

# Package: mvnTest (via r-universe)

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**Title** Goodness of Fit Tests for Multivariate Normality

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**Description** Routines for assessing multivariate normality. Implements three Wald's type chi-squared tests; non-parametric Anderson-Darling and Cramer-von Mises tests; Doornik-Hansen test, Royston test and Henze-Zirkler test.

**Depends** R (>= 2.15.0), mvtnorm

**Imports** methods, stats, graphics, MASS

**License** GPL (>= 2)

**LazyLoad** yes

**NeedsCompilation** no

**Repository** CRAN

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mvnTest-package	<i>Goodness-of-fit tests for multivariate normality</i>
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**Description**

mvnTest provides functions for assessing multivariate normality. It includes eight test statistics such as three Wald's type chi-squared tests (McCulloch, Nikulin-Rao-Robson and Dzhaparidze-Nikulin tests), non-parametric Anderson-Darling and Cramer-von Mises tests; Doornik-Hansen test, Royston test and Henze-Zirkler test.

**Details**

Package: mvnTest  
 Type: Package  
 License: GPL (>= 2)

**Note**

The printing method and plotting are in part adapted from R package MVN (version 4.0, Korkmaz, S. et al., 2015)

**Author(s)**

Vassilly Voinov, Natalya Pya, Rashid Makarov, Yevgeniy Voinov  
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ad-class	<i>Class "ad"</i>
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**Description**

An S4 class for the Anderson-Darling test for multivariate normality.

**Slots**

AD: stores the values of the test statistics  
 p.value: stores the p-value of the test  
 data.name: stores the name of the data

**Author(s)**

Natalya Pya, Vassilly Voinov, Rashid Makarov

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AD.test	<i>Anderson-Darling test for multivariate normality</i>
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**Description**

This function implements the Anderson-Darling test for assessing multivariate normality. It calculates the value of the test and its approximate p-value.

**Usage**

```
AD.test(data, qqplot = FALSE)
```

**Arguments**

data	A numeric matrix or data frame.
qqplot	If TRUE produces a chi-squared QQ plot.

**Value**

AD	the value of the test statistic.
p.value	the p-value of the test.

**Note**

The printing method and plotting are in part adapted from R package MVN (version 4.0, Korkmaz, S. et al., 2015).

The computations are relatively expensive as Monte Carlo procedure is used to calculate empirical p-values.

**Author(s)**

Rashid Makarov, Vassilly Voinov, Natalya Pya

**References**

Paulson, A., Roohan, P., and Sullo, P. (1987). Some empirical distribution function tests for multivariate normality. *Journal of Statistical Computation and Simulation*, 28, 15-30

Henze, N. and Zirkler, B. (1990). A class of invariant consistent tests for multivariate normality. *Communications in Statistics - Theory and Methods*, 19, 3595-3617

Selcuk Korkmaz, Dincer Goksuluk, and Gokmen Zararsiz. MVN: Multivariate Normality Tests, 2015. R package version 4.0

**See Also**

[S2.test](#), [CM.test](#), [DH.test](#), [R.test](#), [HZ.test](#)

**Examples**

```
## Not run:
## generating n bivariate normal random variables...
dat <- rmvnorm(n=100,mean=rep(0,2),sigma=matrix(c(4,2,2,4),2,2))
res <- AD.test(dat)
res

## generating n bivariate t distributed with 10df random variables...
dat <- rmvt(n=200,sigma=matrix(c(4,2,2,4),2,2),df=10,delta=rep(0,2))
res1 <- AD.test(dat)
res1

data(iris)
setosa <- iris[1:50, 1:4] # Iris data only for setosa
res2 <- AD.test(setosa, qqplot = TRUE)
res2

## End(Not run)
```

---

cm-class

*Class "cm"*


---

**Description**

An S4 class for the Cramer-von Mises test for multivariate normality.

**Slots**

**CM:** stores the values of the test statistics

**p.value:** stores the p-value of the test

**data.name:** stores the name of the data

**Author(s)**

Natalya Pya, Vassilly Voinov, Rashid Makarov

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CM.test

*Cramer-von Mises test for Multivariate Normality*


---

**Description**

This function implements the Cramer-von Mises test for assessing multivariate normality.

**Usage**

```
CM.test(data, qqplot = FALSE)
```

**Arguments**

data	A numeric matrix or data frame
qqplot	if TRUE creates a chi-square Q-Q plot

**Details**

Calculates the value of the Cramer-von Mises test and the approximate p-value.

**Value**

CM	the value of the test statistic
p. value	the p-value of the test
data.name	a character string giving the name of the data

**Note**

The printing method and plotting are in part adapted from R package MVN (version 4.0, Korkmaz, S. et al., 2015).

The computations are relatively expensive as Monte Carlo procedure is used to calculate empirical p-values.

**Author(s)**

Rashid Makarov, Vassilly Voinov, Natalya Pya

**References**

Koziol, J. (1982). A class of invariant procedures for assessing multivariate normality. *Biometrika*, 69, 423-427

Henze, N. and Zirkler, B. (1990). A class of invariant consistent tests for multivariate normality. *Communications in Statistics - Theory and Methods*, 19, 3595-3617

**See Also**

[S2.test](#), [AD.test](#), [DH.test](#), [R.test](#), [HZ.test](#)

**Examples**

```
## Not run:
## generating n bivariate normal random variables...
dat <- rmvnorm(n=100,mean=rep(0,2),sigma=matrix(c(4,2,2,4),2,2))
res <- CM.test(dat)
res

## generating n bivariate t distributed with 10df random variables...
dat <- rmvt(n=200,sigma=matrix(c(4,2,2,4),2,2),df=10,delta=rep(0,2))
res1 <- CM.test(dat)
res1
```

```

data(iris)
setosa <- iris[1:50, 1:4] # Iris data only for setosa
res2 <- CM.test(setosa, qqplot = TRUE)
res2

## End(Not run)

```

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dh-class	<i>Class "dh"</i>
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### Description

An S4 class for the Doornik-Hansen test for multivariate normality.

### Slots

DH: stores the values of the test statistics

p.value: stores the p-value of the test

data.name: stores the name of the data

### Author(s)

Natalya Pya, Vassilly Voinov, Rashid Makarov

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DH.test	<i>Doornik-Hansen test for Multivariate Normality</i>
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### Description

This function implements the Doornik-Hansen test for assessing multivariate normality.

### Usage

```
DH.test(data, qqplot = FALSE)
```

### Arguments

data            A numeric matrix or data frame

qqplot         if TRUE creates a chi-square Q-Q plot

### Details

Calculates the value of the Doornik-Hansen test and the approximate p-value.

**Value**

DH	the value of the test statistic
p.value	the p-value of the test
data.name	a character string giving the name of the data

**Note**

The printing method and plotting are in part adapted from R package MVN (version 4.0, Korkmaz, S. et al., 2015).

**Author(s)**

Rashid Makarov, Vassilly Voinov, Natalya Pya

**References**

Doornik, J. and Hansen, H. (2008). An omnibus test for univariate and multivariate normality. *Oxford Bulletin of Economics and Statistics*, 70, 915-925.

**See Also**

[S2.test](#), [AD.test](#), [CM.test](#), [R.test](#), [HZ.test](#)

**Examples**

```
## generating n bivariate normal random variables...
dat <- rmvnorm(n=200,mean=rep(0,2),sigma=matrix(c(4,2,2,4),2,2))
res <- DH.test(dat)
res
## generating n bivariate t distributed with 10df random variables...
dat <- rmvt(n=200,sigma=matrix(c(4,2,2,4),2,2)*.8,df=10,delta=rep(0,2))
res1 <- DH.test(dat)
res1

data(iris)
setosa <- iris[1:50, 1:4] # Iris data only for setosa
res2 <- DH.test(setosa, qqplot = TRUE)
res2
```

---

hz-class

*Class "hz"*

---

**Description**

An S4 class for the Henze-Zirkler test for multivariate normality.

**Slots**

HZ: stores the values of the test statistics

p.value: stores the p-value of the test

data.name: stores the name of the data

**Author(s)**

Natalya Pya, Vassilly Voinov, Rashid Makarov

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HZ.test

*Henze-Zirkler test for Multivariate Normality*

---

**Description**

This function implements the Henze-Zirkler test for assessing multivariate normality.

**Usage**

```
HZ.test(data, qqplot = FALSE)
```

**Arguments**

data	A numeric matrix or data frame
qqplot	if TRUE creates a chi-square Q-Q plot

**Details**

Calculates the value of the Henze-Zirkler test and the approximate p-value.

**Value**

HZ	the value of the test statistic
p.value	the p-value of the test
data.name	a character string giving the name of the data

**Note**

The printing method and plotting are in part adapted from R package MVN (Korkmaz, S. et al., 2015, version 4.0).

**Author(s)**

Rashid Makarov, Vassilly Voinov, Natalya Pya



## References

Henze, N. and Zirkler, B. (1990). A class of invariant consistent tests for multivariate normality. Communications in Statistics-Theory and Methods, 19, 3595-3617

## See Also

[S2.test](#), [DH.test](#), [AD.test](#), [CM.test](#), [R.test](#)

## Examples

```
## generating n bivariate normal random variables...
dat <- rmvnorm(n=200,mean=rep(0,2),sigma=matrix(c(4,2,2,4),2,2))
res <- HZ.test(dat)
res
## generating n bivariate t distributed with 10df random variables...
dat <- rmvt(n=200,sigma=matrix(c(4,2,2,4),2,2)*.8,df=10,delta=rep(0,2))
res1 <- HZ.test(dat)
res1

data(iris)
setosa = iris[1:50, 1:4] # Iris data only for setosa
res2 <- HZ.test(setosa, qqplot = TRUE)
res2
```

---

r-class

Class "r"

---

## Description

An S4 class for the Royston test for multivariate normality.

## Slots

**R:** stores the values of the test statistics

**p.value:** stores the p-value of the test

**data.name:** stores the name of the data

## Author(s)

Natalya Pya, Vassilly Voinov, Rashid Makarov

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`R.test`*Royston test for Multivariate Normality*

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**Description**

This function implements the Royston test for assessing multivariate normality.

**Usage**

```
R.test(data, qqplot = FALSE)
```

**Arguments**

<code>data</code>	A numeric matrix or data frame
<code>qqplot</code>	if TRUE creates a chi-square Q-Q plot

**Details**

Calculates the value of the Royston test and the approximate p-value.

**Value**

<code>R</code>	the value of the test statistic
<code>p.value</code>	the p-value of the test
<code>data.name</code>	a character string giving the name of the data

**Note**

The printing method and plotting are in part adapted from R package MVN (Korkmaz, S. et al., 2015, version 4.0).

**Author(s)**

Rashid Makarov, Vassilly Voinov, Natalya Pya

**References**

Royston, P. (1992). Approximating the Shapiro-Wilk W-test for non-normality. *Statistics and Computing*, 2, 117-119.

**See Also**

[S2.test](#), [DH.test](#), [AD.test](#), [CM.test](#), [HZ.test](#)

**Examples**

```

## generating n bivariate normal random variables...
dat <- rmvnorm(n=200,mean=rep(0,2),sigma=matrix(c(4,2,2,4),2,2))
res <- R.test(dat)
res
## generating n bivariate t distributed with 10df random variables...
dat <- rmvt(n=200,sigma=matrix(c(4,2,2,4),2,2)*.8,df=10,delta=rep(0,2))
res1 <- R.test(dat)
res1

data(iris)
setosa = iris[1:50, 1:4] # Iris data only for setosa
res2 <- R.test(setosa, qqplot = TRUE)
res2

```

---

S2-class

*Class "S2"*


---

**Description**

An S4 class for Chi-squared type tests for multivariate normality.

**Slots**

**s2:** stores the values of the McCulloch test statistics  
**y2:** stores the values of the Nikulin-Rao-Robson test statistics  
**u2:** stores the values of the Dzhaparidze-Nikulin test statistics  
**p.value.s2:** stores the p-value for S2 test  
**p.value.y2:** stores the p-value for Y2 test  
**p.value.u2:** stores the p-value for U2 test  
**data.name:** stores the data set name

**Author(s)**

Natalya Pya, Vassilly Voinov, Rashid Makarov

---

S2.test

*Chi-squared type tests for Multivariate Normality*


---

**Description**

This function implements three chi-squared type goodness-of-fit tests for multivariate normality, namely, the McCulloch S2 test, Nikulin-Rao-Robson Y2 and Dzhaparidze-Nikulin U2 tests.

**Usage**

```
S2.test(data, M=5, qqplot = FALSE)
```

**Arguments**

data	A numeric matrix or data frame
M	A number of equiprobable intervals
qqplot	if TRUE it creates a chi-square Q-Q plot

**Details**

Calculates the values of the three chi-squared type test statistics, the McCulloch S2, Nikulin-Rao-Robson Y2 and Dzhaparidze-Nikulin U2 tests, and the corresponding p-values. The construction of all three tests is based on the Wald's type chi-squared goodness-of-fit tests. The vector of unknown parameters is estimated by the maximum likelihood method. The Karhunen-Loeve transformation is applied to a multi-dimensional sample data in order to diagonalize a sample covariance matrix. The null asymptotic distributions of the S2, Y2 and U2 tests are chi-squared distributions with 1, M-1 and M-2 degrees of freedom correspondingly.

**Value**

s2	the value of the McCulloch test S2
p.value.s2	the p-value of S2 test
y2	the value of the Nikulin-Rao-Robson test Y2
p.value.y2	the p-value of Y2 test
u2	the value of the Dzhaparidze-Nikulin test U2
p.value.u2	the p-value of U2 test
data.name	a character string giving the name of the data

**Note**

The displayed result about multivariate normality is based on the McCulloch S2 test.

**Author(s)**

Vassilly Voinov, Natalya Pya, Rashid Makarov, Yevgeniy Voinov

## References

Voinov, V., Pya, N., Makarov, R., and Voinov, Y. (2015) New invariant and consistent chi-squared type goodness-of-fit tests for multivariate normality and a related comparative simulation study. Communications in Statistics - Theory and Methods. doi link: <http://www.tandfonline.com/doi/full/10.1080/03610926.2014.901370>

Voinov, V., Nikulin, M. and Balakrishnan, N., Chi-squared goodness of fit tests with applications. New York: Academic Press, Elsevier, 2013

## See Also

[AD.test](#), [DH.test](#), [R.test](#), [CM.test](#), [HZ.test](#)

## Examples

```
## generating n bivariate normal random variables...
dat <- rmvnorm(n=200,mean=rep(0,2),sigma=matrix(c(4,2,2,4),2,2))
res <- S2.test(dat, qqplot = FALSE)
res

## generating n bivariate t distributed with 10df random variables...
dat <- rmvt(n=200,sigma=matrix(c(4,2,2,4),2,2)*.8,df=10,delta=rep(0,2))
res1 <- S2.test(dat, qqplot = TRUE)
res1

data(iris)
setosa = iris[1:50, 1:4] # Iris data only for setosa
res2 <- S2.test(setosa, qqplot = TRUE)
res2
```

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