# Package: fence (via r-universe)

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Type Package

```
Title Using Fence Methods for Model Selection
Version 1.0
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Author Jiming Jiang, Jianyang Zhao, J. Sunil Rao, Thuan Nguyen
Maintainer Thuan Nguyen <nguythua@ohsu.edu>
Description This method is a new class of model selection strategies,
     for mixed model selection, which includes linear and
     generalized linear mixed models. The idea involves a procedure
     to isolate a subgroup of what are known as correct models (of
     which the optimal model is a member). This is accomplished by
     constructing a statistical fence, or barrier, to carefully
     eliminate incorrect models. Once the fence is constructed, the
     optimal model is selected from among those within the fence
     according to a criterion which can be made flexible.
     References: 1. Jiang J., Rao J.S., Gu Z., Nguyen T. (2008),
     Fence Methods for Mixed Model Selection. The Annals of
     Statistics, 36(4): 1669-1692. <DOI:10.1214/07-AOS517>
     <https://projecteuclid.org/euclid.aos/1216237296>. 2. Jiang J.,
     Nguyen T., Rao J.S. (2009), A Simplified Adaptive Fence
     Procedure. Statistics and Probability Letters, 79, 625-629.
     <DOI:10.1016/j.spl.2008.10.014>
     <https://www.researchgate.net/publication/23991417_A_simplified_adaptive_</pre>
     fence_procedure>
     3. Jiang J., Nguyen T., Rao J.S. (2010), Fence Method for
     Nonparametric Small Area Estimation. Survey Methodology, 36(1),
     <http://publications.gc.ca/collections/collection_2010/statcan/12-001-X/</pre>
     12-001-x2010001-eng.pdf>.
     4. Jiming Jiang, Thuan Nguyen and J. Sunil Rao (2011),
     Invisible fence methods and the identification of
     differentially expressed gene sets. Statistics and Its
     Interface, Volume 4, 403-415.
     <http://www.intlpress.com/site/pub/files/_fulltext/journals/sii/2011/0004/</pre>
     0003/SII-2011-0004-0003-a014.pdf>.
```

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# Description

Adaptive Fence model selection

# Usage

```
adaptivefence(mf, f, ms, d, lf, pf, bs, grid = 101, bandwidth)
```

# Arguments

| mf        | function for fitting the model                  |
|-----------|---|
| f         | formula of full model                           |
| ms        | list of formula of candidates models            |
| d         | data  |
| lf        | measure lack of fit (to minimize)               |
| pf        | model selection criteria, e.g., model dimension |
| bs        | bootstrap samples                               |
| grid      | grid for c                                      |
| bandwidth | bandwidth for kernel smooth function            |
|           |   |

# Value

| models         | list all model candidates in the model space   |
|----------------|--|
| В              | list the number of bootstrap samples that have been used   |
| lack_of_fit_ma | trix   |
|                | list a matrix of Qs for all model candidates (in columns). Each row is for each bootstrap sample                         |
| Qd_matrix      | list a matrix of QM - QM.tilde for all model candidates. Each row is for each bootrap sample                             |
| bandwidth      | list the value of bandwidth  |
| model_mat      | list a matrix of selected models at each c values in grid (in columns). Each row is for each bootstrap sample            |
| freq_mat       | list a matrix of coverage probabilities (frequency/smooth_frequency) of each selected models for a given c value (index) |
| С              | list the adaptive choice of c value from which the parsimonious model is selected  |
| sel_model      | list the selected (parsimonious) model given the adaptive c value  |

# Author(s)

Jiming Jiang Jianyang Zhao J. Sunil Rao Thuan Nguyen

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#### References

• Jiang J., Rao J.S., Gu Z., Nguyen T. (2008), Fence Methods for Mixed Model Selection. The Annals of Statistics, 36(4): 1669-1692

- Jiang J., Nguyen T., Rao J.S. (2009), A Simplified Adaptive Fence Procedure. Statistics and Probability Letters, 79, 625-629
- Thuan Nguyen, Jie Peng, Jiming Jiang (2014), Fence Methods for Backcross Experiments. Statistical Computation and Simulation, 84(3), 644-662

```
## Not run:
require(fence)
#### Example 1 #####
data(iris)
full = Sepal.Length ~ Sepal.Width + Petal.Length + Petal.Width + (1|Species)
test_af = fence.lmer(full, iris)
plot(test_af)
test_af$sel_model
#### Example 2 #####
r = 1234; set.seed(r)
p=8; n=150; rho = 0.6
id = rep(1:50, each=3)
R = diag(p)
for(i in 1:p){
  for(j in 1:p){
    R[i,j] = rho^{(abs(i-j))}
  }
}
R = 1*R
x=mvrnorm(n, rep(0, p), R) # all x's are time-varying dependence #
colnames(x)=paste('x',1:p, sep='')
tbetas = c(0,0.5,1,0,0.5,1,0,0.5) # non-zero beta 2,3,5,6,8
epsilon = rnorm(150)
y = x\%*\%tbetas + epsilon
colnames(y) = 'y'
data = data.frame(cbind(x,y,id))
full = y \sim x1+x2+x3+x4+x5+x6+x7+x8+(1|id)
#X = paste('x',1:p, sep='', collapse='+')
\#full = as.formula(paste('y^-',X,'+(1|id)', sep="")) \#same as previous one
fence_obj = fence.lmer(full,data) # it takes 3-5 min #
plot(fence_obj)
fence_obj$sel_model
## End(Not run)
```

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| adaptivefence.fh | Adaptive Fence model selection (Small Area Estmation) |  |
|------------------|---|--|
|                  |   |  |

# Description

Adaptive Fence model selection (Small Area Estmation)

# Usage

```
adaptivefence.fh(mf, f, ms, d, lf, pf, bs, grid = 101, bandwidth, method)
```

# Arguments

| mf        | Call function, for example: default calls: function(m, b) eblupFH(formula = m, vardir = D, data = b, method = "FH") |
|-----------|---|
| f         | Full Model  |
| ms        | find candidate model, findsubmodel.fh(full)   |
| d         | Dimension number  |
| lf        | Measures lack of fit using function(res) -res\$fit\$goodness[1]   |
| pf        | Dimensions of model   |
| bs        | Bootstrap   |
| grid      | grid for c  |
| bandwidth | bandwidth for kernel smooth function  |
| method    | Method to be used. Fay-Herriot method is the default.   |

## **Details**

In Jiang et. al (2008), the adaptive c value is chosen from the highest peak in the p\* vs. c plot. In Jiang et. al (2009), 95% CI is taken into account while choosing such an adaptive choice of c. In Thuan Nguyen et. al (2014), the adaptive c value is chosen from the first peak. This approach works better in the moderate sample size or weak signal situations. Empirically, the first peak becomes highest peak when sample size increases or signals become stronger

# Value

| models         | list all model candidates in the model space   |
|----------------|--|
| В              | list the number of bootstrap samples that have been used   |
| lack_of_fit_ma | trix   |
|                | list a matrix of Qs for all model candidates (in columns). Each row is for each bootstrap sample |
| Qd_matrix      | list a matrix of QM - QM.tilde for all model candidates. Each row is for each bootrap sample     |
| bandwidth      | list the value of bandwidth  |

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| model_mat | list a matrix of selected models at each c values in grid (in columns). Each row is for each bootstrap sample            |
|-----------|--|
| freq_mat  | list a matrix of coverage probabilities (frequency/smooth_frequency) of each selected models for a given c value (index) |
| С         | list the adaptive choice of c value from which the parsimonious model is selected  |
| sel_model | list the selected (parsimonious) model given the adaptive c value  |

#### Note

- The current Fence package focuses on variable selection. However, Fence methods can be used to select other parameters of interest, e.g., tunning parameter, variance-covariance structure, etc.
- The number of bootstrap samples is suggested to be increased, e.g., B=1000 when the sample size is small, or signals are weak

#### Author(s)

Jiming Jiang Jianyang Zhao J. Sunil Rao Thuan Nguyen

#### References

- Jiang J., Rao J.S., Gu Z., Nguyen T. (2008), Fence Methods for Mixed Model Selection. The Annals of Statistics, 36(4): 1669-1692
- Jiang J., Nguyen T., Rao J.S. (2009), A Simplified Adaptive Fence Procedure. Statistics and Probability Letters, 79, 625-629
- Thuan Nguyen, Jie Peng, Jiming Jiang (2014), Fence Methods for Backcross Experiments. Statistical Computation and Simulation, 84(3), 644-662

```
## Not run:
require(fence)
### example 1 ####
data("kidney")
data = kidney[-which.max(kidney$x),]
                                       # Delete a suspicious data point #
data$x2 = data$x^2
data$x3 = data$x^3
data$x4 = data$x^4
data$D = data$sqrt.D.^2
plot(data\$y \sim data\$x)
full = y^x+x^2+x^3+x^4
testfh = fence.sae(full, data, B=1000, fence="adaptive", method="F-H", D = D)
testfh$sel_model
testfh$c
## End(Not run)
```

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| fence.lmer Fence model selection (Linear Mixed Model) | election (Linear Mixed Model) |
|---|-------------------------------|
|---|-------------------------------|

# **Description**

Fence model selection (Linear Mixed Model)

## Usage

```
fence.lmer(full, data, B = 100, grid = 101, fence = c("adaptive",
   "nonadaptive"), cn = NA, REML = TRUE, bandwidth = NA,
   cpus = parallel::detectCores())
```

#### **Arguments**

| full      | formula of full model  |
|-----------|--|
| data      | data   |
| В         | number of bootstrap samples, parametric bootstrap is used  |
| grid      | grid for c   |
| fence     | a procedure of the fence method to be used. It's suggested to choose nonadaptive procedure if c is known; otherwise nonadaptive must be chosen |
| cn        | cn value for nonadaptive   |
| REML      | Restricted Maximum Likelihood approach   |
| bandwidth | bandwidth for kernel smooth function   |
| cpus      | Number of parallel computers   |

#### **Details**

In Jiang et. al (2008), the adaptive c value is chosen from the highest peak in the p\* vs. c plot. In Jiang et. al (2009), 95% CI is taken into account while choosing such an adaptive choice of c. In Thuan Nguyen et. al (2014), the adaptive c value is chosen from the first peak. This approach works better in the moderate sample size or weak signal situations. Empirically, the first peak becomes highest peak when sample size increases or signals become stronger

## Value

| models         | list all model candidates in the model space   |
|----------------|--|
| В              | list the number of bootstrap samples that have been used   |
| lack_of_fit_ma | trix   |
|                | list a matrix of Qs for all model candidates (in columns). Each row is for each bootstrap sample |
| Qd_matrix      | list a matrix of QM - QM.tilde for all model candidates. Each row is for each bootrap sample     |
| bandwidth      | list the value of bandwidth  |

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| model_mat | list a matrix of selected models at each c values in grid (in columns). Each row is for each bootstrap sample            |
|-----------|--|
| freq_mat  | list a matrix of coverage probabilities (frequency/smooth_frequency) of each selected models for a given c value (index) |
| С         | list the adaptive choice of c value from which the parsimonious model is selected  |
| sel_model | list the selected (parsimonious) model given the adaptive c value  |
|           |  |

@note The current Fence package focuses on variable selection. However, Fence methods can be used to select other parameters of interest, e.g., tunning parameter, variance-covariance structure, etc.

#### Author(s)

Jiming Jiang Jianyang Zhao J. Sunil Rao Thuan Nguyen

#### References

- Jiang J., Rao J.S., Gu Z., Nguyen T. (2008), Fence Methods for Mixed Model Selection. The Annals of Statistics, 36(4): 1669-1692
- Jiang J., Nguyen T., Rao J.S. (2009), A Simplified Adaptive Fence Procedure. Statistics and Probability Letters, 79, 625-629
- Thuan Nguyen, Jie Peng, Jiming Jiang (2014), Fence Methods for Backcross Experiments. Statistical Computation and Simulation, 84(3), 644-662

### **Examples**

```
require(fence)
library(snow)

#### Example 1 #####
data(iris)
full = Sepal.Length ~ Sepal.Width + Petal.Length + Petal.Width + (1|Species)
# Takes greater than 5 seconds to run
# test_af = fence.lmer(full, iris)
# test_af$c
# test_naf = fence.lmer(full, iris, fence = "nonadaptive", cn = 12)
# plot(test_af)
# test_af$sel_model
# test_naf$sel_model
```

fence.NF

Fence model selection (Nonparametric Model)

# **Description**

Fence model selection (Noparametric Model)

fence.NF

#### Usage

```
fence.NF(full, data, spline, ps = 1:3, qs = NA, B = 100, grid = 101,
bandwidth = NA, lambda)
```

#### **Arguments**

full formula of full model

data data

spline variable needed for spline terms

ps order of power qs number of knots

B number of bootstrap sample, parametric for lmer

grid grid for c

bandwidth bandwidth for kernel smooth function

lambda A grid of lambda values

#### Value

| models list all model candidates with p polynomial degrees and q knots in the models | models | list all model | candidates with | p polynomial | degrees and q | knots in the mode |
|--|--------|----------------|-----------------|--------------|---------------|-------------------|
|--|--------|----------------|-----------------|--------------|---------------|-------------------|

space

Qd\_matrix list a matrix of QM - QM.tilde for all model candidates. Each row is for each

bootrap sample

bandwidth list the value of bandwidth

model\_mat list a matrix of selected models at each c values in grid (in columns). Each row

is for each bootstrap sample

freq\_mat list a matrix of coverage probabilities (frequency/smooth\_frequency) of each

selected models for a given c value (index)

c list the adaptive choice of c value from which the parsimonious model is selected

lambda penalty (or smoothing) parameter estimate given selected p and q sel\_model list the selected (parsimonious) model given the adaptive c value

beta.est.u A list of coefficient estimates given a lambda value

f.x.hat A vector of fitted values obtained from a given lambda value and beta.est.u

@note The current Fence method in Nonparametric model focuses on one spline variable. This method can be extended to a general case with more than one spline variables, and includes non-spline variables.

#### Author(s)

Jiming Jiang Jianyang Zhao J. Sunil Rao Bao-Qui Tran Thuan Nguyen

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#### References

- Jiang J., Rao J.S., Gu Z., Nguyen T. (2008), Fence Methods for Mixed Model Selection. The Annals of Statistics, 36(4): 1669-1692
- Jiang J., Nguyen T., Rao J.S. (2009), A Simplified Adaptive Fence Procedure. Statistics and Probability Letters, 79, 625-629
- Jiang J., Nguyen T., Rao J.S. (2010), Fence Method for Nonparametric Small Area Estimation. Survey Methodology, 36, 1, 3-11

## **Examples**

```
## Not run:
require(fence)
n = 100
set.seed(1234)
x=runif(n,0,3)
y = 1-x+x^2-2*(x-1)^2*(x>1) + 2*(x-2)^2*(x>2) + rnorm(n,sd=.2)
lambda = exp((c(1:60)-30)/3)
data=data.frame(cbind(x,y))
test_NF = fence.NF(full=y~x, data=data, spline='x', ps=c(1:3), qs=c(2,5), B=1000, lambda=lambda)
plot(test_NF)
summary <- summary(test_NF)</pre>
model_sel <- summary[[1]]</pre>
model_sel
lambda_sel <- summary[[2]]</pre>
lambda_sel
## End(Not run)
```

fence.sae

Fence model selection (Small Area Estmation)

# Description

Fence model selection (Small Area Estmation)

## Usage

```
fence.sae(full, data, B = 100, grid = 101, fence = c("adaptive",
   "nonadaptive"), cn = NA, method = c("F-H", "NER"), D = NA,
   REML = FALSE, bandwidth = NA, cpus = parallel::detectCores())
```

# **Arguments**

| full | formular of full model                          |
|------|---|
| data | data  |
| В    | number of bootstrap sample, parametric for lmer |
| grid | grid for c                                      |

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fence fence method to be used, e.g., adaptive, or nonadaptive. It's suggested to choose

nonadaptive procedure if c is known; otherwise nonadaptive must be chosen

cn cn for nonadaptive method Select method to use

D vector containing the D sampling variances of direct estimators for each domain.

The values must be sorted as the variables in formula. Only used in FH model

REML Restricted Maximum Likelihood approach bandwidth bandwidth for kernel smooth function

cpus Number of parallel computers

#### **Details**

In Jiang et. al (2008), the adaptive c value is chosen from the highest peak in the p\* vs. c plot. In Jiang et. al (2009), 95% CI is taken into account while choosing such an adaptive choice of c. In Thuan Nguyen et. al (2014), the adaptive c value is chosen from the first peak. This approach works better in the moderate sample size or weak signal situations. Empirically, the first peak becomes highest peak when sample size increases or signals become stronger

#### Value

models list all model candidates in the model space

B list the number of bootstrap samples that have been used

lack\_of\_fit\_matrix

list a matrix of Qs for all model candidates (in columns). Each row is for each

bootstrap sample

Od\_matrix list a matrix of QM - QM.tilde for all model candidates. Each row is for each

bootrap sample

bandwidth list the value of bandwidth

model\_mat list a matrix of selected models at each c values in grid (in columns). Each row

is for each bootstrap sample

freq\_mat list a matrix of coverage probabilities (frequency/smooth\_frequency) of each

selected models for a given c value (index)

c list the adaptive choice of c value from which the parsimonious model is selected

sel\_model list the selected (parsimonious) model given the adaptive c value

# Note

- The current Fence package focuses on variable selection. However, Fence methods can be used to select other parameters of interest, e.g., tunning parameter, variance-covariance structure, etc.
- The number of bootstrap samples is suggested to be increased, e.g., B=1000 when the sample size is small, or signals are weak

# Author(s)

Jiming Jiang Jianyang Zhao J. Sunil Rao Thuan Nguyen

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#### References

- Jiang J., Rao J.S., Gu Z., Nguyen T. (2008), Fence Methods for Mixed Model Selection. The Annals of Statistics, 36(4): 1669-1692
- Jiang J., Nguyen T., Rao J.S. (2009), A Simplified Adaptive Fence Procedure. Statistics and Probability Letters, 79, 625-629
- Thuan Nguyen, Jie Peng, Jiming Jiang (2014), Fence Methods for Backcross Experiments. Statistical Computation and Simulation, 84(3), 644-662

# Examples

```
require(fence)
library(snow)
### example 1 ####
data("kidney")
data = kidney[-which.max(kidney$x),]
                                      # Delete a suspicious data point #
data$x2 = data$x^2
data$x3 = data$x^3
data$x4 = data$x^4
data$D = data$sqrt.D.^2
plot(data$y ~ data$x)
full = y^x+x^2+x^3+x^4
# Takes more than 5 seconds to run
# testfh = fence.sae(full, data, B=100, fence="adaptive", method="F-H", D = D)
# testfh$sel_model
# testfh$c
```

IF.lm

Invisible Fence model selection (Linear Model)

## **Description**

Invisible Fence model selection (Linear Model)

# Usage

```
IF.lm(full, data, B = 100, cpus = 2, lftype = c("abscoef", "pvalue"))
```

# Arguments

| full   | formula of full model   |
|--------|---|
| data   | data  |
| В      | number of bootstrap sample, parametric for lm                                     |
| cpus   | number of parallel computers  |
| lftype | subtractive measure type, e.g., absolute value of coefficients, p-value, t-value, |
|        | etc.  |

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#### **Details**

This method (Jiang et. al, 2011) is motivated by computational expensive in complex and high dimensional problem. The idea of the method–there is the best model in each dimension (in model space). The boostrapping determines the coverage probability of the selected model in each dimensions. The parsimonious model is the selected model with the highest coverage probabily (except the one for the full model, always probability of 1.)

#### Value

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| TUII  | nst the full model   |
|-------|--|
| В     | list the number of bootstrap samples that have been used                 |
| freq  | list the coverage probabilities of the selected model for each dimension |
| size  | list the number of variables in the parsimonious model                   |
| term  | list variables included in the full model                                |
| model | list the variables selected in-the-order in the parsimonious model       |

@note The current Invisible Fence focuses on variable selection. The current routine is applicable to the case in which the subtractive measure is the absolute value of the coefficients, p-value, t-value. However, the method can be extended to other subtractive measures. See Jiang et. al (2011) for more details.

# Author(s)

Jiming Jiang Jianyang Zhao J. Sunil Rao Thuan Nguyen

list the full model

#### References

- Jiang J., Rao J.S., Gu Z., Nguyen T. (2008), Fence Methods for Mixed Model Selection. The Annals of Statistics, 36(4): 1669-1692
- Jiming Jiang, Thuan Nguyen and J. Sunil Rao (2011), Invisible fence methods and the identification of differentially expressed gene sets. Statistics and Its Interface, Volume 4, 403-415.

```
library(fence)
library(MASS)
library(snow)
r =1234; set.seed(r)
p=10; n=300; rho = 0.6
R = diag(p)
for(i in 1:p){
    for(j in 1:p){
        R[i,j] = rho^(abs(i-j))
    }
}
R = 1*R
x=mvrnorm(n, rep(0, p), R)
colnames(x)=paste('x',1:p, sep='')
X = cbind(rep(1,n),x)
```

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```
tbetas = c(1,1,1,0,1,1,0,1,0,0,0) # non-zero beta 1,2,4,5,7
epsilon = rnorm(n)
y = as.matrix(X)%**tbetas + epsilon
colnames(y) = 'y'
data = data.frame(cbind(X,y))
full = y ~ x1+x2+x3+x4+x5+x6+x7+x8+x9+x10
# Takes greater than 5 seconds (~`17 seconds) to run
# obj1 = IF.lm(full = full, data = data, B = 100, lftype = "abscoef")
# sort((names(obj1$model$coef)[-1]))
# obj2 = IF.lm(full = full, data = data, B = 100, lftype = "pvalue")
# sort(setdiff(names(data[c(-1,-12)]), names(obj2$model$coef)))
```

IF.lmer

Invisible Fence model selection (Linear Mixed Model)

## **Description**

Invisible Fence model selection (Linear Mixed Model)

# Usage

```
IF.lmer(full, data, B = 100, REML = TRUE, method = c("marginal",
   "conditional"), cpus = parallel::detectCores(), lftype = c("abscoef",
   "tvalue"))
```

## **Arguments**

| full   | formula of full model  |
|--------|--|
| data   | data   |
| В      | number of bootstrap sample, parametric for lmer  |
| REML   | Restricted maximum likelihood estimation   |
| method | choose either marginal (e.g., GEE) or conditional model                                |
| cpus   | Number of parallel computers   |
| lftype | subtractive measure type, e.g., absolute value of coefficients, p-value, t-value, etc. |

### **Details**

This method (Jiang et. al, 2011) is motivated by computational expensive in complex and high dimensional problem. The idea of the method—there is the best model in each dimension (in model space). The boostrapping determines the coverage probability of the selected model in each dimensions. The parsimonious model is the selected model with the highest coverage probabily (except the one for the full model, always probability of 1.)

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#### Value

| full  | list the full model  |
|-------|--|
| В     | list the number of bootstrap samples that have been used                 |
| freq  | list the coverage probabilities of the selected model for each dimension |
| size  | list the number of variables in the parsimonious model                   |
| term  | list variables included in the full model                                |
| model | list the variables selected in-the-order in the parsimonious model       |

@note The current Invisible Fence focuses on variable selection. The current routine is applicable to the case in which the subtractive measure is the absolute value of the coefficients, p-value, t-value. However, the method can be extended to other subtractive measures. See Jiang et. al (2011) for more details.

#### Author(s)

Jiming Jiang Jianyang Zhao J. Sunil Rao Thuan Nguyen

#### References

- Jiang J., Rao J.S., Gu Z., Nguyen T. (2008), Fence Methods for Mixed Model Selection. The Annals of Statistics, 36(4): 1669-1692
- Jiming Jiang, Thuan Nguyen and J. Sunil Rao (2011), Invisible fence methods and the identification of differentially expressed gene sets. Statistics and Its Interface, Volume 4, 403-415.

```
require(fence)
library(snow)
library(MASS)
data("X.lmer")
data = data.frame(X.lmer)
# non-zero beta I.col.2, I.col.3a, I.col.3b, V5, V7, V8, V9
beta = matrix(c(0, 1, 1, 1, 1, 0, 0.1, 0.05, 0.25, 0), ncol = 1)
set.seed(1234)
alpha = rep(rnorm(100), each = 3)
mu = alpha + as.matrix(data[,-1]) %*% beta
data$id = as.factor(data$id)
data$y = mu + rnorm(300)
raw = "y ~ (1|id)+I.col.2+I.col.3a+I.col.3b"
for (i in 5:10) {
    raw = paste0(raw, "+V", i)
full = as.formula(raw)
# The following output takes more than 5 seconds (~70 seconds) to run.
# obj1.lmer = IF.lmer(full = full, data = data, B = 100, method="conditional",lftype = "abscoef")
# sort(obj1.lmer$model)
# obj2.lmer = IF.lmer(full = full, data = data, B = 100, method="conditional",lftype = "tvalue")
```

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```
# sort(obj2.lmer$model)

# Similarly, the following scenarios can be run

# obj2.lmer = IF.lmer(full = full, data = data, B = 100, method="conditional",lftype = "tvalue")

# sort(obj2.lmer$model)

# obj1.lm = IF.lmer(full = full, data = data, B = 100, method="marginal", lftype = "abscoef")

# sort(names(obj1.lm$model$coefficients[-1]))

# obj2.lm = IF.lmer(full = full, data = data, B = 100, method="marginal", lftype = "tvalue")

# sort(names(obj2.lm$model$coefficients[-1]))
```

invisiblefence

Invisible Fence model selection

## **Description**

Invisible Fence model selection

# Usage

```
invisiblefence(mf, f, d, lf, bs)
```

#### **Arguments**

| mf | Call function, for example: default calls: function(m, b) eblupFH(formula = m, vardir = D, data = b, method = "FH") |
|----|---|
| f  | Full model  |
| d  | Dimension number  |
| lf | Measures lack of fit using function(res) -res\$fit\$goodness[1]   |
| bs | Bootstrap   |

## **Details**

This method (Jiang et. al, 2011) is motivated by computational expensive in complex and high dimensional problem. The idea of the method–there is the best model in each dimension (in model space). The boostrapping determines the coverage probability of the selected model in each dimensions. The parsimonious model is the selected model with the highest coverage probabily (except the one for the full model, always probability of 1.)

#### Value

| full | list the full model  |
|------|--|
| В    | list the number of bootstrap samples that have been used                 |
| freq | list the coverage probabilities of the selected model for each dimension |
| size | list the number of variables in the parsimonious model                   |

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term list variables included in the full model

model list the variables selected in-the-order in the parsimonious model

@note The current Invisible Fence focuses on variable selection. The current routine is applicable to the case in which the subtractive measure is the absolute value of the coefficients, p-value, t-value. However, the method can be extended to other subtractive measures. See Jiang et. al (2011) for more details.

#### Author(s)

Jiming Jiang Jianyang Zhao J. Sunil Rao Thuan Nguyen

#### References

- Jiang J., Rao J.S., Gu Z., Nguyen T. (2008), Fence Methods for Mixed Model Selection. The Annals of Statistics, 36(4): 1669-1692
- Jiming Jiang, Thuan Nguyen and J. Sunil Rao (2011), Invisible fence methods and the identification of differentially expressed gene sets. Statistics and Its Interface, Volume 4, 403-415.

```
## Not run:
data("X.lmer")
data = data.frame(X.lmer)
beta = matrix(c(0, 1, 1, 1, 1, 0, 0.1, 0.05, 0.25, 0), ncol = 1)
set.seed(1234)
alpha = rep(rnorm(100), each = 3)
mu = alpha + as.matrix(data[,-1]) %*% beta
data$id = as.factor(data$id)
data$y = mu + rnorm(300)
raw = "y ~ (1|id)+I.col.2+I.col.3a+I.col.3b"
for (i in 5:10) {
    raw = paste0(raw, "+V", i)
full = as.formula(raw)
obj1.lmer = IF.lmer(full = full, data = data, B = 100, method="conditional",lftype = "abscoef")
obj1.lmer$model$coefficients
obj2.lmer = IF.lmer(full = full, data = data, B = 100, method="conditional",lftype = "tvalue")
obj2.lmer$model$coefficients
obj1.lm = IF.lmer(full = full, data = data, B = 100, method="marginal", lftype = "abscoef")
obj1.lm$model$coefficients
obj2.lm = IF.lmer(full = full, data = data, B = 100, method="marginal", lftype = "tvalue")
obj2.lm$model$coefficients
## End(Not run)
```

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kidney kidney

# Description

Data used for kidney example

# Usage

kidney

## **Format**

A data frame with 4 variables

nonadaptivefence

Nonadaptive Fence model selection

# Description

Nonadaptive Fence model selection

## Usage

```
nonadaptivefence(mf, f, ms, d, lf, pf, cn)
```

# Arguments

| mf | function for fitting the model                  |
|----|---|
| f  | formula of full model                           |
| ms | list of formula of candidates models            |
| d  | data  |
| lf | measure lack of fit (to minimize)               |
| pf | model selection criteria, e.g., model dimension |
| cn | given a specific c value                        |

## Value

| models      | list all model candidates in the model space |
|-------------|--|
| lack_of_fit | list a vector of Qs for all model candidates |

formula list the model of the selected parsimonious model

sel\_model list the selected (parsimonious) model given the adaptive c value

plot.AF

#### Author(s)

Jiming Jiang Jianyang Zhao J. Sunil Rao Thuan Nguyen

#### References

- Jiang J., Rao J.S., Gu Z., Nguyen T. (2008), Fence Methods for Mixed Model Selection. The Annals of Statistics, 36(4): 1669-1692
- Jiang J., Nguyen T., Rao J.S. (2009), A Simplified Adaptive Fence Procedure. Statistics and Probability Letters, 79, 625-629
- Thuan Nguyen, Jie Peng, Jiming Jiang (2014), Fence Methods for Backcross Experiments. Statistical Computation and Simulation, 84(3), 644-662

## **Examples**

```
## Not run:
require(fence)

#### Example 1 #####
data(iris)
full = Sepal.Length ~ Sepal.Width + Petal.Length + Petal.Width + (1|Species)
test_naf = fence.lmer(full, iris, fence = "nonadaptive", cn = 12)
test_naf$sel_model

## End(Not run)
```

plot.AF

Plot Adaptive Fence model selection

#### **Description**

Plot Adaptive Fence model selection

#### Usage

```
## S3 method for class 'AF'
plot(x = res, ...)
```

## **Arguments**

x Object to be plotted

... Additional arguments. CNot currently used.

20 RF

| ~ T |        | . NF |
|-----|--------|------|
| 1)  | I O T. | INE  |
|     |        |      |

Plot Nonparametric Fence model selection

# **Description**

Plot Nonparametric Fence model selection

## Usage

```
## S3 method for class 'NF'
plot(x = res, ...)
```

# Arguments

x Object to be plotted

... Additional arguments. CNot currently used.

RF

Adaptive Fence model selection (Restricted Fence)

#### **Description**

Adaptive Fence model selection (Restricted Fence)

# Usage

```
RF(full, data, groups, B = 100, grid = 101, bandwidth = NA,
  plot = FALSE, method = c("marginal", "conditional"), id = "id",
  cpus = parallel::detectCores())
```

#### **Arguments**

| full | formula of full | model |
|------|-----------------|-------|
|      |                 |       |

data data

groups A list of formulas of (full) model in each bins (groups) of variables

B number of bootstrap sample, parametric for lmer

grid grid for c

bandwidth bandwidth for kernel smooth function

plot Plot object

method either marginal (GEE) or conditional approach is selected

id Subject or cluster id variablecpus Number of parallel computers

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#### **Details**

In Jiang et. al (2008), the adaptive c value is chosen from the highest peak in the p\* vs. c plot. In Jiang et. al (2009), 95% CI is taken into account while choosing such an adaptive choice of c. In Thuan Nguyen et. al (2014), the adaptive c value is chosen from the first peak. This approach works better in the moderate sample size or weak signal situations. Empirically, the first peak becomes highest peak when sample size increases or signals become stronger

#### Value

| models                        | list all model candidates in the model space   |
|-------------------------------|--|
| В                             | list the number of bootstrap samples that have been used   |
| <pre>lack_of_fit_matrix</pre> |  |
|                               | list a matrix of Qs for all model candidates (in columns). Each row is for each bootstrap sample                         |
| Qd_matrix                     | list a matrix of QM - QM.tilde for all model candidates. Each row is for each bootrap sample                             |
| bandwidth                     | list the value of bandwidth  |
| model_mat                     | list a matrix of selected models at each c values in grid (in columns). Each row is for each bootstrap sample            |
| freq_mat                      | list a matrix of coverage probabilities (frequency/smooth_frequency) of each selected models for a given c value (index) |
| С                             | list the adaptive choice of c value from which the parsimonious model is selected  |
| sel_model                     | list the selected (parsimonious) model given the adaptive c value  |

# Note

bandwidth = (cs[2] - cs[1]) \* 3. So it's chosen as 3 times grid between two c values.

#### References

- Jiang J., Rao J.S., Gu Z., Nguyen T. (2008), Fence Methods for Mixed Model Selection. The Annals of Statistics, 36(4): 1669-1692
- Jiang J., Nguyen T., Rao J.S. (2009), A Simplified Adaptive Fence Procedure. Statistics and Probability Letters, 79, 625-629
- Thuan Nguyen, Jiming Jiang (2012), Restricted fence method for covariate selection in longitudinal data analysis. Biostatistics, 13(2), 303-314
- Thuan Nguyen, Jie Peng, Jiming Jiang (2014), Fence Methods for Backcross Experiments. Statistical Computation and Simulation, 84(3), 644-662

```
## Not run:
r =1234; set.seed(r)
n = 100; p=15; rho = 0.6
beta = c(1,1,1,0,1,1,0,1,0,0,1,0,0,0) # non-zero beta 1,2,3,V6,V7,V9,V12
id = rep(1:n,each=3)
```

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```
V.1 = rep(1, n*3)
I.1 = rep(c(1,-1), each=150)
I.2a = rep(c(0,1,-1),n)
I.2b = rep(c(0,-1,1),n)
x = matrix(rnorm(n*3*11), nrow=n*3, ncol=11)
x = cbind(id, V.1, I.1, I.2a, I.2b, x)
R = diag(3)
for(i in 1:3){
 for(j in 1:3){
   R[i,j] = rho^{(abs(i-j))}
 }
}
e=as.vector(t(mvrnorm(n, rep(0, 3), R)))
y = as.vector(x[,-1]%*%beta) + e
data = data.frame(x,y)
raw = "y \sim V.1 + I.1 + I.2a + I.2b"
for (i in 6:16) { raw = paste0(raw, "+V", i)}; full = as.formula(raw)
bin1="y ~ V.1 + I.1 + I.2a +I.2b"
for (i in 6:8) { bin1 = paste0(bin1, "+V", i)}; bin1 = as.formula(bin1)
bin2="y \sim V9"
for (i in 10:16){ bin2 = paste0(bin2, "+V", i)}; bin2 = as.formula(bin2)
# May take longer than 30 min since there are two stages in this RF procedure
obj1.RF = RF(full = full, data = data, groups = list(bin1,bin2), method="conditional")
obj1.RF$sel_model
obj2.RF = RF(full = full, data = data, groups = list(bin1,bin2), B=100, method="marginal")
obj2.RF$sel_model
## End(Not run)
```

summary.AF

Summary Adaptive Fence model selection

## **Description**

Summary Adaptive Fence model selection

#### Usage

```
## S3 method for class 'AF'
summary(object = res, ...)
```

## **Arguments**

object Object to be summarized

... addition arguments. Not currently used

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summary.NF

Summary Nonparametric Fence model selection

# Description

Summary Nonparametric Fence model selection

# Usage

```
## S3 method for class 'NF'
summary(object = res, ...)
```

# Arguments

object Object to be summarized
... addition arguments. Not currently used

X.lmer

X.lmer

# Description

Data used in the example for X.lmer

# Usage

```
data(X.lmer)
```

## **Format**

A data frame with 10 variables:

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