

Package: fntl (via r-universe)

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Title Numerical Tools for 'Rcpp' and Lambda Functions

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Description Provides a 'C++' API for routinely used numerical tools such as integration, root-finding, and optimization, where function arguments are given as lambdas. This facilitates 'Rcpp' programming, enabling the development of 'R'-like code in 'C++' where functions can be defined on the fly and use variables in the surrounding environment.

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URL <https://github.com/andrewraim/fntl>

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Author Andrew M. Raim [aut, cre] (ORCID:
<<https://orcid.org/0000-0002-4440-2330>>)

Maintainer Andrew M. Raim <andrew.raim@gmail.com>

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Contents

fntl-package	2
args	3
deriv	4
findroot	5
gradient0	6
hessian0	7
integrate0	7
jacobian0	8
matrix_apply	9
multivariate-optimization	10
outer	12
solve_cg	14
trunc	15
univariate-optimization	17
which0	18
Index	19

fntl-package	<i>fntl</i>
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Description

Package documentation

Author(s)

Maintainer: Andrew M. Raim <andrew.raim@gmail.com> ([ORCID](#))

Authors:

- Andrew M. Raim <andrew.raim@gmail.com> ([ORCID](#))

See Also

Useful links:

- <https://github.com/andrewraim/fntl>

args

Arguments

Description

Get an arguments list for internal methods with the default settings. This object can be adjusted and passed to the respective function.

Usage

`findroot_args()`

`optimize_args()`

`integrate_args()`

`cg_args()`

`bfgs_args()`

`lbfgsb_args()`

`neldermead_args()`

`nlm_args()`

`richardson_args()`

Value

An argument list corresponding to the specified function. The elements of the list are named and supplied with default values. See the package vignette for further details.

- `findroot_args` is documented in the section "Root-Finding".
- `optimize_args` is documented in the section "Univariate Optimization".
- `integrate_args` is documented in the section "Integration".
- `cg_args` is documented in the section "Conjugate Gradient".
- `bfgs_args` is documented in the section "BFGS".
- `lbfgsb_args` is documented in the section "L-BFGS-B".
- `neldermead_args` is documented in the section "Nelder-Mead".
- `nlm_args` is documented in the section "Newton-Type Algorithm for Nonlinear Optimization".
- `richardson_args` is documented in the section "Richardson Extrapolated Finite Differences".

deriv

*Numerical Derivatives via Finite Differences***Description**

Numerical Derivatives via Finite Differences

Usage

```
fd_deriv1(f, x, i, h, fd_type)

fd_deriv2(f, x, i, j, h_i, h_j, fd_type)

deriv1(f, x, i, args, fd_type)

deriv2(f, x, i, j, args, fd_type)
```

Arguments

f	Function to differentiate.
x	Scalar at which to evaluate the derivative.
i	First coordinate to differentiate.
h	Step size in the first coordinate.
fd_type	Type of derivative: 0 for symmetric difference, 1 for forward difference, and 2 for backward difference.
j	Second coordinate to differentiate.
h_i	Step size in the first coordinate.
h_j	Step size in the second coordinate.
args	List of additional arguments from the function richardson_args.

Value

fd_deriv1 and fd_deriv2 return a single numeric value corresponding to the first and second derivative via finite differences. deriv1 and deriv2 return a list with the form of a richardson_result described in section "Richardson Extrapolated Finite Differences" of the package vignette.

Examples

```
args = richardson_args()

f = sin # Try 2nd derivatives of a univariate function
x0 = 0.5
print(-sin(x0)) ## Exact answer for f''(x0)

fd_deriv2(f, x0, i = 0, j = 0, h_i = 0.001, h_j = 0.001, fd_type = 0)
```

```

fd_deriv2(f, x0, i = 0, j = 0, h_i = 0.001, h_j = 0.001, fd_type = 1)
fd_deriv2(f, x0, i = 0, j = 0, h_i = 0.001, h_j = 0.001, fd_type = 2)

deriv2(f, x0, i = 0, j = 0, args, fd_type = 0)

# Try 2nd derivatives of a bivariate function
f = function(x) { sin(x[1]) + cos(x[2]) }
x0 = c(0.5, 0.25)

print(-sin(x0[1])) ## Exact answer for f_xx(x0)
print(-cos(x0[2])) ## Exact answer for f_yy(x0)
print(0)          ## Exact answer for f_xy(x0,y0)

numDeriv::hessian(f, x0)

fd_deriv2(f, x0, i = 0, j = 0, h_i = 0.001, h_j = 0.001, fd_type = 0)
fd_deriv2(f, x0, i = 0, j = 0, h_i = 0.001, h_j = 0.001, fd_type = 1)
fd_deriv2(f, x0, i = 0, j = 0, h_i = 0.001, h_j = 0.001, fd_type = 2)

fd_deriv2(f, x0, i = 0, j = 1, h_i = 0.001, h_j = 0.001, fd_type = 0)
fd_deriv2(f, x0, i = 0, j = 1, h_i = 0.001, h_j = 0.001, fd_type = 1)
fd_deriv2(f, x0, i = 0, j = 1, h_i = 0.001, h_j = 0.001, fd_type = 2)

fd_deriv2(f, x0, i = 1, j = 1, h_i = 0.001, h_j = 0.001, fd_type = 0)
fd_deriv2(f, x0, i = 1, j = 1, h_i = 0.001, h_j = 0.001, fd_type = 1)
fd_deriv2(f, x0, i = 1, j = 1, h_i = 0.001, h_j = 0.001, fd_type = 2)

deriv2(f, x0, i = 1, j = 1, args, fd_type = 0)
deriv2(f, x0, i = 1, j = 1, args, fd_type = 1)
deriv2(f, x0, i = 1, j = 1, args, fd_type = 2)

```

findroot

Find Root

Description

Find Root

Usage

```
findroot_bisect(f, lower, upper, args)
```

```
findroot_brent(f, lower, upper, args)
```

Arguments

f	Function for which a root is desired.
lower	Lower limit of search interval. Must be finite.
upper	Upper limit of search interval. Must be finite.
args	List of additional arguments from the function findroot_args.

Value

A list with the form of a `findroot_result` described in section "Root-Finding" of the package vignette.

Examples

```
f = function(x) { x^2 - 1 }
args = findroot_args()
findroot_bisect(f, 0, 10, args)
findroot_brent(f, 0, 10, args)
```

gradient0

Numerical Gradient Vector

Description

Numerical Gradient Vector

Usage

```
gradient0(f, x, args)
```

Arguments

<code>f</code>	Function to differentiate.
<code>x</code>	Vector at which to evaluate the gradient.
<code>args</code>	List of additional arguments from the function <code>richardson_args</code> .

Value

A list with the form of a `gradient_result` described in section "Gradient" of the package vignette.

Examples

```
f = function(x) { sum(sin(x)) }
args = richardson_args()
x0 = seq(0, 1, length.out = 5)
cos(x0) ## Exact answer
gradient0(f, x0, args)
numDeriv::grad(f, x0)
```

hessian0	<i>Numerical Hessian</i>
----------	--------------------------

Description

Numerical Hessian

Usage

```
hessian0(f, x, args)
```

Arguments

f	Function to differentiate.
x	Vector at which to evaluate the Hessian.
args	List of additional arguments from the function <code>richardson_args</code> .

Value

A list with the form of a `hessian_result` described in section "Hessian" of the package vignette.

Examples

```
f = function(x) { sum(x^2) }
x0 = seq(1, 10, length.out = 5)
args = richardson_args()
hessian0(f, x0, args)
numDeriv::hessian(f, x0)
```

integrate0	<i>Integration</i>
------------	--------------------

Description

Compute the integral $\int_a^b f(x)dx$.

Usage

```
integrate0(f, lower, upper, args)
```

Arguments

f	Function to integrate.
lower	Lower limit of integral.
upper	Upper limit of integral.
args	List of additional arguments from the function <code>integrate_args</code> .

Value

A list with the form of a `integrate_result` described in section "Integration" of the package vignette.

Examples

```
f = function(x) { exp(-x^2 / 2) }
args = integrate_args()
integrate0(f, 0, 10, args)
```

jacobian0

Numerical Jacobian Matrix

Description

Numerical Jacobian Matrix

Usage

```
jacobian0(f, x, args)
```

Arguments

f	Function to differentiate.
x	Vector at which to evaluate the Jacobian.
args	List of additional arguments from the function <code>richardson_args</code> .

Value

A list with the form of a `jacobian_result` described in section "Jacobian" of the package vignette.

Examples

```
f = function(x) { cumsum(sin(x)) }
x0 = seq(1, 10, length.out = 5)
args = richardson_args()
out = jacobian0(f, x0, args)
print(out$value)
numDeriv::jacobian(f, x0)
```

Description

Matrix Apply Functions

Usage

```
mat_apply(X, f)
```

```
row_apply(X, f)
```

```
col_apply(X, f)
```

Arguments

X	A matrix
f	The function to apply.

Details

The `mat_apply`, `row_apply`, and `col_apply` C++ functions are intended to operate like the following calls in R, respectively.

```
apply(x, c(1,2), f)
apply(x, 1, f)
apply(x, 2, f)
```

The R functions exposed here are specific to numeric-valued matrices, but the underlying C++ functions are intended to work with any type of Rcpp Matrix.

Value

`mat_apply` returns a matrix. `row_apply` and `col_apply` return a vector. See section "Apply" of the package vignette for details.

Examples

```
X = matrix(1:12, nrow = 4, ncol = 3)
mat_apply(X, f = function(x) { x^(1/3) })
row_apply(X, f = function(x) { sum(x^2) })
col_apply(X, f = function(x) { sum(x^2) })
```

`multivariate-optimization`*Multivariate Optimization*

Description

Multivariate Optimization

Usage

`cg1(init, f, g, args)``cg2(init, f, args)``bfgs1(init, f, g, args)``bfgs2(init, f, args)``lbfgsb1(init, f, g, args)``lbfgsb2(init, f, args)``neldermead(init, f, args)``nlm1(init, f, g, h, args)``nlm2(init, f, g, args)``nlm3(init, f, args)`

Arguments

<code>init</code>	Initial value
<code>f</code>	Function f to optimize
<code>g</code>	Gradient function of f .
<code>args</code>	List of additional arguments for optimization.
<code>h</code>	Hessian function of f .

Details

The argument `args` should be a list constructed from one of the following functions:

- `bfgs_args` for BFGS;
- `lbfgsb_args` for L-BFGS-B;
- `cg_args` for CG;

- `neldermead_args` for Nelder-Mead;
- `nlm_args` for the Newton-type algorithm used in `nlm`.

When `g` or `h` are omitted, the gradient or Hessian will be respectively be computed via finite differences.

Value

A list with results corresponding to the specified function. See the package vignette for further details.

- `cg1` and `cg2` return a `cg_result` which is documented in the section "Conjugate Gradient".
- `bfgs1` and `bfgs2` return a `bfgs_result` which is documented in the section "BFGS".
- `lbfgsb1` and `lbfgsb2` return a `lbfgsb_result` which is documented in the section "L-BFGS-B".
- `neldermead` returns a `neldermead_result` which is documented in the section "Nelder-Mead".
- `nlm1`, `nlm2`, and `nlm3` return a `nlm_result` which is documented in the section "Newton-Type Algorithm for Nonlinear Optimization".

Examples

```
f = function(x) { sum(x^2) }
g = function(x) { 2*x }
h = function(x) { 2*diag(length(x)) }
x0 = c(1,1)
```

```
args = cg_args()
cg1(x0, f, g, args)
cg2(x0, f, args)
```

```
args = bfgs_args()
bfgs1(x0, f, g, args)
bfgs2(x0, f, args)
```

```
args = lbfgsb_args()
lbfgsb1(x0, f, g, args)
lbfgsb2(x0, f, args)
```

```
args = neldermead_args()
neldermead(x0, f, args)
```

```
args = nlm_args()
nlm1(x0, f, g, h, args)
nlm2(x0, f, g, args)
nlm3(x0, f, args)
```

outer

*Outer Matrix***Description**

Compute "outer" matrices and matrix-vector products based on a function that operators on pairs of rows. See details.

Usage

```
outer1(X, f)
```

```
outer2(X, Y, f)
```

```
outer1_matvec(X, f, a)
```

```
outer2_matvec(X, Y, f, a)
```

```
outer1_triplet(X, f, g)
```

```
outer2_triplet(X, Y, f, g)
```

Arguments

X	A numerical matrix.
f	Function $f(x, y)$ that operates on a pair of rows and returns an element for the result.
Y	A numerical matrix.
a	A scalar vector.
g	Function $g(x, y)$ that operates on a pair of rows and returns a logical value; if TRUE, the corresponding output of f is placed into the result. Otherwise, the corresponding output of f is omitted from the result.

Details

Functions $f(x, y)$ and $g(x, y)$ operate on pairs of rows. In the functions with prefix `outer1`, x and y are pairs of rows of X . In the functions with prefix `outer2`, x is a row from X and y is a row from Y .

The `outer1` function computes the $n \times n$ symmetric matrix

$$\text{outer1}(X, f) = \begin{bmatrix} f(x_1, x_1) & \cdots & f(x_1, x_n) \\ \vdots & \ddots & \vdots \\ f(x_n, x_1) & \cdots & f(x_n, x_n) \end{bmatrix}$$

and the `outer1_matvec` operation computes the n -dimensional vector

$$\text{outer1_matvec}(X, f, a) = \begin{bmatrix} f(x_1, x_1) & \cdots & f(x_1, x_n) \\ \vdots & \ddots & \vdots \\ f(x_n, x_1) & \cdots & f(x_n, x_n) \end{bmatrix} \begin{bmatrix} a_1 \\ \vdots \\ a_n \end{bmatrix}.$$

The `outer2` operation computes the $m \times n$ matrix

$$\text{outer2}(X, Y, f) = \begin{bmatrix} f(x_1, y_1) & \cdots & f(x_1, y_n) \\ \vdots & \ddots & \vdots \\ f(x_m, y_1) & \cdots & f(x_m, y_n) \end{bmatrix}$$

and the `outer2_matvec` operation computes the m -dimensional vector

$$\text{outer2_matvec}(X, Y, f, a) = \begin{bmatrix} f(x_1, y_1) & \cdots & f(x_1, y_n) \\ \vdots & \ddots & \vdots \\ f(x_m, y_1) & \cdots & f(x_m, y_n) \end{bmatrix} \begin{bmatrix} a_1 \\ \vdots \\ a_n \end{bmatrix}.$$

The `outer_triplet1` and `outer_triplet2` operations are analogous to `outer1` and `outer2`, respectively, except return sparse matrices in triplet form. The triplet variants take an additional argument `g`, a function `$g(x_i, y_j)$` that returns TRUE if the result is to be stored in the result and FALSE otherwise. The argument `g` can be used for sparseness.

Value

`outer1` and `outer2` return a matrix. `outer1_matvec` and `outer2_matvec` return a vector. `outer1_triplet` and `outer2_triplet` return a list with a sparse matrix (triplet) representation. See section "Outer" of the package vignette for details.

Examples

```
set.seed(1234)
f = function(x,y) { sum( (x - y)^2 ) }
X = matrix(rnorm(12), 6, 2)
Y = matrix(rnorm(10), 5, 2)
outer1(X, f)
outer2(X, Y, f)

a = rep(1, 6)
b = rep(1, 5)
outer1_matvec(X, f, a)
outer2_matvec(X, Y, f, b)
```

solve_cg

Iteratively Solve a Linear System with Conjugate Gradient

Description

Solve the system $l(x) = b$ where $l(x)$ is a matrix-free representation of the linear operation Ax .

Usage

```
solve_cg(l, b, init, args)
```

Arguments

<code>l</code>	A linear transformation of x .
<code>b</code>	A vector.
<code>init</code>	Initial value of solution.
<code>args</code>	List of additional arguments from <code>cg_args</code> .

Value

A list with the form of a `solve_cg_result` described in section "Conjugate Gradient" of the package vignette.

Examples

```
set.seed(1234)

n = 8
idx_diag = cbind(1:n, 1:n)
idx_ldiag = cbind(2:n, 1:(n-1))
idx_udiag = cbind(1:(n-1), 2:n)
b = rep(1, n)

## Solution by explicit computation of solve(A, b)
A = matrix(0, n, n)
A[idx_diag] = 2
A[idx_ldiag] = 1
A[idx_udiag] = 1
solve(A, b)

## Solve iteratively with solve_cg
f = function(x) { A %*% x }
args = cg_args()
init = rep(0, n)
solve_cg(f, b, init, args)
```

trunc

*Functions for Truncated Distributions***Description**

Density, CDF, quantile, and drawing functions for a univariate distribution with density f , cdf, F , and quantile function F^{-1} truncated to the interval $[a, b]$.

Usage

```
d_trunc(x, lo, hi, f, F, log = FALSE)

p_trunc(x, lo, hi, F, lower = TRUE, log = FALSE)

q_trunc(p, lo, hi, F, Finv, lower = TRUE, log = FALSE)

r_trunc(n, lo, hi, F, Finv)
```

Arguments

<code>x</code>	Vector of quantiles.
<code>lo</code>	Vector of lower limits.
<code>hi</code>	Vector of upper limits.
<code>f</code>	Density function with form $f(x, \log)$.
<code>F</code>	CDF function with signature $F(x, \text{lower}, \log)$, where x is numeric and <code>lower</code> and <code>log</code> are logical.
<code>log</code>	logical; if TRUE, probabilities are given on log-scale.
<code>lower</code>	logical; if TRUE, probabilities are $P(X \leq x)$; otherwise, $P(X > x)$.
<code>p</code>	Vector of probabilities.
<code>Finv</code>	Quantile function with signature $\text{Finv}(x, \text{lower}, \log)$, where x is numeric and <code>lower</code> and <code>log</code> are logical.
<code>n</code>	Number of draws.

Value

Vector with results. `d_trunc` computes the density, `r_trunc` generates random deviates, `p_trunc` computes the CDF, and `q_trunc` computes quantiles.

Examples

```
library(tidyverse)

m = 100 ## Length of sequence for density, CDF, etc
shape1 = 5
shape2 = 2
```

```

lo = 0.5
hi = 0.7

# Density, CDF, and quantile function for untruncated distribution
ff = function(x, log) { dbeta(x, shape1, shape2, log = log) }
FF = function(x, lower, log) { pbeta(x, shape1, shape2, lower.tail = lower, log = log) }
FFinv = function(x, lower, log) { qbeta(x, shape1, shape2, lower.tail = lower, log = log) }

# Compare truncated and untruncated densities
xseq = seq(0, 1, length.out = m)
lo_vec = rep(lo, m)
hi_vec = rep(hi, m)
f0seq = ff(xseq, log = FALSE)
fseq = d_trunc(xseq, lo_vec, hi_vec, ff, FF)
data.frame(x = xseq, f = fseq, f0 = f0seq) %>%
  ggplot() +
  geom_line(aes(xseq, fseq)) +
  geom_line(aes(xseq, f0seq), lty = 2) +
  xlab("x") +
  ylab("Density") +
  theme_minimal()

# Compare truncated densities and empirical density of generated draws
n = 100000
lo_vec = rep(lo, n)
hi_vec = rep(hi, n)
x = r_trunc(n = n, lo_vec, hi_vec, FF, FFinv)
hist(x, probability = TRUE, breaks = 15)
points(xseq, fseq)

# Compare empirical CDF of draws with CDF function
Femp = ecdf(x)
lo_vec = rep(lo, m)
hi_vec = rep(hi, m)
Fseq = p_trunc(xseq, lo_vec, hi_vec, FF)
data.frame(x = xseq, FF = Fseq) %>%
  mutate(F0 = Femp(x)) %>%
  ggplot() +
  geom_line(aes(xseq, FF), lwd = 1.2) +
  geom_line(aes(xseq, F0), col = "orange") +
  xlab("x") +
  ylab("Probability") +
  theme_minimal()

# Compare empirical quantiles of draws with quantile function
pseq = seq(0, 1, length.out = m)
lo_vec = rep(lo, m)
hi_vec = rep(hi, m)
Finvseq = q_trunc(pseq, lo_vec, hi_vec, FF, FFinv)
Finvemp = quantile(x, prob = pseq)
data.frame(p = pseq, Finv = Finvseq, Finvemp = Finvemp) %>%
  ggplot() +
  geom_line(aes(pseq, Finv), lwd = 1.2) +

```

```
geom_line(aes(pseq, Finvemp), col = "orange") +  
xlab("p") +  
ylab("Quantile") +  
theme_minimal()
```

univariate-optimization

Univariate Optimization

Description

Univariate Optimization

Usage

```
goldensection(f, lower, upper, args)
```

```
optimize_brent(f, lower, upper, args)
```

Arguments

f	Function to optimize.
lower	Lower limit of search interval. Must be finite.
upper	Upper limit of search interval. Must be finite.
args	List of additional arguments from the function optimize_args.

Value

A list with the form of a `optimize_result` described in section "Univariate Optimization" of the package vignette.

Examples

```
f = function(x) { x^2 - 1 }  
args = optimize_args()  
goldensection(f, 0, 10, args)  
optimize_brent(f, 0, 10, args)
```

which0	<i>Matrix Which Function</i>
--------	------------------------------

Description

Matrix Which Function

Usage

```
which0(X, f)
```

Arguments

X	A matrix
f	A predicate to apply to each element of X .

Details

The which C++ functions are intended to operate like the following call in R.

```
which(f(X), arr.ind = TRUE) - 1
```

The R functions exposed here are specific to numeric-valued matrices, but the underlying C++ functions are intended to work with any type of Rcpp Matrix.

Value

A matrix with two columns. Each row contains a row and column index corresponding to an element of X that matches the criteria of f . See section "Which" of the package vignette for details.

Examples

```
X = matrix(1:12 / 6, nrow = 4, ncol = 3)
f = function(x) { x < 1 }
which0(X, f)
```

Index

args, 3

bfgs1 (multivariate-optimization), 10
bfgs2 (multivariate-optimization), 10
bfgs_args (args), 3

cg1 (multivariate-optimization), 10
cg2 (multivariate-optimization), 10
cg_args (args), 3
col_apply (matrix_apply), 9

d_trunc (trunc), 15
deriv, 4
deriv1 (deriv), 4
deriv2 (deriv), 4

fd_deriv1 (deriv), 4
fd_deriv2 (deriv), 4
findroot, 5
findroot_args (args), 3
findroot_bisect (findroot), 5
findroot_brent (findroot), 5
fntl (fntl-package), 2
fntl-package, 2

goldensection
 (univariate-optimization), 17
gradient0, 6

hessian0, 7

integrate0, 7
integrate_args (args), 3

jacobian0, 8

lbfgsb1 (multivariate-optimization), 10
lbfgsb2 (multivariate-optimization), 10
lbfgsb_args (args), 3

mat_apply (matrix_apply), 9

matrix_apply, 9
multivariate-optimization, 10

neldermead (multivariate-optimization),
 10
neldermead_args (args), 3
nlm1 (multivariate-optimization), 10
nlm2 (multivariate-optimization), 10
nlm3 (multivariate-optimization), 10
nlm_args (args), 3

optimize_args (args), 3
optimize_brent
 (univariate-optimization), 17
outer, 12
outer1 (outer), 12
outer1_matvec (outer), 12
outer1_triplet (outer), 12
outer2 (outer), 12
outer2_matvec (outer), 12
outer2_triplet (outer), 12

p_trunc (trunc), 15

q_trunc (trunc), 15

r_trunc (trunc), 15
richardson_args (args), 3
row_apply (matrix_apply), 9

solve_cg, 14

trunc, 15

univariate-optimization, 17

which0, 18