

# Package: fmerPack (via r-universe)

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**Title** Tools of Heterogeneity Pursuit via Finite Mixture Effects Model

**Version** 0.0-1

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**Description** Heterogeneity pursuit methodologies for regularized finite mixture regression by effects-model formulation proposed by Li et al. (2021) <[arXiv:2003.04787](https://arxiv.org/abs/2003.04787)>.

**Depends** R (>= 3.4.0)

**Imports** utils, flexmix, glmnet, MASS, Rcpp (>= 0.12.0), abind

**LinkingTo** Rcpp, RcppArmadillo

**License** GPL (>= 3.0)

**Encoding** UTF-8

**RoxygenNote** 7.1.1

**NeedsCompilation** yes

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fmrHP

*Finite Mixture Effects Model with Heterogeneity Pursuit***Description**

Produce solution for specified lambda of regularized finite mixture effects model with lasso or adaptive lasso; compute the degrees of freedom, likelihood and information criteria (AIC, BIC and GIC) of the estimators. Model fitting is conducted by EM algorithm and Bregman coordinate descent.

**Usage**

```
fmrHP(y, X, m, intercept = FALSE, lambda, equal.var = FALSE,
      ic.type = c("ALL", "BIC", "AIC", "GIC"),
      B = NULL, prob = NULL, rho = NULL, w = NULL,
      control = list(), report = FALSE)
```

**Arguments**

|           |   |
|-----------|---|
| y         | a vector of response ( $n \times 1$ )   |
| X         | a matrix of covariate ( $n \times p$ )  |
| m         | number of components  |
| intercept | indicating whether intercept should be included   |
| lambda    | value of tuning parameter   |
| equal.var | indicating whether variances of different components are equal  |
| ic.type   | the information criterion to be used; currently supporting "AIC", "BIC", and "GIC".   |
| B         | initial values for the rescaled coefficients with first column being the common effect, and the rest m columns being the heterogeneity for corresponding components |
| prob      | initial values for prior probabilities for different components   |
| rho       | initial values for rho vector ( $1/\sigma$ ), the reciprocal of standard deviation  |
| w         | weight matrix for penalty function. Default option is NULL  |
| control   | a list of parameters for controlling the fitting process  |
| report    | indicating whether printing the value of objective function during EM algorithm for validation checking of initial value.   |

**Details**

The available elements for argument `control` include

- `epsilon`: Convergence threshold for generalized EM algorithm. Defaults value is 1E-6.
- `maxit`: Maximum number of passes over the data for all lambda values. Default is 1000.

- `inner.eps`: Convergence threshold for Bregman coordinate descent algorithm. Defaults value is 1E-6.
- `inner.maxit`: Maximum number of iteration for Bregman coordinate descent algorithm. Defaults value is 200.
- `n.ini`: Number of initial values for EM algorithm. Default is 10. In EM algorithm, it is preferable to start from several different initial values.

## Value

A list consisting of

|                      |  |
|----------------------|--|
| <code>y</code>       | vector of response   |
| <code>X</code>       | matrix of covariates   |
| <code>m</code>       | number of components   |
| <code>B.hat</code>   | estimated rescaled coefficient ( $p \times m + 1 \times nlambda$ ) |
| <code>pi.hat</code>  | estimated prior probabilities ( $m \times nlambda$ )               |
| <code>rho.hat</code> | estimated rho values ( $m \times nlambda$ )                        |
| <code>lambda</code>  | lambda used in model fitting                                       |
| <code>plik</code>    | value of penalized log-likelihood                                  |
| <code>loglik</code>  | value of log-likelihood  |
| <code>conv</code>    | indicator of convergence of EM algorithm                           |
| <code>IC</code>      | values of information criteria                                     |
| <code>df</code>      | degree of freedom  |

## Examples

```
library(fmerPack)
## problem settings
n <- 100; m <- 3; p <- 5;
sigma2 <- c(0.1, 0.1, 0.4); rho <- 1 / sqrt(sigma2)
phi <- rbind(c(1, 1, 1), c(1, 1, 1), c(0, -3, 3), c(-3, 3, 0), c(3, 0, -3))
beta <- t(t(phi) / rho)
## generate response and covariates
z <- rmultinom(n, 1, prob= rep(1 / m, m))
X <- matrix(rnorm(n * p), nrow = n, ncol = p)
y <- MASS::mvrnorm(1, mu = rowSums(t(z) * X[, 1:(nrow(beta))]) %*% beta),
               Sigma = diag(colSums(z * sigma2)))
fmrHP(y, X, m = m, lambda = 0.01, control = list(n.ini = 10))
```

fmrReg

*Finite Mixture Model with lasso and adaptive penalty***Description**

Produce solution for specific lambda of regularized finite mixture model with lasso or adaptive lasso penalty; compute the degrees of freedom, likelihood and information criteria (AIC, BIC and GIC) of the estimators. Model fitting is conducted by EM algorithm and coordinate descent.

**Usage**

```
fmrReg(y, X, m, intercept = FALSE, lambda, equal.var = FALSE, common.var = NULL,
       ic.type = c("ALL", "BIC", "AIC", "GIC"),
       B = NULL, prob = NULL, rho = NULL, w = NULL,
       control = list(), report = FALSE)
```

**Arguments**

|            |   |
|------------|---|
| y          | a vector of response ( $n \times 1$ )   |
| X          | a matrix of covariate ( $n \times p$ )  |
| m          | number of components  |
| intercept  | indicating whether intercept should be included   |
| lambda     | value of tuning parameter   |
| equal.var  | indicating whether variances of different components are equal  |
| common.var | indicating whether the effects over different components are the same for specific covariates                             |
| ic.type    | the information criterion to be used; currently supporting "AIC", "BIC", and "GIC".                                       |
| B          | initial values for the rescaled coefficients with columns being the coefficients for different components                 |
| prob       | initial values for prior probabilities for different components   |
| rho        | initial values for rho vector ( $1/\sigma$ ), the reciprocal of standard deviation  |
| w          | weight matrix for penalty function. Default option is NULL  |
| control    | a list of parameters for controlling the fitting process  |
| report     | indicating whether printing the value of objective function during EM algorithm for validation checking of initial value. |

**Details**

The available elements for argument control include

- epsilon: Convergence threshold for generalized EM algorithm. Defaults value is 1E-6.
- maxit: Maximum number of passes over the data for all lambda values. Default is 1000.

- inner.maxit: Maximum number of iteration for flexmix package to compute initial values. Defaults value is 200.
- n.ini: Number of initial values for EM algorithm. Default is 10. In EM algorithm, it is preferable to start from several different initial values.

### Value

A list consisting of

|         |  |
|---------|--|
| y       | vector of response   |
| X       | matrix of covariates   |
| m       | number of components   |
| B.hat   | estimated rescaled coefficient ( $p \times m \times nlambda$ ) |
| pi.hat  | estimated prior probabilities ( $m \times nlambda$ )           |
| rho.hat | estimated rho values ( $m \times nlambda$ )                    |
| lambda  | lambda used in model fitting                                   |
| plik    | value of penalized log-likelihood                              |
| loglik  | value of log-likelihood  |
| conv    | indicator of convergence of EM algorithm                       |
| IC      | values of information criteria                                 |
| df      | degree of freedom  |

### Examples

```
library(fmerPack)
## problem settings
n <- 100; m <- 3; p <- 5;
sigma2 <- c(0.1, 0.1, 0.4); rho <- 1 / sqrt(sigma2)
phi <- rbind(c(1, 1, 1), c(1, 1, 1), c(0, -3, 3), c(-3, 3, 0), c(3, 0, -3))
beta <- t(t(phi) / rho)
## generate response and covariates
z <- rmultinom(n, 1, prob= rep(1 / m, m))
X <- matrix(rnorm(n * p), nrow = n, ncol = p)
y <- MASS::mvrnorm(1, mu = rowSums(t(z) * X[, 1:(nrow(beta))] %*% beta),
                Sigma = diag(colSums(z * sigma2)))
fmrReg(y, X, m = m, lambda = 0.01, control = list(n.ini = 10))
```

### Description

Produce solution paths of regularized finite mixture effects model with lasso or adaptive lasso penalty; compute the degrees of freedom, likelihood and information criteria (AIC, BIC and GIC) of the estimators. Model fitting is conducted by EM algorithm and Bregman coordinate descent.

**Usage**

```
path.fmrHP(y, X, m, equal.var = FALSE,
           ic.type = "ALL", B = NULL, prob = NULL, rho = NULL,
           control = list(), modstr = list(), report = FALSE)
```

**Arguments**

|           |   |
|-----------|---|
| y         | a vector of response ( $n \times 1$ )   |
| X         | a matrix of covariate ( $n \times p$ )  |
| m         | number of components  |
| equal.var | indicating whether variances of different components are equal  |
| ic.type   | the information criterion to be used; currently supporting "AIC", "BIC", and "GIC".   |
| B         | initial values for the rescaled coefficients with first column being the common effect, and the rest m columns being the heterogeneity for corresponding components |
| prob      | initial values for prior probabilities for different components   |
| rho       | initial values for rho vector ( $1/\sigma$ ), the reciprocal of standard deviation  |
| control   | a list of parameters for controlling the fitting process  |
| modstr    | a list of model parameters controlling the model fitting  |
| report    | indicating whether printing the value of objective function during EM algorithm for validation checking of initial value.   |

**Details**

Model parameters can be specified through argument `modstr`. The available include

- `lambda`: A vector of user-specified lambda values with default NULL.
- `lambda.min.ratio`: Smallest value for lambda, as a fraction of lambda.max, the (data derived) entry value.
- `nlambda`: The number of lambda values.
- `w`: Weight matrix for penalty function. Default option is NULL, which means lasso penalty is used for model fitting.
- `intercept`: Should intercept(s) be fitted (default=TRUE) or set to zero (FALSE).
- `common.only`: A vector of user-specified indicators of the variables only with common effects.
- `common.no.penalty`: A vector of user-specified indicators of the variables with no penalty on the common effect.
- `cluster.no.penalty`: A vector of user-specified indicators of the variables with no penalty on the cluster-specific effects.
- `select.ratio`: A user-specified ratio indicating the ratio of variables to be selected.

The available elements for argument `control` include

- `epsilon`: Convergence threshold for generalized EM algorithm. Defaults value is 1E-6.

- `maxit`: Maximum number of passes over the data for all lambda values. Default is 1000.
- `inner.eps`: Convergence threshold for Bregman coordinate descent algorithm. Defaults value is 1E-6.
- `inner.maxit`: Maximum number of iteration for Bregman coordinate descent algorithm. Defaults value is 200.
- `n.ini`: Number of initial values for EM algorithm. Default is 10. In EM algorithm, it is preferable to start from several different initial values.

### Value

A list consisting of

|                          |   |
|--------------------------|---|
| <code>lambda</code>      | vector of lambda used in model fitting  |
| <code>lambda.used</code> | vector of lambda in model fitting after truncation by <code>select.ratio</code> |
| <code>B.hat</code>       | estimated rescaled coefficient ( $p \times m + 1 \times nlambda$ )              |
| <code>pi.hat</code>      | estimated prior probabilities ( $m \times nlambda$ )                            |
| <code>rho.hat</code>     | estimated rho values ( $m \times nlambda$ )                                     |
| <code>IC</code>          | values of information criteria  |

### References

Li, Y., Yu, C., Zhao, Y., Yao, W., Aseltine, R. H., & Chen, K. (2021). Pursuing Sources of Heterogeneity in Modeling Clustered Population.

### Examples

```
library(fmerPack)
## problem settings
n <- 100; m <- 3; p <- 5;
sigma2 <- c(0.1, 0.1, 0.4); rho <- 1 / sqrt(sigma2)
phi <- rbind(c(1, 1, 1), c(1, 1, 1), c(1, 1, 1), c(-3, 3, 0), c(3, 0, -3))
beta <- t(t(phi) / rho)
## generate response and covariates
z <- rmultinom(n, 1, prob= rep(1 / m, m))
X <- matrix(rnorm(n * p), nrow = n, ncol = p)
y <- MASS::mvrnorm(1, mu = rowSums(t(z) * X[, 1:(nrow(beta))]) %*% beta,
                 Sigma = diag(colSums(z * sigma2)))
## lasso
fit1 <- path.fmrHP(y, X, m = m, modstr = list(nlambda = 10), control = list(n.ini = 1))
## adaptive lasso
fit2 <- path.fmrHP(y, X, m = m,
                  modstr = list(w = abs(select.tuning(fit1)$B + 1e-6)^2))
```

path.fmrReg

*Finite Mixture Model with lasso and adaptive penalty***Description**

Produce solution paths of regularized finite mixture model with lasso or adaptive lasso penalty; compute the degrees of freedom, likelihood and information criteria (AIC, BIC and GIC) of the estimators. Model fitting is conducted by EM algorithm and coordinate descent.

**Usage**

```
path.fmrReg(y, X, m, equal.var = FALSE,
            ic.type = "ALL", B = NULL, prob = NULL, rho = NULL,
            control = list(), modstr = list(), report = FALSE)
```

**Arguments**

|           |  |
|-----------|--|
| y         | a vector of response ( $n \times 1$ )  |
| X         | a matrix of covariate ( $n \times p$ )   |
| m         | number of components   |
| equal.var | indicating whether variances of different components are equal   |
| ic.type   | the information criterion to be used; currently supporting "ALL", "AIC", "BIC", and "GIC".                                 |
| B         | initial values for the rescaled coefficients with columns being the columns being the coefficient for different components |
| prob      | initial values for prior probabilities for different components  |
| rho       | initial values for rho vector ( $1/\sigma$ ), the reciprocal of standard deviation   |
| control   | a list of parameters for controlling the fitting process   |
| modstr    | a list of model parameters controlling the model fitting   |
| report    | indicating whether printing the value of objective function during EM algorithm for validation checking of initial value.  |

**Details**

Model parameters can be specified through argument modstr. The available include

- lambda: A vector of user-specified lambda values with default NULL.
- lambda.min.ratio: Smallest value for lambda, as a fraction of lambda.max, the (data derived) entry value.
- nlambda: The number of lambda values.
- w: Weight matrix for penalty function. Default option is NULL, which means lasso penalty is used for model fitting.
- intercept: Should intercept(s) be fitted (default=TRUE) or set to zero (FALSE).



- no.penalty: A vector of user-specified indicators of the variables with no penalty.
- common.var: A vector of user-specified indicators of the variables with common effect among different components.
- select.ratio: A user-specified ratio indicating the ratio of variables to be selected.

The available elements for argument control include

- epsilon: Convergence threshold for generalized EM algorithm. Defaults value is 1E-6.
- maxit: Maximum number of passes over the data for all lambda values. Default is 1000.
- inner.maxit: Maximum number of iteration for flexmix package to compute initial values. Defaults value is 200.
- n.ini: Number of initial values for EM algorithm. Default is 10. In EM algorithm, it is preferable to start from several different initial values.

## Value

A list consisting of

|         |  |
|---------|--|
| lambda  | vector of lambda used in model fitting                         |
| B.hat   | estimated rescaled coefficient ( $p \times m \times nlambda$ ) |
| pi.hat  | estimated prior probabilities ( $m \times nlambda$ )           |
| rho.hat | estimated rho values ( $m \times nlambda$ )                    |
| IC      | values of information criteria                                 |

## Examples

```
library(fmerPack)
## problem settings
n <- 100; m <- 3; p <- 5;
sigma2 <- c(0.1, 0.1, 0.4); rho <- 1 / sqrt(sigma2)
phi <- rbind(c(1, 1, 1), c(1, 1, 1), c(1, 1, 1), c(-3, 3, 0), c(3, 0, -3))
beta <- t(t(phi) / rho)
## generate response and covariates
z <- rmultinom(n, 1, prob= rep(1 / m, m))
X <- matrix(rnorm(n * p), nrow = n, ncol = p)
y <- MASS::mvrnorm(1, mu = rowSums(t(z) * X[, 1:(nrow(beta))] %*% beta),
                Sigma = diag(colSums(z * sigma2)))
## lasso
fit1 <- path.fmrReg(y, X, m = m, modstr = list(nlambda = 10), control = list(n.ini = 1))
## adaptive lasso
fit2 <- path.fmrReg(y, X, m = m,
                  modstr = list(w = abs(select.tuning(fit1)$B + 1e-6)^2))
```

---

|               |                                   |
|---------------|-----------------------------------|
| select.tuning | <i>Tuning parameter selection</i> |
|---------------|-----------------------------------|

---

**Description**

Select tuning parameter via AIC, BIC or GIC from objects generated by `path.fmrHP`.

**Usage**

```
select.tuning(object, figure = FALSE, criteria = c("BIC", "GIC", "AIC"))
```

**Arguments**

|                       |   |
|-----------------------|---|
| <code>object</code>   | Object generated from <code>path.fmrHP</code> .         |
| <code>figure</code>   | indicator for showing plot of information criteria.     |
| <code>criteria</code> | information criteria for selection of tuning parameter. |

**Value**

list of parameters of selected model.

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