Package: lakhesis (via r-universe)

October 26, 2026

Title Consensus Seriation for Binary Data

Version 1.1.2

Description Determining consensus seriations for binary incidence matrices, using a two-step process of Procrustes-fit correspondence analysis for heuristic selection of partial seriations and iterative regression to establish a single consensus. Contains the Lakhesis Calculator, a graphical platform for identifying seriated sequences. Collins-Elliott (2026) ``Lakhesis: Consensus Seriation via Iterative Regression of Partial Rankings for Binary Data" <doi:10.1080/02664763.2026.2672564>.

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Imports stats, Rcpp, RcppArmadillo, readr, ca, ggplot2, Rdpack, shiny, shinydashboard, bslib

RdMacros Rdpack

Encoding UTF-8

RoxygenNote 7.3.2

LinkingTo Rcpp, RcppArmadillo

Depends R (>= 3.5.0)

LazyData true

Suggests knitr, rmarkdown

VignetteBuilder knitr

NeedsCompilation yes

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Repository https://cran.r-universe.dev

Date/Publication 2026-05-28 19:47:03 UTC

RemoteUrl https://github.com/cran/lakhesis

RemoteRef HEAD

RemoteSha 6a3efef4c5f5d2d20bec579e4058be2f8c3cce39

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`ca_procrustes` *Correspondence Analysis with Procrustes Fitting*

Description

Fit scores of correspondence analysi on an incidence matrix to those produced by reference matrix which contain an ideal seriation using a Procrustes method (on the reference matrix, see `im_ref`). Rotation is determined by minimizing Euclidean distance from each row score to the nearest reference row score. Correspondence analysis is performed using the `ca` package (Nenadic and Greenacre 2007).

Usage

```
ca_procrustes(obj, symmetric = TRUE)

## S3 method for class 'matrix'
ca_procrustes(obj, symmetric = TRUE)

## S3 method for class 'incidence_matrix'
ca_procrustes(obj, symmetric = TRUE)
```

Arguments

obj	An incidence matrix of size n x k.
symmetric	Whether to use standard scores for both rows and columns. Default is TRUE. Setting this to FALSE will result in a asymmetric map of standard scores for rows and principal scores for columns.

Value

A list object of class strand containing the following:

- ref The Procrustes-fit coordinates of the scores of the reference seriation.
- x The coordinates of the row standard scores of the data.
- y The coordinates of the column principal scores of the data.
- x_pr The Procrustes-fit coordinates of the row standard scores of the data.
- y_pr The Procrustes-fit coordinates of the column column scores of the data.

References

Nenadic O, Greenacre MJ (2007). "Correspondence Analysis in R, with Two- and Three-dimensional Graphics: The ca Package." *Journal of Statistical Software*, **20**, 1–13. doi:10.18637/jss.v020.i03.

Examples

```
data("quattrofontanili")
s <- ca_procrustes(quattrofontanili)
# print(s)
```

---

ca_procrustes_ser *Seriate Procrustes-Fit CA Scores*

Description

Obtain a ranking of row and column scores projected onto a reference curve of an ideal seriation (row and column scores are ranked separately). Scores of correspondence analysis have been fit to those produced by reference matrix contain an ideal seriation using a Procrustes method, projecting them. Rotation is determined by minimizing Euclidean distance from each row score to the nearest reference row score. Correspondence analysis is performed using the ca package (Nenadic and Greenacre 2007).

Usage

```
ca_procrustes_ser(obj, projection = "curve", samples = 10^5, symmetric = TRUE)

## S3 method for class 'incidence_matrix'
ca_procrustes_ser(obj, projection = "curve", samples = 10^5, symmetric = TRUE)

## S3 method for class 'matrix'
ca_procrustes_ser(obj, projection = "curve", samples = 10^5, symmetric = TRUE)
```

Arguments

`obj`	An incidence matrix of size n x k.
`projection`	Which projection to use: • `ca1` The first axis for CA scores. • `ca2` The second axis for CA scores. • `procrustes1` The first axis of Procrustes-fit CA scores. • `procrustes2` The second axis of Procrustes-fit CA scores. • `curve` The reference curve of an ideal seriation, using Procrustes fitting (this is the default).
`samples`	Number of samples to use for plotting points along polynomial curve. Default is `10^5`.
`symmetric`	Whether to use standard scores for both rows and columns. Default is `TRUE`. Setting this to `FALSE` will result in a asymmetric map of standard scores for rows and principal scores for columns.

Value

A `list` of class `strand` containing the following:.

- `$dat` A data frame with the following columns:
  - `Procrustes1, Procrustes2` The location of the point on the biplot after fitting.
  - `CurveIndex` The orthogonal projection of the point onto the reference curve, given as the index of the point sampled along $y = \beta_2 x^2 + \beta_0$.
  - `Distance` The squared Euclidean distance of the point to the nearest point on the reference curve.
  - `Rank` The ranking of the row or column, a range of `1:nrow`` and 1:ncol“.
  - `Type` Either `row` or `col`.
  - `sel` Data frame column used in `shiny` app to indicate whether point is selected in biplot/curve projection.
- `$im_seriated` The seriated incidence matrix, of class `incidence_matrix`.

References

Nenadic O, Greenacre MJ (2007). “Correspondence Analysis in R, with Two- and Three-dimensional Graphics: The ca Package.” *Journal of Statistical Software*, **20**, 1–13. doi:10.18637/jss.v020.i03.

Examples

```
data("quattrofontanili")
s <- ca_procrustes_ser(quattrofontanili)
# print(s)
# summary(s)
```

conc_c *Optimality Criterion: Kendall-Doran (Column) Concentration*

Description

The Kendall-Doran measure of concentration (Kendall 1963; Doran 1971). In a seriated matrix, this function computes the total number cells between the first and last non-zero value, column by column.

Usage

```
conc_c(obj)

## S3 method for class 'matrix'
conc_c(obj)

## S3 method for class 'incidence_matrix'
conc_c(obj)
```

Arguments

obj	A seriated binary matrix.

Value

The measure of concentration.

References

Doran J (1971). "Computer Analysis of Data from the la Tène Cemetry at Münsingen-Rain." In Hodson FR, Kendall DG, Táutu P (eds.), *Mathematics in the Archaeological and Historical Sciences*, 422–431. Edinburgh University Press, Edinburgh.

Kendall DG (1963). "A Statistical Approach to Flinders Petrie's Sequence Dating." *Bulletin of the International Statistical Institute*, **40**, 657–680.

Examples

```
data("quattrofontanili")
conc_c(quattrofontanili)
```

conc_wrc *Optimality Criterion: Weighted Row-Column Concentration*

Description

Extends the Kendall-Doran (column) measure of concentration (see conc_c) to include rows and then weights the total measure by the total sum of values in the matrix.

Usage

```
conc_wrc(obj)

## S3 method for class 'matrix'
conc_wrc(obj)

## S3 method for class 'incidence_matrix'
conc_wrc(obj)
```

Arguments

obj	A seriated binary matrix.

Value

The weighted row-column coefficient of concentration.

Examples

```
data("quattrofontanili")
conc_wrc(quattrofontanili)
```

cor_sq *Optimality Criterion: Squared Correlation*

Description

Treating each incidence of 1 in an element (i, j) of a seriated matrix as an (x, y) point, computes the squared correlation coefficient (see McCormick Jr. et al. 1969, 147-148).

Usage

```
cor_sq(obj)

## S3 method for class 'matrix'
cor_sq(obj)

## S3 method for class 'incidence_matrix'
cor_sq(obj)
```

Arguments

obj	A seriated binary matrix.

Value

Spearman's rank correlation coefficient.

References

McCormick Jr. WT, Deutsch SB, J.J. M, Schweitzer PJ (1969). "Identification of Data Structures and Relationships by Matrix Reordering Techniques." Research Paper P-512, Institute for Defense Analyses.

Examples

```
data("quattrofontanili")
cor_sq(quattrofontanili)
```

---

element_eval *Evaluating Element Fit*

Description

Performs a goodness-of-fit test on individual row and column elements using deviance, using a quadratic-logistic model to fit row and column occurrences. In the case of perfect separation of 0/1 values, an NA value is assigned. Results are reported as p values for each row and column.

Usage

```
element_eval(obj)

## S3 method for class 'matrix'
element_eval(obj)

## S3 method for class 'incidence_matrix'
element_eval(obj)
```

Arguments

obj	A seriated binary matrix.

Value

A list containing results in data frames for row and column elements:

- RowFit a data frame containing
  - id Row element
  - p.val p values of the row elements
- ColFit a data frame containing
  - id Column element
  - p.val p values of the column elements

Examples

```
data("quattrofontanili")
element_eval(quattrofontanili)
```

---

im_long *Convert Incidence Matrix to Pairs (Long Format)*

Description

Take an incidence matrix and convert it to a data frame of two columns, where the first column represents the row elements of the incidence matrix and the second column represents the column elements of the incidence matrix. Each row pair represents the incidence (or occurrence) of that row and column element together.

Usage

```
im_long(obj)

## S3 method for class 'matrix'
im_long(obj)

## S3 method for class 'incidence_matrix'
im_long(obj)
```

Arguments

obj	An incidence matrix.

Value

A data frame of two columns (row and column of the incidence matrix), in which row of the data frame represents a pair of an

Examples

```
data(quattrofontanili)
qf <- im_long(quattrofontanili)

# to export for uploading into the Lakhesis Calculator, use write.table() to
# remove both row and column names:

# write.table(qf, file = 'qf.csv', row.names = FALSE, col.names = FALSE, sep = ",")
```

`im_merge` *Merge Two Incidence Matrices*

Description

From two incidience matrices, create a single incidence matrix. Matrices may contain same row or column elements.

Usage

```
im_merge(obj1, obj2)

## S3 method for class 'matrix'
im_merge(obj1, obj2)

## S3 method for class 'incidence_matrix'
im_merge(obj1, obj2)
```

Arguments

`obj1`, `obj2`	Two incidence matrices of any size.

Value

A single incidence matrix.

Examples

```
data(quattrofontanili)
qf1 <- quattrofontanili[1:20, 1:40]
qf1 <- qf1[rowSums(qf1) != 0, colSums(qf1) != 0]

qf2 <- quattrofontanili[30:50, 20:60]
qf2 <- qf2[rowSums(qf2) != 0, colSums(qf2) != 0]

im_merge(qf1, qf2)
```

`im_read_csv` *Read csv File to Incidence Matrix*

Description

Wrapper around the `read_csv` function from the `readr` package (Wickham et al. 2024). Read a `.csv` file in which the first column represents row elements and the second column represents column elements, and convert it into an incidence matrix.

Usage

```
im_read_csv(
  filename,
  header = FALSE,
  characterencoding = "iso-8859-1",
  remove.hapax = FALSE
)
```

Arguments

`filename`	The filename to uploaded (must be in `.csv` format).
`header`	If the `.csv` file contains a header. Default is `FALSE`.
`characterencoding`	File encoding as used by `locale`, which depends on the `csv` file. Default is `"iso-8859-1"` but `"utf-8"` is also recommended.
`remove.hapax`	Remove any row or column which has a sum of 1 (i.e., is only attested once), since they do not directly contribute to the result of the seriation. Default is `FALSE`.

Value

A matrix of binary values (0 = row/column occurrence is absence; 1 = row/column occurrence is present).

References

Wickham H, Hester J, Bryan J (2024). *readr: Read Rectangular Text Data*. R package version 2.1.5, https://github.com/tidyverse/readr, https://readr.tidyverse.org.

im_ref *Create Reference Matrix*

Description

Create an ideal reference matrix of well-seriated values of the same size as the input matrix.

Usage

```
im_ref(obj)

## S3 method for class 'matrix'
im_ref(obj)
```

Arguments

obj	A matrix of size $n \times k$.

Value

A matrix of size $n \times k$ with 1s along the diagonal. If $n > k$, 1s are placed from cell (i, i) to $(i, i + k - n)$, with 0 in all other cells.

Examples

```
im_ref(matrix(NA, 5, 5))
im_ref(matrix(1, 7, 12))
```

lakhesize *Lakhesize*

Description

This function returns the row and column consensus seriation for a `list` object of the `strands` class, containing their rankings, coefficients of association, and criterion. Consensus seriation is achieved by iterative simple linear regression to handle `NA` vales in each strand. To initialize, a regression is performed pairwise, with every strand as the dependent y variate and every other strand as the independent x variate. The independent variate's rankings are then regressed onto $f(x) = \hat{\beta}_1 x + \hat{\beta}_0$. If $y \neq f(x)$, the mean of y and $f(x)$ is used. Then, the values of the dependent variate and those of the regressed independent varaite are re-ranked together, to form a combined ranking, which serves as the dependent variate on the next iteration. The pair of strands is chosen which minimizes a specified optimality criterion. The process is repeated until all strands have been regressed and re-ranked into a single consensus seriation.

Usage

```
lakhesize(strands, crit = "cor_sq", pbar = TRUE)

## S3 method for class 'strands'
lakhesize(strands, crit = "cor_sq", pbar = TRUE)

## Default S3 method:
lakhesize(strands, crit = "cor_sq", pbar = TRUE)
```

Arguments

strands	A list of strands class (see strand_add).
crit	The criterion used to assess the seration resulting from two strands x and y:

- "cor_sq" Computes a squared correlation coefficent for the incidences of 1s as points (i, j). See cor_sq. Higher values are more optimal. This is the default option.
- "conc_wrc" Computes weighted row-column concentration as the optimality criterion. See conc_wrc. Lower values are more optimal.

pbar	Displaying a progress bar. Default is TRUE.

Value

A list of class lakhesis containing the following:

- row A seriated vector of row elements.
- col A seriated vector of column elements
- coef A data frame containing the following columns:
  - Strand The number of the strand.
  - Agreement The measure of agreement, i.e., how well each strand accords with the consensus seriation. Using the square of Spearman's rank correlation coefficient, ρ^2, between each strand and the consensus ranking, agreement is computed as the product of ρ^2 for their row and column rankings, $\rho_r^2 \rho_c^2$.
  - Criterion Criterion of the optimality of each strand (per the "crit" option above).
- im_seriated The seriated incidence matrix, of class incidence_matrix.

Examples

```
data("qf_strands")
L <- lakhesize(qf_strands, pbar = FALSE)
# summary(L)
```

LC *Lakhesis Calculator*

Description

Launch Lakhesis Calculator, a graphical interface to explore binary matrices via correspondence analysis, select potentially well-seriated sequences, and perform consensus seriation. Interface is made with `ggplot2`, `shiny`, `shinydashboard`, and `bslib` (Wickham 2016; Chang et al. 2024; Chang and Borges Ribeiro 2021; Sievert et al. 2024).

Usage

```
LC()
```

Details

Input is done in the calculator, via a "long" format a two-column `.csv` file giving pairs of row and column incidences. See `im_read_csv` for details. Conversion of a pre-existing incidence matrix to long format can be performed with `im_long`.

Results can be downloaded from the calculator as an `.rds` file containing a `list` of the following:

- `consensus` The consensus seriations, diagnostic coefficients of agreement and optimality criterion, and seriated incidence matrix. (`lakhesize`).
- `strands` The strands selected by the investigator.

Value

Opens the Lakhesis Calculator.

References

Chang W, Borges Ribeiro B (2021). *shinydashboard: Create Dashboards with 'Shiny'*. https://CRAN.R-project.org/package=shinydashboard.

Chang W, Cheng J, Allaire JJ, Sievert C, Schloerke B, Xie Y, Allen J, McPherson J, Dipert A, Borges B (2024). *shiny: Web Application Framework for R*. R package version 1.8.1.9001; https://github.com/rstudio/shiny, https://shiny.posit.co.

Sievert C, Cheng J, Aden-Buie G (2024). *bslib: Custom 'Bootstrap' 'Sass' Themes for 'shiny' and 'rmarkdown'*. R package version 0.7.0, https://github.com/rstudio/bslib, https://rstudio.github.io/bslib/.

Wickham H (2016). *ggplot2: Elegant Graphics for Data Analysis*. Springer, New York.

qf_strands *Quattro Fontanili - Strands*

Description

Three seriated strands selected from quattrofontanili data, identified by the package author as an example for the documentation of functions.

Usage

```
data("qf_strands")
```

Format

A strands object containing strands output by ca_procrustes.

Examples

```
data("qf_strands")
print(qf_strands)
```

quattrofontanili *Quattro Fontanili*

Description

The seriation of tombs from necropoleis at Veii, primarily Quattro Fontanili, but also Valle la Fata, Vaccareccia, and Picazzano, in southern Etruria, established by Close-Brooks and Ridgway (1979).

Usage

```
data("quattrofontanili")
```

Format

A seriated incidence matrix of 81 rows (tombs) and 82 columns (types).

Data entered from Close-Brooks and Ridgway (1979), an English translation of the authors' original publication in *Notizie degli Scavi* (1963). Descriptions of types may be found in that paper.

References

Close-Brooks J, Ridgway D (1979). "Veii in the Iron Age." In Ridgway D, Ridgway FR (eds.), *Italy Before the Romans*, 95–127. Academic Press, London.

Examples

```
data("quattrofontanili")
print(quattrofontanili)
```

`spearman_sq` *Spearman Correlation Squared*

Description

The square of Spearman's rank correlation coefficient applied to two rankings (Spearman 1904). Rows with `NA` values are automatically removed.

Usage

```
spearman_sq(r1, r2)

## S3 method for class 'numeric'
spearman_sq(r1, r2)
```

Arguments

`r1`, `r2`	Two vectors of paired ranks.

Value

The square of Spearman's rank correlation coefficient with NA values removed.

References

Spearman C (1904). "The Proof and Measurement of Association between Two Things." *American Journal of Psychology*, **15**, 72–101. doi:10.2307/1412159.

Examples

```
# e.g., for two partial seriations:
x <- c(1, 2, 3, 4, NA, 5, 6, NA, 7.5, 7.5, 9)
y <- c(23, 17, 19, NA, 21, 22, 25, 26, 27, 36, 32)
spearman_sq(x, y)
```

strand_add *Add Strand to List of Strands*

Description

Given a list of strands, remove a row or column element and re-run seriation by correspondence analysis with Procrustes fitting (ca_procrustes_ser) to generate a new list of strands that exclude the specified elements. If the resulting strand lacks sufficient points to perform correspondence analysis, that strand is deleted in the output.

Usage

```
strand_add(strand, strands)

## S3 method for class 'strand'
strand_add(strand, strands)
```

Arguments

strand	An object of class strand returned by ca_procrustes_ser.
strands	A list of strands.

Value

A list of class strands.

strand_create *Create Strand Object from Seriated Incidence Matrix*

Description

Given a seriated incidence matrix with unique row and column names, create a strand object.

Usage

```
strand_create(obj, method = NULL)

## S3 method for class 'matrix'
strand_create(obj, method = NULL)

## S3 method for class 'incidence_matrix'
strand_create(obj, method = NULL)
```

Arguments

obj	A list of strands.
method	The method used to create the strand (optional).

Value

A list of class strands.

---

strand_extract *Strand Extract*

Description

From a list of strands produced by ca_procrustes_ser, extract two matrices containing the ranks of the rows and columns. The row/column elements are contained in the rows, and the strands are contained in the columns. NA values are entered where a given row/column element is missing from that strand.

Usage

```
strand_extract(strands)
```

Arguments

strands	A list of class strands.

Value

A list of two matrices:

- Row A matrix of the ranks of the row elements.
- Col A matrix of the ranks of the column elements.

Examples

```
data("quattrofontanili")
data("qf_strands")
strand_extract(qf_strands)
```

strand_suppress *Suppress Element from Strands*

Description

Given a `list` of `strands` produced by correspondence analysis with Procrustes fitting (`ca_procrustes_ser`), remove one or more row or column elements, re-seriating each strand. This generates a new list of strands that exclude the specified elements. If a resulting strand lacks sufficient points to perform correspondence analysis, that strand is deleted in the output.

Usage

```
strand_suppress(strands, elements)

## S3 method for class 'strands'
strand_suppress(strands, elements)

## Default S3 method:
strand_suppress(strands, elements)
```

Arguments

`strands`	A `list` of class `strands`.
`elements`	A vector of one or more row or column ids to suppress.

Value

A list of the strands.

Examples

```
data("qf_strands")
strand_suppress(qf_strands, "QF II 15-16")

strand_suppress(qf_strands, c("QF II 15-16", "I", "XIV"))
```

strands_create *Create List of Strands*

Description

Given one or more individual strand objects, create a single `list` of class `strands`.

Usage

```
strands_create(strands)

## S3 method for class 'list'
strands_create(strands)
```

Arguments

strands	A list of strands.

Value

A list of class strands.

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