

# Package: ordinalTables (via r-universe)

May 16, 2026

**Type** Package

**Title** Fit Models to Two-Way Tables with Correlated Ordered Response Categories

**Version** 1.0.0.3

**Description** Fit a variety of models to two-way tables with ordered categories. Most of the models are appropriate to apply to tables of that have correlated ordered response categories. There is a particular interest in rater data and models for rescore tables. Some utility functions (e.g., Cohen's kappa and weighted kappa) support more general work on rater agreement. Because the names of the models are very similar, the functions that implement them are organized by last name of the primary author of the article or book that suggested the model, with the name of the function beginning with that author's name and an underscore. This may make some models more difficult to locate if one doesn't have the original sources. The vignettes and tests can help to locate models of interest. For more details see the following references: Agresti, A. (1983) <[doi:10.1016/0167-7152\(83\)90051-2](https://doi.org/10.1016/0167-7152(83)90051-2)> ``A Simple Diagonals-Parameter Symmetry And Quasi-Symmetry Model", Agresti A. (1983) <[doi:10.2307/2531022](https://doi.org/10.2307/2531022)> ``Testing Marginal Homogeneity for Ordinal Categorical Variables", Agresti, A. (1988) <[doi:10.2307/2531866](https://doi.org/10.2307/2531866)> ``A Model For Agreement Between Ratings On An Ordinal Scale", Agresti, A. (1989) <[doi:10.1016/0167-7152\(89\)90104-1](https://doi.org/10.1016/0167-7152(89)90104-1)> ``An Agreement Model With Kappa As Parameter", Agresti, A. (2010 ISBN:978-0470082898) ``Analysis Of Ordinal Categorical Data", Bhapkar, V. P. (1966) <[doi:10.1080/01621459.1966.10502021](https://doi.org/10.1080/01621459.1966.10502021)> ``A Note On The Equivalence Of Two Test Criteria For Hypotheses In Categorical Data", Bhapkar, V. P. (1979) <[doi:10.2307/2530344](https://doi.org/10.2307/2530344)> ``On Tests Of Marginal Symmetry And Quasi-Symmetry In Two And Three-Dimensional Contingency Tables", Bowker, A. H. (1948) <[doi:10.2307/2280710](https://doi.org/10.2307/2280710)> ``A Test For Symmetry In Contingency Tables", Clayton, D. G. (1974) <[doi:10.2307/2335638](https://doi.org/10.2307/2335638)> ``Some Odds Ratio Statistics For The Analysis Of Ordered Categorical Data",

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Agresti_bisection	<i>Solves equation <math>Agresti\_f() = 0</math> for delta by method of bisection..</i>
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### Description

Solves equation  $Agresti\_f() = 0$  for delta by method of bisection..

### Usage

```
Agresti_bisection(p, pi_margin, x_low = 0, x_high = 1)
```

### Arguments

p	matrix of observed proportions
pi_margin	current value of (row and column) marginal proportion
x_low	lower bound for search. Default value is 0.0
x_high	upper bound for search. Default value is 1.0

### Value

value of kappa that makes the function 0.0

---

Agresti_compute_lambda	<i>Computes value of lambda parameter</i>
------------------------	---

---

### Description

Computes value of lambda parameter

### Usage

```
Agresti_compute_lambda(p, pi)
```

**Arguments**

p                    matrix of observed proportions  
 pi                   matrix of model-supplied proportions

**Value**

value of the lambda parameter

---

Agresti\_compute\_pi     *Computes the matrix pi of model-based proportions*

---

**Description**

Computes the matrix pi of model-based proportions

**Usage**

Agresti\_compute\_pi(pi\_margin, kappa)

**Arguments**

pi\_margin            current value of (row and column) marginal proportion  
 kappa                current estimate of kappa coefficient

**Value**

matrix of model-based proportions

---

Agresti\_create\_design\_matrix  
                                  *Creates the design matrix for Agresti's simple diagonal quasi-symmetry model.*

---

**Description**

This parameterization does not match equation (2.2) in the paper, but it yields results that are identical to those in the paper. Agresti, A. (1983), A simple diagonals-parameter symmetry and quasi-symmetry model. Statistics and Probability Letters I, 313-316.

**Usage**

Agresti\_create\_design\_matrix(n\_dim)

**Arguments**

n\_dim                the size of the date matrix

**Value**

the design matrix for the model, that can be used with `ml_for_log_linear`

---

Agresti\_equation\_1     *First equation in section 3. Solved for kappa.*

---

**Description**

First equation in section 3. Solved for kappa.

**Usage**

Agresti\_equation\_1(`p`, `pi_margin`, `kappa`)

**Arguments**

<code>p</code>	matrix of observed proportions
<code>pi_margin</code>	current value of (row and column) marginal proportion
<code>kappa</code>	current value of coefficient kappa

---

Agresti\_equation\_2     *Second equation in section 3. Solved for pi\_margin.*

---

**Description**

Second equation in section 3. Solved for `pi_margin`.

**Usage**

Agresti\_equation\_2(`p`, `pi_margin`, `lambda`, `kappa`)

**Arguments**

<code>p</code>	matrix of observed proportions
<code>pi_margin</code>	current value of (row and column) marginal proportion
<code>lambda</code>	value of quantity lambda defined in third equation
<code>kappa</code>	current value of coefficient kappa

---

Agresti\_equation\_3      *Third equation in section 3. Solved for lambda*

---

**Description**

Third equation in section 3. Solved for lambda

**Usage**

Agresti\_equation\_3(p, pi\_margin, kappa)

**Arguments**

p	matrix of observed proportions
pi_margin	current value of (row and column) marginal proportion
kappa	current value of coefficient kappa

---

Agresti\_extract\_delta      *Extracts the quasi-symmetry information from the result provided.*

---

**Description**

Extracts the quasi-symmetry information from the result provided.

**Usage**

Agresti\_extract\_delta(result)

**Arguments**

result	result of call to log_linear_fit()
--------	------------------------------------

**Value**

list consisting of beta: the beta coefficient se: the standard error of beta z: the ratio beta / se delta:  
the delta coefficient =  $\exp(2.0 * \text{beta})$

---

 Agresti\_f

*Function value for first equation in section 3.*


---

**Description**

Used by Agresti\_bisection()

**Usage**

Agresti\_f(p, pi\_margin, kappa)

**Arguments**

p	matrix of observed proportions
pi_margin	current value of (row and column) marginal proportion
kappa	current estimate of kappa coefficient

---

 Agresti\_kappa\_agreement

*Fits Agresti's agreement model that includes kappa as a parameter.*


---

**Description**

Agresti, A. (1989). An agreement model with kappa as a parameter. *Statistics and Probability Letters*, 7, 271-273.

**Usage**

Agresti\_kappa\_agreement(n, verbose = FALSE)

**Arguments**

n	matrix of observed counts
verbose	should cycle-by-cycle info be printed as messages? The default is FALSE.

**Value**

a list containing kappa: value of kappa coefficient pi\_margin: value of marginal p-values. They apply to rows and columns chisq: Pearson  $X^2$  df: degrees of freedom expected: fitted frequencies

---

 Agresti\_simple\_diagonals\_parameter\_quasi\_symmetry

*Agresti's simple diagonal quasi-symmetry model.*


---

### Description

This parameterization does not match equation (2.2) in the paper, but it yields results that are identical to those in the paper. Agresti, A. (1983), A simple diagonals-parameter symmetry and quasi-symmetry model. Statistics and Probability Letters I, 313-316.

### Usage

```
Agresti_simple_diagonals_parameter_quasi_symmetry(n)
```

### Arguments

n                    the matrix of observed counts

### Value

a list containing expected: matrix of expected cell frequencies, chisq: Pearson  $X^2$  g\_squared: likelihood ratio  $G^2$  df: degrees of freedom beta: the parameter estimated sigma\_beta: standard error of beta z: z-score for beta delta: transformation of the the parameter into the model formulation

### Examples

```
Agresti_simple_diagonals_parameter_quasi_symmetry(vision_data)
```

---

 Agresti\_starting\_values

*Computes starting values for marginal pi.*


---

### Description

Computes starting values for marginal pi.

### Usage

```
Agresti_starting_values(p)
```

### Arguments

p                    matrix of observed proportions

### Value

vector containing pi

---

Agresti\_w\_diff      *Computes the weighted statistics listed in section 2.3.*

---

**Description**

Computes weighted contrast of the two margins. Agresti, A. (1983). Testing marginal homogeneity for ordinal categorical variables. *Biometrics*, 39(2), 505-510.

**Usage**

```
Agresti_w_diff(w, n)
```

**Arguments**

w                    a vector of weights to be treated as scores  
n                    matrix of observed counts

**Value**

a list containing diff: the weighted contrast computed using weights w sigma\_diff: SE(diff) z\_diff: z-score for diff

**Examples**

```
weights = c(-3.0, -1.0, 1.0, 3.0)
Agresti_w_diff(weights, vision_data)
```

---

Agresti\_weighted\_tau      *Computes weighted tau from Section 2.1. Agresti, A. (1983). Testing marginal homogeneity for ordinal categorical variables. Biometrics, 39(2), 505-510.*

---

**Description**

Computes weighted tau from Section 2.1. Agresti, A. (1983). Testing marginal homogeneity for ordinal categorical variables. *Biometrics*, 39(2), 505-510.

**Usage**

```
Agresti_weighted_tau(n)
```

**Arguments**

n                    matrix of observed counts

**Value**

a list containing tau: value of tau-d coefficient sigma\_tau: SE(tau) z\_tau: z-score for tau

---

Bhapkar\_marginal\_homogeneity  
*Bhapkar's (1979) test for marginal homogeneity*

---

**Description**

Fits the marginal homogeneity model using WLS.

**Usage**

Bhapkar\_marginal\_homogeneity(n)

**Arguments**

n                    matrix containing the table to analyze

**Details**

See: Bhapkar, V. P. (1966). A Note on the Equivalence of Two Test Criteria for Hypotheses in Categorical Data. Journal of the American Statistical Association, 61(313), pp.228-235.

**Value**

a list containing the chi-square statistic, the df and p-value.

**Examples**

Bhapkar\_marginal\_homogeneity(vision\_data)

---

Bhapkar\_quasi\_symmetry  
*Bhapkar's 1979 test for quasi-symmetry.*

---

**Description**

Fits the quasi-symmetry model using WLS. Bhapkar, V. P. (1979). On tests of marginal symmetry and quasi-symmetry in two and three-dimensional contingency tables. Biometrics 35(2), 417-426.

**Usage**

Bhapkar\_quasi\_symmetry(n)

**Arguments**

n                    the matrix to be analyzed

**Value**

a list containing the chi-square and df.

**Examples**

```
Bhapkar_quasi_symmetry(vision_data)
```

---

Bowker_symmetry	<i>Computes Bowker's test of symmetry.</i>
-----------------	--

---

**Description**

Computes the test of table symmetry in Bowker (1948). Bowker, A. H. (1948). A test for symmetry in contingency tables. Journal of the American Statistical Association 43, 572-574.

**Usage**

```
Bowker_symmetry(n)
```

**Arguments**

n                    the matrix to be tested for symmetry

**Value**

a list containing the chi-square: Pearson  $X^2$  g\_square: likelihood ratio  $G^2$  df: degrees of freedom  
p-value: p-value for Pearson  $X^2$  expected: fitted values

**Examples**

```
Bowker_symmetry(vision_data)
```

---

budget_actual	<i>Participation in household budgeting by psychiatric patients. Rows are ratings by patient, columns are ratings by relative. 1 - not at all 2 - doing some 3 - doing regularly</i>
---------------	--

---

**Description**

Participation in household budgeting by psychiatric patients. Rows are ratings by patient, columns are ratings by relative. 1 - not at all 2 - doing some 3 - doing regularly

**Usage**

```
budget_actual
```

**Format**

## 'budget\_actual' A matrix with 3 rows and 3 columns

**Source**

Schuster, C, (2001). Kappa as a parameter of a symmetry model for rater agreement. Journal of Educational and Behavioral Statistics, 26(3), 331-342.

---

budget_expected	<i>Ratings of expected participation in household budgeting by psychiatric patients. Rows are ratings by patient, columns are ratings by relative. 1 - not at all 2 - doing some 3 - doing regularly</i>
-----------------	--

---

**Description**

Ratings of expected participation in household budgeting by psychiatric patients. Rows are ratings by patient, columns are ratings by relative. 1 - not at all 2 - doing some 3 - doing regularly

**Usage**

budget\_expected

**Format**

## 'budget\_expected' a matrix with 3 rows and 3 columns.

**Source**

Schuster, C, (2001). Kappa as a parameter of a symmetry model for rater agreement. Journal of Educational and Behavioral Statistics, 26(3), 331-342.

---

Clayton_marginal_location	<i>Fits the tests comparing locations of the margins of a two-way table.</i>
---------------------------	--

---

**Description**

The measure is based on the weighted cdfs. No "scores" are used, just the weighted (cumulative sums). Clayton, D. G. (1974) Odds ratio statistics for the analysis of ordered categorical data. Biometrika, 61(3), 525-531.

**Usage**

Clayton\_marginal\_location(wx, wy)

**Arguments**

wx                    vector containing frequencies for the first margin of the table  
 wy                    vector containing frequencies for the second margin of the table

**Value**

a list of results odds\_ratios: odds ratios comparing cumulative frequencies of adjacent categories  
 log\_theta\_hat: log of estimate of the common odds-ratio theta\_hat: estimate of the common odds-ratio  
 log\_mh\_theta\_hat: log of the Mantel-Haenssel type odds-ratio mh\_theta\_hat: Mantel-Haenszel  
 type odds-ratio var\_log\_theta\_hat = variance of the log of the odds-ratios chisq\_theta\_hat: chi-square  
 for odds-ratio chisq\_mh\_theta\_hat: chi-square for Mantel-Haenszel odds-ratio df: degrees  
 of freedom for chis-square = 1

**Examples**

```
Clayton_marginal_location(tonsils[1,], tonsils[2,])
```

---

```
Clayton_stratified_marginal_location
```

*Clayton's stratified version of the marginal location comparison.*

---

**Description**

Compares marginal location conditional on a stratifying variable. Clayton, D. G. (1974) Odds ratio statistics for the analysis of ordered categorical data. *Biometrika*, 61(3), 525-531.

**Usage**

```
Clayton_stratified_marginal_location(mx, my)
```

**Arguments**

mx                    matrix with  
 my                    matrix with

**Value**

a list of results odds\_ratios: odds ratios comparing cumulative frequencies of adjacent categories  
 log\_theta\_hat: log of estimate of the common odds-ratio theta\_hat: estimate of the common odds-ratio  
 log\_mh\_theta\_hat: log of the Mantel-Haenssel type odds-ratio mh\_theta\_hat: Mantel-Haenszel  
 type odds-ratio var\_log\_theta\_hat = variance of the log of the odds-ratios chisq\_theta\_hat: chi-square  
 for odds-ratio chisq\_mh\_theta\_hat: chi-square for Mantel-Haenszel odds-ratio df: degrees  
 of freedom for chis-square = 1

**See Also**

[Clayton\_marginal\_location()]

---

Clayton\_summarize      *Computes summary, cumulative proportions up to index provided*

---

**Description**

Computes summary, cumulative proportions up to index provided

**Usage**

```
Clayton_summarize(weights, m)
```

**Arguments**

weights	matrix of counts
m	index of summation, weights[1:m]

**Value**

a list containing: n: the sum of the weights p: matrix of proportion values gamma: cumulative proportions l:m

---

Clayton\_summarize\_stratified  
*Analysis stratified by column variable j.*

---

**Description**

Analysis stratified by column variable j.

**Usage**

```
Clayton_summarize_stratified(weight_matrix, m)
```

**Arguments**

weight_matrix	matrix of cell weights from the table
m	the column index to stratify on

**Value**

a list containing: n: the number of strata p: matrix of proportion values gamma: cumulative proportions

**See Also**

[Clayton\_summarize()]

---

Clayton\_two\_way\_association  
*Clayton's stratified measure of association*

---

### Description

Quantifies association between two ordinal variables. Clayton, D. G. (1974) Odds ratio statistics for the analysis of oordered categorical data. *Biometrika*, 61(3), 525-531.

### Usage

Clayton\_two\_way\_association(f)

### Arguments

f                    matrix of frequencies

### Value

a list of results log\_theta\_hat: log odds-ratio measure of association theta\_hat: odds-ratio measure of association log\_mh\_theta\_hat: log of Mantel-Haenszel odds-ratio measure of association mh\_theta\_hat: Mantel-Haenszel odds-ratio measure of association var\_log\_theta\_hat: variance of the log odds-ratio measures chisq\_theta\_hat: chi-square for measure of association chisq\_mh\_theta\_hat: chi-square for Mantel-Haenszel measure of association df: degrees of freedom = 1, corr\_theta\_hat: theta-hat association converted to correlation metric corr\_mh\_theta\_hat: Mantel-Haenszel theta-hat converted to correlation metric

---

Cliff\_as\_d\_matrix      *Converts two vectors containing scores and integer frequencies (cell counts) into a d-matrix*

---

### Description

Converts two vectors containing scores and integer frequencies (cell counts) into a d-matrix

### Usage

Cliff\_as\_d\_matrix(scores, cells, nrow = NULL)

### Arguments

scores                vector of scores, typically 1:r  
 cells                 vector of integer weights, i.e. cell frequencies  
 nrow                  number of score categories in table. Default is NULL. If NULL, takes 1:length(scores)

**Value**

d-matrix of results

---

Cliff_compute_d	<i>Computes between groups dominance matrix "d".</i>
-----------------	--

---

**Description**

Computes between groups dominance matrix "d".

**Usage**

Cliff\_compute\_d(x, y)

**Arguments**

x	first vector of scores
y	second vector of scores

**Value**

N X N dominance matrix

---

Cliff_counts_2	<i>Generates counts from table frequencies for 2 category items</i>
----------------	---

---

**Description**

Generates counts from table frequencies for 2 category items

**Usage**

Cliff\_counts\_2(mij)

**Arguments**

mij	Matrix of counts.
-----	-------------------

**Value**

a list containing wm1m1: for -1, -1 wm10: for -1, 0 wm11: for -1, 1 w00: for 0, 0 w01: for 0, 1 w11: for 1, 1

---

Cliff\_counts\_3      *Generates counts from table frequencies for 3 category items*

---

**Description**

Generates counts from table frequencies for 3 category items

**Usage**

Cliff\_counts\_3(mij)

**Arguments**

mij      Matrix of counts.

**Value**

a list containing wm1m1: for -1, -1 wm10: for -1, 0 wm11: for -1, 1 w00: for 0, 0 w01: for 0, 1 w11: for 1, 1

---

Cliff\_counts\_4      *Generates counts from table frequencies for 4 category items*

---

**Description**

Generates counts from table frequencies for 4 category items

**Usage**

Cliff\_counts\_4(mij)

**Arguments**

mij      Matrix of counts.

**Value**

a list containing wm1m1: for -1, -1 wm10: for -1, 0 wm11: for -1, 1 w00: for 0, 0 w01: for 0, 1 w11: for 1, 1

---

Cliff\_counts\_5      *Generates counts from table frequencies for 5 category items*

---

**Description**

Generates counts from table frequencies for 5 category items

**Usage**

Cliff\_counts\_5(mij)

**Arguments**

mij      Matrix of counts.

**Value**

a list containing wm1m1: for -1, -1 wm10: for -1, 0 wm11: for -1, 1 w00: for 0, 0 w01: for 0, 1 w11: for 1, 1

---

Cliff\_counts\_6      *Generates counts from table frequencies for 6 category items*

---

**Description**

Generates counts from table frequencies for 6 category items

**Usage**

Cliff\_counts\_6(mij)

**Arguments**

mij      Matrix of counts.

**Value**

a list containing wm1m1: for -1, -1 wm10: for -1, 0 wm11: for -1, 1 w00: for 0, 0 w01: for 0, 1 w11: for 1, 1

---

Cliff_dependent	<i>Computes Cliff's dependent d-statistics based on a dominance matrix.</i>
-----------------	---

---

**Description**

Takes the dominance matrix provided and computes the d-statistics: dw - within-subjects d-statistic db - between-subjects d-statistic db\_dw - sum of dw and db, omnibus test of whether one group is higher than the other Cliff, N. (1993). Dominance statistics: Ordinal analyses to answer ordinal questions. Psychological Bulletin, 114(3), 494-509. Cliff, N. (1996). Ordinal methods for behavioral data analysis. Mahwah NJ: Lawrence Erlbaum.

**Usage**

```
Cliff_dependent(d_matrix)
```

**Arguments**

d_matrix	N x N within-subjects dominance matrix
----------	--

**Value**

a list containing dw: within-subjects d-statistic sigma\_dw: SE of dw z\_dw: z-score for dw db: between-subjects d-statistic sigma\_db: SE of db z\_db: z-score for db db\_dw: sum db + dw, omnibus measure sigma\_db\_dw: SE of db + dw z\_db\_dw: z-score of db \_ dw cov\_db\_dw: covariance between db and dw

**Examples**

```
Cliff_dependent(interference_control_1)
```

---

Cliff_dependent_compute_cov	<i>Computes sum term in covariance db-dw for weighted dominance matrix.</i>
-----------------------------	---

---

**Description**

Computes sum term in covariance db-dw for weighted dominance matrix.

**Usage**

```
Cliff_dependent_compute_cov(wd)
```

**Arguments**

wd	weighted dominance matrix
----	---------------------------

---

 Cliff\_dependent\_compute\_cov\_from\_d

*Compute the sum in the covariance of db+dw*


---

**Description**

Compute the sum in the covariance of db+dw

**Usage**

Cliff\_dependent\_compute\_cov\_from\_d(d\_matrix)

**Arguments**

d\_matrix            d-matrix of dominances

**Value**

the sum for the covariance term

---

Cliff\_dependent\_compute\_from\_matrix

*Computes Cliff's dependent d-statistics based on a dominance matrix.*


---

**Description**

Takes the dominance matrix provided and computes the d-statistics: dw - within-subjects d-statistic db - between-subjects d-statistic db\_dw - sum of db and dw, omnibus test of whether one group is higher than the other Cliff, N. (1993). Dominance statistics: Ordinal analyses to answer ordinal questions. Psychological Bulletin, 114(3), 494-509. Cliff, N. (1996). Ordinal methods for behavioral data analysis. Mahwah NJ: Lawrence-Erlbaum.

**Usage**

Cliff\_dependent\_compute\_from\_matrix(d\_matrix)

**Arguments**

d\_matrix            N x N within-subjects dominance matrix

**Value**

a list containing dw: within-subjects d-statistic sigma\_dw: SE of dw z\_dw: z-score for dw db: between-subjects d-statistic sigma\_db: SE of db z\_db: z-score for db db\_dw: sum db + dw, omnibus measure sigma\_db\_dw: SE of db + dw z\_db\_dw: z-score of db \_ dw cov\_db\_dw: covariance between db and dw

**Examples**

```
Cliff_dependent_compute_from_matrix(interference_control_1)
```

---

```
Cliff_dependent_compute_from_table
```

*Computes Cliff's dependent d-statistics based on a table of frequency counts.*

---

**Description**

Takes the  $r \times r$  table and returns: *dw* - within-subjects d-statistic *db* - between-subjects d-statistic *db\_dw* - sum of *dw* and *db*, omnibus test of whether one group is higher than the other. No intermediate dominance matrix is computed, so this is much faster than `Cliff_dependent_compute_from_matrix()`. Large number of terms are needed to compute intermediate  $d_{ij_{ji}}$ . These are contained in separate functions for  $r \leq 6$ . Results for  $r [7, 10]$  are available, but the files are so large that they cause an error if included in the library.

**Usage**

```
Cliff_dependent_compute_from_table(mij)
```

**Arguments**

*mij*                    an  $r \times r$  table of paired observations

**Details**

See: Cliff, N. (1993). Dominance statistics: Ordinal analyses to answer ordinal questions. *Psychological Bulletin*, 114(3), 494-509. Cliff, N. (1996). *Ordinal methods for behavioral data analysis*. Mahwah NJ: Lawrence-Erlbaum.

**Value**

a list containing *dw*: within-subjects d-statistic *sigma\_dw*: SE of *dw* *z\_dw*: z-score for *dw* *db*: between-subjects d-statistic *sigma\_db*: SE of *db* *z\_db*: z-score for *db* *db\_dw*: sum *db* + *dw*, omnibus measure *sigma\_db\_dw*: SE of *db* + *dw* *z\_db\_dw*: z-score of *db* + *dw* *cov\_db\_dw*: covariance between *db* and *dw*

**See Also**

```
[Cliff_dependent_compute_paired_d()]
```

**Examples**

```
Cliff_dependent_compute_from_table(movies)
```

---

`Cliff_dependent_compute_paired_d`*Computes Cliff's dependent d-statistics based on cell frequencies.*

---

### Description

Computes d-matrix and then analyzes it. This can be time consuming. Try `Cliff_dependent_from_table()` instead. The current function is provided mainly for comparison & validation. For an example, compare running this function on `vision_data` to running `Cliff_dependent_from_table(vision_data)`.

### Usage

```
Cliff_dependent_compute_paired_d(cells)
```

### Arguments

`cells`            `r x r` matrix of frequencies

### Details

`dw` - within-subjects d-statistic `db` - between-subjects d-statistic `db_dw` - sum of `dw` and `db`, omnibus test of whether one group is higher than the other Cliff, N. (1993). Dominance statistics: Ordinal analyses to answer ordinal questions. *Psychological Bulletin*, 114(3), 494-509. Cliff, N. (1996). *Ordinal methods for behavioral data analysis*. Mahwah NJ: Lawrence-Erlbaum.

### Value

a list containing `dw`: within-subjects d-statistic `sigma_dw`: SE of `dw` `z_dw`: z-score for `dw` `db`: between-subjects d-statistic `sigma_db`: SE of `db` `z_db`: z-score for `db` `db_dw`: sum `db` + `dw`, omnibus measure `sigma_db_dw`: SE of `db` + `dw` `z_db_dw`: z-score of `db` + `dw` `cov_db_dw`: covariance between `db` and `dw`

### See Also

[`Cliff_dependent_compute_from_table()`]

### Examples

```
Cliff_dependent_compute_paired_d(movies)
```

Cliff\_independent      *Computes the independent groups d-statistic comparing the two vectors provided.*

---

**Description**

Computes the independent groups d-statistic comparing the two vectors provided.

**Usage**

```
Cliff_independent(x, y)
```

**Arguments**

x                      vector of scores for first group  
y                      vector of scores for second group

**Value**

list containing d, SE(d) and z(d)

---

Cliff\_independent\_from\_matrix  
*Computes d-statistic from dominance matrix provided.*

---

**Description**

Computes d-statistic from dominance matrix provided.

**Usage**

```
Cliff_independent_from_matrix(d)
```

**Arguments**

d                      N X M dominance matrix

**Value**

list containing d, SE(d) and z(d)

---

Cliff\_independent\_from\_table

*Computes independent group's d-statistic from the matrix of frequencies provided.*

---

**Description**

Computes intermediate d-matrix, so can be slow for large N

**Usage**

Cliff\_independent\_from\_table(n)

**Arguments**

n                    matrix of counts

**Value**

list containing d, SE(d) and z(d)

---

Cliff\_independent\_weighted

*Computes d-statistic based on scores and integer weights(frequencies) for each group.*

---

**Description**

Computes d-statistic based on scores and integer weights(frequencies) for each group.

**Usage**

Cliff\_independent\_weighted(x, w\_x, y, w\_y)

**Arguments**

x                    first vector of scores  
w\_x                  weights associated with first vector of scores  
y                    second vector of scores  
w\_y                  weights associated with second vector of scores

**Value**

list containing d, SE(d) and z(d)

---

Cliff\_weighted\_d\_matrix

*Computes weighted version of dominance matrix "d"*

---

### Description

Arguments are scores and associated weights. Not useful for tables. Use Cliff\_compute\_d\_matrix instead.

### Usage

```
Cliff_weighted_d_matrix(x, y, w.x = rep(1, length(x)), w.y = rep(1, length(y)))
```

### Arguments

x	first vector of scores
y	second vector of scores
w.x	first vector of weights, to apply to x. Defaults to vector of 1.0
w.y	second vector of weights, to apply to y. Defaults to vector of 1.0

### Value

an n X m d-matrix, where n is length(x) and m is length(y)

---

coal\_g

*Degree of disease measured at two points in time for mine workers.*

---

### Description

Based on radiological measurements, the matrix contains the degree of pneumoconiosis in coal workers. 1 = least severe disease and 4 = most severe.

### Usage

```
coal_g
```

### Format

```
## 'coal_g' A matrix with 4 rows and 4 columns.
```

### Source

McCullagh, P. (1977). A logistic model for paired comparisons with ordered categorical data. *Biometrika*, 64(3), 449-453.

---

 constant\_of\_integration

*Computes the constant of integration of a multinomial sample.*


---

**Description**

$$N! / \text{product}(n[i]!)$$
**Usage**

```
constant_of_integration(n, exclude_diagonal = FALSE)
```

**Arguments**

`n` Matrix of observed counts

`exclude_diagonal` logical. Should the diagonal cells of a square matrix be excluded from the computation. Default is FALSE,

**Value**

value of constant of integration for observed matrix provided

---

depression

*Ratings of severity of patient's depression by two therapists.*


---

**Description**

1 = slight 2 = moderate 3 = severe

**Usage**

```
depression
```

**Format**

```
## 'depression' A matrix with 3 rows and 3 columns.
```

**Source**

von Eye, A. & Mun, E. Y. (2005, p.41). Analyzing rater agreement: Manifest variable methods. Mahwah, NJ: Lawrence Erlbaum.

---

 dogs

*Dehydration in dogs data set.*


---

**Description**

An interrater agreement data set from Shourki, M. M. (2005, p.80). It is agreement study of two clinicians evaluating whether dogs were dehydrated. The lowest score indicates normal, and the highest score indicates dehydrated (above 10 The "g" in the name indicates that this is taken from mine "G" in the original study.

**Usage**

dogs

**Format**

## 'dogs' A matrix with 4 rows and 4 columns.

**Source**

Shoukri, M. M. (2005). The measurement of interobserver agreement. New York: Chapman & Hall.

---

 dreams

*Severity of disturbing dreams in adolescent boys, measured at two ages..*


---

**Description**

Severity of disturbing dreams in adolescent boys, measured at two ages..

**Usage**

dreams

**Format**

## 'dreams' A matrix with 4 rows and 4 columns.

**Source**

McCullagh, P. (1980, p.117). Regression models for ordinal data. Journal of the Royal Statistical Society, Series B, 42(2), 109-142.

---

dumping	<i>Occurrence of side effects after gastro-intestinal surgery.</i>
---------	--

---

**Description**

Columns 1 = None 2 = Slight 3 = Moderate

**Usage**

dumping

**Format**

## 'dumping' A matrix with 4 rows and 3 columns

**Details**

Rows Hospital A Hospital B Hospital C Hospital D

**Source**

Agresti, A. (1984, p. 63). Analysis of ordinal categorical data. Naew York: Wiley.

---

esophageal_cancer	<i>Ratings of number of hot drinks consumed by cases with cancer of the esophagus, compared with control subjects.</i>
-------------------	--

---

**Description**

Ratings of number of hot drinks consumed by cases with cancer of the esophagus, compared with control subjects.

**Usage**

esophageal\_cancer

**Format**

## 'esophageal\_cancer' A matrix with 4 rows and 4 columns.

**Source**

Agresti, A. (1984, p. 217). Analysis of ordinal categorical data. New York, Wiley.

---

expand	<i>Converts weighted (x, w) pairs into unweighted data by replicating x[i] w[i] times</i>
--------	---

---

**Description**

Takes a set of (value, weight) pairs and converts into unweighted vector (w[i]) for each i Weights are assumed to be integers

**Usage**

```
expand(x, w)
```

**Arguments**

x	Numeric vector of scores.
w	Numeric vector of weights. These are assumed to be integers

**Value**

new unweighted vector of scores

---

expit	<i>Computes the "expit" function – inverse of logit.</i>
-------	--

---

**Description**

Computes the "expit" function – inverse of logit.

**Usage**

```
expit(z)
```

**Arguments**

z	Numeric. Real valued argument to expit() function.
---	--

**Value**

$\exp(z) / (1.0 + \exp(z))$

---

family_income	<i>Family income for two years from US census.</i>
---------------	--

---

**Description**

Family income for two years from US census.

**Usage**

family\_income

**Format**

## 'family\_income' A matrix with 2 rows and 7 columns. Rows are years 1960 and 1970. Columns are income range.

**Source**

McCullagh, P. (1980, p.114). Regression models for ordinal data. Journal of the Royal Statistical Society, Series B, 42(2), 109-142.

---

gender_vision	<i>Ratings of visual acuity for men and women employed at the Royal Ordinance factories, 1943-1946.</i>
---------------	---

---

**Description**

1 = best visual acuity 4 = worst visual acuity

**Usage**

gender\_vision

**Format**

## 'gender\_vision' A matrix with 2 rows for the genders and 4 columns for visual acuity.

**Source**

McCullagh, P. (1980, p. 119). Regression models for ordinal data. Journal of the Royal Statistical Society, Series B, 42(2), 109-142.

---

Goodman\_constrained\_diagonals\_parameter\_symmetry

*Fits the model where some of the delta parameters are constrained to be equal to one another.*

---

### Description

Fits the model where some of the delta parameters are constrained to be equal to one another.

### Usage

```
Goodman_constrained_diagonals_parameter_symmetry(n, equality)
```

### Arguments

n	the matrix of observed counts
equality	logical vector indicating whether corresponding delta the parameter is part of the equality set.

### Value

a list containing pooled\_chisq: Pearson chi-square for the pooled delta values pooled\_df: degrees of freedom for pooled chisq omnibus\_chisq: Pearson chi-square for overall model fit, subject to equality constraints omnibus\_df: degrees of freedom for omnibus\_chisq equality\_chisq: Pearson chi-square for test that remaining deltas are all equal equality\_df: degrees of freedom for equality\_chisq delta\_pooled: estimate of pooled delta

### Examples

```
equality = c(TRUE, TRUE, FALSE)
Goodman_diagonals_parameter_symmetry(vision_data)
```

---

Goodman\_diagonals\_parameter\_symmetry

*Fit's Goodman's diagonals parameter symmetry model.*

---

### Description

Goodman, L. A. (1979). Multiplicative models for square contingency tables with ordered categories. *Biometrika*, 66(3), 413-316.

### Usage

```
Goodman_diagonals_parameter_symmetry(n)
```

**Arguments**

n                    the matrix of observer counts

**Value**

a list containing individual\_chisq: chi-square value for each diagonal individual\_df: degrees of freedom for individual\_chisq omnibus\_chisq: overall chi-square for the model omnibus\_df: degrees of freedom for omnibus\_chisq equality\_chisq: chi-square for test that all delta values are equal equality\_df: degrees of freedom from equality\_chisq delta: the vector of estimated delta values (without any equality constraints)

**Examples**

```
Goodman_diagonals_parameter_symmetry(vision_data)
```

---

```
Goodman_fixed_parameter
```

*Fits the model with given parameters fixed to specific values.*

---

**Description**

The model has simple closed form solutions when fitting either the unconstrained version of the version that species equality of delta parameters. However, I could not see how to adapt that to the case where specific parameters were constrained to have a specific value. This routine is to fit that model. It will also fit the unconstrained model, but Goodman gives the estimator for that case.

**Usage**

```
Goodman_fixed_parameter(
  n,
  delta,
  fixed,
  convergence = 1e-04,
  max_iter = 50,
  verbose = FALSE
)
```

**Arguments**

n                    the  $r \times r$  matrix of observed counts

delta                the vector of asymmetry  $r - 1$  parameters

fixed                 $r - 1$  logical vector that specifies whether a delta parameter is fixed (TRUE) or allowed to be estimated (FALSE).

convergence        maximum change in a parameter across iterations. Default is  $1.0e-4$

max\_iter            maximum number of iterations, Default is 50.

verbose             should progress information be printed to the console. Default is FALSE, do not print.

**Value**

list containing phi, delta, max\_change largest change in parameter for last the iteration, chisq: Pearson chi-square g\_squared: likelihood ratio  $G^2$  df: degrees of freedom

**See Also**

[Goodman\_diagonals\_parameter\_symmetry()]

[Goodman\_ml()]

**Examples**

```
fixed <- c(FALSE, TRUE, FALSE)
delta <- c(1.0, 1.0, 1.0)
phi <- matrix(0.0, nrow=4, ncol=4)
diag(phi) = rep(1.0, 4)
Goodman_fixed_parameter(vision_data, delta, fixed)
```

---

Goodman\_ml

*Performs ML estimation of the model.*

---

**Description**

The model has simple closed form solutions when fitting either the unconstrained version of the version that species equality of delta parameters. However, I could not see how to adapt that to the case where specific parameters were constrained to have a specific value. This routine is to fit that model. It will also fit the unconstrained model, but Goodman gives the estimator for that case.

**Usage**

```
Goodman_ml(n, phi, delta, fixed)
```

**Arguments**

n	the $r \times r$ matrix of observed counts
phi	the symmetric matrix parameter
delta	the vector of asymmetry $r - 1$ parameters
fixed	$r - 1$ logical vector that specifies whether a delta parameter is fixed (TRUE) or allowed to be estimated (FALSE).

**Value**

list containing new estimates of phi and delta

**See Also**

[Goodman\_diagonals\_parameter\_symmetry()]

**Examples**

```

fixed <- c(FALSE, TRUE, FALSE)
delta <- c(1.0, 1.0, 1.0)
phi <- matrix(0.0, nrow=4, ncol=4)
for (i in 1:4) {
  phi[i, i] = 1.0
}
Goodman_ml(vision_data, phi, delta, fixed)

```

---

Goodman\_model\_i

*Fits Goodman's (1979) Model I*


---

**Description**

Fits Goodman's (1979) Model I

**Usage**

```

Goodman_model_i(
  n,
  row_effects = TRUE,
  column_effects = TRUE,
  max_iter = 25,
  verbose = FALSE,
  exclude_diagonal = FALSE
)

```

**Arguments**

n	matrix of observed counts
row_effects	should row effects be included in the model? Default is TRUE
column_effects	should column effects be included in the model? Default is TRUE
max_iter	maximum number of iterations. Default is 10
verbose	logical. Should cycle-by-cycle output be printed? Default is no
exclude_diagonal	logical. For square tables, should the cells on the diagonal be excluded? Default is FALSE, include all cells

**Value**

a list containing alpha: row effects beta: column effects gamma: row location weights delta: column location weights log\_likelihood: log(likelihood) g\_squared: G<sup>2</sup> fit measure chisq: X<sup>2</sup> fit measure df: degrees of freedom

---

Goodman\_model\_i\_star    *Fits Goodman's (1979) Model I\**

---

### Description

Fits Goodman's (1979) Model I\*

### Usage

```
Goodman_model_i_star(
  n,
  max_iter = 25,
  verbose = FALSE,
  exclude_diagonal = FALSE
)
```

### Arguments

n	matrix of observed counts
max_iter	maximum number of iterations
verbose	should cycle-by-cycle information be printed out? Default is FALSE, do not print
exclude_diagonal	should the cells along the main diagonal be excluded? Default is FALSE, include all cells

### Value

a list containing alpha: vector of row parameters beta: vector of column parameters theta: vector of common row/column estimates log\_likelihood: log(likelihood) at completion g\_squared: G<sup>2</sup> fit measure chisq: X<sup>2</sup> fit measure df: degrees of freedom

---

Goodman\_model\_ii    *Fits Goodman's (1979) Model II*

---

### Description

Fits Goodman's (1979) Model II

**Usage**

```

Goodman_model_ii(
  n,
  rho = 1:nrow(n) - (nrow(n) + 1)/2,
  sigma = 1:ncol(n) - (ncol(n) + 1)/2,
  update_rows = TRUE,
  update_columns = TRUE,
  max_iter = 25,
  verbose = FALSE,
  exclude_diagonal = FALSE
)

```

**Arguments**

n	matrix of observed counts
rho	values of row locations. Default is $1:nrow(n) - (nrow(n) + 1) / 2$
sigma	values of column locations. Default is $1:ncol(n) - (ncol(n) + 1) / 2$
update_rows	should values of row locations be updated? Default is TRUE, update
update_columns	should value of column locations be updated? Default is TRUE, update
max_iter	maximum number of iterations to perform. Default is 10
verbose	should cycle-by-cycle output be produced? Default is FALSE
exclude_diagonal	logical. Should the diagonal be excluded from the computation. Default is FALSE.

**Value**

a list containing alpha: row effects beta: column effects rho: centered row locations mu: row locations sigma: centered column locations nu: column locations log\_likelihood: log(likelihood) g\_squared:  $G^2$  fit measure chisq:  $X^2$  fit measure df: degrees of freedom

---

Goodman\_model\_ii\_star *Fits Goodman's (1979) model II\*, where row and column effects are equal.*

---

**Description**

Fits Goodman's (1979) model II\*, where row and column effects are equal.

**Usage**

```

Goodman_model_ii_star(
  n,
  exclude_diagonal = FALSE,
  max_iter = 25,
  verbose = FALSE
)

```

**Arguments**

n matrix of observed counts  
 exclude\_diagonal should the cells of the main diagonal be excluded? Default is FALSE, include all cells  
 max\_iter maximum number of iterations  
 verbose should cycle-by-cycle information be printed out? Default is FALSE, do not print

**Value**

a list containing alpha: vector of alpha (row) parameters beta: vector of beta (column) parameters phi: vector of common row/column effects log\_likelihood: value of the log(likelihood) function at completion g\_squared: G<sup>2</sup> fit measure chisq: X<sup>2</sup> fit measure df: degrees of freedom

---

Goodman\_null\_association

*Fits Goodman's L. A. (1979) Simple Models for the Analysis of Association in Cross-Classifications Having Ordered Categories*

---

**Description**

null association model

**Usage**

```
Goodman_null_association(
  n,
  max_iter = 25,
  verbose = FALSE,
  exclude_diagonal = FALSE
)
```

**Arguments**

n matrix of observed counts  
 max\_iter maximum number of iterations. Default is 10  
 verbose should cycle-by-cycle info be printed? Default is FALSE  
 exclude\_diagonal logical, Should the diagonal be excluded from the computations. Default is FALSE

**Value**

a list containing alpha: row effects beta: column effects log\_likelihood: log(likelihood) g\_squared: G<sup>2</sup> fit measure chisq: X<sup>2</sup> fit measure df: degrees of freedom

---

Goodman_pi	<i>Computes the model-based probability for cell i, j</i>
------------	---

---

**Description**

Computes the model-based probability for cell i, j

**Usage**

```
Goodman_pi(phi, delta, i, j)
```

**Arguments**

phi	symmetry matrix
delta	vector of asymmetry parameters
i	row index
j	column index

**Value**

pi for that cell

---

Goodman_pi_matrix	<i>Computes the full matrix of model-based cell probabilities.</i>
-------------------	--

---

**Description**

Computes the full matrix of model-based cell probabilities.

**Usage**

```
Goodman_pi_matrix(phi, delta)
```

**Arguments**

phi	the symmetric matrix
delta	the vector of asymmetry parameters

**Value**

matrix of model-based probabilities

---

Goodman\_symmetric\_association\_model

*Fits the symmetric association model from Goodman (1979). Note the model is a reparameterized version of the quasi-symmetry model, so the quasi-symmetry model has the same fit indices.*

---

### Description

Fits the symmetric association model from Goodman (1979). Note the model is a reparameterized version of the quasi-symmetry model, so the quasi-symmetry model has the same fit indices.

### Usage

```
Goodman_symmetric_association_model(n)
```

### Arguments

n                    matrix of observed counts

### Value

a list containing x: design matrix used for the glm() regression beta: parameter estimates se: standard errors of beta g\_squared: G<sup>2</sup> measure of fit chisq: X<sup>2</sup> measure of fit df: degrees of freedom expected: model-based expected cell counts

---

Goodman\_uniform\_association

*Fits Goodman's (1979) uniform association model*

---

### Description

Fits Goodman's (1979) uniform association model

### Usage

```
Goodman_uniform_association(
  n,
  max_iter = 25,
  verbose = FALSE,
  exclude_diagonal = FALSE
)
```

**Arguments**

n	matrix of observed counts
max_iter	maximum number of iterations. Default is 10.
verbose	should cycle-by-cycle info be printed out? Default is FALSE
exclude_diagonal	logical. Should the cells of the main diagonal be excluded from the computations? Default is FALSE, include all cells.

**Value**

a list containing alpha: row effects beta: column effects theta: uniform association parameter log\_likelihood: log(likelihood) g\_squared:  $G^2$  fit measure chisq:  $X^2$  fit measure df: degrees of freedom

---

handle_max_i_i	<i>Case where <math>j == r, i == k == k2</math></i>
----------------	---

---

**Description**

Case where  $j == r, i == k == k2$

**Usage**

```
handle_max_i_i(i, marginal_pi, kappa, v)
```

**Arguments**

i	index into marginal_pi
marginal_pi	expected proportions for each category
kappa	current estimate of kappa coefficient
v	symmetry matrix

**Value**

second-order derivative

---

handle_max_i_k	<i>Case where <math>j == r, i != k, i == k2</math></i>
----------------	--

---

**Description**

Case where  $j == r, i != k, i == k2$

**Usage**

handle\_max\_i\_k(i, k, marginal\_pi, kappa, v)

**Arguments**

i	index into pi
k	index into v (other is i)
marginal_pi	expected proportions for each category
kappa	current estimate of kappa coefficient
v	symmetry matrix

**Value**

second-order derivative

---

handle_max_k_k2	<i>Case where <math>j == r, i != k \&amp;\&amp; i != k2</math></i>
-----------------	--

---

**Description**

Case where  $j == r, i != k \&\& i != k2$

**Usage**

handle\_max\_k\_k2(i, k, k2, marginal\_pi, kappa, v)

**Arguments**

i	index into pi
k	first index into marginal_pi
k2	second index into marginal_pi
marginal_pi	expected proportions for each category
kappa	current estimate of kappa coefficient
v	symmetry matrix

**Value**

second-order derivative

---

handle\_one\_maximum      *Case where  $\pi[i, r]$  with  $k$  and  $k2$*

---

**Description**

Case where  $\pi[i, r]$  with  $k$  and  $k2$

**Usage**

handle\_one\_maximum( $i, j, k, k2, \text{marginal\_pi}, \text{kappa}, v$ )

**Arguments**

$i$	first index of $\pi$
$j$	second index of $\pi$
$k$	first index into marginal_pi
$k2$	second index into marginal_pi
marginal_pi	expected proportions for each category
kappa	current estimate of kappa coefficient
$v$	symmetry matrix

**Value**

second order derivative

---

handle\_tied\_below\_maximum  
*Case where  $i == j, i < r, j < r$*

---

**Description**

Case where  $i == j, i < r, j < r$

**Usage**

handle\_tied\_below\_maximum( $j, k, k2, \text{marginal\_pi}, \text{kappa}, v$ )

**Arguments**

$j$	index of $\pi$
$k$	first index into marginal_pi
$k2$	second index into marginal_pi
marginal_pi	expected proportions for each of the categories
kappa	current estimate of kappa coefficient
$v$	symmetry matrix

**Value**

derivative

---

handle\_tied\_maximum     *Case where  $\pi[r, r]$  with  $k$  and  $k2$*

---

**Description**

Case where  $\pi[r, r]$  with  $k$  and  $k2$

**Usage**

handle\_tied\_maximum( $k$ ,  $k2$ , marginal\_pi, kappa, v)

**Arguments**

$k$	first index into marginal_pi
$k2$	second index into marginal_pi
marginal_pi	expected proportions for each category
kappa	current estimate of kappa coefficient
v	symmetry matrix

**Value**

second order derivative

---

handle\_untied\_below\_maximum  
                                   *Case where  $i \neq j, i < r \ \&\& \ j < r$*

---

**Description**

Case where  $i \neq j, i < r \ \&\& \ j < r$

**Usage**

handle\_untied\_below\_maximum( $i$ ,  $j$ ,  $k$ ,  $k2$ , marginal\_pi, kappa, v)

**Arguments**

i	first index of pi
j	second index of pi
k	first index of marginal_pi
k2	second index of marginal_pi
marginal_pi	expected proportions of each of the categories
kappa	current value of kappa coefficient
v	symmetry matrix

---

homicide\_black\_black *Data about charges of homicide in the state of Florida.*

---

**Description**

Counts of cases charged with homicide. The rows and columns indicate whether there was an additional charge of a felony occurring in addition to the homicide. The data is actually 3-dimensional. It is stored as 4 related matrices, each with the leading word "homicide\_" The rest of the name gives the race of the defendant and the race of the victim, separated by an underscore

**Usage**

```
homicide_black_black
```

**Format**

```
## 'homicide_black_black' Each is a matrix with 3 rows and 3 columns. Rows are classification by
police and columns are classification by the court/prosecutor. 1 = No felony 2 = Possible felony 2
= Felony
```

**Source**

Agresti, A. (1984, p. 211). Analysis of ordinal categorical data. New York: Wiley.

---

homicide\_black\_white *Data about charges of homicide in the state of Florida.*

---

### Description

Counts of cases charged with homicide. The rows and columns indicate whether there was an additional charge of a felony occurring in addition to the homicide. The data is actually 3-dimensional. It is stored as 4 related matrices, each with the leading word "homicide\_" The rest of the name gives the race of the defendant and the race of the victim, separated by an underscore.

### Usage

homicide\_black\_white

### Format

## 'homicide\_black\_white' Each is a matrix with 3 rows and 3 columns. Rows are classification by police and columns are classification by the court/prosecutor. 1 = No felony 2 = Possible felony 2 = Felony

### Source

Agresti, A. (1984, p. 211). Analysis of ordinal categorical data. New York: Wiley.

---

homicide\_white\_black *Data about charges of homicide in the state of Florida.*

---

### Description

Counts of cases charged with homicide. The rows and columns indicate whether there was an additional charge of a felony occurring in addition to the homicide. The data is actually 3-dimensional. It is stored as 4 related matrices, each with the leading word "homicide\_" The rest of the name gives the race of the defendant and the race of the victim, separated by an underscore

### Usage

homicide\_white\_black

### Format

## 'homicide\_white\_black' Each is a matrix with 3 rows and 3 columns. Rows are classification by police and columns are classification by the court/prosecutor. 1 = No felony 2 = Possible felony 2 = Felony

### Source

Agresti, A. (1984, p. 211). Analysis of ordinal categorical data. New York: Wiley.

---

homicide\_white\_white    *Data about charges of homicide in the state of Florida.*

---

**Description**

Counts of cases charged with homicide. The rows and columns indicate whether there was an additional charge of a felony occurring in addition to the homicide. The data is actually 3-dimensional. It is stored as 4 related matrices, each with the leading word "homicide\_" The rest of the name gives the race of the defendant and the race of the victim, separated by an underscore

**Usage**

homicide\_white\_white

**Format**

## 'homicide\_white\_white' Each is a matrix with 3 rows and 3 columns. Rows are classification by police and columns are classification by the court/prosecutor. 1 = No felony 2 = Possible felony 3 = Felony

**Source**

Agresti, A. (1984, p. 211). Analysis of ordinal categorical data. New York: Wiley.

---

hypothalamus\_1            *Measures of men's hypothalamus taken from cadavers. First data set.*

---

**Description**

Measures of men's hypothalamus taken from cadavers. First data set.

**Usage**

hypothalamus\_1

**Format**

# 'hypothalamus\_1' Each set is a dominance matrix (see e.g., Cliff 1996).

**Source**

Cliff, N. (1996), Ordinal methods for behavioral data analysis. Mahwah NJ: Lawrence Erlbaum.

---

hypothalamus_2	<i>Measures of men's hypothalamus taken from cadavers. Second data set.</i>
----------------	---

---

**Description**

Measures of men's hypothalamus taken from cadavers. Second data set.

**Usage**

hypothalamus\_2

**Format**

# 'hypothalamus\_2' Each set is a dominance matrix (see e.g., Cliff 1996).

**Source**

Cliff, N. (1996), Ordinal methods for behavioral data analysis. Mahwah NJ: Lawrence Erlbaum.

---

interference_12	<i>Measures of interference in memory recall study.</i>
-----------------	---

---

**Description**

Measures are within subjects, comparing a control condition to two conditions with interference. Interference condition 1 v. interference condition 2

**Usage**

interference\_12

**Format**

## 'interference\_control\_1', 'interference\_control\_2', 'interference\_12' Within-persons dominance matrices.

**Source**

Cliff, N. (1996). Ordinal methods for behavioral data analysis. Mahwah NJ: Lawrence Erlba

---

interference\_control\_1

*Measures of interference in memory recall study.*

---

**Description**

Measures are within subjects, comparing a control condition to two conditions with interference. Control v. interference condition 1

**Usage**

interference\_control\_1

**Format**

## 'interference\_control\_1', 'interference\_control\_2', 'interference\_12' Within-persons dominance matrices.

**Source**

Cliff, N. (1996). Ordinal methods for behavioral data analysis. Mahwah NJ: Lawrence Erlbaum.

---

interference\_control\_2

*Measures of interference in memory recall study.*

---

**Description**

Measures are within subjects, comparing a control condition to two conditions with interference. Control v. interference condition 2

**Usage**

interference\_control\_2

**Format**

## 'interference\_control\_1', 'interference\_control\_2', 'interference\_12' Within-persons dominance matrices.

**Source**

Cliff, N. (1996). Ordinal methods for behavioral data analysis. Mahwah NJ: Lawrence Erlba

---

Ireland\_marginal\_homogeneity  
*Fits marginal homogeneity model*

---

### Description

Fits the marginal homogeneity model according to the minimum discriminant information. Ireland, C. T., Ku, H. H., & Kullback, S. (1969). Symmetry and marginal homogeneity of an  $r \times r$  contingency table. *Journal of the American Statistical Association*, 64(328), 1323-1341.

### Usage

```
Ireland_marginal_homogeneity(  
  n,  
  truncated = FALSE,  
  max_iter = 15,  
  verbose = FALSE  
)
```

### Arguments

n	matrix of observed counts
truncated	should the diagonal be excluded. Default is FALSE, include the diagonal.
max_iter	maximum number of iterations to perform
verbose	should cycle-by-cycle information be printed out. Default is FALSE.

### Value

a list containing mdis: value of the minimum discriminant information statistic (approx chi-squared)  
df: degrees of freedom x\_star: matrix of model-based counts p\_star: matrix of model-based p-values

### Examples

```
Ireland_marginal_homogeneity(vision_data)
```

---

Ireland\_mdis                      *Computes the MDIS between the two matrices provided.*

---

### Description

Computes the MDIS between the two matrices provided.

### Usage

```
Ireland_mdis(n, x_star, truncated = FALSE)
```

**Arguments**

n	first matrix (usually observed counts)
x_star	second matrix (usually model-based)
truncated	should the diagonal be ignored. Default is FALSE, include the diagonal elements.

**Value**

value of the MDIS criterion

---

Ireland\_normalize\_for\_truncation

*Renormalize counts to account for truncation of diagonal*

---

**Description**

Renormalize counts to account for truncation of diagonal

**Usage**

Ireland\_normalize\_for\_truncation(n)

**Arguments**

n	matrix of observed counts
---	---------------------------

**Value**

matrix n with diagonal set to 0.0

---

Ireland\_quasi\_symmetry

*Fit for quasi-symmetry model. Obtained by subtraction, so no model-based probabilities.*

---

**Description**

Fit for quasi-symmetry model. Obtained by subtraction, so no model-based probabilities.

**Usage**

Ireland\_quasi\_symmetry(n, truncated = FALSE)

**Arguments**

n                    matrix of observed counts  
truncated            should the diagonal be excluded, Default is FALSE, include the diagonal.

**Value**

a list with mdis = MDIS value and df = degrees of freedom for quasi-symmetry model

**See Also**

[Ireland\_quasi\_symmetry\_model()]

**Examples**

```
Ireland_quasi_symmetry(vision_data)
```

---

```
Ireland_quasi_symmetry_model
```

*Fits the quasi-symmetry model.*

---

**Description**

Fits the model according to the MDIS criterion.

**Usage**

```
Ireland_quasi_symmetry_model(  
  n,  
  truncated = FALSE,  
  max_iter = 5,  
  verbose = FALSE  
)
```

**Arguments**

n                    matrix of observed counts  
truncated            should the diagonal be excluded. Default is FALSE, include diagonal cells.  
max\_iter            maximum number of iterations in minimizing the criterion. Default is 4  
verbose             logical variable, should cycle-by-cycle info be printed. Default is FALSE.

**Value**

a list containing mdis: value of the MDIS at termination df: degrees of freedom x\_star: matrix of model-reproduced counts p\_star: matrix of model-reproduced p-values

**See Also**

[Ireland\_quasi\_symmetry()]

**Examples**

```
Ireland_quasi_symmetry_model(vision_data)
```

---

Ireland_symmetry	<i>Fits symmetry model.</i>
------------------	-----------------------------

---

**Description**

Ireland, C. T., Ku, H. H., & Kullback, S. (1969). Symmetry and marginal homogeneity of an  $r \times r$  contingency table. *Journal of the American Statistical Association*, 64(328), 1323-1341.

**Usage**

```
Ireland_symmetry(n, truncated = FALSE)
```

**Arguments**

n                    matrix of observed counts  
truncated            should the diagonal be excluded. Default is FALSE, include the diagonal.

**Value**

a list containing mdis: value of the minimum discriminant information statistic (approx chi-squared)  
df: degrees of freedom x\_star: matrix of model-based counts p\_star: matrix of model-based p-values

**Examples**

```
Ireland_symmetry(vision_data)
```

---

is_invertible	<i>Tests whether a square matrix is invertible (non singular)</i>
---------------	---

---

**Description**

from stackoverflow: <https://stackoverflow.com/questions/24961983/how-to-check-if-a-matrix-has-an-inverse-in-the-r-language>

**Usage**

```
is_invertible(X)
```

**Arguments**

x                      Matrix to be tested. It is assumed X is square

**Value**

logical: TRUE if inversion succeeds, FALSE otherwise

is\_missing\_or\_infinite

*Determines if its argument is not a valid number.*

**Description**

Determines if its argument is not a valid number.

**Usage**

is\_missing\_or\_infinite(x)

**Arguments**

x                      Numeric. Number of be evaluated

**Value**

TRUE if is.na(), is.nan(), or is.infinite() returns TRUE. FALSE otherwise.

kappa

*Computes Cohen's 1960 kappa coefficient*

**Description**

Computes Cohen's 1960 kappa coefficient

**Usage**

kappa(n)

**Arguments**

n                      matrix of observed counts

**Value**

kappa coefficient

---

 likelihood\_ratio\_chisq

*Computes the likelihood ratio  $G^2$  measure of fit.*


---

**Description**

Computes the likelihood ratio  $G^2$  measure of fit.

**Usage**

```
likelihood_ratio_chisq(n, pi, exclude_diagonal = FALSE)
```

**Arguments**

n	Matrix of observed counts
pi	Matrix of same dimensions as n. Model-based matrix of predicted proportions
exclude_diagonal	logical. Should the diagonal cells of a square matrix be excluded from the computation. Default is FALSE. The effect of setting it to TRUE for non-square matrices may be unintuitive and should be avoided.

**Value**

$G^2$

---

loadRData

*Function to load a data set written out using save().*


---

**Description**

The first (should be the only) element read from the RData file is returned From: <https://stackoverflow.com/questions/557721/can-i-load-an-object-into-a-variable-name-that-i-specify-from-an-r-data-file>

**Usage**

```
loadRData(file_name)
```

**Arguments**

file_name	Character. Name of the file containing the RData
-----------	--

**Details**

```
usage x <- loadRData(file_name="")
```

**Value**

the first object from the restored RData

---

log_likelihood	<i>Computes the multinomial log(likelihood).</i>
----------------	--

---

**Description**

Computes the multinomial log(likelihood).

**Usage**

```
log_likelihood(n, pi, exclude_diagonal = FALSE)
```

**Arguments**

n	Matrix of observed counts
pi	Matrix of same dimensions as n. Model-based matrix of predicted proportions
exclude_diagonal	logical. Should diagonal cells of square matrix be excluded from the computation? Default is FALSE. The effect of setting it to TRUE for non-square matrices may be unintuitive and should be avoided.

**Value**

log(likelihood)

---

log_linear_add_all_diagonals	<i>Adds indicator variables for the diagonal cells in table n.</i>
------------------------------	--

---

**Description**

Adds indicator variables for the diagonal cells in table n.

**Usage**

```
log_linear_add_all_diagonals(n, x)
```

**Arguments**

n	the matrix of observed counts
x	the design matrix to be augmented

**Value**

new design matrix with nrow(n) columns added. The columns are all 0 unless the row corresponds to a diagonal cell in n, in which case the entry is 1

**Examples**

```
x <- log_linear_main_effect_design(vision_data)
x_prime <- log_linear_add_all_diagonals(vision_data, x)
```

---

log\_linear\_append\_column

*Appends a column to an existing design matrix.*

---

**Description**

Takes the design matrix provided and appends the new column

**Usage**

```
log_linear_append_column(x, x_new, position = ncol(x) + 1)
```

**Arguments**

x	the original design matrix
x_new	the column to be appended
position	column index within the new matrix for the new column. Defaults to last position = appending the column

**Value**

the new design matrix

**Examples**

```
x <- log_linear_main_effect_design(vision_data)
new_column <- c(1, 0, 0, 0,
               0, 1, 0, 0,
               0, 0, 1, 0,
               0, 0, 0, 1)
x_prime <- log_linear_append_column(x, new_column)
```

---

log\_linear\_create\_coefficient\_names  
*Creates missing column names*

---

**Description**

Creates missing column names

**Usage**

```
log_linear_create_coefficient_names(x, n, effect_names = NULL)
```

**Arguments**

x	the design matrix being modified
n	the matrix of observed counts
effect_names	user specified names to be applied to effects after the intercept and main effects. Default is NULL

**Value**

vector of names to apply to x

---

log\_linear\_create\_linear\_by\_linear  
*Creates a vector containing the linear-by-linear vector.*

---

**Description**

Uses the ordinal ranks (1, 2, ..., nrow(n)) as data.

**Usage**

```
log_linear_create_linear_by_linear(n, centered = FALSE)
```

**Arguments**

n	the matrix of observed cell counts
centered	should the variables be centered before the product is computed

**Value**

a vector containing the new variable

**Examples**

```
linear <- log_linear_create_linear_by_linear(vision_data)
x <- log_linear_equal_weight_agreement_design(vision_data)
x_prime <- log_linear_append_column(x, linear)
```

---

```
log_Linear_create_log_n
```

*Computes the logs of the cell frequencies.*

---

**Description**

In the case of an observed 0, epsilon is inserted into the cell before the log is taken.

**Usage**

```
log_Linear_create_log_n(n, epsilon = 1e-06, all_cells = FALSE)
```

**Arguments**

n	matrix of cell counts
epsilon	amount to be inserted into cell with observed 0.
all_cells	add epsilon to all cells or just those with 0 observed frequencies

**Value**

a list containing: log\_n – a vector of log frequencies and dat – modified version of the cell counts data

---

```
log_linear_equal_weight_agreement_design
```

*Creates design matrix for model with main effects and a single agreement parameter delta.*

---

**Description**

The model has main effects for rows and for columns, plus an additional parameter for the agreement (diagonal) cells.

**Usage**

```
log_linear_equal_weight_agreement_design(n, n_raters = 2)
```

**Arguments**

n	the matrix of cell counts
n_raters	number of raters. Currently only 2 (the default) are supported. This is an extension point for future work.

**Value**

design matrix for the model

**Examples**

```
x <- log_linear_equal_weight_agreement_design(vision_data)
```

---

log_linear_fit	<i>Fits a log-linear model to the data provided, using the design matrix provided. Names for the effects will be "rows1", "cols1" etc. If there are remaining entries, they can be specified as the "effect_names" character vector. This function is a wrapper around a call to glm() that handles some of the details of the call and packages the output in a more convenient form.</i>
----------------	--

---

**Description**

Fits a log-linear model to the data provided, using the design matrix provided. Names for the effects will be "rows1", "cols1" etc. If there are remaining entries, they can be specified as the "effect\_names" character vector. This function is a wrapper around a call to glm() that handles some of the details of the call and packages the output in a more convenient form.

**Usage**

```
log_linear_fit(n, x, effect_names = NULL)
```

**Arguments**

n	matrix of observed counts to be fit
x	design matrix for predictor variables
effect_names	character vector of additional names to apply to the columns of x The default is NULL, in which case the columns will be labeled "model1" etc.

**Value**

a list containing x: the design matrix beta: the regression parameters se: the vector of standard errors g\_squared: G<sup>2</sup> fit measure chisq: X<sup>2</sup> fit measure df: degrees of freedom expected: matrix of expected frequencies

---

`log_linear_main_effect_design`

*Design matrix for baseline independence model with main effects for rows and columns.*

---

**Description**

It is intended as a straw-man model as it assumes no agreement beyond chance.

**Usage**

```
log_linear_main_effect_design(n, n_raters = 2)
```

**Arguments**

<code>n</code>	the matrix of cell counts
<code>n_raters</code>	number of raters. Currently only 2 (the default) are supported. This is an extension point for future work.

**Value**

the design matrix for the model

**Examples**

```
x <- log_linear_main_effect_design(vision_data)
```

---

`log_linear_matrix_to_vector`

*Converts a matrix of data into a vector suitable for use in analysis with the design matrices created. Unlike simply calling `vector()` on the matrix the resulting vector is organized by rows, then columns. This order corresponds to the order in the design matrix.*

---

**Description**

Converts a matrix of data into a vector suitable for use in analysis with the design matrices created. Unlike simply calling `vector()` on the matrix the resulting vector is organized by rows, then columns. This order corresponds to the order in the design matrix.

**Usage**

```
log_linear_matrix_to_vector(dat)
```

**Arguments**

dat                    the matrix to be converted a vector

**Value**

a vector suitable to use as dependent variable, e.g. in a call to glm()

log\_linear\_quasi\_symmetry\_model\_design

*Creates the design matrix for a quasi-symmetry design*

**Description**

Creates the design matrix for a quasi-symmetry design

**Usage**

log\_linear\_quasi\_symmetry\_model\_design(n)

**Arguments**

n                    matrix of observed counts

**Value**

design matrix for quasi-symmetry design

log\_linear\_remove\_column

*Removes a column from an existing design matrix.*

**Description**

Takes the design matrix provided and removes the column in the position specified

**Usage**

log\_linear\_remove\_column(x, position = ncol(x))

**Arguments**

x                    the original design matrix

position            column index within the new matrix for the new column. Defaults to last position

**Value**

the new design matrix

**Examples**

```
x <- log_linear_main_effect_design(vision_data)
linear <- log_linear_create_linear_by_linear(vision_data)
x_prime <- log_linear_append_column(x, linear)
x_again <- log_linear_remove_column(x_prime, ncol(x_prime))
```

---

log\_linear\_symmetry\_design

*Creates design matrix for symmetry model.*

---

**Description**

Creates design matrix for symmetry model.

**Usage**

```
log_linear_symmetry_design(n)
```

**Arguments**

n                    matrix of observed counts

**Value**

design matrix for the model

---

logit

*Computes the log-odds (logit) for the value provided*

---

**Description**

Computes the log-odds (logit) for the value provided

**Usage**

```
logit(p)
```

**Arguments**

p                    Numeric. Assumed to lie in interval(0, 1)

**Value**

$\log(p / (1.0 - p))$

McCullagh\_compute\_c\_plus

*Computes sums c+ used in maximizing the log(likelihood)*

---

**Description**

Computes sums c+ used in maximizing the log(likelihood)

**Usage**

McCullagh\_compute\_c\_plus(phi, alpha)

**Arguments**

phi                    matrix of symmetry parameters

alpha                 vector of asymmetry parameters

**Value**

list of c\_i\_plus and c\_plus\_i

---

McCullagh\_compute\_condition

*Compute the linear constraint on psi elements for identifiability.*

---

**Description**

Compute the linear constraint on psi elements for identifiability.

**Usage**

McCullagh\_compute\_condition(psi)

**Arguments**

psi                    symmetry matrix

**Value**

value of the constraint

---

`McCullagh_compute_cumulative_sums`*Computes cumulative sums for rows,*

---

**Description**

Computes cumulative sums for rows,

**Usage**

```
McCullagh_compute_cumulative_sums(n)
```

**Arguments**

`n` matrix of observed counts

**Value**

R where  $R[i, j]$  contains cumulative sum of  $n[i, j]$

---

`McCullagh_compute_cumulatives`*Computes the model-based cumulative probability matrices pij and qij*

---

**Description**

Computes the model-based cumulative probability matrices pij and qij

**Usage**

```
McCullagh_compute_cumulatives(psi, delta, alpha, c = 1)
```

**Arguments**

`psi` the matrix of symmetry parameters  
`delta` the scalar asymmetry parameter  
`alpha` the vector of asymmetry parameters  
`c` the normalizing constant for the pis to sum to 1.0 Default value is 1.0

**Value**

list containing matrices pij and qij

---

McCullagh\_compute\_df *Computes the degrees of freedom for the model*

---

**Description**

Computes the degrees of freedom for the model

**Usage**

```
McCullagh_compute_df(M, generalized = FALSE)
```

**Arguments**

M                    the size of the M X M observed matrix  
generalized        is the generalized model being fit? Default is FALSE, regular model

---

McCullagh\_compute\_gamma  
*Computes gamma from x and beta*

---

**Description**

Computes gamma from x and beta

**Usage**

```
McCullagh_compute_gamma(x, beta, s, c)
```

**Arguments**

x                    predictor variables  
beta                vector of regression coefficients  
s                    number of rows in the table  
c                    number of score levels in table

**Value**

vector of model-based gamma coefficients

---

`McCullagh_compute_gamma_from_phi`*Computes value of gamma from phi. Inverse of usual computation.*

---

**Description**

Computes value of gamma from phi. Inverse of usual computation.

**Usage**

```
McCullagh_compute_gamma_from_phi(phi, j, gamma)
```

**Arguments**

<code>phi</code>	value to compute from
<code>j</code>	index to use in computation
<code>gamma</code>	vector of gamma values (model-based cumulative logits)

**Value**

`gamma[j]` given `phi` and `gamma[j + 1]`

---

`McCullagh_compute_gamma_plus_1_from_phi`*Computes value of gamma[j + 1] from phi.*

---

**Description**

Computes value of gamma[j + 1] from phi.

**Usage**

```
McCullagh_compute_gamma_plus_1_from_phi(phi, j, gamma)
```

**Arguments**

<code>phi</code>	value used in computation
<code>j</code>	index to use in computation
<code>gamma</code>	vector of gamma values (model-based cumulative logits)

**Value**

`gamma[j + 1]` given `phi` and `gamma[j]`

---

McCullagh\_compute\_generalized\_cumulatives

*Coompute the model-based cumulative probabilities pij and qij.*

---

### Description

Coompute the model-based cumulative probabilities pij and qij.

### Usage

McCullagh\_compute\_generalized\_cumulatives(psi, delta\_vec, alpha, c = 1)

### Arguments

psi	symmetry matrix
delta_vec	vector of asymmetry parameters
alpha	vector of asymmetry parameters
c	normalizing constant so pis sum to 1. Defaults to 1.0

### Value

matrices of model-based cumulative probabilities pij and qij

---

McCullagh\_compute\_generalized\_pi

*Cpompute matrix pi under generalized model.*

---

### Description

Cpompute matrix pi under generalized model.

### Usage

McCullagh\_compute\_generalized\_pi(psi, delta\_vec, alpha, c = 1)

### Arguments

psi	the matrix of symmetry parameters
delta_vec	the vector asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

### Value

the matrix pi

---

McCullagh\_compute\_lambda

*Computes lambda, log of cumulative odds.*

---

**Description**

Computes lambda, log of cumulative odds.

**Usage**

```
McCullagh_compute_lambda(n, use_half = TRUE)
```

**Arguments**

n	matrix of observed counts
use_half	logical whether or not to add half to the cell count before taking the logit. Default value is TRUE.

---

McCullagh\_compute\_log\_l

*Computes the log(likelihood) for the general nonlinear model.*

---

**Description**

Computes the log(likelihood) for the general nonlinear model.

**Usage**

```
McCullagh_compute_log_l(n, phi)
```

**Arguments**

n	matrix of observed counts
phi	vector of model-based parameters

**Value**

log(likelihood)

---

McCullagh\_compute\_Nij *Compute the observed sums Nij*

---

**Description**

Compute the observed sums Nij

**Usage**

McCullagh\_compute\_Nij(n)

**Arguments**

n                      the matrix of observed counts

**Value**

a list containing Pij and Qij

---

McCullagh\_compute\_omega  
*Compute the value of the Lagrange multiplier for the constraint on psi.*

---

**Description**

Compute the value of the Lagrange multiplier for the constraint on psi.

**Usage**

McCullagh\_compute\_omega(n, pi)

**Arguments**

n                      matrix of observed counts  
pi                     matrix of model-based probabilities pi.

**Value**

the value of the Lagrange multiplier.

---

McCullagh\_compute\_phi *Computes phi based on gamma*

---

**Description**

Computes phi based on gamma

**Usage**

```
McCullagh_compute_phi(gamma, j)
```

**Arguments**

gamma	vector of gamma parameters
j	index of phi to compute

**Value**

phi[j]

---

McCullagh\_compute\_phi\_matrix  
*Compute matrix of model-based logits*

---

**Description**

Compute matrix of model-based logits

**Usage**

```
McCullagh_compute_phi_matrix(gamma)
```

**Arguments**

gamma	matrix of model-based cumulative odds
-------	---------------------------------------

**Value**

matrix of model-based logits

---

McCullagh\_compute\_pi    *Compute the regular (non-cumulative) model-based pi values*

---

**Description**

Compute the regular (non-cumulative) model-based pi values

**Usage**

McCullagh\_compute\_pi(psi, delta, alpha, c)

**Arguments**

psi	the matrix of symmetry parameters
delta	the scalar asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

**Value**

the matrix pi

---

McCullagh\_compute\_pi\_from\_beta  
*Computes matrix of p-values pi based on x and current value of beta.*

---

**Description**

Computes matrix of p-values pi based on x and current value of beta.

**Usage**

McCullagh\_compute\_pi\_from\_beta(n, x, beta)

**Arguments**

n	matrix of observed counts
x	design matrix
beta	current values of location model regression parameters

**Value**

matrix of model-based pi values

---

 McCullagh\_compute\_pi\_from\_gamma

*Compute the cell probabilities pi from gamma.*


---

**Description**

Compute the cell probabilities pi from gamma.

**Usage**

McCullagh\_compute\_pi\_from\_gamma(gamma)

**Arguments**

gamma                    matrix of gamma values

**Value**

c X c matrix of p-values pi

---

 McCullagh\_compute\_regression\_weights

*Computes regression weights w;  $R_{dot_j} * (N - R_{dot_j[j]}) * (n_{do\_j[j]} a = na_{dot\_j[j+ 1]})$* 


---

**Description**

Computes regression weights w;  $R_{dot_j} * (N - R_{dot_j[j]}) * (n_{do\_j[j]} a = na_{dot\_j[j+ 1]})$

**Usage**

McCullagh\_compute\_regression\_weights(n)

**Arguments**

n                            matrix of observed counts

**Value**

list of w, and sum(w)

McCullagh\_compute\_s\_plus

*Compute sums too use in maximizing log(likelihood)*

---

**Description**

Compute sums too use in maximizing log(likelihood)

**Usage**

McCullagh\_compute\_s\_plus(n)

**Arguments**

n                    matrix of observed counts

**Value**

list of s\_i\_plus and s\_plus\_i

---

McCullagh\_compute\_update

*Compute the Newton-Raphson update.*

---

**Description**

Compute the Newton-Raphson update.

**Usage**

McCullagh\_compute\_update(gradient, hessian)

**Arguments**

gradient            gradient vector of log(likelihood) wrt parameters

hessian             hessian of log(likelihood) wrt parameters

**Value**

vector with update values for each of the parameters

---

McCullagh\_compute\_z    *Computes Z, where z is w \* lambda.*

---

**Description**

Computes Z, where z is w \* lambda.

**Usage**

```
McCullagh_compute_z(lambda, w)
```

**Arguments**

lambda	cumulative logits
w	weights to apply to the logits

**Value**

z, sum of product of lambda

---

McCullagh\_conditional\_symmetry

*Fits the McCullagh (1978) conditional-symmetry model.*

---

**Description**

McCullagh, P. (1978). A class of parametric models for the analysis of square contingency tables with ordered categories. *Biometrika*, 65(2) 413-418.

**Usage**

```
McCullagh_conditional_symmetry(n, max_iter = 5, verbose = FALSE)
```

**Arguments**

n	matrix of observed counts
max_iter	maximum number of iterations to maximize the log(likelihood)
verbose	should cycle-by-cycle info be printed. Default is FALSE.

**Value**

a list containing theta: the asymmetry parameter chisq: chi-square g\_squared: likelihood ratio  $G^2$   
df: degrees of freedom

**Examples**

```
McCullagh_conditional_symmetry(vision_data)
```

---

McCullagh\_conditional\_symmetry\_compute\_s  
*Computes sums used in maximizing theta.*

---

**Description**

Computes sums used in maximizing theta.

**Usage**

McCullagh\_conditional\_symmetry\_compute\_s(n)

**Arguments**

n                    matrix of observed counts

**Value**

list with s\_i\_plus and s\_plus-i

---

McCullagh\_conditional\_symmetry\_initialize\_phi  
*Initializes symmetry matrix phi*

---

**Description**

Initializes symmetry matrix phi

**Usage**

McCullagh\_conditional\_symmetry\_initialize\_phi(M)

**Arguments**

M                    the number of rows/columns in phi

**Value**

the phi matrix

---

McCullagh\_conditional\_symmetry\_maximize\_phi  
*Maximizes log(likelihood) wrt phi.*

---

**Description**

Maximizes log(likelihood) wrt phi.

**Usage**

McCullagh\_conditional\_symmetry\_maximize\_phi(n)

**Arguments**

n                    matrix of observed counts

**Value**

phi matrix

---

McCullagh\_conditional\_symmetry\_maximize\_theta  
*Maximizes the log(likelihood) wrt theta.*

---

**Description**

Maximizes the log(likelihood) wrt theta.

**Usage**

McCullagh\_conditional\_symmetry\_maximize\_theta(n)

**Arguments**

n                    matrix of observed counts

**Value**

value of asymmetry parameter theta

McCullagh\_conditional\_symmetry\_pi

*Computes model-based proportions.*

---

**Description**

Computes model-based proportions.

**Usage**

McCullagh\_conditional\_symmetry\_pi(phi, theta)

**Arguments**

phi	the symmetric matrix
theta	the asymmetry parameter

**Value**

matrix of model-based p-values

---

McCullagh\_derivative\_condition\_wrt\_psi

*Derivative of the condition wrt psi[i, j].*

---

**Description**

Derivative of the condition wrt psi[i, j].

**Usage**

McCullagh\_derivative\_condition\_wrt\_psi(i, j)

**Arguments**

i	first index of psi
j	second index of psi

**Value**

derivative

---

McCullagh\_derivative\_gamma\_plus\_1\_wrt\_phi  
*Derivative of gamma j + 1 wrt phi.*

---

**Description**

Derivative of gamma j + 1 wrt phi.

**Usage**

McCullagh\_derivative\_gamma\_plus\_1\_wrt\_phi(gamma, j, phi)

**Arguments**

gamma	vector
j	index of gamma to take derivative of
phi	scalar phi taking derivative wrt

**Value**

derivative

---

McCullagh\_derivative\_gamma\_wrt\_phi  
*Derivative of gamma wrt phi.*

---

**Description**

Version given in McCullagh isn't right.

**Usage**

McCullagh\_derivative\_gamma\_wrt\_phi(gamma, j, phi)

**Arguments**

gamma	vector of cumulative logits
j	index of derivative sought
phi	scalar phi taking derivative wrt

**Value**

derivative

---

McCullagh\_derivative\_gamma\_wrt\_y  
*Derivative of y wrt gamma.*

---

**Description**

Assumes a logit link is being used.

**Usage**

McCullagh\_derivative\_gamma\_wrt\_y(gamma, i, j)

**Arguments**

gamma	matrix of gamma values
i	row index of gamma
j	column index of gamma

**Value**

derivative

---

McCullagh\_derivative\_lagrangian\_wrt\_delta  
*Derivative of Lagrange multiplier wrt scalar delta.*

---

**Description**

Derivative of Lagrange multiplier wrt scalar delta.

**Usage**

McCullagh\_derivative\_lagrangian\_wrt\_delta(n, psi, delta, alpha, c = 1)

**Arguments**

n	matrix of observed counts
psi	symmetry matrix
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing coefficient so that sum of pi = 1. Default value is 1.0

**Value**

value of the derivative

---

McCullagh\_derivative\_lagrangian\_wrt\_delta\_vec  
*Derivative of Lagrangian wrt delta\_vec.*

---

**Description**

Derivative of Lagrangian wrt delta\_vec.

**Usage**

```
McCullagh_derivative_lagrangian_wrt_delta_vec(
  n,
  k,
  psi,
  delta_vec,
  alpha,
  c = 1
)
```

**Arguments**

n	matrix of observed counts
k	index of delta_vec to compute derivative wrt
psi	matrix of symmetry parameters
delta_vec	vector asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh\_derivative\_lagrangian\_wrt\_psi  
*Derivative of Lagrangian wrt psi[i1, j1].*

---

**Description**

Derivative of Lagrangian wrt psi[i1, j1].

**Usage**

```
McCullagh_derivative_lagrangian_wrt_psi(n, i1, j1, psi, delta, alpha, c = 1)
```

**Arguments**

n	matrix of observed counts
i1	first index of psi
j1	first index of psi
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh\_derivative\_log\_l\_wrt\_alpha

*Derivative of log(likelihood) wrt alpha[index].*

---

**Description**

Derivative of log(likelihood) wrt alpha[index].

**Usage**

McCullagh\_derivative\_log\_l\_wrt\_alpha(n, index, psi, delta, alpha, c = 1)

**Arguments**

n	matrix of observed counts
index	index of alpha
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

 McCullagh\_derivative\_log\_l\_wrt\_beta

*Derivative of log(likelihood) wrt beta, as given in appendix of McCullagh.*

---

### Description

McCullagh, P. (1980). Regression models for ordinal data. *Journal of the Royal Statistical Society, Series B*, 42(2), 109-142. With assist from appendix of Agresti, (1984). Agresti, A. (1984). *Analysis of ordinal categorical data*. New York, Wiley, p. 244-246.

### Usage

```
McCullagh_derivative_log_l_wrt_beta(n, x, gamma)
```

### Arguments

n	matrix of observed counts
x	design matrix for location
gamma	matrix of model-based cumulative logits

### Value

derivative

---

McCullagh\_derivative\_log\_l\_wrt\_c

*Derivative of log(likelihood) wrt c.*

---

### Description

Derivative of log(likelihood) wrt c.

### Usage

```
McCullagh_derivative_log_l_wrt_c(n, psi, delta, alpha, c)
```

### Arguments

n	matrix of observed counts
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh\_derivative\_log\_l\_wrt\_delta

*Derivative of log(likelihood) wrt delta (scalar or vector).*

---

**Description**

Derivative of log(likelihood) wrt delta (scalar or vector).

**Usage**

McCullagh\_derivative\_log\_l\_wrt\_delta(n, psi, delta, alpha, c = 1, k = 1)

**Arguments**

n	matrix of observed counts
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.
k	index into delta_vec. Defaults to 1.

**Value**

derivative

---

McCullagh\_derivative\_log\_l\_wrt\_delta\_vec

*Derivative of log(likelihood) wrt delta\_vec[k].*

---

**Description**

Derivative of log(likelihood) wrt delta\_vec[k].

**Usage**

McCullagh\_derivative\_log\_l\_wrt\_delta\_vec(n, k, psi, delta\_vec, alpha, c = 1)

**Arguments**

n	matrix of observed counts
k	index of delta_vec
psi	matrix of symmetry parameters
delta_vec	vector asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh\_derivative\_log\_l\_wrt\_params

*Derivative of log(likelihood) wrt parameters.*

---

**Description**

Derivative of log(likelihood) wrt parameters.

**Usage**

McCullagh\_derivative\_log\_l\_wrt\_params(n, x, beta)

**Arguments**

n	matrix of observed counts
x	design matrix for location model
beta	vector of regression parameters for location model

**Value**

gradient vector

---

McCullagh\_derivative\_log\_l\_wrt\_phi  
*Derivative of log(likelihood) wrt phi[i, j]*

---

**Description**

Derivative of log(likelihood) wrt phi[i, j]

**Usage**

McCullagh\_derivative\_log\_l\_wrt\_phi(n, phi, i, j)

**Arguments**

n	matrix of observed counts
phi	matrix of phi-values
i	row index of phi
j	column index of phi

**Value**

derivative

---

McCullagh\_derivative\_log\_l\_wrt\_psi  
*Derivative of log(likelihood) wrt psi.*

---

**Description**

Derivative of log(likelihood) wrt psi.

**Usage**

McCullagh\_derivative\_log\_l\_wrt\_psi(n, i1, j1, psi, delta, alpha, c = 1)

**Arguments**

n	matrix of observed counts
i1	row index of psi
j1	column index of psi
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh\_derivative\_omega\_wrt\_alpha

*Derivative of Lagrange multiplier omega wrt alpha[index].*

---

**Description**

Derivative of Lagrange multiplier omega wrt alpha[index].

**Usage**

McCullagh\_derivative\_omega\_wrt\_alpha(n, index, psi, delta, alpha, c = 1)

**Arguments**

n	matrix of observed counts
index	index of alpha
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh\_derivative\_omega\_wrt\_c

*Derivative of Lagrange multiplier omega wrt c.*

---

**Description**

Derivative of Lagrange multiplier omega wrt c.

**Usage**

McCullagh\_derivative\_omega\_wrt\_c(n, psi, delta, alpha, c)

**Arguments**

n	matrix of observed counts
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh\_derivative\_omega\_wrt\_delta

*Derivative of Lagrange multiplier omega wrt scalar delta.*

---

**Description**

Derivative of Lagrange multiplier omega wrt scalar delta.

**Usage**

```
McCullagh_derivative_omega_wrt_delta(n, psi, delta, alpha, c = 1)
```

**Arguments**

n	matrix of observed counts
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

 McCullagh\_derivative\_omega\_wrt\_delta\_vec

*Derivative of Lagrange multiplier omega wrt vector delta[k].*


---

**Description**

Derivative of Lagrange multiplier omega wrt vector delta[k].

**Usage**

```
McCullagh_derivative_omega_wrt_delta_vec(n, k, psi, delta_vec, alpha, c = 1)
```

**Arguments**

n	matrix of observed counts
k	index of delta_vec
psi	matrix of symmetry parameters
delta_vec	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

 McCullagh\_derivative\_omega\_wrt\_psi

*Derivative of Lagrange multiplier omega wrt psi[i, j].*


---

**Description**

Derivative of Lagrange multiplier omega wrt psi[i, j].

**Usage**

```
McCullagh_derivative_omega_wrt_psi(n, i, j, psi, delta, alpha, c = 1)
```

**Arguments**

n	matrix of observed counts
i	first index of psi
j	second index of psi
psi	symmetry matrix
delta	scalar or vector asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Defaults to 1.0

---

McCullagh\_derivative\_phi\_wrt\_gamma  
*Derivative of phi wrt gamma.*

---

**Description**

Derivative of phi wrt gamma.

**Usage**

McCullagh\_derivative\_phi\_wrt\_gamma(gamma, j)

**Arguments**

gamma	vector of gamma values
j	index of gamma for which to compute the derivative

**Value**

derivative

---

McCullagh\_derivative\_pi\_wrt\_alpha  
*Derivative of pi[i, j] wrt alpha[index].*

---

**Description**

Derivative of pi[i, j] wrt alpha[index].

**Usage**

McCullagh\_derivative\_pi\_wrt\_alpha(i, j, index, psi, delta, alpha, c = 1)

**Arguments**

i	row index of pi
j	column index of pi
index	index of alpha
psi	the matrix of symmetry parameters
delta	the scalar asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

**Value**

derivative

---

McCullagh\_derivative\_pi\_wrt\_c  
*Derivative pi[i, j] wrt c.*

---

**Description**

Derivative pi[i, j] wrt c.

**Usage**

McCullagh\_derivative\_pi\_wrt\_c(i, j, psi, delta, alpha, c)

**Arguments**

i	row index of pi
j	column index of pi
psi	the matrix of symmetry parameters
delta	the scalar or vector asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0

**Value**

derivative

---

McCullagh\_derivative\_pi\_wrt\_delta  
*Derivative of pi[i, j] wrt delta.*

---

**Description**

Derivative of pi[i, j] wrt delta.

**Usage**

McCullagh\_derivative\_pi\_wrt\_delta(i, j, psi, delta, alpha, c = 1)

**Arguments**

i	row index of pi
j	column index of pi
psi	the matrix of symmetry parameters
delta	the scalar asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

**Value**

derivative

---

McCullagh\_derivative\_pi\_wrt\_delta\_vec  
*Derivative pi[i, j] wrt delta[k].*

---

**Description**

Derivative pi[i, j] wrt delta[k].

**Usage**

McCullagh\_derivative\_pi\_wrt\_delta\_vec(i, j, k, psi, delta\_vec, alpha, c = 1)

**Arguments**

i	row index of pi
j	column index of pi
k	index of delta_vec
psi	the matrix of symmetry parameters
delta_vec	the vector asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

**Value**

derivative

---

McCullagh\_derivative\_pi\_wrt\_psi

*Derivative of  $\pi[i, j]$  wrt  $\psi[i1, j1]$ .*

---

**Description**

Derivative of  $\pi[i, j]$  wrt  $\psi[i1, j1]$ .

**Usage**

McCullagh\_derivative\_pi\_wrt\_psi(i, j, i1, j1, psi, delta, alpha, c = 1)

**Arguments**

i	row index of pi
j	column index of pi
i1	row index of psi
j1	column index of psi
psi	the matrix of symmetry parameters
delta	the scalar asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

**Value**

derivative

---

McCullagh\_derivative\_pij\_wrt\_alpha

*Derivative of  $\pi[i, j]$  wrt  $\alpha[index]$*

---

**Description**

Derivative of  $\pi[i, j]$  wrt  $\alpha[index]$

**Usage**

McCullagh\_derivative\_pij\_wrt\_alpha(i, j, index, psi, delta, alpha, c = 1)

**Arguments**

i	row index of pij
j	column index of pij
index	index of alpha
psi	matrix of symmetry parameters
delta	scalar or vector of asymmetry parameters
alpha	vector of asymmetry parameters
c	normalizing constant to make pi sum to 1.0. Default ot 1.0

**Value**

derivative

---

McCullagh\_derivative\_pij\_wrt\_c  
*Derivative pij[i, j] wrt c.*

---

**Description**

Derivative pij[i, j] wrt c.

**Usage**

```
McCullagh_derivative_pij_wrt_c(i, j, psi, delta, alpha, c)
```

**Arguments**

i	row index of pij
j	column index of pij
psi	matrix of symmetry parameters
delta	scalar or vector of asymmetry parameters
alpha	vector of asymmetry parameters
c	normalizing constant to make pi sum to 1.0

**Value**

derivative

---

 McCullagh\_derivative\_pij\_wrt\_delta

*Derivative of  $p_{ij}[i, j]$  wrt scalar delta.*


---

**Description**

Derivative of  $p_{ij}[i, j]$  wrt scalar delta.

**Usage**

McCullagh\_derivative\_pij\_wrt\_delta(i, j, psi, delta, alpha, c = 1)

**Arguments**

i	row index of pij
j	column index of pij
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing constant so that pi sum to 1.0. Default value is 1.0

**Value**

derivative

---

McCullagh\_derivative\_pij\_wrt\_delta\_vec

*Derivative  $p_{ij}[i, j]$  wrt vector  $delta[k]$ .*


---

**Description**

Derivative  $p_{ij}[i, j]$  wrt vector  $delta[k]$ .

**Usage**

McCullagh\_derivative\_pij\_wrt\_delta\_vec(i, j, k, psi, delta\_vec, alpha, c = 1)

**Arguments**

i	row index of pij
j	column index of pij
k	index of delta
psi	the matrix of symmetry parameters
delta_vec	the vector asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

**Value**

list containing matrices pij and qij

---

McCullagh\_derivative\_pij\_wrt\_psi

*Derivative of pij[a, b] wrt psi[h, k]*

---

**Description**

Derivative of pij[a, b] wrt psi[h, k]

**Usage**

McCullagh\_derivative\_pij\_wrt\_psi(a, b, h, k, delta, alpha, c = 1)

**Arguments**

a	row index of pi
b	column index of pi
h	row index of phi
k	column index of phi
delta	scalar or vector version of asymmetry parameters
alpha	vector of asymmetry parameters
c	normalizing constant for to make pi sum to 1. Defaults to 1.0

**Value**

derivative

---

McCullagh\_extract\_weights

*Extracts the weights to convert cumulative model-based probabilities to regular probabilities.*

---

**Description**

Extracts the weights to convert cumulative model-based probabilities to regular probabilities.

**Usage**

McCullagh\_extract\_weights(i, j, M)

**Arguments**

i	row index sought
j	column index sought
M	the number of rows/columns in observed matrix

**Value**

a list containing  $w_{\psi}$  for when  $i == j$   $w_{\pi j}$  for when  $i < j$   $w_{\pi i j}$  for when  $j < i$  weight populated with correct entry based on actual  $i$  and  $j$

---

McCullagh\_fit\_location\_regression\_model  
*Fit location model*

---

**Description**

Fit location model

**Usage**

```
McCullagh_fit_location_regression_model(n, x, max_iter = 5, verbose = FALSE)
```

**Arguments**

n	matrix of observed counts
x	design matrix for regression model
max_iter	maximum number of Fisher scoring iterations
verbose	logical: should cycle-by-cycle info be printed out? Default value is FALSE, do not print

**Value**

a list containing beta: regression parameter estimates se: matrix of estimated standard errors cov: covariance matrix of parameter estimates g\_squared:  $G^2$  likelihood ratio chi-square for model chisq: Pearson chi-square for model df: degrees of freedom

---

 McCullagh\_generalized\_palindromic\_symmetry

*Generalized version of palindromic symmetry model*


---

### Description

delta now is a vector, varying by index McCullagh, P. (1978). A class of parametric models for the analysis of square contingency tables with ordered categories. *Biometrika*, 65(2). 413-416.

### Usage

```
McCullagh_generalized_palindromic_symmetry(
  n,
  max_iter = 15,
  verbose = FALSE,
  start_values = FALSE
)
```

### Arguments

n	matrix of observed counts
max_iter	maximum number of iterations to maximize log(likelihood)
verbose	should cycle-by-cycle information be printed out? Default is FALSE, do not print
start_values	logical should the regular palindromic symmetry model be fit first to get good starting values. Default is FALSE.

### Value

a list containing

a list containing delta: the vector of asymmetry parameter delta sigma\_delta: vector of SE(delta)  
 logL: value of log(likelihood) for final estimates chisq: Pearson chi-square for solution df: degrees of freedom for solution chisq psi: matrix of symmetry parameters alpha: c: constraint, sum of pi - values condition: constraint on psi to make model identified, Lagrange multiplier SE: vector of standard errors for all parameters

### Examples

```
McCullagh_generalized_palindromic_symmetry(vision_data)
```

---

 McCullagh\_generalized\_pij\_qij

*Computes culuative model probabilities for the generalized model using vector delta.*

---

**Description**

Computes culuative model probabilities for the generalized model using vector delta.

**Usage**

```
McCullagh_generalized_pij_qij(i, j, psi, delta_vec, alpha, c1 = 1)
```

**Arguments**

i	row index
j	column index
psi	symmetry matrix
delta_vec	vector of delta values
alpha	vector of asymmetry values
c1	normalizing value for pi. Defaults to 1.0

**Value**

model-based cumulative probability pi\_ij

---

McCullagh\_generate\_names

*Generates names to label the parameters.*

---

**Description**

Generates names to label the parameters.

**Usage**

```
McCullagh_generate_names(psi, delta, alpha, c)
```

**Arguments**

psi	matrix of symmetry parameters
delta	scalar of matrix of asymmetry parameters
alpha	vector of asymmetry parameters
c	sclng factor to ensure sup of pi is 1.0

**Value**

character vector of labels for the SE values

---

McCullagh\_get\_statistics

*Computes summary statistics needed to compute estimate of delta.*

---

**Description**

Computes summary statistics needed to compute estimate of delta.

**Usage**

McCullagh\_get\_statistics(m)

**Arguments**

m                    matrix of observed counts

**Value**

a list containing: N: matrix of sums above and below the diagonal n: vector, size of binomial r: vector, observed sums, number of successes for binomial

---

McCullagh\_gradient\_log\_l

*Gradient vector of log(likelihood)*

---

**Description**

Gradient vector of log(likelihood)

**Usage**

McCullagh\_gradient\_log\_l(n, psi, delta, alpha, c = 1)

**Arguments**

n                    matrix of observed counts  
 psi                matrix of symmetry parameters  
 delta              scalar or vector asymmetry parameter  
 alpha              vector of asymmetry parameters  
 c                    normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

gradient vector of first-order partials wrt log(likelihood)

---

McCullagh\_hessian\_log\_l  
*Hessian matrix of log(likelihood)*

---

**Description**

Hessian matrix of log(likelihood)

**Usage**

McCullagh\_hessian\_log\_l(n, psi, delta, alpha, c = 1)

**Arguments**

n	matrix of observed counts
psi	matrix of symmetry parameters
delta	scalar or vector asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

hessian matrix of second-order partials wrt log(likelihood0)

---

McCullagh\_initialize\_beta  
*Initializes the beta vector.*

---

**Description**

Initializes the beta vector.

**Usage**

McCullagh\_initialize\_beta(n, c, v)

**Arguments**

n	matrix of observed counts
c	number of score levels in table
v	number of levels of beta beyond c

**Value**

initialized beta vector

McCullagh\_initialize\_delta

*Compute initial values for scalar delta*

---

**Description**

Compute initial values for scalar delta

**Usage**

McCullagh\_initialize\_delta(n)

**Arguments**

n                    matrix of observed counts

**Value**

value of delta

---

McCullagh\_initialize\_delta\_vec

*Initialize vector delta*

---

**Description**

Initialize vector delta

**Usage**

McCullagh\_initialize\_delta\_vec(n)

**Arguments**

n                    matrix of observed counts

**Value**

vector of delta values

---

McCullagh\_initialize\_psi  
*Initialize the symmetry matrix psi*

---

**Description**

Initialize the symmetry matrix psi

**Usage**

```
McCullagh_initialize_psi(n, delta, alpha, c = 1)
```

**Arguments**

n	matrix of observed counts
delta	scalar delta value
alpha	vector of asymmetry parameters
c	normalizing value of pi. Default is 1.0

**Value**

matrix psi

---

McCullagh\_initialize\_x  
*Initialize design matrix for location model.*

---

**Description**

This is the simplest possible implementation, that fits thresholds and a single group contrast. More complex problems will implement the matrix X themselves.

**Usage**

```
McCullagh_initialize_x(s, c, v)
```

**Arguments**

s	number of levels of stratification variable
c	number of score levels
v	number of predictors above thresholds

**Value**

design matrix X

---

McCullagh\_is\_in\_constraint\_set

*Logical test of whether a specific psi will be in the constraint set.*

---

**Description**

Logical test of whether a specific psi will be in the constraint set.

**Usage**

McCullagh\_is\_in\_constraint\_set(i, j)

**Arguments**

i	first index of psi
j	second index of psi

**Value**

TRUE if it falls within the set, FALSE otherwise.

---

McCullagh\_is\_pi\_invalid

*Test whether pi matrix is valid, i.e.,  $0 <$  all values.*

---

**Description**

Test whether pi matrix is valid, i.e.,  $0 <$  all values.

**Usage**

McCullagh\_is\_pi\_invalid(pi)

**Arguments**

pi	matrix of pi values to be tested.
----	-----------------------------------

**Value**

TRUE if all  $\pi > 0$ , FALSE otherwise.

---

McCullagh\_log\_L      *Computes the log(likelihood).*

---

**Description**

Computes the log(likelihood).

**Usage**

McCullagh\_log\_L(n, psi, delta, alpha, c = 1)

**Arguments**

n	matrix of observed counts
psi	matrix of symmetry parameters
delta	scalar or vector asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh\_logistic\_model  
*MCCullagh's logistic model.*

---

**Description**

McCullah, P. (1977). A logistic model for paired comparisons with ordered categorical data. *Biometrika*, 64(3), 449-453.

**Usage**

McCullagh\_logistic\_model(m)

**Arguments**

m	matrix of observed counts
---	---------------------------

**Value**

a list containing w\_tilde: vector of model weights for sum of normally distributed components  
 delta\_tilde: delta parameter computed using w\_tilde w\_star: vector of weights for Mantel-Haenszel  
 type numerator and denominator delta\_star: delta parameter computed using w\_star var: variance  
 of delta estimate

**Examples**

```
McCullagh_logistic_model(coal_g)
```

---

McCullagh_logits	<i>Computed cumulative logits.</i>
------------------	------------------------------------

---

**Description**

Computed cumulative logits.

**Usage**

```
McCullagh_logits(cumulative, use_half = TRUE)
```

**Arguments**

cumulative	vector of cumulative counts
use_half	logical indicating whether or not to add 0.5 to numerator and denominator counts before computing logits, Default value is TRUE, add 0.5.

---

McCullagh_maximize_q_symmetry	<i>Maximize the log(likelihood) wrt parameters phi and alpha</i>
-------------------------------	--

---

**Description**

Maximize the log(likelihood) wrt parameters phi and alpha

**Usage**

```
McCullagh_maximize_q_symmetry(n, phi, alpha)
```

**Arguments**

n	matrix of observed counts
phi	matrix of symmetry parameters
alpha	vector of asymmetry parameters

**Value**

list with new values of phi and alpha

---

McCullagh\_newton\_raphson\_update  
*Newton-Raphson update.*

---

### Description

Using gradient and hessian, it finds the update direction. Then it tries increasingly smaller step sizes until the step\*update yields a valid pi matrix.

### Usage

```
McCullagh_newton_raphson_update(  
  n,  
  gradient,  
  hessian,  
  psi,  
  delta,  
  alpha,  
  c = 1,  
  max_iter = 50,  
  verbose = FALSE  
)
```

### Arguments

n	matrix of observed counts
gradient	gradient vector
hessian	hessian matrix
psi	matrix of symmetry parameters
delta	scalar or vector of asymmetry parameters
alpha	vector of asymmetry parameters
c	scaling factor to ensure pi sums to 1.0. Default is 1.0
max_iter	maximum number of iterations. Default is 50.
verbose	should cycle-by-cycle into be printed out. Default is FALSE, do not print.

### Value

list containing new parameters psi: matrix of symmetry parameters delta; scalar or vector of asymmetry parameters alpha: vector of asymmetry parameters c: scaling coefficient to ensure pi sums to 1.0

---

 McCullagh\_palindromic\_symmetry

*McCullagh's palindromic symmetry model*


---

### Description

McCullagh, P. (1978). A class of parametric models for the analysis of square contingency tables with ordered categories. *Biometrika*, 65(2). 413-416.

### Usage

```
McCullagh_palindromic_symmetry(n, max_iter = 15, verbose = FALSE)
```

### Arguments

n	matrix of observed counts
max_iter	maximum number of iterations to maximize the log(likelihood)
verbose	should cycle-by-cycle info be printed out? Default is FALSE, don't print.

### Value

a list containing delta: the value of the asymmetry parameter delta sigma\_delta: SE(delta) logL: value of log(likelihood) for final estimates chisq: Pearson chi-square for solution df: degrees of freedom for solution chisq psi: matrix of symmetry parameters alpha: c: constraint, sum of pi - values condition: constraint on psi to make model identified, Lagrange multiplier SE: vector of standard errors for all parameters

### Examples

```
McCullagh_palindromic_symmetry(vision_data)
```

---

 McCullagh\_penalized *Computes the penalized value of a derivative by adding the derivative of the penalty to it.*


---

### Description

Computes the penalized value of a derivative by adding the derivative of the penalty to it.

### Usage

```
McCullagh_penalized(derivative, i1, j1, n, psi, delta, alpha, c = 1)
```

**Arguments**

derivative	the base derivative
i1	first index of psi
j1	second index of psi
n	matrix of observed counts
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh\_pij\_qij      *Compute model-based cumulative probabilities*

---

**Description**

Compute model-based cumulative probabilities

**Usage**

```
McCullagh_pij_qij(i, j, psi, delta, alpha, c = 1)
```

**Arguments**

i	row index
j	column index
psi	the symmetry matrix
delta	the asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for pi. Default is 1.0

**Value**

the model-based cumulative probability  $\pi_{ij}$

McCullagh\_proportional\_hazards

*Computes the proportional hazards.*

---

**Description**

Computes the proportional hazards.

**Usage**

McCullagh\_proportional\_hazards(n)

**Arguments**

n                    matrix of observed counts

**Value**

loga(-log(survival))

---

McCullagh\_q\_symmetry\_initialize\_alpha

*Initializes the asymmetry vector alpha*

---

**Description**

Initializes the asymmetry vector alpha

**Usage**

McCullagh\_q\_symmetry\_initialize\_alpha(M)

**Arguments**

M                    size of alpha vector to create = nrow(matrix to analyze)

**Value**

vector of asymmetry parameters alpha

---

McCullagh\_q\_symmetry\_initialize\_phi  
*Initializes the phi matrix*

---

**Description**

Initializes the phi matrix

**Usage**

McCullagh\_q\_symmetry\_initialize\_phi(M)

**Arguments**

M                      size of the psi matrix to create

**Value**

the symmetry matrix phi

---

McCullagh\_q\_symmetry\_pi  
*Computes the model-based p-values*

---

**Description**

Computes the model-based p-values

**Usage**

McCullagh\_q\_symmetry\_pi(phi, alpha)

**Arguments**

phi                    the matrix of symmetry parameters  
alpha                  the vector of asymmetry parameters

**Value**

matrix pi of model-based p-values

---

McCullagh\_quasi\_symmetry

*Fits McCullagh's (1978) quasi-symmetry model.*

---

### Description

McCullagh, P. (1978). A class of parametric models for the analysis of square contingency tables with ordered categories. *Biometrika*, 65(2) 413-418.

### Usage

```
McCullagh_quasi_symmetry(n, max_iter = 15, verbose = FALSE)
```

### Arguments

n	matrix of observed counts
max_iter	maximum number of iterations in maximizing log(likelihood), Default is 15.
verbose	should cycle-by-cycle information be printed out? Default is FALSE, do not print

### Value

a list containing phi: symmetry matrix alpha: vector of asymmetry parameters chisq: Pearson chi-square value df: degrees of freedom

### Examples

```
McCullagh_quasi_symmetry(vision_data)
```

---

McCullagh\_second\_order\_lagrangian\_wrt\_psi\_2

*Second derivative of Lagrangian wrt psi^2.*

---

### Description

Second derivative of Lagrangian wrt psi^2.

**Usage**

```
McCullagh_second_order_lagrangian_wrt_psi_2(
  n,
  i1,
  j1,
  i2,
  j2,
  psi,
  delta,
  alpha,
  c = 1
)
```

**Arguments**

n	matrix of observed counts
i1	first row index of psi
j1	first column index of psi
i2	second row index of psi
j2	second column index of psi
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh\_second\_order\_lagrangian\_wrt\_psi\_alpha

*Second derivative of Lagrangian wrt psi[i1, j1] and alpha[index].*

---

**Description**

Second derivative of Lagrangian wrt psi[i1, j1] and alpha[index].

**Usage**

```
McCullagh_second_order_lagrangian_wrt_psi_alpha(
  n,
  i1,
  j1,
  index,
```

```

    psi,
    delta,
    alpha,
    c = 1
  )

```

### Arguments

n	matrix of observed counts
i1	row index of psi
j1	column index of psi
index	second row index of alpha
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

### Value

derivative

---

McCullagh\_second\_order\_lagrangian\_wrt\_psi\_delta

*Second derivative of Lagrangian wrt psi[i1, j1] and delta.*

---

### Description

Second derivative of Lagrangian wrt psi[i1, j1] and delta.

### Usage

```

McCullagh_second_order_lagrangian_wrt_psi_delta(
  n,
  i1,
  j1,
  psi,
  delta,
  alpha,
  c = 1
)

```

**Arguments**

n	matrix of observed counts
i1	row index of psi
j1	column index of psi
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh\_second\_order\_lagrangian\_wrt\_psi\_delta\_vec  
*Second derivative of Lagrangian wrt psi[i1, j1] and delta\_vec[k].*

---

**Description**

Second derivative of Lagrangian wrt psi[i1, j1] and delta\_vec[k].

**Usage**

```
McCullagh_second_order_lagrangian_wrt_psi_delta_vec(
  n,
  i1,
  j1,
  k,
  psi,
  delta_vec,
  alpha,
  c = 1
)
```

**Arguments**

n	matrix of observed counts
i1	row index of psi
j1	column index of psi
k	index of delta_vec
psi	matrix of symmetry parameters
delta_vec	vector asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh\_second\_order\_log\_1\_wrt\_alpha\_2  
*Second derivative of log(likelihood) wrt alpha^2.*

---

**Description**

Second derivative of log(likelihood) wrt alpha^2.

**Usage**

```
McCullagh_second_order_log_1_wrt_alpha_2(
  n,
  index_a,
  index_b,
  psi,
  delta,
  alpha,
  c = 1
)
```

**Arguments**

n	matrix of observed counts
index_a	first index of alpha
index_b	second column index of alpha
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

 McCullagh\_second\_order\_log\_l\_wrt\_alpha\_c

*Second derivative of log(likelihood) wrt alpha[index] and c.*


---

**Description**

Second derivative of log(likelihood) wrt alpha[index] and c.

**Usage**

McCullagh\_second\_order\_log\_l\_wrt\_alpha\_c(n, index, psi, delta, alpha, c)

**Arguments**

n	matrix of observed counts
index	index of alpha
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0.

**Value**

derivative

---

McCullagh\_second\_order\_log\_l\_wrt\_beta\_2

*Expected values of second order derivatives of log(likelihood) wrt beta.*


---

**Description**

Appendix of McCullagh, P. (1980). Regression models for ordinal data. Journal of the Royal Statistical Society, Series B, 42(2), 109-142. and appendix B3 of Agresti, A. (1984). Analysis of ordinal categorical data, New York, Wiley, p. 242-244.

**Usage**

McCullagh\_second\_order\_log\_l\_wrt\_beta\_2(n, x, gamma)

**Arguments**

n	matrix of observed counts
x	design matrix for location model
gamma	current value of model-based cumulative logits.

**Value**

matrix of second order partial derivatives

---

McCullagh\_second\_order\_log\_1\_wrt\_c\_2

*Second derivative of log(likelihood) wrt c^2.*

---

**Description**

Second derivative of log(likelihood) wrt c^2.

**Usage**

McCullagh\_second\_order\_log\_1\_wrt\_c\_2(n, psi, delta, alpha, c)

**Arguments**

n	matrix of observed counts
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh\_second\_order\_log\_1\_wrt\_delta\_2

*Second derivative of log(likelihood) wrt delta^2.*

---

**Description**

Second derivative of log(likelihood) wrt delta^2.

**Usage**

McCullagh\_second\_order\_log\_1\_wrt\_delta\_2(n, psi, delta, alpha, c = 1)

**Arguments**

n	matrix of observed counts
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh\_second\_order\_log\_l\_wrt\_delta\_alpha  
*Second derivative of log(likelihood) wrt delta and alpha[index].*

---

**Description**

Second derivative of log(likelihood) wrt delta and alpha[index].

**Usage**

```
McCullagh_second_order_log_l_wrt_delta_alpha(  
  n,  
  index,  
  psi,  
  delta,  
  alpha,  
  c = 1  
)
```

**Arguments**

n	matrix of observed counts
index	index of alpha
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh\_second\_order\_log\_1\_wrt\_delta\_c

*Second derivative of log(likelihood) wrt scalar delta and c.*

---

### Description

Second derivative of log(likelihood) wrt scalar delta and c.

### Usage

```
McCullagh_second_order_log_1_wrt_delta_c(n, psi, delta, alpha, c)
```

### Arguments

n	matrix of observed counts
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0..

### Value

derivative

---

McCullagh\_second\_order\_log\_1\_wrt\_delta\_vec\_2

*Second derivative of log(likelihood) wrt delta\_vec^2.*

---

### Description

Second derivative of log(likelihood) wrt delta\_vec^2.

### Usage

```
McCullagh_second_order_log_1_wrt_delta_vec_2(
  n,
  k1,
  k2,
  psi,
  delta_vec,
  alpha,
  c = 1
)
```

**Arguments**

n	matrix of observed counts
k1	first index of delta_vec
k2	second index of delta_vec
psi	matrix of symmetry parameters
delta_vec	vector asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh\_second\_order\_log\_l\_wrt\_delta\_vec\_alpha  
*Second derivative of log(likelihood) wrt delta[k] and alpha[index].*

---

**Description**

Second derivative of log(likelihood) wrt delta[k] and alpha[index].

**Usage**

```
McCullagh_second_order_log_l_wrt_delta_vec_alpha(
  n,
  k,
  index,
  psi,
  delta_vec,
  alpha,
  c = 1
)
```

**Arguments**

n	matrix of observed counts
k	index of delta_vec
index	index of alpha
psi	matrix of symmetry parameters
delta_vec	vector asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh\_second\_order\_log\_l\_wrt\_delta\_vec\_c

*Second derivative of log(likelihood) wrt delta\_vec[k] and c.*

---

### Description

Second derivative of log(likelihood) wrt delta\_vec[k] and c.

### Usage

McCullagh\_second\_order\_log\_l\_wrt\_delta\_vec\_c(n, k, psi, delta\_vec, alpha, c)

### Arguments

n	matrix of observed counts
k	index of delta_vec
psi	matrix of symmetry parameters
delta_vec	vector asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0

### Value

derivative

---

McCullagh\_second\_order\_log\_l\_wrt\_parms

*Expected second order derivatives of log(likelihood)*

---

### Description

Expected second order derivatives of log(likelihood)

### Usage

McCullagh\_second\_order\_log\_l\_wrt\_parms(n, x, beta)

### Arguments

n	matrix of observed counts
x	design matrix for location model
beta	vector of regression parameters for location model

### Value

matrix of expected second derivatives

---

`McCullagh_second_order_log_1_wrt_psi_2`*Second derivative of log(likelihood) wrt  $\psi^2$ .*

---

**Description**

Second derivative of log(likelihood) wrt  $\psi^2$ .

**Usage**

```
McCullagh_second_order_log_1_wrt_psi_2(  
  n,  
  i1,  
  j1,  
  i2,  
  j2,  
  psi,  
  delta,  
  alpha,  
  c = 1  
)
```

**Arguments**

<code>n</code>	matrix of observed counts
<code>i1</code>	first row index of $\psi$
<code>j1</code>	first column index of $\psi$
<code>i2</code>	second row index of $\psi$
<code>j2</code>	second column index of $\psi$
<code>psi</code>	matrix of symmetry parameters
<code>delta</code>	scalar asymmetry parameter
<code>alpha</code>	vector of asymmetry parameters
<code>c</code>	normalizing factor to make $\pi$ sum to 1.0. Default is 1.0.

**Value**

derivative

---

 McCullagh\_second\_order\_log\_l\_wrt\_psi\_alpha

*Second derivative of log(likelihood) wrt  $\psi[i1, j1]$  and  $\alpha[index]$ .*


---

### Description

Second derivative of log(likelihood) wrt  $\psi[i1, j1]$  and  $\alpha[index]$ .

### Usage

```
McCullagh_second_order_log_l_wrt_psi_alpha(
  n,
  i1,
  j1,
  index,
  psi,
  delta,
  alpha,
  c = 1
)
```

### Arguments

n	matrix of observed counts
i1	row index of psi
j1	column index of psi
index	index of alpha
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

### Value

derivative

---

 McCullagh\_second\_order\_log\_l\_wrt\_psi\_c

*Second derivative of log(likelihood) wrt psi[i1, j1] and c.*


---

**Description**

Second derivative of log(likelihood) wrt psi[i1, j1] and c.

**Usage**

McCullagh\_second\_order\_log\_l\_wrt\_psi\_c(n, i1, j1, psi, delta, alpha, c)

**Arguments**

n	matrix of observed counts
i1	row index of psi
j1	column index of psi
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0.

**Value**

derivative

---

 McCullagh\_second\_order\_log\_l\_wrt\_psi\_delta

*Second derivative of log(likelihood) wrt psi[i1, j1] and scalar delta..*


---

**Description**

Second derivative of log(likelihood) wrt psi[i1, j1] and scalar delta..

**Usage**

McCullagh\_second\_order\_log\_l\_wrt\_psi\_delta(n, i1, j1, psi, delta, alpha, c = 1)

**Arguments**

n	matrix of observed counts
i1	row index of psi
j1	column index of psi
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh\_second\_order\_log\_l\_wrt\_psi\_delta\_vec

*Second derivative of log(likelihood) wrt psi[i1, j1] and delta\_vec[k].*

---

**Description**

Second derivative of log(likelihood) wrt psi[i1, j1] and delta\_vec[k].

**Usage**

```
McCullagh_second_order_log_l_wrt_psi_delta_vec(
  n,
  i1,
  j1,
  k,
  psi,
  delta_vec,
  alpha,
  c = 1
)
```

**Arguments**

n	matrix of observed counts
i1	row index of psi
j1	column index of psi
k	second row index of delta
psi	matrix of symmetry parameters
delta_vec	vector asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh\_second\_order\_omega\_wrt\_alpha\_2  
*Second derivative of Lagrange multiplier omega wrt alpha<sup>2</sup>.*

---

**Description**

Second derivative of Lagrange multiplier omega wrt alpha<sup>2</sup>.

**Usage**

McCullagh\_second\_order\_omega\_wrt\_alpha\_2(n, k1, k2, psi, delta, alpha, c = 1)

**Arguments**

n	matrix of observed counts
k1	first index of alpha
k2	second index of alpha
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh\_second\_order\_omega\_wrt\_alpha\_c  
*Second derivative of Lagrange multiplier omega wrt alpha[index] and c.*

---

**Description**

Second derivative of Lagrange multiplier omega wrt alpha[index] and c.

**Usage**

McCullagh\_second\_order\_omega\_wrt\_alpha\_c(n, index, psi, delta, alpha, c)

**Arguments**

n	matrix of observed counts
index	row index of psi
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0.

**Value**

derivative

---

McCullagh\_second\_order\_omega\_wrt\_c\_2

*Second derivative of Lagrange multiplier omega wrt c^2.*

---

**Description**

Second derivative of Lagrange multiplier omega wrt c^2.

**Usage**

McCullagh\_second\_order\_omega\_wrt\_c\_2(n, psi, delta, alpha, c)

**Arguments**

n	matrix of observed counts
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0.

**Value**

derivative

---

 McCullagh\_second\_order\_omega\_wrt\_delta\_2

*Second derivative of Lagrange multiplier omega wrt scalae delta^2.*


---

**Description**

Second derivative of Lagrange multiplier omega wrt scalae delta^2.

**Usage**

```
McCullagh_second_order_omega_wrt_delta_2(n, psi, delta, alpha, c = 1)
```

**Arguments**

n	matrix of observed counts
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh\_second\_order\_omega\_wrt\_delta\_alpha

*Second derivative of Lagrange multiplier omega wrt delta and alpha[index].*


---

**Description**

Second derivative of Lagrange multiplier omega wrt delta and alpha[index].

**Usage**

```
McCullagh_second_order_omega_wrt_delta_alpha(
  n,
  index,
  psi,
  delta,
  alpha,
  c = 1
)
```

**Arguments**

n	matrix of observed counts
index	index of alpha
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh\_second\_order\_omega\_wrt\_delta\_c

*Second derivative of Lagrange multiplier omega wrt scalar delta and c.*

---

**Description**

Second derivative of Lagrange multiplier omega wrt scalar delta and c.

**Usage**

McCullagh\_second\_order\_omega\_wrt\_delta\_c(n, psi, delta, alpha, c)

**Arguments**

n	matrix of observed counts
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

 McCullagh\_second\_order\_omega\_wrt\_delta\_vec\_2

*Second derivative of Lagrange multiplier omega wrt delta\_vec^2.*


---

**Description**

Second derivative of Lagrange multiplier omega wrt delta\_vec^2.

**Usage**

```
McCullagh_second_order_omega_wrt_delta_vec_2(
  n,
  k1,
  k2,
  psi,
  delta_vec,
  alpha,
  c = 1
)
```

**Arguments**

n	matrix of observed counts
k1	first index of delta_vec
k2	second index of delta_vec
psi	matrix of symmetry parameters
delta_vec	vector asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

 McCullagh\_second\_order\_omega\_wrt\_delta\_vec\_alpha

*Second derivative of Lagrange multiplier omega wrt delta\_vec[k] and alpha[index].*


---

**Description**

Second derivative of Lagrange multiplier omega wrt delta\_vec[k] and alpha[index].

**Usage**

```
McCullagh_second_order_omega_wrt_delta_vec_alpha(
  n,
  k,
  index,
  psi,
  delta_vec,
  alpha,
  c = 1
)
```

**Arguments**

n	matrix of observed counts
k	index of delta_vec
index	index of alpha
psi	matrix of symmetry parameters
delta_vec	vector asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh\_second\_order\_omega\_wrt\_delta\_vec\_c

*Second derivative of Lagrange multiplier omega wrt delta\_vec[k] and c.*

---

**Description**

Second derivative of Lagrange multiplier omega wrt delta\_vec[k] and c.

**Usage**

```
McCullagh_second_order_omega_wrt_delta_vec_c(n, k, psi, delta_vec, alpha, c)
```

**Arguments**

n	matrix of observed counts
k	index of delta_vec
psi	matrix of symmetry parameters
delta_vec	vector of asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0.

**Value**

derivative

---

McCullagh\_second\_order\_omega\_wrt\_psi\_2  
*Second derivative of Lagrange multiplier omega wrt psi^2.*

---

**Description**

Second derivative of Lagrange multiplier omega wrt psi^2.

**Usage**

```
McCullagh_second_order_omega_wrt_psi_2(  
  n,  
  i1,  
  j1,  
  i2,  
  j2,  
  psi,  
  delta,  
  alpha,  
  c = 1  
)
```

**Arguments**

n	matrix of observed counts
i1	first row index of psi
j1	first column index of psi
i2	second row index of psi
j2	second column index of psi
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh\_second\_order\_omega\_wrt\_psi\_alpha

*Second derivative of Lagrange multiplier omega wrt psi[i1, j1] and alpha[index].*

---

### Description

Second derivative of Lagrange multiplier omega wrt psi[i1, j1] and alpha[index].

### Usage

```
McCullagh_second_order_omega_wrt_psi_alpha(
  n,
  i1,
  j1,
  index,
  psi,
  delta,
  alpha,
  c = 1
)
```

### Arguments

n	matrix of observed counts
i1	row index of psi
j1	column index of psi
index	index of alpha
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

### Value

derivative

---

 McCullagh\_second\_order\_omega\_wrt\_psi\_c

*Second derivative of Lagrange multiplier omega wrt psi[i1, j1] and c.*


---

**Description**

Second derivative of Lagrange multiplier omega wrt psi[i1, j1] and c.

**Usage**

McCullagh\_second\_order\_omega\_wrt\_psi\_c(n, i1, j1, psi, delta, alpha, c)

**Arguments**

n	matrix of observed counts
i1	row index of psi
j1	column index of psi
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

 McCullagh\_second\_order\_omega\_wrt\_psi\_delta

*Second derivative of Lagrange multiplier omega wrt psi and scalar delta.*


---

**Description**

Second derivative of Lagrange multiplier omega wrt psi and scalar delta.

**Usage**

McCullagh\_second\_order\_omega\_wrt\_psi\_delta(n, i1, j1, psi, delta, alpha, c = 1)

**Arguments**

n	matrix of observed counts
i1	row index of psi
j1	column index of psi
psi	matrix of symmetry parameters
delta	scalar asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh\_second\_order\_omega\_wrt\_psi\_delta\_vec

*Second derivative of Lagrange multiplier omega wrt psi[i1, j1] and delta\_vec[k].*

---

**Description**

Second derivative of Lagrange multiplier omega wrt psi[i1, j1] and delta\_vec[k].

**Usage**

```
McCullagh_second_order_omega_wrt_psi_delta_vec(
  n,
  i1,
  j1,
  k,
  psi,
  delta_vec,
  alpha,
  c = 1
)
```

**Arguments**

n	matrix of observed counts
i1	row index of psi
j1	column index of psi
k	index of delta_vec
psi	matrix of symmetry parameters
delta_vec	vector asymmetry parameter
alpha	vector of asymmetry parameters
c	normalizing factor to make pi sum to 1.0. Default is 1.0.

**Value**

derivative

---

McCullagh\_second\_order\_pi\_wrt\_alpha\_2  
*Second derivative of pi[i, j] wrt alpha^2.*

---

**Description**

Second derivative of pi[i, j] wrt alpha^2.

**Usage**

```
McCullagh_second_order_pi_wrt_alpha_2(
  i,
  j,
  index1,
  index2,
  psi,
  delta,
  alpha,
  c = 1
)
```

**Arguments**

i	row index of pi
j	column index of pi
index1	index of first alpha
index2	index of second aloha
psi	the matrix of symmetry parameters
delta	the scalar asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

**Value**

derivative

---

McCullagh\_second\_order\_pi\_wrt\_alpha\_c

*Second derivative of pi[i, j] wrt alpha[index] and c.*

---

### Description

Second derivative of pi[i, j] wrt alpha[index] and c.

### Usage

McCullagh\_second\_order\_pi\_wrt\_alpha\_c(i, j, index, psi, delta, alpha, c)

### Arguments

i	row index of pi
j	column index of pi
index	index of alpha
psi	the matrix of symmetry parameters
delta	the scalar asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0

### Value

derivative

---

McCullagh\_second\_order\_pi\_wrt\_c\_2

*Second order derivative of pi[i, j] wrt c^2.*

---

### Description

Second order derivative of pi[i, j] wrt c^2.

### Usage

McCullagh\_second\_order\_pi\_wrt\_c\_2(i, j, psi, delta, alpha, c)

### Arguments

i	row index of pi
j	column index of pi
psi	the matrix of symmetry parameters
delta	the scalar asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

**Value**

derivative

---

McCullagh\_second\_order\_pi\_wrt\_delta\_2

*Second order derivative of pi[i, j] wrt scalar delta.*

---

**Description**

Second order derivative of pi[i, j] wrt scalar delta.

**Usage**

```
McCullagh_second_order_pi_wrt_delta_2(i, j, psi, delta, alpha, c = 1)
```

**Arguments**

i	row index of pi
j	column index of pi
psi	the matrix of symmetry parameters
delta	the scalar asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

**Value**

derivative

---

McCullagh\_second\_order\_pi\_wrt\_delta\_alpha

*Second order derivative of pi[i, j] wrt scalar delta and alpha[index]*

---

**Description**

Second order derivative of pi[i, j] wrt scalar delta and alpha[index]

**Usage**

```
McCullagh_second_order_pi_wrt_delta_alpha(
  i,
  j,
  index,
  psi,
  delta,
  alpha,
  c = 1
)
```

**Arguments**

i	row index of pi
j	column index of pi
index	index of alpha
psi	the matrix of symmetry parameters
delta	the scalar asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

**Value**

derivative

---

McCullagh\_second\_order\_pi\_wrt\_delta\_c

*Second order derivative of pi[i, j] wrt scalae delta and c.*

---

**Description**

Second order derivative of pi[i, j] wrt scalae delta and c.

**Usage**

McCullagh\_second\_order\_pi\_wrt\_delta\_c(i, j, psi, delta, alpha, c)

**Arguments**

i	row index of pi
j	column index of pi
psi	the matrix of symmetry parameters
delta	the scalar asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0

**Value**

derivative

---

McCullagh\_second\_order\_pi\_wrt\_delta\_vec\_2  
*Derivative of pi[i, j] wrt delta^2.*

---

**Description**

Derivative of pi[i, j] wrt delta^2.

**Usage**

```
McCullagh_second_order_pi_wrt_delta_vec_2(  
  i,  
  j,  
  k1,  
  k2,  
  psi,  
  delta_vec,  
  alpha,  
  c = 1  
)
```

**Arguments**

i	row index of pi
j	column index of pi
k1	first index of delta
k2	second index of delta
psi	the matrix of symmetry parameters
delta_vec	the vector asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

**Value**

derivative

---

 McCullagh\_second\_order\_pi\_wrt\_delta\_vec\_alpha

*Second order derivative of pi[i, j] wrtt delta[k] alpha[index].*


---

### Description

Second order derivative of pi[i, j] wrtt delta[k] alpha[index].

### Usage

```
McCullagh_second_order_pi_wrt_delta_vec_alpha(
  i,
  j,
  k,
  index,
  psi,
  delta_vec,
  alpha,
  c = 1
)
```

### Arguments

i	row index of pi
j	column index of pi
k	index of delta
index	index of alpha
psi	the matrix of symmetry parameters
delta_vec	the vector asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

### Value

derivative

---

McCullagh\_second\_order\_pi\_wrt\_delta\_vec\_c  
*Second derivative of pi[i, j] wrt delta[k] and c.*

---

**Description**

Second derivative of pi[i, j] wrt delta[k] and c.

**Usage**

McCullagh\_second\_order\_pi\_wrt\_delta\_vec\_c(i, j, k, psi, delta\_vec, alpha, c)

**Arguments**

i	row index of pi
j	column index of pi
k	index of delta
psi	the matrix of symmetry parameters
delta_vec	the vector asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

**Value**

derivative

---

McCullagh\_second\_order\_pi\_wrt\_psi\_2  
*Second order derivative wrt psi^2.*

---

**Description**

Second order derivative wrt psi^2.

**Usage**

McCullagh\_second\_order\_pi\_wrt\_psi\_2(  
 i,  
 j,  
 i1,  
 j1,  
 i2,  
 j2,  
 psi,

```

    delta,
    alpha,
    c = 1
)

```

### Arguments

i	row index of pi
j	column index of pi
i1	first row index of psi
j1	first column index of psi
i2	second row index of psi
j2	second column index of psi
psi	the matrix of symmetry parameters
delta	the scalar asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

### Value

derivative

---

McCullagh\_second\_order\_pi\_wrt\_psi\_alpha  
*Second order derivative of pi[i, j] wrt psi[i1, j1] and alpha[index].*

---

### Description

Second order derivative of pi[i, j] wrt psi[i1, j1] and alpha[index].

### Usage

```

McCullagh_second_order_pi_wrt_psi_alpha(
  i,
  j,
  i1,
  j1,
  index,
  psi,
  delta,
  alpha,
  c = 1
)

```

**Arguments**

i	row index of pi
j	column index of pi
i1	row index of psi
j1	column index of psi
index	index of alpha
psi	the matrix of symmetry parameters
delta	the scalar asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

**Value**

derivative

---

McCullagh\_second\_order\_pi\_wrt\_psi\_c

*Second order derivative of pi[i, j] wrt psi[i1, j1] and c.*

---

**Description**

Second order derivative of pi[i, j] wrt psi[i1, j1] and c.

**Usage**

McCullagh\_second\_order\_pi\_wrt\_psi\_c(i, j, i1, j1, psi, delta, alpha, c)

**Arguments**

i	row index of pi
j	column index of pi
i1	row index of psi
j1	column index of psi
psi	the matrix of symmetry parameters
delta	the scalar asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0

**Value**

derivative

---

McCullagh\_second\_order\_pi\_wrt\_psi\_delta

*Second order derivaitve of pi wrt pshi and scalar delta.*

---

### Description

Second order derivaitve of pi wrt pshi and scalar delta.

### Usage

McCullagh\_second\_order\_pi\_wrt\_psi\_delta(i, j, i1, j1, psi, delta, alpha, c = 1)

### Arguments

i	row index of pi
j	column index of pi
i1	row index of psi
j1	column index of psi
psi	the matrix of symmetry parameters
delta	the scalar asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

### Value

derivative

---

McCullagh\_second\_order\_pi\_wrt\_psi\_delta\_vec

*Second order derivaitve of pi[i, j] wrt psi[i1, j1] and kelta[k].*

---

### Description

Second order derivaitve of pi[i, j] wrt psi[i1, j1] and kelta[k].

**Usage**

```
McCullagh_second_order_pi_wrt_psi_delta_vec(
  i,
  j,
  i1,
  j1,
  k,
  psi,
  delta_vec,
  alpha,
  c = 1
)
```

**Arguments**

i	row index of pi
j	column index of pi
i1	row index of psi
j1	column index of psi
k	index of delta
psi	the matrix of symmetry parameters
delta_vec	the vector asymmetry parameter
alpha	the vector of asymmetry parameters
c	the normalizing constant for the pis to sum to 1.0 Default value is 1.0

**Value**

derivative

---

McCullagh\_update\_parameters

*Update the parameters based on Newton-Raphson step.*

---

**Description**

Update the parameters based on Newton-Raphson step.

**Usage**

```
McCullagh_update_parameters(update, step, psi, delta, alpha, c = 1)
```

**Arguments**

update	vector of update values
step	size of candidate step along direction of update
psi	vector of symmetry parameters
delta	scalar or vector of asymmetry parameters
alpha	vector of asymmetry parameters
c	normalization factor to make sum of pi = 1.0. Default value is 1.0.

**Value**

list containing new parameters psi: matrix of symmetry parameters delta; scalar or vector of asymmetry parameters alpha: vector of asymmetry parameters c: scaling coefficient to ensure pi sums to 1.0

---

McCullagh\_v\_inverse    *Compute v\_inverse (from appendix).*

---

**Description**

Compute v\_inverse (from appendix).

**Usage**

```
McCullagh_v_inverse(gamma, i, j)
```

**Arguments**

gamma	matrix of cumulative logits
i	row index
j	column index

**Value**

$V^{-1}$  : d phi / d gamma[i, j]

---

mental_health	<i>Relationship between child's mental health and parents' socioeconomic status.</i>
---------------	--

---

**Description**

Rows are child's mental health (ranging from 1 = well to 4 = impaired), and columns are parents' socioeconomic status, A - F.

**Usage**

```
mental_health
```

**Format**

```
## 'mental_health' A matrix with 4 rows and 6 columns
```

**Source**

Goodman, L. A. (1979). Simple models for the analysis of association in cross-classifications having ordered categories.

---

model_i_column_theta	<i>Computes the column association values theta-hat</i>
----------------------	---

---

**Description**

Computes the column association values theta-hat

**Usage**

```
model_i_column_theta(fHat)
```

**Arguments**

fHat	matrix of model-based expected counts
------	---------------------------------------

**Value**

thetaHat vector of association parameters

---

model_i_effects	<i>Gets the overall effects for Model I.</i>
-----------------	--

---

**Description**

Gets the overall effects for Model I.

**Usage**

```
model_i_effects(result)
```

**Arguments**

result            a Model I result object

**Value**

a list containing theta: the overall association zeta\_i\_dot: row effects for association zeta\_dot\_j:  
column effects for association

---

model_i_fHat	<i>Computes model-based expected cell counts for Model I</i>
--------------	--

---

**Description**

Computes model-based expected cell counts for Model I

**Usage**

```
model_i_fHat(alpha, beta, gamma, delta)
```

**Arguments**

alpha            row effects  
beta             column effects  
gamma            row location weights  
delta            column location weights

**Value**

matrix of model-based expected counts

---

model\_i\_normalize\_fHat

*Normalizes  $\pi(\hat{f})$  to sum to 1.0. If `exclude_diagonal` is `TRUE`, the sum of the off-diagonal terms sums to 1.0.*

---

### Description

Normalizes  $\pi(\hat{f})$  to sum to 1.0. If `exclude_diagonal` is `TRUE`, the sum of the off-diagonal terms sums to 1.0.

### Usage

```
model_i_normalize_fHat(fHat, exclude_diagonal = FALSE)
```

### Arguments

`fHat` matrix of model-based cell frequencies

`exclude_diagonal`

logical. Should the cells on the main diagonal be excluded? Default is `FALSE`, include all cells

### Value

matrix of model-based proportions  $\pi$

---

model\_i\_row\_column\_odds\_ratios

*Computes the table of adjacent odds-ratios  $\theta$ -hat.*

---

### Description

Computes the table of adjacent odds-ratios  $\theta$ -hat.

### Usage

```
model_i_row_column_odds_ratios(fHat)
```

### Arguments

`fHat` matrix of model-based expected counts

### Value

$\theta$ hat matrix of adjacent odds-ratios

---

model\_i\_row\_theta      *Computes the row association values theta-hat*

---

**Description**

Computes the row association values theta-hat

**Usage**

```
model_i_row_theta(fHat)
```

**Arguments**

fHat                    matrix of model-based expected counts

**Value**

thetaHat vector of association parameters

---

model\_i\_star\_effects      *Gets the Model I\* effects.*

---

**Description**

Gets the Model I\* effects.

**Usage**

```
model_i_star_effects(result)
```

**Arguments**

result                    a Model I\* effect object

**Value**

a list containing theta: the overall association zeta: the row/column effect

---

model\_i\_star\_fHat      *Computes expected frequencies for Model I\**

---

**Description**

Computes expected frequencies for Model I\*

**Usage**

```
model_i_star_fHat(alpha, beta, theta)
```

**Arguments**

alpha	row effect parameters
beta	column effect parameters
theta	row/column parameters

**Value**

matrix of model-based expected cell counts

---

model\_i\_star\_update\_theta  
*Updates the row/column parameters for Model I\*.*

---

**Description**

Updates the row/column parameters for Model I\*.

**Usage**

```
model_i_star_update_theta(theta, n, fHat, exclude_diagonal = FALSE)
```

**Arguments**

theta	vector of estimated row/column effects
n	matrix of observed counts
fHat	matrix of model-based expected frequencies
exclude_diagonal	should the cells of the main diagonal be excluded? Default is FALSE, include all cells

**Value**

new value of theta vector

---

model\_i\_starting\_values

*Computes crude starting values for Model I.*

---

### Description

Computes crude starting values for Model I.

### Usage

model\_i\_starting\_values(n)

### Arguments

n                    matrix of observed counts

### Value

a list containing alpha: vector of row parameters beta: vector of column parameters gamma: vector of row locations delta: vector of column locations

---

model\_i\_update\_alpha    *Updates the estimate of the alpha vector for Model I*

---

### Description

Updates the estimate of the alpha vector for Model I

### Usage

model\_i\_update\_alpha(alpha, n, fHat, exclude\_diagonal = FALSE)

### Arguments

alpha                current estimate of beta  
n                    matrix of observed counts  
fHat                current model-based counts for each cell  
exclude\_diagonal    logical. Should the diagonal be excluded from the computation? Default is FALSE, use all cells.

### Value

updated estimate of alpha vector

---

model\_i\_update\_beta    *Updates the estimate of the beta vector for Model I*

---

**Description**

Updates the estimate of the beta vector for Model I

**Usage**

```
model_i_update_beta(beta, n, fHat, exclude_diagonal = FALSE)
```

**Arguments**

beta	current estimate of alpha
n	matrix of observed counts
fHat	current model-based counts for each cell
exclude_diagonal	logical. Should the diagonal be excluded from the computation? Default is FALSE, use all cells

**Value**

updated estimate of beta vector

---

model\_i\_update\_delta    *Updates the estimate of the delta vector for Model I*

---

**Description**

Updates the estimate of the delta vector for Model I

**Usage**

```
model_i_update_delta(delta, n, fHat, exclude_diagonal = FALSE)
```

**Arguments**

delta	current estimate of delta
n	matrix of observed counts
fHat	current model-based counts for each cell
exclude_diagonal	logical. Should the diagonal be excluded from the computation? Default is FALSE, use all cells

**Value**

updated estimate of delta vector

---

model\_i\_update\_gamma    *Updates the estimate of the gamma vector for Model I*

---

### Description

Updates the estimate of the gamma vector for Model I

### Usage

```
model_i_update_gamma(gamma, n, fHat, exclude_diagonal = FALSE)
```

### Arguments

gamma	current estimate of gamma
n	matrix of observed counts
fHat	current model-based counts for each cell
exclude_diagonal	logical. Should the diagonal be excluded from the computation? Default is FALSE, use all cells

### Value

updated estimate of gamma vector

---

model\_i\_zeta    *Computes the overall association theta and the row and column effects zeta*

---

### Description

Computes the overall association theta and the row and column effects zeta

### Usage

```
model_i_zeta(odds)
```

### Arguments

odds	matrix of adjacent odds-ratios
------	--------------------------------

### Value

a list containing theta: the overall association zeta\_i\_dot: row effects for association zeta\_dot\_j: column effects for association

---

model_ii_effects	<i>Gets the effects phi, ksi_i_dot and ksi_dot_j for Model II results.</i>
------------------	--

---

**Description**

Gets the effects phi, ksi\_i\_dot and ksi\_dot\_j for Model II results.

**Usage**

```
model_ii_effects(result)
```

**Arguments**

result            a result object from Model II

**Value**

a list containing: phi: the overall effect ksi\_i\_dot: the row effects ksi\_dot\_j: the column effects

---

model_ii_fHat	<i>Computes expected counts for Model II</i>
---------------	--

---

**Description**

Computes expected counts for Model II

**Usage**

```
model_ii_fHat(alpha, beta, rho, sigma)
```

**Arguments**

alpha	row effects
beta	column effects
rho	row locations
sigma	column locations

**Value**

matrix of model-based expected counts

---

model_ii_ksi	<i>Gets the effects phi, ksi_i_dot and ksi_dot_j for Model II matrix of odds-ratios.</i>
--------------	--

---

**Description**

Gets the effects phi, ksi\_i\_dot and ksi\_dot\_j for Model II matrix of odds-ratios.

**Usage**

```
model_ii_ksi(odds)
```

**Arguments**

odds                    matrix of adjacent odds-ratios

**Value**

a list containing: phi: the overall effect in log metric ksi\_i\_dot: the row effects ksi\_dot\_j: the column effects

---

model_ii_star_effects	<i>Gets the effects for Model II*</i>
-----------------------	---------------------------------------

---

**Description**

Gets the effects for Model II\*

**Usage**

```
model_ii_star_effects(result)
```

**Arguments**

result                    a Model II\* result object

**Value**

a list containing phi: common effect in log metric ksi: vector of ksi parameters

---

model\_ii\_star\_fHat      *Computes expected counts for Model II\**

---

**Description**

Computes expected counts for Model II\*

**Usage**

```
model_ii_star_fHat(alpha, beta, phi)
```

**Arguments**

alpha	row effects
beta	column effects
phi	row/column locations

**Value**

matrix of model-based expected counts

---

model\_ii\_star\_update\_phi  
*Updates estimate of phi vector*

---

**Description**

Updates estimate of phi vector

**Usage**

```
model_ii_star_update_phi(n, fHat, mu, phi, exclude_diagonal = FALSE)
```

**Arguments**

n	matrix of observed counts
fHat	current model-based counts for each cell
mu	alternative row coefficients
phi	vector of column location parameters
exclude_diagonal	logical, Should the cells on the main diagonal be excluded? Default is FALSE, use all cells

**Value**

list containing: phi: updated estimate of the phi vector mu: updated estimate of vector mu

---

model\_ii\_starting\_values

*Computes crude starting values for Model II*

---

### Description

Computes crude starting values for Model II

### Usage

```
model_ii_starting_values(n)
```

### Arguments

n                    matrix of observed counts

### Value

a list containing alpha: vector of row parameters beta: vector of column parameters rho: row coefficients sigma: column coefficients mu: alternative row coefficients nu: alternative column coefficients

---

model\_ii\_update\_alpha *Updates the estimate of the alpha vector for Model II*

---

### Description

Updates the estimate of the alpha vector for Model II

### Usage

```
model_ii_update_alpha(alpha, n, fHat, exclude_diagonal = FALSE)
```

### Arguments

alpha                current estimate of alpha  
n                    matrix of observed counts  
fHat                current model-based counts for each cell  
exclude\_diagonal    logical, Should the cells on the main diagonal be excluded? Default is FALSE, use all cells

### Value

updated estimate of alpha vector

---

model\_ii\_update\_beta *Updates the estimate of the beta vector for Model II*

---

**Description**

Updates the estimate of the beta vector for Model II

**Usage**

```
model_ii_update_beta(beta, n, fHat, exclude_diagonal = FALSE)
```

**Arguments**

beta	current estimate of beta
n	matrix of observed counts
fHat	current model-based counts for each cell
exclude_diagonal	logical, Should the cells on the main diagonal be excluded? Default is FALSE, use all cells

**Value**

updated estimate of beta vector

---

model\_ii\_update\_rho *Updates the estimate of the rho vector for Model II*

---

**Description**

Updates the estimate of the rho vector for Model II

**Usage**

```
model_ii_update_rho(n, fHat, mu, sigma, exclude_diagonal = FALSE)
```

**Arguments**

n	matrix of observed counts
fHat	current model-based counts for each cell
mu	alternative row coefficients
sigma	vector of column location parameters
exclude_diagonal	logical, Should the cells on the main diagonal be excluded? Default is FALSE, use all cells

**Value**

updated estimate of alpha vector

---

`model_ii_update_sigma` *Updates the estimate of the sigma vector for Model II*

---

**Description**

Updates the estimate of the sigma vector for Model II

**Usage**

```
model_ii_update_sigma(n, fHat, nu, rho, exclude_diagonal = FALSE)
```

**Arguments**

<code>n</code>	matrix of observed counts
<code>fHat</code>	current model-based counts for each cell
<code>nu</code>	vector of column coefficients
<code>rho</code>	vector of row location parameters
<code>exclude_diagonal</code>	logical, Should the cells on the main diagonal be excluded? Default is FALSE, use all cells

**Value**

updated estimate of sigma vector

---

`movies` *Movie ratings by two film critics, Siskel and Ebert.*

---

**Description**

Movie ratings by two film critics, Siskel and Ebert.

**Usage**

```
movies
```

**Format**

```
## 'movies' A matrix with 3 rows and 3 columns 1 is con 2 is mixed 3 is pro
```

**Source**

<https://online.stat.psu.edu/stat504/lesson/11/11.3>

---

new_orleans_data	<i>Agreement between two clinicians on presence of multiple sclerosis based on file.</i>
------------------	--

---

**Description**

See companion winnipeg\_data.

**Usage**

```
new_orleans_data
```

**Format**

## 'new\_orleans\_data' A matrix with 4 rows and 4 columns Ratings range from definite presence of disease to definite absence.

**Source**

???

---

null_association_fHat	<i>Computes expected counts for null association model</i>
-----------------------	--

---

**Description**

Computes expected counts for null association model

**Usage**

```
null_association_fHat(alpha, beta)
```

**Arguments**

alpha	row effects
beta	column effects

**Value**

matrix of model-based expected counts

---

occupational\_status     *Cross tabulation of father's employment status with son's employment status.*

---

**Description**

Higher numbers correspond to higher status occupation

**Usage**

occupational\_status

**Format**

## 'occupational\_status' A matrix with 6 rows and 6 columns

**Source**

???

---

paranoia     *Interrater agreement of two psychologists' ratings of paranoia.*

---

**Description**

Severity corresponds to level 1 low 3 high

**Usage**

paranoia

**Format**

## 'paranoia' A matrix with 3 rows and 3 columns.

**Source**

von Eye, A. & Mun, E. Y. (2005, p. 70). Analyzing rater agreement: Manifest variable methods. Mahwah, NJ: Lawrence Erlbaum.

---

pearson_chisq	<i>Computes the Pearson X<sup>2</sup> statistic.</i>
---------------	--

---

**Description**

Computes the Pearson X<sup>2</sup> statistic.

**Usage**

```
pearson_chisq(n, pi, exclude_diagonal = FALSE)
```

**Arguments**

n	Matrix of observed counts
pi	Matrix with same dimensions as n. Model-based matrix of predicted proportions
exclude_diagonal	logical. Should diagonal cells of square matrix be excluded from the computation? Default is FALSE. The effect of setting it to TRUE for non-square matrices may be unintuitive and should be avoided.

**Value**

X<sup>2</sup>

---

radiology	<i>Interrater agreement of two radiologists diagnosis of severity of carcinoma.</i>
-----------	---

---

**Description**

The data contains a comparison vector of (simulated) covariate data.

**Usage**

```
radiology
```

**Format**

```
## 'radiology' 'covariate' A matrix with 4 rows and 4 columns, and a vector of 16 elements.
```

**Source**

von Eye, A. & Mun, E. Y. (2005, p. 60). Analyzing rater agreement: Manifest variable methods. Mahwah, NJ: Lawrence Erlbaum.

---

Schuster\_compute\_df    *Computes the degrees of freedom for the model.*

---

**Description**

Computes the degrees of freedom for the model.

**Usage**

```
Schuster_compute_df(pi_margin)
```

**Arguments**

pi\_margin        expected proportions for each of the categories

**Value**

the df for the model

---

Schuster\_compute\_pi    *Compute matrix of model-based proportions pi.*

---

**Description**

Compute matrix of model-based proportions pi.

**Usage**

```
Schuster_compute_pi(marginal_pi, kappa, v, validate = TRUE)
```

**Arguments**

marginal\_pi    expected proportions for each category  
kappa          current estimate of the kappa coefficient  
v              symmetry matrix  
validate       logical. should the cells be validated within this function? Defaults to TRUE

**Value**

matrix of model-based cell proportions

---

Schuster\_compute\_starting\_values

*Computes starting values for the model.*

---

**Description**

Patterned after example in code in appendix to article

**Usage**

Schuster\_compute\_starting\_values(n)

**Arguments**

n                    matrix of observed counts

**Value**

a list containing marginal\_pi: vector of expected proportions for each category kappa: kappa coefficient of agreement v: matrix of symmetry parameters

---

Schuster\_derivative\_log\_l\_wrt\_kappa

*Derivative of log(likelihood) wrt kappa.*

---

**Description**

Derivative of log(likelihood) wrt kappa.

**Usage**

Schuster\_derivative\_log\_l\_wrt\_kappa(n, marginal\_pi, kappa, v)

**Arguments**

n                    matrix of observed counts  
marginal\_pi        expected proportions for each category  
kappa                current value of kappa coefficient  
v                    symmetry matrix

**Value**

derivative of log(L) wrt kappa

---

Schuster\_derivative\_log\_l\_wrt\_marginal\_pi  
*Derivative of log(likelihood) wrt marginal\_pi[k]*

---

**Description**

Derivative of log(likelihood) wrt marginal\_pi[k]

**Usage**

Schuster\_derivative\_log\_l\_wrt\_marginal\_pi(n, k, marginal\_pi, kappa, v)

**Arguments**

n	matrix of observed counts
k	index into marginal_pi
marginal_pi	expected proportions of each of the categories
kappa	current value of the kappa coefficient
v	symmetry matrix

**Value**

derivative of log(L) wrt marginal\_pi[k]

---

Schuster\_derivative\_log\_l\_wrt\_v  
*Derivative of log(likelihood) wrt v[i1, j1]*

---

**Description**

Derivative of log(likelihood) wrt v[i1, j1]

**Usage**

Schuster\_derivative\_log\_l\_wrt\_v(n, i1, j1, marginal\_pi, kappa, v)

**Arguments**

n	matrix of observed counts
i1	first index into v
j1	second index into v
marginal_pi	expected marginal proportions
kappa	current value of kappa coefficient
v	symmetry matrix

**Value**

derivative of  $\log(L)$  wrt  $v[i1, j1]$

---

Schuster\_derivative\_pi\_wrt\_kappa

*Derivative of  $\pi[i, j]$  wrt kappa coefficient.*

---

**Description**

Derivative of  $\pi[i, j]$  wrt kappa coefficient.

**Usage**

Schuster\_derivative\_pi\_wrt\_kappa(i, j, marginal\_pi, kappa, v)

**Arguments**

i	first index into pi
j	second index into pi
marginal_pi	expected proportions in each category
kappa	current value of kappa coefficient
v	symmetry matrix

**Value**

the derivative of  $\pi[i, j]$  wrt kappa

---

Schuster\_derivative\_pi\_wrt\_marginal\_pi

*Derivative of  $\pi[i, j]$  wrt marginal\_pi[k].*

---

**Description**

Derivative of  $\pi[i, j]$  wrt marginal\_pi[k].

**Usage**

Schuster\_derivative\_pi\_wrt\_marginal\_pi(i, j, k, marginal\_pi, kappa, v)

**Arguments**

i	first index into pi
j	second index into pi
k	index into marginal_pi
marginal_pi	expected proportions for each category
kappa	current estimate of kappa coefficient
v	symmetry matrix

**Value**

derivative of  $\pi[i, j]$  wrt  $\text{marginal\_pi}[k]$

---

Schuster\_derivative\_pi\_wrt\_v

*Computes derivative of  $\pi[i, j]$  wrt  $v[i1, j1]$*

---

**Description**

Computes derivative of  $\pi[i, j]$  wrt  $v[i1, j1]$

**Usage**

Schuster\_derivative\_pi\_wrt\_v(i, j, i1, j1, marginal\_pi, kappa, v)

**Arguments**

i	first index into pi
j	second index into pi
i1	first index into v
j1	second index into v
marginal_pi	expected marginal proportions
kappa	current estimate of kappa coefficient
v	symmetry matrix

**Value**

value of derivative of specified pi wrt specified element of v

---

 Schuster\_derivative\_v\_wrt\_v

*Computes derivative of  $v[i1, j1]$  wrt  $v[i2, j2]$* 


---

**Description**

Needed because of computed v terms in column r

**Usage**

Schuster\_derivative\_v\_wrt\_v(i1, j1, i2, j2, marginal\_pi, kappa, v)

**Arguments**

i1	first index into target v
j1	second index into target v
i2	first index into
j2	second index into
marginal_pi	expected marginal proportions
kappa	current estimate of kappa coefficient
v	matrix of symmetry parameters

**Value**

derivative of  $v[i1, j1]$  wrt  $v[i2, j2]$

---

Schuster\_enforce\_constraints\_on\_v

*Compute v matrix subject to constraints on rows 1..r-1.*


---

**Description**

Compute v matrix subject to constraints on rows 1..r-1.

**Usage**

Schuster\_enforce\_constraints\_on\_v(marginal\_pi, kappa, v)

**Arguments**

marginal_pi	expected proportions for each category
kappa	current estimate of kappa coefficient
v	symmetry matrix

**Value**

new v matrix with last row/column set to agree with constraints. Element  $v[r, r]$  is set to  $v\text{-tilde}$

---

Schuster_gradient	<i>Gradient vector <math>\log(L)</math> wrt parameters.</i>
-------------------	---

---

**Description**

Work is delegated to functions that compute partial derivatives. This function is responsible for laying them out in correct positions in the vector.

**Usage**

```
Schuster_gradient(n, marginal_pi, kappa, v)
```

**Arguments**

n	matrix of observed counts
marginal_pi	expected proportions for each response category
kappa	current estimate of kappa coefficient
v	symmetry matrix

**Value**

gradient vector

---

Schuster_hessian	<i>Computes the hessian matrix of second-order partial derivatives of <math>\log(L)</math>.</i>
------------------	---

---

**Description**

Work is delegated to functions that compute second-order partial derivatives. This function is responsible for laying them out in correct positions in the matrix.

**Usage**

```
Schuster_hessian(n, marginal_pi, kappa, v)
```

**Arguments**

n	matrix of observed counts
marginal_pi	expected proportions for each category
kappa	current estimate of the kappa coefficient
v	symmetry matrix

**Value**

hessian matrix

---

Schuster\_is\_pi\_valid *Determines whether the candidate pi matrix is valid.*

---

**Description**

All elements must lie in (0, 1)

**Usage**

Schuster\_is\_pi\_valid(pi)

**Arguments**

pi                    matrix of model-based proportions

**Value**

logical value indicating whether or not the matrix is valid.

---

Schuster\_newton\_raphson  
*Performs Newton-Raphson step.*

---

**Description**

The step size is determined to be the largest that yields valid results for all quantities marginal\_pi and v. Both must be positive, and the elements of marginal\_pi must be valid proportions that sum to 1.0.

**Usage**

Schuster\_newton\_raphson(n, marginal\_pi, kappa, v)

**Arguments**

n                    matrix of observed counts  
marginal\_pi        expected proportions for each category  
kappa                current estimate of the kappa coefficient  
v                    symmetry matrix

**Value**

a list containing updated versions of model quantities marginal\_pi kappa v

---

Schuster\_second\_deriv\_log\_l\_wrt\_kappa\_2  
*Second order partial log(L) wrt kappa^2.*

---

**Description**

Second order partial log(L) wrt kappa^2.

**Usage**

Schuster\_second\_deriv\_log\_l\_wrt\_kappa\_2(n, marginal\_pi, kappa, v)

**Arguments**

n	matrix of observed counts
marginal_pi	expected proportions for each response category
kappa	current estimate of kappa coefficient
v	symmetry matrix second derivative of log(L) wrt kappa^2

---

Schuster\_second\_deriv\_log\_l\_wrt\_kappa\_v  
*Second order partial log(L) wrt kappa and v.*

---

**Description**

Second order partial log(L) wrt kappa and v.

**Usage**

Schuster\_second\_deriv\_log\_l\_wrt\_kappa\_v(n, marginal\_pi, kappa, v)

**Arguments**

n	matrix of observed counts
marginal_pi	expected proportions for each response category
kappa	current estimate of kappa coefficient
v	symmetry matrix second derivative of log(L) wrt kappa and v

---

Schuster\_second\_deriv\_log\_l\_wrt\_marginal\_pi\_2  
*Second order partial log(L) wrt marginal\_pi^2.*

---

**Description**

Second order partial log(L) wrt marginal\_pi^2.

**Usage**

Schuster\_second\_deriv\_log\_l\_wrt\_marginal\_pi\_2(n, marginal\_pi, kappa, v)

**Arguments**

n	matrix of observed counts
marginal_pi	expected proportions for each response category
kappa	current estimate of kappa coefficient
v	symmetry matrix second derivative of log(L) wrt marginal_pi^2

---

Schuster\_second\_deriv\_log\_l\_wrt\_marginal\_pi\_kappa  
*Second order partial log(L) wrt marginal\_pi and kappa.*

---

**Description**

Second order partial log(L) wrt marginal\_pi and kappa.

**Usage**

Schuster\_second\_deriv\_log\_l\_wrt\_marginal\_pi\_kappa(n, marginal\_pi, kappa, v)

**Arguments**

n	matrix of observed counts
marginal_pi	expected proportions for each response category
kappa	current estimate of kappa coefficient
v	symmetry matrix second derivative of log(L) wrt marginal_pi and kappa

---

Schuster\_second\_deriv\_log\_l\_wrt\_marginal\_pi\_v

*Second order partial log(L) wrt marginal\_pi and v.*

---

### Description

Second order partial log(L) wrt marginal\_pi and v.

### Usage

Schuster\_second\_deriv\_log\_l\_wrt\_marginal\_pi\_v(n, marginal\_pi, kappa, v)

### Arguments

n	matrix of observed counts
marginal_pi	expected proportions for each response category
kappa	current estimate of kappa coefficient
v	symmetry matrix second derivative of log(L) wrt marginal_pi and v

---

Schuster\_second\_deriv\_log\_l\_wrt\_v\_2

*Second order partial log(L) wrt v^2.*

---

### Description

Second order partial log(L) wrt v^2.

### Usage

Schuster\_second\_deriv\_log\_l\_wrt\_v\_2(n, marginal\_pi, kappa, v)

### Arguments

n	matrix of observed counts
marginal_pi	expected proportions for each response category
kappa	current estimate of kappa coefficient
v	symmetry matrix second derivative of log(L) wrt v^2

---

Schuster\_second\_deriv\_pi\_wrt\_kappa\_2  
*Second order partial wrt kappa, kappa*

---

**Description**

Derivative is uniformly 0

**Usage**

Schuster\_second\_deriv\_pi\_wrt\_kappa\_2(i, j, marginal\_pi, kappa, v)

**Arguments**

i	first index of pi
j	second index of pi
marginal_pi	expected proportions for each category
kappa	current estimate of the kappa coefficient
v	symmetry matrix

**Value**

second order partial derivative

---

Schuster\_second\_deriv\_pi\_wrt\_kappa\_v  
*Second order partial wrt kappa, v*

---

**Description**

Derivative is uniformly 0

**Usage**

Schuster\_second\_deriv\_pi\_wrt\_kappa\_v(i, j, i1, j1, marginal\_pi, kappa, v)

**Arguments**

i	first index of pi
j	second index of pi
i1	first index of v
j1	second index of v
marginal_pi	expected proportions for each category
kappa	current estimate of the kappa coefficient
v	symmetry matrix

**Value**

second order partial derivative

---

Schuster\_second\_deriv\_pi\_wrt\_marginal\_pi\_2  
*Second derivative of pi[i, j] wrt marginal\_pi[k]^2*

---

**Description**

Second derivative of pi[i, j] wrt marginal\_pi[k]^2

**Usage**

Schuster\_second\_deriv\_pi\_wrt\_marginal\_pi\_2(i, j, k, k2, marginal\_pi, kappa, v)

**Arguments**

i	first index into pi
j	second index into pi
k	index into marginal_pi
k2	second index into marginal_pi
marginal_pi	expected proportions for each category
kappa	current estimate of kappa coefficient
v	symmetry matrix

**Value**

second derivative of pi[i, j] wrt marginal\_pi^2

---

Schuster\_second\_deriv\_pi\_wrt\_marginal\_pi\_kappa  
*Second order partial wrt kappa, marginal\_pi*

---

**Description**

Derivative is uniformly 0

**Usage**

Schuster\_second\_deriv\_pi\_wrt\_marginal\_pi\_kappa(i, j, k, marginal\_pi, kappa, v)

**Arguments**

i	first index of pi
j	second index of pi
k	index of marginal_pi
marginal_pi	expected proportions for each category
kappa	current estimate of the kappa coefficient
v	symmetry matrix

**Value**

second order partial derivative

---

Schuster\_second\_deriv\_pi\_wrt\_marginal\_pi\_v  
*Second order partial pi wrt marginal\_pi and v*

---

**Description**

Second order partial pi wrt marginal\_pi and v

**Usage**

```
Schuster_second_deriv_pi_wrt_marginal_pi_v(
  i,
  j,
  k,
  i1,
  j1,
  marginal_pi,
  kappa,
  v
)
```

**Arguments**

i	first index of pi
j	second index of pi
k	index of marginal_pi
i1	first index of v
j1	second index of v
marginal_pi	expected proportions of each of the categories
kappa	current value of kappa coefficient
v	symmetry matrix

**Value**

derivative

---

Schuster\_second\_deriv\_pi\_wrt\_v\_2  
*Second order partial wrt v<sup>2</sup>*

---

**Description**

Derivative is uniformly 0

**Usage**

Schuster\_second\_deriv\_pi\_wrt\_v\_2(i, j, i1, j1, i2, j2, marginal\_pi, kappa, v)

**Arguments**

i	first index of pi
j	second index of pi
i1	first index of first v
j1	second index of first v
i2	first index of second v
j2	second index of second
marginal_pi	expected proportions for each category
kappa	current estimate of the kappa coefficient
v	symmetry matrix

**Value**

second order partial derivative

---

Schuster\_solve\_for\_v *Solves for the last row and diagonal of symmetry matrix v (v-tilde) using constraint equations*

---

**Description**

Solves for the last row and diagonal of symmetry matrix v (v-tilde) using constraint equations

**Usage**

Schuster\_solve\_for\_v(marginal\_pi, kappa, v)

**Arguments**

marginal_pi	expected proportions for each category
kappa	current estimate of kappa coefficient
v	symmetry matrix

**Value**

revised version of v matrix with last row and diagonal modified

---

Schuster\_solve\_for\_v1 *Solves for the last row and diagonal of symmetry matrix v (parameter v-tilde) using linear algebra formulation from paper.*

---

**Description**

Solves for the last row and diagonal of symmetry matrix v (parameter v-tilde) using linear algebra formulation from paper.

**Usage**

Schuster\_solve\_for\_v1(marginal\_pi, kappa, v)

**Arguments**

marginal_pi	expected proportions for each category
kappa	current estimate of kappa coefficient
v	symmetry matrix

**Value**

revised version of v matrix with last row and diagonal modified

---

Schuster\_symmetric\_rater\_agreement\_model

*Computes the model that has kappa as a coefficient and symmetry.*

---

### Description

Schuster, C. (2001). Kappa as a parameter of a symmetry model for rater agreement. *Journal of Educational and Behavioral Statistics*, 26(3), 331-342.

### Usage

```
Schuster_symmetric_rater_agreement_model(
  n,
  verbose = FALSE,
  max_iter = 10000,
  criterion = 1e-07,
  min_iter = 1000
)
```

### Arguments

n	the matrix of observed counts
verbose	logical. should cycle-by-cycle information be printed out
max_iter	integer. maximum number of iterations to perform
criterion	number. maximum change in log(likelihood) to decide convergence
min_iter	integer. minimum number of iterations to perform

### Value

a list containing marginal\_pi: vector of expected proportions for each category kappa numeric: kappa coefficient v: matrix of symmetry parameters chisq: Pearson  $X^2$  g\_squared: likelihood ratio  $G^2$  df: degrees of freedom

---

Schuster\_update

*Computes the Newton-Raphson update*

---

### Description

Computes both gradient and hessian, and then solves the system of equations

### Usage

```
Schuster_update(n, marginal_pi, kappa, v)
```

**Arguments**

n	matrix of observed counts
marginal_pi	expected proportions for each category
kappa	current value of kappa coefficient
v	symmetry matrix

**Value**

the vector of updates

---

Schuster_v_tilde	<i>Computes the common diagonal term v-tilde.</i>
------------------	---

---

**Description**

Computes the common diagonal term v-tilde.

**Usage**

```
Schuster_v_tilde(marginal_pi, kappa, validate = TRUE)
```

**Arguments**

marginal_pi	expected proportions for each category
kappa	current estimate of kappa coefficient
validate	logical. should the value of pi[r,r] be checked for validity? Default is TRUE

**Value**

v-tilde

---

social_status	<i>Social mobility data with father's occupational social status and son's occupational social status.</i>
---------------	--

---

**Description**

Social mobility data with father's occupational social status and son's occupational social status.

**Usage**

```
social_status
```

**Format**

```
## 'social_status' A matrix with 7 rows and 7 columns
```

**Source**

Goodman, L. A. (1979). Simple models for the analysis of association in cross-classifications having ordered categories. *Journal of the American Statistical Association*, 74(367), 537-552.

---

social_status2	<i>Social mobility data with father's occupational social status and son's occupational social status. * categories instead of 7 in social status..</i>
----------------	---

---

**Description**

Social mobility data with father's occupational social status and son's occupational social status. \* categories instead of 7 in social status..

**Usage**

```
social_status2
```

**Format**

```
## 'social_status2' A matrix with 8 rows and 8 columns
```

**Source**

Goodman, L. A. (1979). Simple models for the analysis of association in cross-classifications having ordered categories. *Journal of the American Statistical Association*, 74(367), 537-552.

---

Stuart_marginal_homogeneity	<i>Computes Stuart's Q test of marginal homogeneity.</i>
-----------------------------	--

---

**Description**

Stuart, A. (1955). A test for homogeneity of the marginal distributions in a two-way classification. *Biometrika*, 42(3/4), 412-416.

**Usage**

```
Stuart_marginal_homogeneity(n)
```

**Arguments**

n	matrix of observed counts
---	---------------------------

**Value**

a list containing q: value of q test-statistic df: degrees of freedom p: upper tail p-value of q

**Examples**

```
Stuart_marginal_homogeneity(vision_data)
```

---

taste	<i>Taste ratings</i>
-------	----------------------

---

**Description**

Taste ratings

**Usage**

```
taste
```

**Format**

```
## 'taste' A matrix with 5 rows and 5 columns.
```

**Source**

McCullagh, P. (1980, p. 119). Regression models for ordinal data. *Journal of the Royal Statistical Society, Series B*, 42(2), 109-142.

---

teachers	<i>Teachers ratings of their students intelligence.</i>
----------	---

---

**Description**

Interrater agreement data for two teachers asked to rate the intelligence of their students.

**Usage**

```
teachers
```

**Format**

```
## 'teachers' A matrix with 4 rows and 4 columns. Higher scores correspond to higher estimated intelligence.
```

**Source**

von Eye, A. & Mun, E. Y. (2005, p. 36). *Analyzing rater agreement: Manifest variable methods*. Mahwah, NJ: Lawrence Erlbaum.

---

teaching_style	<i>Style of teachers rated by supervisors</i>
----------------	---

---

**Description**

Ratings of style of teaching by supervisors. 1 indicates Authoritarian, 2 indicates Democratic, 3 indicates Permissive.

**Usage**

teaching\_style

**Format**

An object of class `matrix` (inherits from `array`) with 3 rows and 3 columns.

**Details**

@format ## 'teaching\_style' A matrix with 3 rows and 3 columns.

@source Agresti, A. (1989). An agreement model with kappa as parameter. *Statistics & Probability Letters*, 7, 271-273.

---

tonsils	<i>Relationship between size of child's tonsils and their status as a carrier of a disease.</i>
---------	---

---

**Description**

Relationship between size of child's tonsils and their status as a carrier of a disease.

**Usage**

tonsils

**Format**

## 'tonsils' A matrix with 2 rows and 3 columns. Rows are disease status and columns are ratings of tonsil size.

**Source**

McCullagh, P. (1980). Regression models for ordinal data. *Journal of the Royal Statistical Society, Series B*, 42(2), 109-142.

---

tv	<i>Interrater agreement of two journalists' evaluation of proposed TV programs.</i>
----	---

---

**Description**

Ratings go from low to high probability of the show's success.

**Usage**

tv

**Format**

## 'tv' A matrix of 6 rows and 6 columns.

**Source**

von Eye, A. & Mun, E. Y. (2005, p. 56). Analyzing rater agreement: Manifest variable methods. Mahwah, NJ: Lawrence Erlbaum.

---

uniform_association_fHat	<i>Computes expected counts for uniform association model</i>
--------------------------	---

---

**Description**

Computes expected counts for uniform association model

**Usage**

uniform\_association\_fHat(alpha, beta, theta)

**Arguments**

alpha	row effects
beta	column effects
theta	association parameter

**Value**

matrix of model-based expected counts

---

```
uniform_association_update_theta
```

*Updates estimate of theta value of the uniform association model*

---

### Description

Updates estimate of theta value of the uniform association model

### Usage

```
uniform_association_update_theta(theta, n, fHat, exclude_diagonal = FALSE)
```

### Arguments

theta	current estimate of theta
n	matrix of observed counts
fHat	current model-based counts for each cell
exclude_diagonal	logical. Should the cells of the main diagonal be excluded from the computations? Default is FALSE, include all cells.

### Value

updated estimate of theta parameter

---

```
var_kappa
```

*Computes the sampling variance of kappa.*

---

### Description

Formulas are from the paper by Fleiss, J. L., Cohen, J., & Everitt, B. S. (1969). Large sample standard errors of kappa and weighted kappa. Two results are returned in a list. `var_kappa0` is the null case and would be used for testing the hypothesis that  $\kappa = 0$ . The second is `var_kappa` and is for the non-null case, such as constructing CI for estimated kappa. Note that both are in the variance metric. Take the square root to get the standard error.

### Usage

```
var_kappa(n)
```

### Arguments

n	matrix of observe counts
---	--------------------------

### Value

a list containing; `var_kappa0`: variance for the null case `var_kappa`: variance for the non-null case.

---

var\_weighted\_kappa      *Computes the sampling variance of weighted kappa.*

---

### Description

Formulas are from the paper by Fleiss, J. L., Cohen, J., & Everitt, B. S. (1969). Large sample standard errors of kappa and weighted kappa. Two results are returned in a list. var\_kappa0 is the null case and would be used for testing the hypothesis that kappa = 0. The second is var\_kappa and is for the non-null case, such as constructing CI for estimated kappa. Note that both are in the variance metric. Take the square root to get the standard error.

### Usage

```
var_weighted_kappa(n, w)
```

### Arguments

n	matrix of observe counts
w	matrix of penalty weights

### Value

a list containing; var\_kappa0: variance for the null case var\_kappa: variance for the non-null case.

---

vision\_data      *Visual acuity of women factory workers.*

---

### Description

Measurements of unaided visual acuity for women working at the Royal Ordnance factories 1943-1946. Rows are right eye, columns are left eye. 1 indicates best vision, 4 is poorest.

### Usage

```
vision_data
```

### Format

```
## 'visual_data' A matrix with 4 rows and 4 columns.
```

### Source

Stuart, A. (1953). The estimation and comparison of strengths of association in contingency tables. *Biometrika*, 40(1/2), 105-110.

---

vision_data_men	<i>Visual acuity of men factory workers.</i>
-----------------	--

---

**Description**

Measurements of unaided visual acuity for men working at the Royal Ordnance factories 1943-1946. Rows are right eye, columns are left eye. 1 indicates best vision, 4 is poorest.

**Usage**

```
vision_data_men
```

**Format**

```
## 'visual_data_men' A matrix with 4 rows and 4 columns.
```

**Source**

Stuart, A. (1953). The estimation and comparison of strengths of association in contingency tables. *Biometrika*, 40(1/2), 105-110.

---

von_Eye_diagonal	<i>Fits the diagonal effects model, where each category has its own parameter delta[k].</i>
------------------	---

---

**Description**

Fits the diagonal effects model, where each category has its own parameter delta[k].

**Usage**

```
von_Eye_diagonal(n)
```

**Arguments**

n                    the matrix of observed counts

**Value**

a list containing beta: the regression parameters. delta parameters are the final elements of beta  
g\_squared: G^2 fit measure chisq: X^2 fit measure df: degrees of freedom expected: matrix of expected frequencies

---

 von\_Eye\_diagonal\_linear\_by\_linear

*Fits the diagonal effects model, where each category has its own parameter delta[k], while also incorporating a linear-by-linear term.*

---

### Description

Fits the diagonal effects model, where each category has its own parameter delta[k], while also incorporating a linear-by-linear term.

### Usage

```
von_Eye_diagonal_linear_by_linear(n, center = TRUE)
```

### Arguments

n	the matrix of observed counts
center	should the linear-by-linear components be centered to have mean 0? Default is TRUE

### Value

a list containing beta: the regression parameters. delta parameters come after rows and columns and finally the linear-by-linear term g\_squared: G^2 fit measure chisq: X^2 fit measure df: degrees of freedom expected: matrix of expected frequencies

---

von\_Eye\_equal\_weight\_diagonal\_linear

*Fits the diagonal effects model, where there is a single delta parameter for all categories, while also incorporating a linear-by-linear term.*

---

### Description

Fits the diagonal effects model, where there is a single delta parameter for all categories, while also incorporating a linear-by-linear term.

### Usage

```
von_Eye_equal_weight_diagonal_linear(n, center = TRUE)
```

### Arguments

n	the matrix of observed counts
center	should the linear-by-linear components be centered to have mean 0? Default is TRUE

**Value**

a list containing beta: the regression parameters. delta parameters come after rows and columns and finally the linear-by-linear term g\_squared: G^2 fit measure chisq: X^2 fit measure df: degrees of freedom expected: matrix of expected frequencies

---

von\_Eye\_equal\_weighted\_diagonal

*Fits the equal weighted diagonal model, where the diagonals all have an additional parameter delta, with the constraint that delta is equal across all categories.*

---

**Description**

Fits the equal weighted diagonal model, where the diagonals all have an additional parameter delta, with the constraint that delta is equal across all categories.

**Usage**

von\_Eye\_equal\_weighted\_diagonal(n)

**Arguments**

n                    the matrix of observed counts

**Value**

a list containing beta: the regression parameters g\_squared: G^2 fit measure chisq: X^2 fit measure df: degrees of freedom expected: matrix of expected frequencies

---

von\_Eye\_linear\_by\_linear

*Fits the basic independent rows and columns model incorporating a linear-by-linear term.*

---

**Description**

Fits the basic independent rows and columns model incorporating a linear-by-linear term.

**Usage**

von\_Eye\_linear\_by\_linear(n, center = TRUE)

**Arguments**

n                    matrix of observed counts  
 center              should the linear-by-linear components be centered to have mean 0? Default is TRUE

**Value**

a list containing beta: the regression parameters. The linear-by-linear parameter is last g\_squared: G^2 fit measure chisq: X^2 fit measure df: degrees of freedom expected: matrix of expected frequencies

---

von\_Eye\_main\_effect    *Fits the base model with only independent row and column effects.*

---

**Description**

Fits the base model with only independent row and column effects.

**Usage**

```
von_Eye_main_effect(n)
```

**Arguments**

n                    the matrix of observed counts

**Value**

a list containing beta: the regression parameters g\_squared: G^2 fit measure chisq: X^2 fit measure df: degrees of freedom expected: matrix of expected frequencies

---

von\_Eye\_weight\_by\_response\_category\_design  
*Creates design matrix for weight by response category model.*

---

**Description**

The model specifies main effects for row and column, and a parameter for the agreement (diagonal) cells. This takes a design matrix for that model and applies domain-specific weights to the agreement parameters.

**Usage**

```
von_Eye_weight_by_response_category_design(n, x, w, n_raters = 2)
```

**Arguments**

n	the matrix of cell counts
x	the original design matrix.
w	the vector of weights to apply to the agreement cells. Should have same number of entries as the number of diagonal elements (number of rows & of columns)
n_raters	number of raters. Currently only 2 (the default) are supported. This is an extension point for future work.

**Value**

new design matrix with weights applied to the agreement cells.

---

weighted_cov	<i>Computes the weighted covariance</i>
--------------	---

---

**Description**

Computes covariance between x and y using case weights in w

**Usage**

```
weighted_cov(x, y, w, use_df = TRUE)
```

**Arguments**

x	Numeric vector. First variable
y	Numeric vector. Second variable
w	Numeric vector. case weights
use_df	Logical. should the divisor be sum of weights - 1 (TRUE) or N - 1 (FALSE)

**Value**

the weighted covariance between x and y

---

weighted_kappa	<i>Computes Cohen's 1968 weighted kappa coefficient</i>
----------------	---

---

**Description**

Computes Cohen's 1968 weighted kappa coefficient

**Usage**

```
weighted_kappa(n, w = diag(rep(1, nrow(n))), quadratic = FALSE)
```

**Arguments**

n	matrix of observed counts
w	matrix of weights. Defaults to identity matrix
quadratic	logical. Should quadratic weights be used? Default is FALSE. If TRUE, quadratic weights are used. These override the values in w. If FALSE, weights in w are used

**Value**

value of weighted kappa

---

weighted_var	<i>Computes the weighted variance</i>
--------------	---------------------------------------

---

**Description**

Computes variance between x and y using case weights in w

**Usage**

```
weighted_var(x, w, use_df = TRUE)
```

**Arguments**

x	Numeric vector. First variable
w	Numeric vector. Case weights
use_df	Logical. Should the divisor be sum of weights - 1 (TRUE) or N - 1 (FALSE)

**Value**

the weighted covariance between x and y

---

winnipeg_data	<i>Agreement between two clinicians on presence of multiple sclerosis based on file.</i>
---------------	--

---

**Description**

See companion new\_orleans\_data.

**Usage**

```
winnipeg_data
```

**Format**

```
## 'winnipeg_data' A matrix with 4 rows and 4 columns Ratings range from definite presence of disease to definite absence.
```

**Source**

```
???
```

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