Package: hyperbolicDEA (via r-universe)

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Title Hyperbolic DEA Estimation
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Description Implements Data Envelopment Analysis (DEA) with a hyperbolic orientation using a non-linear programming solver. It enables flexible estimations with weight restrictions, non-discretionary variables, and a generalized distance function. Additionally, it allows for the calculation of slacks and super-efficiency scores. The methods are detailed in Öttl et al. (2023), <doi:10.1016 j.dajour.2023.100343="">. Furthermore, the package provides a non-linear profitability estimation built upon the DEA framework.</doi:10.1016>
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Contents
costDEA

2 costDEA

	nlprofitDEA	 			 												6
	wrDEA	 			 												8
Index																	10

costDEA

Cost DEA model

Description

Cost DEA model optimizing the input allocation with given prices. It returns the estimated lambdas as well as the optimal values for inputs and a cost efficiency score that is the ratio of optimal costs over observed costs.

Usage

```
costDEA(X, Y, pX, RTS = "crs")
```

Arguments

Χ	Vector, matrix or dataframe with DMUs as rows and inputs as columns
Υ	Vector, matrix or dataframe with DMUs as rows and outputs as columns
pX	Vector, matrix or dataframe with prices for each DMU and input. Therefore it must have the same dimensions as \boldsymbol{X} .
RTS	Character string indicating the returns-to-scale, e.g. "crs", "vrs".

Value

A list object containing the following:

lambdas Estimated values for the composition of the respective Benchmarks. The lamb-

das are stored in a matrix with dimensions nrow(X) x nrow(X), where the row is the DMU under observation and the columns are the peers used for the Bench-

mark.

opt_value Optimal inputs.

cost_eff Cost efficiency as the ratio of the optimal cost to the observed cost.

Author(s)

Alexander Öttl

See Also

[Benchmarking::cost.opt] for a similar function

hyperbolicDEA 3

Examples

```
X <- matrix(c(1,2,3,3,2,1,2,2), ncol = 2)
Y <- matrix(c(1,1,1,1), ncol = 1)

pX <- matrix(c(2,1,2,1,2,1,1,2), ncol = 2, byrow = TRUE)

cost_eff_input <- costDEA(X,Y,pX)</pre>
```

hyperbolicDEA

Hyperbolic estimation of DEA efficiency scores

Description

Hyperbolic DEA implementation including weight restrictions, non-discretionary variables, gerenralized distance function, external referencing, estimation of slacks and super-efficiency scores. The mathematical and theoretical foundations of the code are presented in the paper "Data Envelopment Analysis and Hyperbolic Efficiency Measures: Extending Applications and Possibilities for Between-Group Comparisons" (2023) by Alexander Öttl, Mette Asmild, and Daniel Gulde.

Usage

```
hyperbolicDEA(
    X,
    Y,
    RTS = "vrs",
    WR = NULL,
    SLACK = FALSE,
    ACCURACY = 1e-10,
    XREF = NULL,
    YREF = NULL,
    SUPEREFF = FALSE,
    NONDISC_IN = NULL,
    NONDISC_OUT = NULL,
    PARALLEL = 1,
    ALPHA = 0.5
)
```

Arguments

Vector, matrix or dataframe with DMUs as rows and inputs as columns
 Vecotr, matrix or dataframe with DMUs as rows and outputs as columns
 Character string indicating the returns-to-scale, e.g. "crs", "vrs", "ndrs", "nirs", "fdh"

4 hyperbolicDEA

WR Matrix with one row per homogeneous linear weight restriction in standard

form. The columns are ncol(WR) = ncol(Y) + ncol(X). Hence the first ncol(Y) columns are the restrictions on outputs and the last ncol(X) columns are the

restrictions on inputs.

SLACK Boolean variable indicating whether an additional estimation of slacks shall be

performed when set to 'TRUE'. Be aware that SLACK estimation can change

the lambda values.

ACCURACY Accuracy value for non-linear programm solver.

XREF Vector, matrix or dataframe with firms defining the technology as rows and in-

puts as columns

YREF Vector, matrix or dataframe with firms defining the technology as rows and out-

puts as columns

SUPEREFF Boolean variable indicating whether super-efficiencies shall be estimated

NONDISC_IN Vector containing column indices of the input matrix that are non-discretionary

variables e.g. c(1,3) so the first and the third input are non-discretionary

NONDISC_OUT Vector containing column indices of the output matrix that are non-discretionary

variables e.g. c(1,3) so the first and the third output are non-discretionary

PARALLEL Integer of amount of cores that should be used for parallel computing (Check

availability of computer)

ALPHA can be chosen between [0,1]. It indicates the relative weights given to

the distance function to both outputs and inputs when approaching the frontier. More weight on the input orientation is set by alpha < 0.5. Here, the input efficiency score is estimated in the package. To receive the corresponding output efficiency score, estimate: $e^{(1-alpha)/alpha)}$. Vice versa for an output weighted model alpha > 0.5. The output efficiency is given and the input efficiency can be

recovered with: e^(alpha/(1-alpha))

Value

A list object containing the following information:

eff Are the estimated efficiency scores for the DMUs under observation stored in a

vector with the length nrow(X).

lambdas Estimated values for the composition of the respective Benchmarks. The lamb-

das are stored in a matrix with the dimensions nrow(X) x nrow(X), where the row is the DMU under observation and the columns the peers used for the

Benchmark.

mus If WR!= NULL, the estimated decision variables for the imposed weight restric-

tions are stored in a matrix with the dimensions nrow(X) x nrow(WR), where the rows are the DMUs and columns the weight restrictions. If the values are

positive, the WR is binding for the respective DMU.

slack If SLACK = TRUE, the slacks are estimated and stored in a matrix with the

dimensions $nrow(X) \times (ncol(X) + ncol(Y))$. Showing the Slack of each DMU

(row) for each input and output (column).

lprofitDEA 5

Author(s)

Alexander Öttl Daniel Gulde

Examples

```
X <- c(1,1,2,4,1.5,2,4,3)
Y <- c(1,2,4,4,0.5,2.5,3.5,4)
# we now impose linked weght restrictions. We assume outputs decrease by
# four units when inputs are reduced by one. And we assume that outputs can
# can be increased by one when inputs are increased by four

WR <- matrix(c(-4,-1,1,4), nrow = 2, byrow = TRUE)
hyperbolicDEA(X,Y,RTS="vrs", WR = WR)

# Another example having the same data but just estimate the results for DMU 1
# using XREF YREF and and a higher focus on inputs adjusting the ALPHA towards 0.
# Additionally, slacks are estimated.

hyperbolicDEA(X[1],Y[1],RTS="vrs", XREF = X, YREF = Y, WR = WR, ALPHA = 0.1, SLACK = TRUE)</pre>
```

lprofitDEA

Linear profit DEA model

Description

Linear profit DEA model optimizing the difference of cost to revenue. It returns the estimated lambdas as well as the optimal values for inputs and outputs. The linear profit estimation does not account for scale differences and also has issues with negative profits. Therefore, it is recommended to use the non-linear profit model.

Usage

```
lprofitDEA(X, Y, pX, pY, RTS = "crs")
```

Arguments

X	Vector, matrix or dataframe with DMUs as rows and inputs as columns
Υ	Vector, matrix or dataframe with DMUs as rows and outputs as columns
pX	Vector, matrix or dataframe with prices for each DMU and input. Therefore it must have the same dimensions as \mathbf{X} .
pΥ	Vector, matrix or dataframe with prices for each DMU and output. Therefore it must have the same dimensions as Y.
RTS	Character string indicating the returns-to-scale, e.g. "crs", "vrs".

6 nlprofitDEA

Value

A list object containing the following:

lambdas Estimated values for the composition of the respective Benchmarks. The lamb-

das are stored in a matrix with dimensions nrow(X) x nrow(X), where the row is the DMU under observation and the columns are the peers used for the Bench-

mark.

opt_value Optimal inputs and outputs.

profit_eff Profit efficiency as the ratio of the differences between the observed and optimal

difference of cost to revenue.

Author(s)

Alexander Öttl

See Also

[Benchmarking::profit.opt] for a similar function

Examples

```
X <- matrix(c(1,2,3,3,2,1,2,2), ncol = 2)
Y <- matrix(c(1,1,1,1), ncol = 1)

pX <- matrix(c(2,1,2,1,2,1,1,2), ncol = 2, byrow = TRUE)
pY <- matrix(c(1,1,1,1), ncol = 1)

max_prof_lin<- lprofitDEA(X,Y,pX,pY)</pre>
```

nlprofitDEA

Non-linear profit DEA model

Description

This function implements a non-linear profit DEA model that optimizes the ratio of cost over revenue given the prices for a DMU. It returns the estimated lambdas, optimal values for inputs and outputs, and a profit efficiency score. The profit efficiency score is calculated as the square root of the ratio of the observed revenue-cost ratio to the optimal revenue-cost ratio.

Usage

```
nlprofitDEA(X, Y, pX, pY, RTS = "crs")
```

nlprofitDEA 7

Arguments

X	Vector, matrix or dataframe with DMUs as rows and inputs as columns.
Υ	Vector, matrix or dataframe with DMUs as rows and outputs as columns.
pX	Vector, matrix or dataframe with prices for each DMU and input. It must have the same dimensions as \boldsymbol{X} .
pΥ	Vector, matrix or dataframe with prices for each DMU and output. It must have the same dimensions as Y.
RTS	Character string indicating the returns-to-scale, e.g. "crs", "vrs".

Value

A list object containing the following:

lambdas	Estimated values for the composition of the respective Benchmarks. The lambdas are stored in a matrix with dimensions $\operatorname{nrow}(X) \times \operatorname{nrow}(X)$, where the row is the DMU under observation and the columns are the peers used for the Benchmark.
opt_value	Optimal inputs and outputs.
profit_eff	New profit efficiency score that accounts for simultaneous adjustments in inputs and outputs.

Author(s)

Alexander Öttl

See Also

'deaprofitability()' function in the Julia package BenchmarkingEconomicEfficiency.jl.

Examples

```
X <- matrix(c(1,2,3,3,2,1,2,2), ncol = 2)
Y <- matrix(c(1,1,1), ncol = 1)

pX <- matrix(c(2,1,2,1,2,1,1,2), ncol = 2, byrow = TRUE)
pY <- matrix(c(1,1,1,1), ncol = 1)

max_prof_nolin <- nlprofitDEA(X,Y,pX,pY)</pre>
```

8 wrDEA

wrDEA Estimation of DEA efficiency scores with linear input or output orientation and trade-off weight restrictions

Description

Linear DEA estimation including the possibility of trade-off weight restrictions, external referencing, and super-efficiency scores. Furthermore, in a second stage slacks can be estimated. The function returns efficiency scores and adjusted lambdas according to the imposed weight restrictions and slack estimation. Additionally, mus are returned if weight restrictions are imposed that highlight binding restrictions for DMUs and the absolute slack values if slack-based estimation is applied.

Usage

```
wrDEA(
   X,
   Y,
   ORIENTATION = "out",
   RTS = "vrs",
   WR = NULL,
   XREF = NULL,
   YREF = NULL,
   SUPEREFF = FALSE,
   SLACK = FALSE,
   ECONOMIC = FALSE
)
```

Arguments x

^	vector, matrix or dataframe with Divios as lows and inputs as columns
Υ	Vector, matrix or dataframe with DMUs as rows and outputs as columns
ORIENTATION	Character string indicating the orientation of the DEA model, e.g. "in", "out"
RTS	Character string indicating the returns-to-scale, e.g. "crs", "vrs", "ndrs", "nirs", "fdh"
WR	Matrix with one row per homogeneous linear weight restriction in standard form. The columns are $ncol(WR) = ncol(Y) + ncol(X)$. Hence the first $ncol(Y)$ columns are the restrictions on outputs and the last $ncol(X)$ columns are the restrictions on inputs.
XREF	Vector, matrix or dataframe with firms defining the technology as rows and inputs as columns
YREF	Vector, matrix or dataframe with firms defining the technology as rows and outputs as columns
SUPEREFF	Boolean variable indicating whether super-efficiencies shall be estimated
SLACK	Boolean variable indicating whether slack-based estimation should be applied

Vector matrix or dataframe with DMUs as rows and inputs as columns

wrDEA 9

ECONOMIC

Boolean variable indicating whether economic efficiency (cost or revenue) is estimated using trade-off weight restrictions. Therefore mus can be positive and negative when set to TRUE and you have a multi-stage optimization where the first stage is the efficiency estimation and the second stage is the minimization of the mus. You have to use single trade-off, hence a 1 to 1 substitution of either inputs or outputs given by the focus on either cost or revenue efficiency. The data must be value data.

Value

A list object containing the following information:

eff Are the estimated efficiency scores for the DMUs under observation stored in a

vector with the length nrow(X).

lambdas Estimated values for the composition of the respective Benchmarks. The lamb-

das are stored in a matrix with the dimensions nrow(X) x nrow(X), where the row is the DMU under observation and the columns the peers used for the

Benchmark. NOTE: Lambdas are automatically slack optimized.

mus If WR!= NULL, the estimated decision variables for the imposed weight restric-

tions are stored in a matrix with the dimensions nrow(X) x nrow(WR), where the rows are the DMUs and columns the weight restrictions. If the values are

positive, the WR is binding for the respective DMU.

slack If SLACK = TRUE, the slacks are estimated and stored in a matrix with the

dimensions $nrow(X) \times (ncol(X) + ncol(Y))$. Showing the Slack of each DMU

(row) for each input and output (column).

Author(s)

Alexander Öttl

Examples

```
X <- c(1,1,2,4,1.5,2,4,3)
Y <- c(1,2,4,4,0.5,2.5,3.5,4)

# Two weight restrictions in standard form first on output then input.
# The first WR shows the trade-off that inputs can be reduced by one unit
# which reduces outputs by four units. The second WR shows that outputs can
# be increased by one unit when inputs are increased by four units.

WR <- matrix(c(-4,-1,1,4), nrow = 2, byrow = TRUE)

wrDEA(X, Y, ORIENTATION = "in", RTS="vrs", WR = WR)

# For an estimation just focusing on one DMU one can for example use
# XREF and YREF to define the technology and then estimate the efficiency for
# the DMU under observation (here DMU 1). Let's additionally estimate the slacks.

wrDEA(X[1], Y[1], ORIENTATION = "in", RTS="vrs", XREF = X, YREF = Y, SLACK = TRUE, WR = WR)</pre>
```

Index

```
costDEA, 2
hyperbolicDEA, 3
lprofitDEA, 5
nlprofitDEA, 6
wrDEA, 8
```