# Package: partition (via r-universe)

October 29, 2026

**Type** Package

**Title** Agglomerative Partitioning Framework for Dimension Reduction

**Version** 0.2.2

**Maintainer** Malcolm Barrett <malcolmbarrett@gmail.com>

**Description** A fast and flexible framework for agglomerative partitioning. 'partition' uses an approach called Direct-Measure-Reduce to create new variables that maintain the user-specified minimum level of information. Each reduced variable is also interpretable: the original variables map to one and only one variable in the reduced data set. 'partition' is flexible, as well: how variables are selected to reduce, how information loss is measured, and the way data is reduced can all be customized. 'partition' is based on the Partition framework discussed in Millstein et al. (2020) <doi:10.1093/bioinformatics/btz661>.

**License** MIT + file LICENSE

**URL** https://uscbiostats.github.io/partition/, https://github.com/USCbiostats/partition

**BugReports** https://github.com/USCbiostats/partition/issues

**Depends** R (>= 3.3.0)

**Imports** crayon, dplyr (>= 0.8.0), forcats, ggplot2 (>= 3.3.0), infotheo, magrittr, MASS, pillar, progress, purrr, Rcpp, rlang, stringr, tibble, tidyr (>= 1.0.0)

**Suggests** covr, genieclust, ggcorrplot, gtools, knitr, rmarkdown, spelling, testthat (>= 3.0.0)

**LinkingTo** Rcpp, RcppArmadillo

**VignetteBuilder** knitr

**Config/testthat/edition** 3

**Config/testthat/parallel** true

**Encoding** UTF-8

**Language** en-US

**LazyData** true

**RoxygenNote** 7.3.1

**NeedsCompilation** yes

**Author** Joshua Millstein [aut], Malcolm Barrett [aut, cre]
(<https://orcid.org/0000-0003-0299-5825>), Katelyn Queen [aut]
(<https://orcid.org/0000-0002-8070-3042>)

**Repository** https://cran.r-universe.dev

**Date/Publication** 2024-10-09 17:00:02 UTC

**RemoteUrl** https://github.com/cran/partition

**RemoteRef** HEAD

**RemoteSha** 12c9447aa6d9edc326bbd05ad4957cc440175e55

# Contents

as_director . . . 3
as_measure . . . 4
as_partition_step . . . 5
as_partitioner . . . 6
as_reducer . . . 7
baxter_data . . . 8
corr . . . 9
direct_distance . . . 9
direct_k_cluster . . . 10
filter_reduced . . . 11
icc . . . 12
is_partition . . . 13
is_partition_step . . . 13
is_partitioner . . . 14
map_partition . . . 14
mapping_key . . . 15
measure_icc . . . 16
measure_min_icc . . . 17
measure_min_r2 . . . 17
measure_std_mutualinfo . . . 18
measure_variance_explained . . . 19
mutual_information . . . 19
part_icc . . . 20
part_kmeans . . . 21
part_minr2 . . . 22
part_pc1 . . . 23
part_stdmi . . . 24
partition . . . 25
partition_scores . . . 27
permute_df . . . 28

plot_area_clusters . . . . . 28
plot_permutation . . . . . 30
reduce_cluster . . . . . 31
reduce_first_component . . . . . 32
reduce_kmeans . . . . . 32
reduce_scaled_mean . . . . . 33
replace_partitioner . . . . . 34
scaled_mean . . . . . 34
simulate_block_data . . . . . 35
super_partition . . . . . 36
test_permutation . . . . . 38

**Index** **39**

---

`as_director` *Create a custom director*

---

## Description

Directors are functions that tell the partition algorithm what to try to reduce. `as_director()` is a helper function to create new directors to be used in `partitioners`. `partitioners` can be created with `as_partitioner()`.

## Usage

```
as_director(.pairs, .target, ...)
```

## Arguments

| | |
|---|---|
| `.pairs` | a function that returns a matrix of targets (e.g. a distance matrix of variables) |
| `.target` | a function that returns a vector of targets (e.g. the minimum pair) |
| `...` | Extra arguments passed to `.f`. |

## Value

a function to use in `as_partitioner()`

## See Also

Other directors: `direct_distance()`, `direct_k_cluster()`

## Examples

```
# use euclidean distance to calculate distances
euc_dist <- function(.data) as.matrix(dist(t(.data)))

# find the pair with the minimum distance
min_dist <- function(.x) {
  indices <- arrayInd(which.min(.x), dim(as.matrix(.x)))

  #  get variable names with minimum distance
  c(
    colnames(.x)[indices[1]],
    colnames(.x)[indices[2]]
  )
}

as_director(euc_dist, min_dist)
```

---

# as_measure *Create a custom metric*

---

## Description

Metrics are functions that tell how much information would be lost for a given reduction in the data. reduce. as_measure() is a helper function to create new metrics to be used in partitioners. partitioners can be created with as_partitioner().

## Usage

```
as_measure(.f, ...)
```

## Arguments

| | |
|---|---|
| .f | a function that returns either a numeric vector or a data.frame |
| ... | Extra arguments passed to .f. |

## Value

a function to use in as_partitioner()

## See Also

Other metrics: measure_icc(), measure_min_icc(), measure_min_r2(), measure_std_mutualinfo(), measure_variance_explained()

Other metrics: measure_icc(), measure_min_icc(), measure_min_r2(), measure_std_mutualinfo(), measure_variance_explained()

## Examples

```
inter_item_reliability <- function(mat) {
  corrs <- corr(mat)
  corrs[lower.tri(corrs, diag = TRUE)] <- NA

  corrs %>%
    colMeans(na.rm = TRUE) %>%
    mean(na.rm = TRUE)
}

measure_iir <- as_measure(inter_item_reliability)
measure_iir
```

---

# as_partition_step *Create a partition object from a data frame*

---

## Description

`as_partition_step()` creates a `partition_step` object. `partition_steps` are used while iterating through the partition algorithm: it stores necessary information about how to proceed in the partitioning, such as the information threshold. `as_partition_step()` is primarily called internally by `partition()` but can be helpful while developing `partitioners`.

## Usage

```
as_partition_step(
  .x,
  threshold = NA,
  reduced_data = NA,
  target = NA,
  metric = NA,
  tolerance = 0.01,
  var_prefix = NA,
  partitioner = NA,
  ...
)
```

## Arguments

| | |
|---|---|
| `.x` | a `data.frame` or `partition_step` object |
| `threshold` | The minimum information loss allowable |
| `reduced_data` | A data set with reduced variables |
| `target` | A character or integer vector: the variables to reduce |
| `metric` | A measure of information |
| `tolerance` | A tolerance around the threshold to accept a reduction |

| | |
|---|---|
| var_prefix | Variable name for reduced variables |
| partitioner | A partitioner, a part_*() function or one created with as_partitioner(). |
| ... | Other objects to store during the partition step |

## Value

a partition_step object

## Examples

```
.df <- data.frame(x = rnorm(100), y = rnorm(100))
as_partition_step(.df, threshold = .6)
```

---

# as_partitioner *Create a partitioner*

---

## Description

Partitioners are functions that tell the partition algorithm 1) what to try to reduce 2) how to measure how much information is lost from the reduction and 3) how to reduce the data. In partition, functions that handle 1) are called directors, functions that handle 2) are called metrics, and functions that handle 3) are called reducers. partition has a number of pre-specified partitioners for agglomerative data reduction. Custom partitioners can be created with as_partitioner().

Pass partitioner objects to the partitioner argument of partition().

## Usage

```
as_partitioner(direct, measure, reduce)
```

## Arguments

| | |
|---|---|
| direct | a function that directs, possibly created by as_director() |
| measure | a function that measures, possibly created by as_measure() |
| reduce | a function that reduces, possibly created by as_reducer() |

## Value

a partitioner

## See Also

Other partitioners: part_icc(), part_kmeans(), part_minr2(), part_pc1(), part_stdmi(), replace_partitioner()

## Examples

```
as_partitioner(
  direct = direct_distance_pearson,
  measure = measure_icc,
  reduce = reduce_scaled_mean
)
```

---

# as_reducer *Create a custom reducer*

---

## Description

Reducers are functions that tell the partition algorithm how to reduce the data. `as_reducer()` is a helper function to create new reducers to be used in `partitioners`. `partitioners` can be created with `as_partitioner()`.

## Usage

```
as_reducer(.f, ..., returns_vector = TRUE, first_match = NULL)
```

## Arguments

| | |
|---|---|
| `.f` | a function that returns either a numeric vector or a `data.frame` |
| `...` | Extra arguments passed to `.f`. |
| `returns_vector` | logical. Does `.f` return a vector? `TRUE` by default. If `FALSE`, assumes that `.f` returns a `data.frame`. |
| `first_match` | logical. Should the partition algorithm stop when it finds a reduction that is equal to the threshold? Default is `TRUE` for reducers that return a `data.frame` and `FALSE` for reducers that return a vector |

## Value

a function to use in `as_partitioner()`

## See Also

Other reducers: `reduce_first_component()`, `reduce_kmeans()`, `reduce_scaled_mean()`

Other reducers: `reduce_first_component()`, `reduce_kmeans()`, `reduce_scaled_mean()`

## Examples

```
reduce_row_means <- as_reducer(rowMeans)
reduce_row_means
```

baxter_data *Microbiome data*

## Description

Clinical and microbiome data derived from "Microbiota-based model improves the sensitivity of fecal immunochemical test for detecting colonic lesions" by Baxter et al. (2016). These data represent a subset of 172 health participants. `baxter_clinical` contains 8 clinical variables for each of the participants: `sample_name`, `id`, `age`, `bmi`, `gender`, `height`, `total_reads`, and `disease_state` (all `H` for healthy). `baxter_otu` has 1,234 columns, where each columns represent an Operational Taxonomic Unit (OTU). OTUs are species-like relationships among bacteria determined by analyzing their RNA. The cells are logged counts for how often the OTU was detected in a participant's stool sample. Each column name is a shorthand name, e.g. `otu1`; you can find the true name of the OTU mapped in `baxter_data_dictionary`. `baxter_family` and `baxter_genus` are also logged counts but instead group OTUs at the family and genus level, respectively, a common approach to reducing microbiome data. Likewise, the column names are shorthands, which you can find mapped in `baxter_data_dictionary`.

## Usage

```
baxter_clinical

baxter_otu

baxter_family

baxter_genus

baxter_data_dictionary
```

## Format

5 data frames

An object of class `tbl_df` (inherits from `tbl`, `data.frame`) with 172 rows and 1234 columns.

An object of class `tbl_df` (inherits from `tbl`, `data.frame`) with 172 rows and 35 columns.

An object of class `tbl_df` (inherits from `tbl`, `data.frame`) with 172 rows and 82 columns.

An object of class `tbl_df` (inherits from `tbl`, `data.frame`) with 1351 rows and 3 columns.

## Source

Baxter et al. (2016) doi:10.1186/s1307301602903

## corr *Efficiently fit correlation coefficient for matrix or two vectors*

### Description

Efficiently fit correlation coefficient for matrix or two vectors

### Usage

```
corr(x, y = NULL, spearman = FALSE)
```

### Arguments

| | |
|---|---|
| x | a matrix or vector |
| y | a vector. Optional. |
| spearman | Logical. Use Spearman's correlation? |

### Value

a numeric vector, the correlation coefficient

### Examples

```
library(dplyr)
# fit for entire data set
iris %>%
  select_if(is.numeric) %>%
  corr()

# just fit for two vectors
corr(iris$Sepal.Length, iris$Sepal.Width)
```

## direct_distance *Target based on minimum distance matrix*

### Description

Directors are functions that tell the partition algorithm what to try to reduce. as_director() is a helper function to create new directors to be used in partitioners. partitioners can be created with as_partitioner().

direct_distance() fits a distance matrix using either Pearson's or Spearman's correlation and finds the pair with the smallest distance to target. If the distance matrix already exists, direct_distance() only fits the distances for any new reduced variables. direct_distance_pearson() and direct_distance_spearman() are convenience functions that directly call the type of distance matrix.

## Usage

```
direct_distance(.partition_step, spearman = FALSE)

direct_distance_pearson(.partition_step)

direct_distance_spearman(.partition_step)
```

## Arguments

| | |
|---|---|
| .partition_step | a partition_step object |
| spearman | Logical. Use Spearman's correlation? |

## Value

a partition_step object

## See Also

Other directors: as_director(), direct_k_cluster()

---

# direct_k_cluster *Target based on K-means clustering*

---

## Description

Directors are functions that tell the partition algorithm what to try to reduce. as_director() is a helper function to create new directors to be used in partitioners. partitioners can be created with as_partitioner().

direct_k_cluster() assigns each variable to a cluster using K-means. As the partition looks for the best reduction, direct_k_cluster() iterates through values of k to assign clusters. This search is handled by the binary search method by default and thus does not necessarily need to fit every value of k.

## Usage

```
direct_k_cluster(
  .partition_step,
  algorithm = c("armadillo", "Hartigan-Wong", "Lloyd", "Forgy", "MacQueen"),
  search = c("binary", "linear"),
  init_k = NULL,
  seed = 1L
)
```

### Arguments

| | |
|---|---|
| .partition_step | a partition_step object |
| algorithm | The K-Means algorithm to use. The default is a fast version of the LLoyd algorithm written in armadillo. The rest are options in kmeans(). In general, armadillo is fastest, but the other algorithms can be faster in high dimensions. |
| search | The search method. Binary search is generally more efficient but linear search can be faster in very low dimensions. |
| init_k | The initial k to test. If NULL, then the initial k is the threshold times the number of variables. |
| seed | The seed to set for reproducibility |

### Value

a partition_step object

### See Also

Other directors: as_director(), direct_distance()

---

## filter_reduced *Filter the reduced mappings*

---

### Description

filter_reduced() and unnest_reduced() are convenience functions to quickly retrieve the mappings for only the reduced variables. filter_reduced() returns a nested tibble while unnest_reduced() unnests it.

### Usage

```
filter_reduced(.partition)

unnest_reduced(.partition)
```

### Arguments

| | |
|---|---|
| .partition | a partition object |

### Value

a tibble with mapping key

## Examples

```
set.seed(123)
df <- simulate_block_data(c(3, 4, 5), lower_corr = .4, upper_corr = .6, n = 100)
# fit partition
prt <- partition(df, threshold = .6)


# A tibble: 3 x 4
filter_reduced(prt)

# A tibble: 9 x 4
unnest_reduced(prt)
```

---

# icc *Calculate the intraclass correlation coefficient*

---

## Description

`icc()` efficiently calculates the ICC for a numeric data set.

## Usage

```
icc(.x, method = c("r", "c"))
```

## Arguments

| | |
|---|---|
| `.x` | a data set |
| `method` | The method source: both the pure R and C++ versions are efficient |

## Value

a numeric vector of length 1

## Examples

```
library(dplyr)
iris %>%
  select_if(is.numeric) %>%
  icc()
```

## is_partition *Is this object a partition?*

### Description

Is this object a partition?

### Usage

```
is_partition(x)
```

### Arguments

| | |
|---|---|
| x | an object to be tested |

### Value

logical: TRUE or FALSE

## is_partition_step *Is this object a* partition_step*?*

### Description

Is this object a partition_step?

### Usage

```
is_partition_step(x)
```

### Arguments

| | |
|---|---|
| x | an object to be tested |

### Value

logical: TRUE or FALSE

## is_partitioner *Is this object a partitioner?*

### Description

Is this object a partitioner?

### Usage

```
is_partitioner(x)
```

### Arguments

| | |
|---|---|
| x | an object to be tested |

### Value

logical: TRUE or FALSE

## map_partition *Map a partition across a range of minimum information*

### Description

map_partition() fits partition() across a range of minimum information values, specified in the information argument. The output is a tibble with a row for each value of information, a summary of the partition, and a list-col containing the partition object.

### Usage

```
map_partition(
  .data,
  partitioner = part_icc(),
  ...,
  information = seq(0.1, 0.5, by = 0.1)
)
```

### Arguments

| | |
|---|---|
| .data | a data set to partition |
| partitioner | the partitioner to use. The default is part_icc(). |
| ... | arguments passed to partition() |
| information | a vector of minimum information to fit in partition() |

## Value

a tibble

## Examples

```
set.seed(123)
df <- simulate_block_data(c(3, 4, 5), lower_corr = .4, upper_corr = .6, n = 100)

map_partition(df, partitioner = part_pc1())
```

---

`mapping_key` *Return partition mapping key*

---

## Description

`mapping_key()` returns a data frame with each reduced variable and its mapping and information loss; the mapping and indices are represented as `list-cols` (so there is one row per variable in the reduced data set). `unnest_mappings()` unnests the list columns to return a tidy data frame. `mapping_groups()` returns a list of mappings (either the variable names or their column position).

## Usage

```
mapping_key(.partition)

unnest_mappings(.partition)

mapping_groups(.partition, indices = FALSE)
```

## Arguments

| | |
|---|---|
| `.partition` | a `partition` object |
| `indices` | logical. Return just the indices instead of the names? Default is `FALSE`. |

## Value

a `tibble`

## Examples

```
set.seed(123)
df <- simulate_block_data(c(3, 4, 5), lower_corr = .4, upper_corr = .6, n = 100)
# fit partition
prt <- partition(df, threshold = .6)

# tibble: 6 x 4
mapping_key(prt)
```

```
# tibble: 12 x 4
unnest_mappings(prt)

# list: length 6
mapping_groups(prt)
```

---

`measure_icc` *Measure the information loss of reduction using intraclass correlation coefficient*

---

## Description

Metrics are functions that tell how much information would be lost for a given reduction in the data. reduce. `as_measure()` is a helper function to create new metrics to be used in `partitioners`. `partitioners` can be created with `as_partitioner()`.

`measure_icc()` assesses information loss by calculating the intraclass correlation coefficient for the target variables.

## Usage

```
measure_icc(.partition_step)
```

## Arguments

| | |
|---|---|
| `.partition_step` | a `partition_step` object |

## Value

a `partition_step` object

## See Also

Other metrics: `as_measure()`, `measure_min_icc()`, `measure_min_r2()`, `measure_std_mutualinfo()`, `measure_variance_explained()`

## measure_min_icc *Measure the information loss of reduction using the minimum intra-class correlation coefficient*

### Description

Metrics are functions that tell how much information would be lost for a given reduction in the data. reduce. `as_measure()` is a helper function to create new metrics to be used in `partitioners`. `partitioners` can be created with `as_partitioner()`.

`measure_min_icc()` assesses information loss by calculating the intraclass correlation coefficient for each set of the target variables and finding their minimum.

### Usage

```
measure_min_icc(.partition_step, search_method = c("binary", "linear"))
```

### Arguments

| | |
|---|---|
| `.partition_step` | a `partition_step` object |
| `search_method` | The search method. Binary search is generally more efficient but linear search can be faster in very low dimensions. |

### Value

a `partition_step` object

### See Also

Other metrics: `as_measure()`, `measure_icc()`, `measure_min_r2()`, `measure_std_mutualinfo()`, `measure_variance_explained()`

## measure_min_r2 *Measure the information loss of reduction using minimum R-squared*

### Description

Metrics are functions that tell how much information would be lost for a given reduction in the data. reduce. `as_measure()` is a helper function to create new metrics to be used in `partitioners`. `partitioners` can be created with `as_partitioner()`.

`measure_min_r2()` assesses information loss by calculating the minimum R-squared for the target variables.

### Usage

```
measure_min_r2(.partition_step)
```

### Arguments

.partition_step
: a partition_step object

### Value

a partition_step object

### See Also

Other metrics: as_measure(), measure_icc(), measure_min_icc(), measure_std_mutualinfo(), measure_variance_explained()

---

## measure_std_mutualinfo

*Measure the information loss of reduction using standardized mutual information*

---

### Description

Metrics are functions that tell how much information would be lost for a given reduction in the data. reduce. as_measure() is a helper function to create new metrics to be used in partitioners. partitioners can be created with as_partitioner().

measure_std_mutualinfo() assesses information loss by calculating the standardized mutual information for the target variables. See mutual_information().

### Usage

```
measure_std_mutualinfo(.partition_step)
```

### Arguments

.partition_step
: a partition_step object

### Value

a partition_step object

### See Also

Other metrics: as_measure(), measure_icc(), measure_min_icc(), measure_min_r2(), measure_variance_explained

## measure_variance_explained *Measure the information loss of reduction using the variance explained.*

### Description

Metrics are functions that tell how much information would be lost for a given reduction in the data. reduce. `as_measure()` is a helper function to create new metrics to be used in `partitioners`. `partitioners` can be created with `as_partitioner()`.

`measure_variance_explained()` assesses information loss by calculating the variance explained by the first component of a principal components analysis. Because the PCA calculates the components and the variance explained at the same time, if the reducer is `reduce_first_component()`, then `measure_variance_explained()` will store the first component for later use to avoid recalculation.

### Usage

```
measure_variance_explained(.partition_step)
```

### Arguments

| | |
|---|---|
| `.partition_step` | a `partition_step` object |

### Value

a `partition_step` object

### See Also

Other metrics: `as_measure()`, `measure_icc()`, `measure_min_icc()`, `measure_min_r2()`, `measure_std_mutualinfo()`

## mutual_information *Calculate the standardized mutual information of a data set*

### Description

`mutual_information` calculate the standardized mutual information of a data set using the `infotheo` package.

### Usage

```
mutual_information(.data)
```

### Arguments

| | |
|---|---|
| .data | a dataframe of numeric values |

### Value

a list containing the standardized MI and the scaled row means

### Examples

```
library(dplyr)
iris %>%
  select_if(is.numeric) %>%
  mutual_information()
```

---

## part_icc *Partitioner: distance, ICC, scaled means*

---

### Description

Partitioners are functions that tell the partition algorithm 1) what to try to reduce 2) how to measure how much information is lost from the reduction and 3) how to reduce the data. In partition, functions that handle 1) are called directors, functions that handle 2) are called metrics, and functions that handle 3) are called reducers. partition has a number of pre-specified partitioners for agglomerative data reduction. Custom partitioners can be created with `as_partitioner()`.

Pass `partitioner` objects to the `partitioner` argument of `partition()`.

`part_icc()` uses the following direct-measure-reduce approach:

- **direct**: `direct_distance()`, Minimum Distance
- **measure**: `measure_icc()`, Intraclass Correlation
- **reduce**: `reduce_scaled_mean()`, Scaled Row Means

### Usage

```
part_icc(spearman = FALSE)
```

### Arguments

| | |
|---|---|
| spearman | logical. Use Spearman's correlation for distance matrix? |

### Value

a `partitioner`

### See Also

Other partitioners: `as_partitioner()`, `part_kmeans()`, `part_minr2()`, `part_pc1()`, `part_stdmi()`, `replace_partitioner()`

## Examples

```
set.seed(123)
df <- simulate_block_data(c(3, 4, 5), lower_corr = .4, upper_corr = .6, n = 100)

# fit partition using part_icc()
partition(df, threshold = .6, partitioner = part_icc())
```

---

`part_kmeans` *Partitioner: K-means, ICC, scaled means*

---

## Description

Partitioners are functions that tell the partition algorithm 1) what to try to reduce 2) how to measure how much information is lost from the reduction and 3) how to reduce the data. In partition, functions that handle 1) are called directors, functions that handle 2) are called metrics, and functions that handle 3) are called reducers. partition has a number of pre-specified partitioners for agglomerative data reduction. Custom partitioners can be created with `as_partitioner()`.

Pass `partitioner` objects to the `partitioner` argument of `partition()`.

`part_kmeans()` uses the following direct-measure-reduce approach:

- **direct**: `direct_k_cluster()`, K-Means Clusters
- **measure**: `measure_min_icc()`, Minimum Intraclass Correlation
- **reduce**: `reduce_kmeans()`, Scaled Row Means

## Usage

```
part_kmeans(
  algorithm = c("armadillo", "Hartigan-Wong", "Lloyd", "Forgy", "MacQueen"),
  search = c("binary", "linear"),
  init_k = NULL,
  n_hits = 4
)
```

## Arguments

| | |
|---|---|
| `algorithm` | The K-Means algorithm to use. The default is a fast version of the LLoyd algorithm written in armadillo. The rest are options in `kmeans()`. In general, armadillo is fastest, but the other algorithms can be faster in high dimensions. |
| `search` | The search method. Binary search is generally more efficient but linear search can be faster in very low dimensions. |
| `init_k` | The initial k to test. If `NULL`, then the initial k is the threshold times the number of variables. |
| `n_hits` | In linear search method, the number of iterations that should be under the threshold before reducing; useful for preventing false positives. |

## Value

a partitioner

## See Also

Other partitioners: as_partitioner(), part_icc(), part_minr2(), part_pc1(), part_stdmi(), replace_partitioner()

## Examples

```
set.seed(123)
df <- simulate_block_data(c(3, 4, 5), lower_corr = .4, upper_corr = .6, n = 100)

# fit partition using part_kmeans()
partition(df, threshold = .6, partitioner = part_kmeans())
```

---

# part_minr2 *Partitioner: distance, minimum R-squared, scaled means*

---

## Description

Partitioners are functions that tell the partition algorithm 1) what to try to reduce 2) how to measure how much information is lost from the reduction and 3) how to reduce the data. In partition, functions that handle 1) are called directors, functions that handle 2) are called metrics, and functions that handle 3) are called reducers. partition has a number of pre-specified partitioners for agglomerative data reduction. Custom partitioners can be created with as_partitioner().

Pass partitioner objects to the partitioner argument of partition().

part_minr2() uses the following direct-measure-reduce approach:

- **direct**: direct_distance(), Minimum Distance
- **measure**: measure_min_r2(), Minimum R-Squared
- **reduce**: reduce_scaled_mean(), Scaled Row Means

## Usage

```
part_minr2(spearman = FALSE)
```

## Arguments

| | |
|---|---|
| spearman | logical. Use Spearman's correlation for distance matrix? |

## Value

a partitioner

## See Also

Other partitioners: as_partitioner(), part_icc(), part_kmeans(), part_pc1(), part_stdmi(), replace_partitioner()

## Examples

```
set.seed(123)
df <- simulate_block_data(c(3, 4, 5), lower_corr = .4, upper_corr = .6, n = 100)

# fit partition using part_minr2()
partition(df, threshold = .6, partitioner = part_minr2())
```

---

# part_pc1 *Partitioner: distance, first principal component, scaled means*

---

## Description

Partitioners are functions that tell the partition algorithm 1) what to try to reduce 2) how to measure how much information is lost from the reduction and 3) how to reduce the data. In partition, functions that handle 1) are called directors, functions that handle 2) are called metrics, and functions that handle 3) are called reducers. partition has a number of pre-specified partitioners for agglomerative data reduction. Custom partitioners can be created with as_partitioner().

Pass partitioner objects to the partitioner argument of partition().

part_pc1() uses the following direct-measure-reduce approach:

- **direct**: direct_distance(), Minimum Distance
- **measure**: measure_variance_explained(), Variance Explained (PCA)
- **reduce**: reduce_first_component(), First Principal Component

## Usage

```
part_pc1(spearman = FALSE)
```

## Arguments

| | |
|---|---|
| spearman | logical. Use Spearman's correlation for distance matrix? |

## Value

a partitioner

## See Also

Other partitioners: as_partitioner(), part_icc(), part_kmeans(), part_minr2(), part_stdmi(), replace_partitioner()

## Examples

```
set.seed(123)
df <- simulate_block_data(c(3, 4, 5), lower_corr = .4, upper_corr = .6, n = 100)

# fit partition using part_pc1()
partition(df, threshold = .6, partitioner = part_pc1())
```

---

`part_stdmi` *Partitioner: distance, mutual information, scaled means*

---

## Description

Partitioners are functions that tell the partition algorithm 1) what to try to reduce 2) how to measure how much information is lost from the reduction and 3) how to reduce the data. In partition, functions that handle 1) are called directors, functions that handle 2) are called metrics, and functions that handle 3) are called reducers. partition has a number of pre-specified partitioners for agglomerative data reduction. Custom partitioners can be created with `as_partitioner()`.

Pass `partitioner` objects to the `partitioner` argument of `partition()`.

`part_stdmi()` uses the following direct-measure-reduce approach:

- **direct**: `direct_distance()`, Minimum Distance
- **measure**: `measure_std_mutualinfo()`, Standardized Mutual Information
- **reduce**: `reduce_scaled_mean()`, Scaled Row Means

## Usage

```
part_stdmi(spearman = FALSE)
```

## Arguments

| | |
|---|---|
| `spearman` | logical. Use Spearman's correlation for distance matrix? |

## Value

a `partitioner`

## See Also

Other partitioners: `as_partitioner()`, `part_icc()`, `part_kmeans()`, `part_minr2()`, `part_pc1()`, `replace_partitioner()`

## Examples

```
set.seed(123)
df <- simulate_block_data(c(3, 4, 5), lower_corr = .4, upper_corr = .6, n = 100)

# fit partition using part_stdmi()
partition(df, threshold = .6, partitioner = part_stdmi())
```

---

`partition` *Agglomerative partitioning*

---

## Description

`partition()` reduces data while minimizing information loss using an agglomerative partitioning algorithm. The partition algorithm is fast and flexible: at every iteration, `partition()` uses an approach called Direct-Measure-Reduce (see Details) to create new variables that maintain the user-specified minimum level of information. Each reduced variable is also interpretable: the original variables map to one and only one variable in the reduced data set.

## Usage

```
partition(
  .data,
  threshold,
  partitioner = part_icc(),
  tolerance = 1e-04,
  niter = NULL,
  x = "reduced_var",
  .sep = "_"
)
```

## Arguments

| | |
|---|---|
| `.data` | a data.frame to partition |
| `threshold` | the minimum proportion of information explained by a reduced variable; `threshold` sets a boundary for information loss because each reduced variable must explain at least as much as `threshold` as measured by the metric. |
| `partitioner` | a `partitioner`. See the `part_*()` functions and `as_partitioner()`. |
| `tolerance` | a small tolerance within the threshold; if a reduction is within the threshold plus/minus the tolerance, it will reduce. |
| `niter` | the number of iterations. By default, it is calculated as 20% of the number of variables or 10, whichever is larger. |
| `x` | the prefix of the new variable names |
| `.sep` | a character vector that separates `x` from the number (e.g. "reduced_var_1"). |

## Details

`partition()` uses an approach called Direct-Measure-Reduce. Directors tell the partition algorithm what to reduce, metrics tell it whether or not there will be enough information left after the reduction, and reducers tell it how to reduce the data. Together these are called a partitioner. The default partitioner for `partition()` is `part_icc()`: it finds pairs of variables to reduce by finding the pair with the minimum distance between them, it measures information loss through ICC, and it reduces data using scaled row means. There are several other partitioners available (`part_*()` functions), and you can create custom partitioners with `as_partitioner()` and `replace_partitioner()`.

## Value

a `partition` object

## References

Millstein, Joshua, Francesca Battaglin, Malcolm Barrett, Shu Cao, Wu Zhang, Sebastian Stintzing, Volker Heinemann, and Heinz-Josef Lenz. 2020. "Partition: A Surjective Mapping Approach for Dimensionality Reduction." *Bioinformatics* 36 (3): https://doi.org/676–81.10.1093/bioinformatics/btz661.

Barrett, Malcolm and Joshua Millstein (2020). partition: A fast and flexible framework for data reduction in R. Journal of Open Source Software, 5(47), 1991, https://doi.org/10.21105/joss.01991

## See Also

`part_icc()`, `part_kmeans()`, `part_minr2()`, `part_pc1()`, `part_stdmi()`, `as_partitioner()`, `replace_partitioner()`

## Examples

```
set.seed(123)
df <- simulate_block_data(c(3, 4, 5), lower_corr = .4, upper_corr = .6, n = 100)

#  don't accept reductions where information < .6
prt <- partition(df, threshold = .6)
prt

# return reduced data
partition_scores(prt)

# access mapping keys
mapping_key(prt)
unnest_mappings(prt)

# use a lower threshold of information loss
partition(df, threshold = .5, partitioner = part_kmeans())

# use a custom partitioner
part_icc_rowmeans <- replace_partitioner(part_icc, reduce = as_reducer(rowMeans))
partition(df, threshold = .6, partitioner = part_icc_rowmeans)
```

partition_scores *Return the reduced data from a partition*

## Description

The reduced data is stored as `reduced_data` in the partition object and can thus be returned by subsetting `object$reduced_data`. Alternatively, the functions `partition_score()` and `fitted()` also return the reduced data.

## Usage

```
partition_scores(object, ...)

## S3 method for class 'partition'
fitted(object, ...)
```

## Arguments

| | |
|---|---|
| `object` | a `partition` object |
| `...` | not currently used (for S3 consistency with `fitted()`) |

## Value

a tibble containing the reduced data for the partition

## Examples

```
set.seed(123)
df <- simulate_block_data(c(3, 4, 5), lower_corr = .4, upper_corr = .6, n = 100)
# fit partition
prt <- partition(df, threshold = .6)


# three ways to retrieve reduced data
partition_scores(prt)
fitted(prt)
prt$reduced_data
```

## permute_df *Permute a data set*

### Description

permute_df() permutes a data set: it randomizes the order within each variable, which breaks any association between them. Permutation is useful for testing against null statistics.

### Usage

```
permute_df(.data)
```

### Arguments

| | |
|---|---|
| .data | a data.frame |

### Value

a permuted data.frame

### Examples

```
permute_df(iris)
```

## plot_area_clusters *Plot partitions*

### Description

plot_stacked_area_clusters() and plot_area_clusters() plot the partition against a permuted partition. plot_ncluster() plots the number of variables per cluster. If .partition is the result of map_partition() or test_permutation(), plot_ncluster() facets the plot by each partition. plot_information() plots a histogram or density plot of the information of each variable in the partition. If .partition is the result of map_partition() or test_permutation(), plot_information() plots a scatterplot of the targeted vs. observed information with a 45 degree line indicating perfect alignment.

### Usage

```
plot_area_clusters(
  .data,
  partitioner = part_icc(),
  information = seq(0.1, 0.5, length.out = 25),
  ...,
  obs_color = "#E69F00",
  perm_color = "#56B4E9"
```

```
)

plot_stacked_area_clusters(
  .data,
  partitioner = part_icc(),
  information = seq(0.1, 0.5, length.out = 25),
  ...,
 stack_colors = c("#E69F00", "#56B4E9", "#009E73", "#F0E442", "#0072B2", "#D55E00")
)

plot_ncluster(
  .partition,
  show_n = 100,
  fill = "#0172B1",
  color = NA,
  labeller = "target information:"
)

plot_information(
  .partition,
  fill = "#0172B1",
  color = NA,
  geom = ggplot2::geom_density
)
```

## Arguments

| | |
|---|---|
| .data | a data.frame to partition |
| partitioner | a partitioner. See the part_*() functions and as_partitioner(). |
| information | a vector of minimum information to fit in partition() |
| ... | arguments passed to partition() |
| obs_color | the color of the observed partition |
| perm_color | the color of the permuted partition |
| stack_colors | the colors of the cluster sizes |
| .partition | either a partition or a tibble, the result of map_partition() or test_permutation() |
| show_n | the number of reduced variables to plot |
| fill | the color of the fill for geom |
| color | the color of the geom |
| labeller | the facet label |
| geom | the geom to use. The default is geom_density. |

## Value

a ggplot

## Examples

```
set.seed(123)
df <- simulate_block_data(c(3, 4, 5), lower_corr = .4, upper_corr = .6, n = 100)

df %>%
  partition(.6, partitioner = part_pc1()) %>%
  plot_ncluster()
```

---

`plot_permutation` *Plot permutation tests*

---

## Description

`plot_permutation()` takes the results of `test_permutation()` and plots the distribution of permuted partitions compared to the observed partition.

## Usage

```
plot_permutation(
  permutations,
  .plot = c("information", "nclusters", "nreduced"),
  labeller = "target information:",
  perm_color = "#56B4EA",
  obs_color = "#CC78A8",
  geom = ggplot2::geom_density
)
```

## Arguments

| | |
|---|---|
| `permutations` | a `tibble`, the result of `test_permutation()` |
| `.plot` | the variable to plot: observed information, the number of clusters created, or the number of observed variables reduced |
| `labeller` | the facet label |
| `perm_color` | the color of the permutation fill |
| `obs_color` | the color of the observed statistic line |
| `geom` | the `geom` to use. The default is `geom_density`. |

## Value

a ggplot

reduce_cluster *Reduce a target*

## Description

reduce_cluster() and map_cluster() apply the data reduction to the targets found in the director step. They only do so if the metric is above the threshold, however. reduce_cluster() is for functions that return vectors while map_cluster() is for functions that return data.frames. If you're using as_reducer(), there's no need to call these functions directly.

## Usage

```
reduce_cluster(.partition_step, .f, first_match = FALSE)

map_cluster(.partition_step, .f, rewind = FALSE, first_match = FALSE)
```

## Arguments

| | |
|---|---|
| .partition_step | a partition_step object |
| .f | a function to reduce the data to either a vector or a data.frame |
| first_match | logical. Should the partition algorithm stop when it finds a reduction that is equal to the threshold? Default is TRUE for reducers that return a data.frame and FALSE for reducers that return a vector |
| rewind | logical. Should the last target be used instead of the current target? |

## Value

a partition_step object

## Examples

```
reduce_row_means <- function(.partition_step, .data) {
  reduce_cluster(.partition_step, rowMeans)
}

replace_partitioner(
  part_icc,
  reduce = reduce_row_means
)
```

## reduce_first_component *Reduce selected variables to first principal component*

### Description

Reducers are functions that tell the partition algorithm how to reduce the data. as_reducer() is a helper function to create new reducers to be used in partitioners. partitioners can be created with as_partitioner().

reduce_first_component() returns the first component from the principal components analysis of the target variables. Because the PCA calculates the components and the variance explained at the same time, if the metric is measure_variance_explained(), that function will store the first component for use in reduce_first_component() to avoid recalculation. If the partitioner uses a different metric, the first component will be calculated by reduce_first_component().

### Usage

```
reduce_first_component(.partition_step)
```

### Arguments

.partition_step
: a partition_step object

### Value

a partition_step object

### See Also

Other reducers: as_reducer(), reduce_kmeans(), reduce_scaled_mean()

## reduce_kmeans *Reduce selected variables to scaled means*

### Description

Reducers are functions that tell the partition algorithm how to reduce the data. as_reducer() is a helper function to create new reducers to be used in partitioners. partitioners can be created with as_partitioner().

reduce_kmeans() is efficient in that it doesn't reduce until the closest k to the information threshold is found.

### Usage

```
reduce_kmeans(.partition_step, search = c("binary", "linear"), n_hits = 4)
```

### Arguments

| | |
|---|---|
| .partition_step | a partition_step object |
| search | The search method. Binary search is generally more efficient but linear search can be faster in very low dimensions. |
| n_hits | In linear search method, the number of iterations that should be under the threshold before reducing; useful for preventing false positives. |

### Value

a partition_step object

### See Also

Other reducers: as_reducer(), reduce_first_component(), reduce_scaled_mean()

---

## reduce_scaled_mean *Reduce selected variables to scaled means*

---

### Description

Reducers are functions that tell the partition algorithm how to reduce the data. as_reducer() is a helper function to create new reducers to be used in partitioners. partitioners can be created with as_partitioner().

reduce_scaled_mean() returns the scaled row means of the target variables to reduce.

### Usage

```
reduce_scaled_mean(.partition_step)
```

### Arguments

| | |
|---|---|
| .partition_step | a partition_step object |

### Value

a partition_step object

### See Also

Other reducers: as_reducer(), reduce_first_component(), reduce_kmeans()

## replace_partitioner *Replace the director, metric, or reducer for a partitioner*

### Description

Replace the director, metric, or reducer for a partitioner

### Usage

```
replace_partitioner(partitioner, direct = NULL, measure = NULL, reduce = NULL)
```

### Arguments

| | |
|---|---|
| partitioner | a partitioner |
| direct | a function that directs, possibly created by as_director() |
| measure | a function that measures, possibly created by as_measure() |
| reduce | a function that reduces, possibly created by as_reducer() |

### Value

a partitioner

### See Also

Other partitioners: as_partitioner(), part_icc(), part_kmeans(), part_minr2(), part_pc1(), part_stdmi()

### Examples

```
replace_partitioner(
  part_icc,
  reduce = as_reducer(rowMeans)
)
```

## scaled_mean *Average and scale rows in a* data.frame

### Description

scaled_mean() calculates scaled row means for a dataframe.

### Usage

```
scaled_mean(.x, method = c("r", "c"))
```

### Arguments

| | |
|---|---|
| .x | a data.frame |
| method | The method source: both the pure R and C++ versions are efficient |

### Value

a numeric vector

### Examples

```
library(dplyr)
iris %>%
  select_if(is.numeric) %>%
  scaled_mean()
```

---

## simulate_block_data *Simulate correlated blocks of variables*

---

### Description

simulate_block_data() creates a dataset of blocks of data where variables within each block are correlated. The correlation for each pair of variables is sampled uniformly from lower_corr to upper_corr, and the values of each are sampled using MASS::mvrnorm().

### Usage

```
simulate_block_data(
  block_sizes,
  lower_corr,
  upper_corr,
  n,
  block_name = "block",
  sep = "_",
  var_name = "x"
)
```

### Arguments

| | |
|---|---|
| block_sizes | a vector of block sizes. The size of each block is the number of variables within it. |
| lower_corr | the lower bound of the correlation within each block |
| upper_corr | the upper bound of the correlation within each block |
| n | the number of observations or rows |
| block_name | description prepended to the variable to indicate the block it belongs to |
| sep | a character, what to separate the variable names with |
| var_name | the name of the variable within the block |

## Value

a tibble with sum(block_sizes) columns and n rows.

## Examples

```
# create a 100 x 15 data set with 3 blocks
simulate_block_data(
  block_sizes = rep(5, 3),
  lower_corr = .4,
  upper_corr = .6,
  n = 100
)
```

---

# super_partition *super_partition*

---

## Description

super_partition implements the agglomerative, data reduction method Partition for datasets with large numbers of features by first 'super-partitioning' the data into smaller clusters to Partition.

## Usage

```
super_partition(
  full_data,
  threshold = 0.5,
  cluster_size = 4000,
  partitioner = part_icc(),
  tolerance = 1e-04,
  niter = NULL,
  x = "reduced_var",
  .sep = "_",
  verbose = TRUE,
  progress_bar = TRUE
)
```

## Arguments

| | |
|---|---|
| full_data | sample by feature data frame or matrix |
| threshold | the minimum proportion of information explained by a reduced variable; threshold sets a boundary for information loss because each reduced variable must explain at least as much as threshold as measured by the metric. |
| cluster_size | maximum size of any single cluster; default is 4000 |
| partitioner | a partitioner. See the part_*() functions and as_partitioner(). |
| tolerance | a small tolerance within the threshold; if a reduction is within the threshold plus/minus the tolerance, it will reduce. |

| | |
|---|---|
| niter | the number of iterations. By default, it is calculated as 20% of the number of variables or 10, whichever is larger. |
| x | the prefix of the new variable names; must not be contained in any existing data names |
| .sep | a character vector that separates x from the number (e.g. "reduced_var_1"). |
| verbose | logical for whether or not to display information about super partition step; default is TRUE |
| progress_bar | logical for whether or not to show progress bar; default is TRUE |

## Details

super_partition scales up partition with an approximation, using Genie, a fast, hierarchical clustering algorithm with similar qualities of those to Partition, to first super-partition the data into ceiling(N/c) clusters, where N is the number of features in the full dataset and c is the user-defined maximum cluster size (default value = 4,000). Then, if any cluster from the super-partition has a size greater than c, use Genie again on that cluster until all cluster sizes are less than c. Finally, apply the Partition algorithm to each of the super-partitions.

It may be the case that large super-partitions cannot be easily broken with Genie due to high similarity between features. In this case, we use k-means to break the cluster.

## Value

Partition object

## Author(s)

Katelyn Queen, <kjqueen@usc.edu>

## References

Barrett, Malcolm and Joshua Millstein (2020). partition: A fast and flexible framework for data reduction in R. Journal of Open Source Software, 5(47), 1991, https://doi.org/10.21105/joss.01991Millstein J, Battaglin F, Barrett M, Cao S, Zhang W, Stintzing S, et al. Partition: a surjective mapping approach for dimensionality reduction. *Bioinformatics* **36** (2019) 676–681. doi:10.1093/bioinformatics/btz661.

Gagolewski, Marek, Maciej Bartoszuk, and Anna Cena. "Genie: A new, fast, and outlier-resistant hierarchical clustering algorithm." Information Sciences 363 (2016): 8-23.

Millstein, Joshua, Francesca Battaglin, Malcolm Barrett, Shu Cao, Wu Zhang, Sebastian Stintzing, Volker Heinemann, and Heinz-Josef Lenz. 2020. "Partition: A Surjective Mapping Approach for Dimensionality Reduction." *Bioinformatics* 36 (3): https://doi.org/676–81.10.1093/bioinformatics/btz661.

## See Also

partition()

## Examples

```
set.seed(123)
df <- simulate_block_data(c(15, 20, 10), lower_corr = .4, upper_corr = .6, n = 100)

#  don't accept reductions where information < .6
prt <- super_partition(df, threshold = .6, cluster_size = 30)
prt
```

---

`test_permutation` *Permute partitions*

---

## Description

`test_permutation()` permutes data and partitions the results to generate a distribution of null statistics for observed information, number of clusters, and number of observed variables reduced to clusters. The result is a `tibble` with a summary of the observed data results and the averages of the permuted results. The partitions and and permutations are also available in `list-cols`. `test_permutation()` tests across a range of target information values, as specified in the `information` argument.

## Usage

```
test_permutation(
  .data,
  information = seq(0.1, 0.6, by = 0.1),
  partitioner = part_icc(),
  ...,
  nperm = 100
)
```

## Arguments

| | |
|---|---|
| `.data` | a data set to partition |
| `information` | a vector of minimum information to fit in `partition()` |
| `partitioner` | the partitioner to use. The default is `part_icc()`. |
| `...` | arguments passed to `partition()` |
| `nperm` | Number of permuted data sets to test. Default is 100. |

## Value

a tibble with summaries on observed and permuted data (the means of the permuted summaries), as well as list-cols containing them

# Index


∗ **datasets**
baxter_data, 8
∗ **directors**
as_director, 3
direct_distance, 9
direct_k_cluster, 10
∗ **metrics**
as_measure, 4
measure_icc, 16
measure_min_icc, 17
measure_min_r2, 17
measure_std_mutualinfo, 18
measure_variance_explained, 19
∗ **partitioners**
as_partitioner, 6
part_icc, 20
part_kmeans, 21
part_minr2, 22
part_pc1, 23
part_stdmi, 24
replace_partitioner, 34
∗ **reducers**
as_reducer, 7
reduce_first_component, 32
reduce_kmeans, 32
reduce_scaled_mean, 33

as_director, 3, *10, 11*
as_director(), *3*, *6*, *9, 10*, *34*
as_measure, 4, *16–19*
as_measure(), *4*, *6*, *16–19*, *34*
as_partition_step, 5
as_partitioner, 6, *20*, *22–24*, *34*
as_partitioner(), *3, 4*, *6, 7*, *9, 10*, *16–26*, *29*, *32, 33*, *36*
as_reducer, 7, *32, 33*
as_reducer(), *6, 7*, *31–34*

baxter_clinical *(*baxter_data*)*, 8
baxter_data, 8
baxter_data_dictionary *(*baxter_data*)*, 8
baxter_family *(*baxter_data*)*, 8
baxter_genus *(*baxter_data*)*, 8
baxter_otu *(*baxter_data*)*, 8

corr, 9

direct_distance, *3*, 9, *11*
direct_distance_pearson *(*direct_distance*)*, 9
direct_distance_spearman *(*direct_distance*)*, 9
direct_k_cluster, *3*, 10, *10*

filter_reduced, 11
fitted.partition *(*partition_scores*)*, 27

icc, 12
is_partition, 13
is_partition_step, 13
is_partitioner, 14

kmeans(), *11*, *21*

map_cluster *(*reduce_cluster*)*, 31
map_partition, 14
map_partition(), *28, 29*
mapping_groups *(*mapping_key*)*, 15
mapping_key, 15
MASS::mvrnorm(), *35*
measure_icc, *4*, 16, *17–19*
measure_min_icc, *4*, *16*, 17, *18, 19*
measure_min_r2, *4*, *16*, 17, *17–19*
measure_std_mutualinfo, *4*, *16, 17*, 18, *18, 19*
measure_variance_explained, *4*, *16–18*, 19
mutual_information, 19
mutual_information(), *18*

part_icc, *6*, 20, *22–24*, *34*
part_icc(), *14*, *26*, *38*

part_kmeans, *6*, *20*, 21, *23, 24*, *34*
part_kmeans(), *26*
part_minr2, *6*, *20*, 22, *22–24*, *34*
part_minr2(), *26*
part_pc1, *6*, *20*, *22*, 23, *23, 24*, *34*
part_pc1(), *26*
part_stdmi, *6*, *20*, *22, 23*, 24, *34*
part_stdmi(), *26*
partition, 25
partition(), *6*, *14*, *20–24*, *29*, *37, 38*
partition_scores, 27
permute_df, 28
plot_area_clusters, 28
plot_information *(*plot_area_clusters*)*, 28
plot_ncluster *(*plot_area_clusters*)*, 28
plot_permutation, 30
plot_stacked_area_clusters *(*plot_area_clusters*)*, 28

reduce_cluster, 31
reduce_first_component, *7*, 32, *33*
reduce_kmeans, *7*, 32, *32, 33*
reduce_scaled_mean, *7*, *32*, 33, *33*
replace_partitioner, *6*, *20*, *22–24*, 34
replace_partitioner(), *26*

scaled_mean, 34
simulate_block_data, 35
super_partition, 36

test_permutation, 38
test_permutation(), *28–30*

unnest_mappings *(*mapping_key*)*, 15
unnest_reduced *(*filter_reduced*)*, 11