho\_function

*List Available Rho Functions***Description**

List Available Rho Functions

**Usage**

rho\_function(rho)

**Arguments**rho            the name of the  $\rho$  function to check for existence.**Value**

if rho is missing returns a vector of supported  $\rho$  function names, otherwise the internal integer representation of the  $\rho$  function.

**See Also**

Other miscellaneous functions: [consistency\\_const\(\)](#)

---

starting_point	<i>Create Starting Points for the PENSE Algorithm</i>
----------------	---

---

**Description**

Create a starting point for starting the PENSE algorithm in [pense\(\)](#). Multiple starting points can be created by combining starting points via `c(starting_point_1, starting_point_2, ...)`.

**Usage**

```
starting_point(beta, intercept, lambda, alpha)

as_starting_point(object, specific = FALSE, ...)

## S3 method for class 'enpy_starting_points'
as_starting_point(object, specific = FALSE, ...)

## S3 method for class 'pense_fit'
as_starting_point(object, specific = FALSE, alpha, lambda, ...)

## S3 method for class 'pense_cvfit'
as_starting_point(
  object,
  specific = FALSE,
  alpha,
  lambda = c("min", "se"),
  se_mult = 1,
  ...
)
```

**Arguments**

beta	beta coefficients at the starting point. Can be a numeric vector, a sparse vector of class <a href="#">dsparseVector</a> , or a sparse matrix of class <a href="#">dgCMatrix</a> with a single column.
intercept	intercept coefficient at the starting point.
lambda	optionally either a string specifying which penalty level to use ("min" or "se") or a numeric vector of the penalty levels to extract from object. Penalization levels not present in object are ignored with a warning. If NULL, all estimates in object are extracted. If a numeric vector, alpha must be given and a single number.
alpha	optional value for the alpha hyper-parameter. If given, only estimates with matching alpha values are extracted. Values not present in object are ignored with a warning.

object	an object with estimates to use as starting points.
specific	whether the estimates should be used as starting points only at the penalization level they are computed for. Defaults to using the estimates as starting points for all penalization levels.
...	further arguments passed to or from other methods.
se_mult	If lambda = "se", the multiple of standard errors to tolerate.

### Details

A starting points can either be *shared*, i.e., used for every penalization level PENSE estimates are computed for, or *specific* to one penalization level. To create a specific starting point, provide the penalization parameters lambda and alpha. If lambda or alpha are missing, a shared starting point is created. Shared and specific starting points can all be combined into a single list of starting points, with `pense()` handling them correctly. Note that specific starting points will lead to the lambda value being added to the grid of penalization levels. See `pense()` for details.

Starting points computed via `enpy_initial_estimates()` are by default *shared* starting points but can be transformed to *specific* starting points via `as_starting_point(..., specific = TRUE)`.

When creating starting points from cross-validated fits, it is possible to extract only the estimate with best CV performance (lambda = "min"), or the estimate with CV performance statistically indistinguishable from the best performance (lambda = "se"). This is determined to be the estimate with prediction performance within `se_mult * cv_se` from the best model.

### Value

an object of type `starting_points` to be used as starting point for `pense()`.

### See Also

Other functions for initial estimates: `enpy_initial_estimates()`, `prinsens()`

---

summary.pense\_cvfit    *Summarize Cross-Validated PENSE Fit*

---

### Description

If lambda = "se" and object contains fitted estimates for every penalization level in the sequence, extract the coefficients of the most parsimonious model with prediction performance statistically indistinguishable from the best model. This is determined to be the model with prediction performance within `se_mult * cv_se` from the best model.

### Usage

```
## S3 method for class 'pense_cvfit'
summary(object, alpha, lambda = "min", se_mult = 1, ...)

## S3 method for class 'pense_cvfit'
print(x, alpha, lambda = "min", se_mult = 1, ...)
```

**Arguments**

object, x	an (adaptive) PENSE fit with cross-validation information.
alpha	Either a single number or missing. If given, only fits with the given alpha value are considered. If lambda is a numeric value and object was fit with multiple alpha values, the parameter alpha must not be missing.
lambda	either a string specifying which penalty level to use ("min", "se", "{x}-se") or a single numeric value of the penalty parameter. See details.
se_mult	If lambda = "se", the multiple of standard errors to tolerate.
...	ignored.

**See Also**

[prediction\\_performance\(\)](#) for information about the estimated prediction performance.

[coef.pense\\_cvfit\(\)](#) for extracting only the estimated coefficients.

Other functions for plotting and printing: [plot.pense\\_cvfit\(\)](#), [plot.pense\\_fit\(\)](#), [prediction\\_performance\(\)](#)

---

tau\_size

---

*Compute the Tau-Scale of Centered Values*


---

**Description**

Compute the  $\tau$ -scale without centering the values.

**Usage**

```
tau_size(x)
```

**Arguments**

x numeric values. Missing values are verbosely ignored.

**Value**

the  $\tau$  estimate of scale of centered values.

**See Also**

Other functions to compute robust estimates of location and scale: [mloc\(\)](#), [mlocscale\(\)](#), [mscale\(\)](#)

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