

# Package: momst (via r-universe)

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**Type** Package

**Title** Multi-Objective Minimum Spanning Tree via NSGA-II with Local Search

**Version** 0.1.1

**Description** Solves the Multi-Criteria Minimum Spanning Tree (mc-MST) problem on complete weighted graphs by combining the Non-dominated Sorting Genetic Algorithm II (NSGA-II) with optional Pareto local search operators. Chromosomes are represented as Prüfer sequences so that every random individual decodes to a valid spanning tree (Cayley's theorem), avoiding repair operators. Four solver variants are provided: pure NSGA-II (``base``), Path Relinking (``PR``), Pareto Local Search (``PLS``), and Tabu Search (``TS``). The package supports 2 and 3 objective formulations and provides convenience functions to plot Pareto fronts and best-compromise spanning trees. This package is the reference implementation of the method described in Parraga-Alava, Inostroza-Ponta and Dorn (2017) [doi:10.1109/CEC.2017.7969432](https://doi.org/10.1109/CEC.2017.7969432).

**License** GPL (>= 3)

**URL** <https://github.com/jorgeklz/momst>,  
<https://jorgeklz.github.io/momst/>

**BugReports** <https://github.com/jorgeklz/momst/issues>

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momst-package	<i>momst: Multi-Objective Minimum Spanning Tree via NSGA-II with Local Search</i>
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## Description

The **momst** package implements the Multi-Criteria Minimum Spanning Tree (mc-MST) algorithm using the NSGA-II (Non-dominated Sorting Genetic Algorithm II). Four variants are supported depending on the local search operator applied after each generation:

"base" Pure NSGA-II without local search.

"PR" NSGA-II plus Path Relinking.

"PLS" NSGA-II plus Pareto Local Search.

"TS" NSGA-II plus Tabu Search.

## Details

Chromosomes are encoded as Prufer sequences, taking advantage of Cayley's theorem (every sequence of length  $n-2$  with values in  $\{1, \dots, n\}$  decodes to a unique spanning tree of  $n$  nodes). This bijection makes every random chromosome a valid solution, avoiding repair operators.

The main entry point is `run_momst`.

## Reference

This package is the reference implementation of the method described in:

Parraga-Alava, J., Inostroza-Ponta, M., & Dorn, M. (2017). Using local search strategies to improve the performance of NSGA-II for the Multi-Criteria Minimum Spanning Tree problem. In *2017 IEEE Congress on Evolutionary Computation (CEC)* (pp. 1818-1825). IEEE. doi:10.1109/CEC.2017.7969432

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## See Also

Useful links:

- <https://github.com/jorgeklz/momst>
- <https://jorgeklz.github.io/momst/>
- Report bugs at <https://github.com/jorgeklz/momst/issues>

---

apply\_local\_search      *Apply the Configured Local-Search Variant*

---

## Description

Apply the Configured Local-Search Variant

## Usage

```
apply_local_search(  
  instance,  
  pareto_pop,  
  num_obj,  
  n,  
  variant,  
  pop_size,  
  lookup = NULL,  
  verbose = FALSE  
)
```

**Arguments**

instance	Edge-list data.frame.
pareto_pop	Integer matrix.
num_obj	Integer.
n	Integer.
variant	One of "base", "PR", "PLS", "TS".
pop_size	Integer.
lookup	Optional lookup.
verbose	Logical.

**Value**

data.frame.

---

build\_weight\_lookup    *Pre-build Edge-Weight Lookup Matrices*

---

**Description**

Constructs one  $n \times n$  matrix per objective so that the weight of any edge  $(i, j)$  can be queried in  $O(1)$  via standard matrix indexing.

**Usage**

```
build_weight_lookup(instance, n, num_obj)
```

**Arguments**

instance	data.frame returned by <a href="#">generate_instance</a> or one with columns from, to, weight_1, weight_2 (and optionally weight_3).
n	Integer. Number of nodes.
num_obj	Integer. Number of objectives (2 or 3).

**Value**

A list of length num\_obj; element k is the symmetric  $n \times n$  weight matrix of objective k.

**Examples**

```
inst <- generate_instance(10, 2, seed = 1)
L <- build_weight_lookup(inst, 10, 2)
L[[1]][1, 2]
```

---

compute\_objectives      *Compute Multi-Objective Costs for a Population*

---

**Description**

Compute Multi-Objective Costs for a Population

**Usage**

```
compute_objectives(instance, chromosomes, num_obj, lookup = NULL)
```

**Arguments**

instance	Edge-list data.frame (only used when lookup = NULL).
chromosomes	Numeric matrix [pop_size x (n - 2)].
num_obj	Integer.
lookup	Optional list returned by <a href="#">build_weight_lookup</a> .

**Value**

Numeric matrix [pop\_size x (n - 2 + num\_obj)].

**Examples**

```
inst <- generate_instance(10, 2, seed = 1)
lk <- build_weight_lookup(inst, 10, 2)
pop <- generate_prufer_population(10, 5)
compute_objectives(inst, pop, 2, lk)
```

---

decode\_prufer      *Decode a Prufer Sequence to its Spanning Tree (Linear Time)*

---

**Description**

Returns the edge list of the spanning tree encoded by a Prufer sequence of length  $n - 2$ . Uses Wang's pointer-based linear-time algorithm, replacing the classic  $O(n^2)$  "search smallest leaf each step" approach.

**Usage**

```
decode_prufer(seq_prufer, n)
```

**Arguments**

seq\_prufer Integer vector of length  $n - 2$  with values in  $\{1, \dots, n\}$ .  
 n Integer. Number of nodes of the underlying graph.

**Value**

Integer matrix of dimensions  $(n - 1) \times 2$ ; each row is an undirected edge (from, to).

**Examples**

```
decode_prufer(c(3, 1, 5), n = 5)
```

---

generate\_instance *Generate a Complete-Graph Instance for MO-MST*

---

**Description**

Produces a complete undirected weighted graph with random multi-objective edge weights. Each edge gets two or three independent uniform weights, one per objective.

**Usage**

```
generate_instance(  
  n,  
  num_obj,  
  range_a = c(10, 100),  
  range_b = c(10, 50),  
  range_c = c(30, 200),  
  seed = NULL  
)
```

**Arguments**

n Integer. Number of nodes of the graph (must be at least 3).  
 num\_obj Integer in  $\{2, 3\}$ . Number of objectives.  
 range\_a Numeric vector  $c(\min, \max)$  for weights of objective 1.  
 range\_b Numeric vector  $c(\min, \max)$  for weights of objective 2.  
 range\_c Numeric vector  $c(\min, \max)$  for weights of objective 3. Ignored when  $\text{num\_obj} == 2$ .  
 seed Optional integer. If supplied, the RNG seed is fixed before sampling and restored afterwards, leaving the global RNG untouched.

**Value**

A data.frame with  $n*(n-1)/2$  rows and columns from, to, weight\_1, weight\_2 (and weight\_3 when  $\text{num\_obj} == 3$ ).

**Examples**

```
inst <- generate_instance(n = 10, num_obj = 2, seed = 12345)
head(inst)
```

---

`generate_prufer_population`  
*Generate an Initial Prufer-Encoded Population*

---

**Description**

Generate an Initial Prufer-Encoded Population

**Usage**

```
generate_prufer_population(n, pop_size)
```

**Arguments**

`n` Integer. Number of nodes.  
`pop_size` Integer. Number of individuals to generate.

**Value**

Integer matrix of dimensions `pop_size` x  $(n - 2)$ .

**Examples**

```
generate_prufer_population(n = 6, pop_size = 4)
```

---

`non_dominated_crowding`  
*Assign Pareto Rank and Crowding Distance*

---

**Description**

Assign Pareto Rank and Crowding Distance

**Usage**

```
non_dominated_crowding(population, num_obj)
```

**Arguments**

population      Numeric matrix [N x (vars + num\_obj)].  
 num\_obj          Integer.

**Value**

Matrix with extra columns rankingIndex and density.

---

pareto\_local\_search      *Pareto Local Search*

---

**Description**

Pareto Local Search

**Usage**

```
pareto_local_search(  
  instance,  
  pareto_pop,  
  num_obj,  
  n,  
  neighbour_frac = 0.1,  
  pop_size,  
  lookup = NULL,  
  verbose = FALSE  
)
```

**Arguments**

instance          Edge-list data.frame.  
 pareto\_pop       Integer matrix [k x (n - 2)].  
 num\_obj          Integer.  
 n                Integer.  
 neighbour\_frac   Numeric.  
 pop\_size        Integer.  
 lookup           Optional lookup.  
 verbose          Logical.

**Value**

data.frame of chromosomes.

---

path_relinking	<i>Path Relinking on the Current Pareto Front</i>
----------------	---

---

**Description**

Path Relinking on the Current Pareto Front

**Usage**

```
path_relinking(  
  instance,  
  pareto_pop,  
  num_obj,  
  n,  
  pop_size,  
  lookup = NULL,  
  verbose = FALSE  
)
```

**Arguments**

instance	Edge-list data. frame.
pareto_pop	Integer matrix [k x (n - 2)].
num_obj	Integer.
n	Integer.
pop_size	Integer.
lookup	Optional lookup.
verbose	Logical.

**Value**

data.frame of non-dominated chromosomes.

---

plot_best_tree	<i>Plot the Best-Compromise Spanning Tree</i>
----------------	---

---

**Description**

Plot the Best-Compromise Spanning Tree

**Usage**

```
plot_best_tree(result, n)
```

**Arguments**

result            List returned by `run_momst`.  
n                 Integer.

**Value**

Invisible NULL.

---

plot\_pareto\_front     *Plot a Pareto Front (2-objective case)*

---

**Description**

Plot a Pareto Front (2-objective case)

**Usage**

```
plot_pareto_front(result, show_dominated = FALSE)
```

**Arguments**

result            List returned by `run_momst`.  
show\_dominated   Logical.

**Value**

Invisible NULL.

---

random\_mutation       *Random Mutation on Prufer Sequences*

---

**Description**

Random Mutation on Prufer Sequences

**Usage**

```
random_mutation(population, pop_size, mut_rate)
```

**Arguments**

population        Numeric matrix [`pop_size` x (`n` - 2)].  
pop\_size           Integer.  
mut\_rate           Numeric in  $[0, 1]$ .

**Value**

Integer matrix [`pop_size` x (`n` - 2)].

---

`run_momst`*Run the MO-MST NSGA-II Solver*

---

**Description**

Single entry point that replaces the original main.R script.

**Usage**

```
run_momst(  
  instance = NULL,  
  instance_file = NULL,  
  n = 10L,  
  num_obj = 2L,  
  variant = c("base", "PR", "PLS", "TS"),  
  iterations = 10L,  
  pop_size = 50L,  
  tour_size = 2L,  
  cross_rate = 0.8,  
  mut_rate = 0.05,  
  max_generations = 100L,  
  convergence_window = 10L,  
  range_a = c(10, 100),  
  range_b = c(10, 50),  
  range_c = c(30, 200),  
  save_dir = NULL,  
  verbose = TRUE,  
  seed = NULL  
)
```

**Arguments**

<code>instance</code>	Optional data.frame.
<code>instance_file</code>	Optional path.
<code>n</code>	Integer.
<code>num_obj</code>	Integer in {2, 3}.
<code>variant</code>	One of "base", "PR", "PLS", "TS".
<code>iterations</code>	Integer or two-length integer c(min_iter, max_iter).
<code>pop_size</code>	Integer (must be even).
<code>tour_size</code>	Integer.
<code>cross_rate</code>	Numeric in $\setminus[0, 1\setminus]$ .
<code>mut_rate</code>	Numeric in $\setminus[0, 1\setminus]$ .
<code>max_generations</code>	Integer.

convergence\_window  
                           Integer.  
 range\_a, range\_b, range\_c  
                           Weight ranges for instance generation.  
 save\_dir                  Optional directory for per-iteration result files.  
 verbose                  Logical.  
 seed                      Optional integer.

**Value**

Invisible list with the solution data.

**References**

Parraga-Alava, J., Inostroza-Ponta, M., & Dorn, M. (2017). Using local search strategies to improve the performance of NSGA-II for the Multi-Criteria Minimum Spanning Tree problem. In *2017 IEEE Congress on Evolutionary Computation (CEC)* (pp. 1818-1825). IEEE. doi:10.1109/CEC.2017.7969432

**Examples**

```
res <- run_momst(n = 10, num_obj = 2, iterations = 3,
               pop_size = 20, max_generations = 30,
               variant = "base", seed = 1)
head(res$global_pareto)
```

---

 tabu\_search

---

*Tabu Search on the Current Pareto Front*


---

**Description**

Tabu Search on the Current Pareto Front

**Usage**

```
tabu_search(
  instance,
  pareto_pop,
  num_obj,
  n,
  neighbour_frac = 0.05,
  pop_size,
  lookup = NULL,
  verbose = FALSE
)
```

**Arguments**

instance	Edge-list data.frame.
pareto_pop	Integer matrix [k x (n - 2)].
num_obj	Integer.
n	Integer.
neighbour_frac	Numeric.
pop_size	Integer.
lookup	Optional lookup.
verbose	Logical.

**Value**

data.frame of non-dominated chromosomes.

---

tournament\_selection *Tournament Selection*

---

**Description**

Tournament Selection

**Usage**

```
tournament_selection(population, pop_size, tour_size)
```

**Arguments**

population	Matrix with last two columns being rankingIndex and density.
pop_size	Integer.
tour_size	Integer.

**Value**

Selected subpopulation matrix.

---

uniform\_crossover      *Uniform Crossover for Prufer Sequences*

---

**Description**

Uniform Crossover for Prufer Sequences

**Usage**

```
uniform_crossover(pool, pop_size, cross_rate)
```

**Arguments**

pool	Numeric matrix [ $\text{pop\_size} \times (n - 2)$ ].
pop_size	Integer (must be even).
cross_rate	Numeric in $\setminus[0, 1\setminus]$ .

**Value**

Integer matrix [ $\text{pop\_size} \times (n - 2)$ ].

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