Package: fastei (via r-universe)

October 23, 2026

Title Methods for "An accurate, fast, and scalable ecological inference algorithm for the R x C case"

Version 0.0.21

Description Estimates the probability matrix for the R×C Ecological Inference problem using the Expectation-Maximization Algorithm with four approximation methods for the E-Step, and an exact method as well. It also provides a bootstrap function to estimate the standard deviation of the estimated probabilities. In addition, it has functions that aggregate rows optimally to have more reliable estimates in cases of having few data points. For comparing the probability estimates of two groups, a Wald test routine is implemented. The library has data from the first round of the Chilean Presidential Election 2021 and can also generate synthetic election data. Methods described in Ubilla Pavez, Pablo; Hermosilla, Daniel; Thraves, Charles (2026) "An accurate, fast, and scalable ecological inference algorithm for the R×C case", Statistics and Computing 36, Article 195 <doi:10.1007/s11222-026-10946-1>.

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`fastei-package` *fastei: Methods for "An accurate, fast, and scalable ecological inference algorithm for the R×C case"*

Description

Package that implements the methods of Ubilla Pavez, P., Hermosilla, D. and Thraves, C. (2026): *"An accurate, fast, and scalable ecological inference algorithm for the R×C case"*. Statistics and Computing, 36, Article 195.

Details

Includes a method (run_em) to solve the R×C ecological inference problem using the EM algorithm with different approximation methods for the E-step. Covariates are supported but not required. Standard errors of the estimated probabilities can be computed via bootstrapping (bootstrap).

It also provides a function that generates synthetic election data (simulate_election) and a function that imports real election data (chile_election_2021) from the Chilean first-round presidential election of 2021.

The setting in which the documentation presents the Ecological Inference problem is an election context where for a set of ballot-boxes we observe (i) the votes obtained by each candidate and (ii) the number of voters of each demographic group (for example, these can be defined by age ranges or sex). See Ubilla Pavez, P., Hermosilla, D. and Thraves, C. (2026): *"An accurate, fast, and scalable ecological inference algorithm for the R×C case"*. Statistics and Computing, 36, Article 195.

The methods to compute the conditional probabilities of the E-Step included in this package are the following:

- **Markov Chain Monte Carlo** (`mcmc`): Performs MCMC to sample vote outcomes for each ballot-box consistent with the observed data. This sample is used to estimate the conditional probability of the *E*-Step.
- **Multivariate Normal PDF** (`mvn_pdf`): Uses the PDF of a Multivariate Normal to approximate the conditional probability.
- **Multivariate Normal CDF** (`mvn_cdf`): Uses the CDF of a Multivariate Normal to approximate the conditional probability.
- **Multinomial** (`mult`): A single Multinomial is used to approximate the sum of Multinomial distributions.
- **Exact** (`exact`): Solves the E-Step exactly using the Total Probability Law, which requires enumerating an exponential number of terms.

On average, the **Multinomial** method is the most efficient and precise. Its precision matches the **Exact** method.

The documentation uses the following notation:

- b: number of ballot-boxes.
- g: number of demographic groups.
- c: number of candidates.
- a: number of aggregated macro-groups.

To learn more about `fastei`, please consult the available vignettes:

```
browseVignettes("fastei")
```

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References

Ubilla Pavez, P., Hermosilla, D. and Thraves, C. (2026): *"An accurate, fast, and scalable ecological inference algorithm for the R×C case"*. Statistics and Computing, 36, Article 195.

See Also

Useful links:

- https://danielhermosilla.github.io/ecological-inference-elections/reference/fastei-package.html
- Report bugs at https://github.com/DanielHermosilla/ecological-inference-elections/issues

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`bootstrap` *Runs a Bootstrap to Estimate the* **Standard Deviation** *of Predicted Probabilities*

Description

This function computes the Expected-Maximization (EM) algorithm "`nboot`" times. It then computes the standard deviation from the `nboot` estimated probability matrices on each component.

Usage

```
bootstrap(
  object = NULL,
  X = NULL,
  W = NULL,
  json_path = NULL,
  nboot = 100,
  allow_mismatch = TRUE,
  seed = NULL,
  ...
)
```

Arguments

`object`	An object of class `eim`, which can be created using the eim function. This parameter should not be used if either (i) `X` and `W` matrices or (ii) `json_path` is supplied. See **Note**.
`X`	A `(b x c)` matrix representing candidate votes per ballot box.
`W`	A `(b x g)` matrix representing group votes per ballot box.
`json_path`	A path to a JSON file containing `X` and `W` fields, stored as nested arrays. It may contain additional fields with other attributes, which will be added to the returned object.
`nboot`	Integer specifying how many times to run the EM algorithm.

allow_mismatch	Boolean, if TRUE, allows a mismatch between the voters and votes for each ballot-box. If FALSE, throws an error if there is a mismatch. By default it is TRUE. See **Notes** for more details.
seed	An optional integer indicating the random seed for the randomized algorithms. This argument is only applicable if initial_prob = "random" or method is either "mcmc" or "mvn_cdf". Aditionally, it sets the random draws of the ballot boxes.
...	Additional arguments passed to the run_em function that will execute the EM algorithm.

Value

Returns an eim object with the sd field containing the estimated standard deviations of the probabilities and the avg_prob field with the average bootstrapped probability matrix. If an eim object is provided, its attributes (see run_em) are retained in the returned object.

Note

This function can be executed using one of three mutually exclusive approaches:

1. By providing an existing eim object.
2. By supplying both input matrices (X and W) directly.
3. By specifying a JSON file (json_path) containing the matrices.

These input methods are **mutually exclusive**, meaning that you must provide **exactly one** of these options. Attempting to provide more than one or none of these inputs will result in an error.

When called with an eim object, the function updates the object with the computed results. If an eim object is not provided, the function will create one internally using either the supplied matrices or the data from the JSON file before executing the algorithm.

If there are ballot-boxes with mismatch between W and X, and allow_mismatch = TRUE, then: if method = "exact", at each ballot-box with mismatch D'Hont is applied to add or remove the necessary voters from (W) so that its total match the total number of votes (X); if method is "mvn_pdf", "mvn_cdf" or "mcmc", the number of voters (W) of the ballot-box with mismatch is scaled to match its total number of votes (X).

See Also

The eim object and run_em implementation.

Examples

```
# Example 1: Using an 'eim' object directly
simulations <- simulate_election(
    num_ballots = 200,
    num_candidates = 5,
    num_groups = 3,
)

model <- eim(X = simulations$X, W = simulations$W)
```

```
model <- bootstrap(
    object = model,
    nboot = 30,
    method = "mult",
    maxiter = 500,
    verbose = FALSE,
)

# Access standard deviation throughout 'model'
print(model$sd)


# Example 2: Providing 'X' and 'W' matrices directly
model <- bootstrap(
    X = simulations$X,
    W = simulations$W,
    nboot = 15,
    method = "mvn_pdf",
    maxiter = 100,
    maxtime = 5,
    param_threshold = 0.01,
    allow_mismatch = FALSE
)

print(model$sd)


# Example 3: Using a JSON file as input

## Not run:
model <- bootstrap(
    json_path = "path/to/election_data.json",
    nboot = 70,
    method = "mult",
)

print(model$sd)

## End(Not run)
```

`chile_election_2021` *Chilean 2021 First Round Presidential Election*

Description

This dataset contains the results of the first round of the 2021 Chilean presidential elections. It provides 9 possible voting options (7 candidates, blank, and null). Each ballot-box is identified by its id (`BALLOT.BOX`) and an electoral circumscription (`ELECTORAL.DISTRICT`). Additionally, it provides demographic information on voters' age range for each ballot box.

Usage

```
data("chile_election_2021")
```

Format

A data frame with 46,639 rows and 14 variables:

`REGION` The region of the `ELECTORAL.DISTRICT`

`ELECTORAL.DISTRICT` The electoral circumscription of the ballot box.

`BALLOT.BOX` An identifier for the ballot box within the `ELECTORAL.DISTRICT`.

`C1` The number of votes cast for the candidate *Gabriel Boric*.

`C2` The number of votes cast for the candidate *José Antonio Kast*.

`C3` The number of votes cast for the candidate *Yasna Provoste*.

`C4` The number of votes cast for the candidate *Sebastián Sichel*.

`C5` The number of votes cast for the candidate *Eduardo Artés*.

`C6` The number of votes cast for the candidate *Marco Enríquez-Ominami*.

`C7` The number of votes cast for the candidate *Franco Parisi*.

`BLANK.VOTES` The number of blank votes.

`NULL.VOTES` The number of null votes.

`X18.19` Number of voters aged 18–19.

`X20.29` Number of voters aged 20–29.

`X30.39` Number of voters aged 30–39.

`X40.49` Number of voters aged 40–49.

`X50.59` Number of voters aged 50–59.

`X60.69` Number of voters aged 60–69.

`X70.79` Number of voters aged 70–79.

`X80.` Number of voters aged 80 and older.

`MISMATCH` Boolean that takes value `TRUE` if the ballot-box has a mismatch between the total number of votes and the total number of voters. If this is not the case, its value is `FALSE`.

`F` Number of female voters in the ballot box.

`M` Number of male voters in the ballot box.

Source

Chilean Electoral Service (SERVEL)

Examples

```
data("chile_election_2021")
head(chile_election_2021)
```

eim *S3 Object for the Expectation-Maximization Algorithm*

Description

This constructor creates an `eim` S3 object, either by using matrices `X` and `W` directly or by reading them from a JSON file. Each `eim` object encapsulates the data (votes for candidates and demographic groups) required by the underlying Expectation-Maximization algorithm.

Usage

```
eim(X = NULL, W = NULL, json_path = NULL)
```

Arguments

`X`	A `(b x c)` matrix representing candidate votes per ballot box.
`W`	A `(b x g)` matrix representing group votes per ballot box.
`json_path`	A path to a JSON file containing `X` and `W` fields, stored as nested arrays. It may contain additional fields with other attributes, which will be added to the returned object.

Details

If `X` and `W` are directly supplied, they must match the dimensions of ballot boxes `(b)`. Alternatively, if `json_path` is provided, the function expects the JSON file to contain elements named `"X"` and `"W"` under the top-level object. This two approaches are **mutually exclusable**, yielding an error otherwise.

Internally, this function also initializes the corresponding instance within the low-level (C-based) API, ensuring the data is correctly registered for further processing by the EM algorithm.

Value

A list of class `eim` containing:

`X` The candidate votes matrix `(b x c)`.

`W` The group votes matrix `(b x g)`.

Methods

In addition to this constructor, the "eim" class provides several S3 methods for common operations. Some of these methods are fully documented, while others are ommited due to its straightfoward implementantion. The available methods are:

- `run_em` - Runs the EM algorithm.
- `bootstrap` - Estimates the standard deviation.
- `save_eim` - Saves the object to a file.

- get_agg_proxy - Estimates an ideal group aggregation given their standard deviations.
- get_agg_opt - Estimates an ideal group aggregation among all combinations, given the log-likelihood.
- plot.eim - Plots the probability matrix.
- print.eim - Print info about the object.
- summary.eim - Summarize the object.
- as.matrix.eim - Returns the probability matrix.
- logLik.eim - Returns the final log-likelihood, or evaluates log-likelihood at a fixed probability matrix.

Note

A way to generate synthetic data for X and W is by using the simulate_election function. See Example 2 below.

Examples

```
# Example 1: Create an eim object from a JSON file
## Not run:
model1 <- eim(json_path = "path/to/file.json")

## End(Not run)

# Example 2: Use simulate_election with optional parameters, then create an eim object
# from matrices

# Simulate data for 500 ballot boxes, 4 candidates and 5 groups
sim_result <- simulate_election(
    num_ballots = 500,
    num_candidates = 3,
    num_groups = 5,
    group_proportions = c(0.2, 0.2, 0.4, 0.1, 0.1)
)

model2 <- eim(X = sim_result$X, W = sim_result$W)

# Example 3: Create an object from a user defined matrix with 8 ballot boxes,
# 2 candidates and 7 groups.

x_mat <- matrix(c(
    57, 90,
    60, 84,
    43, 102,
    72, 71,
    63, 94,
    52, 80,
    60, 72,
    54, 77
), nrow = 8, ncol = 2, byrow = TRUE)
```

```
w_mat <- matrix(c(
    10, 15, 25, 21, 10, 40, 26,
    11, 21, 37, 32, 8, 23, 12,
    17, 12, 43, 27, 12, 19, 15,
    20, 18, 25, 15, 22, 17, 26,
    21, 19, 27, 16, 23, 22, 29,
    18, 16, 20, 14, 19, 22, 23,
    10, 15, 21, 18, 20, 16, 32,
    12, 17, 19, 22, 15, 18, 28
), nrow = 8, ncol = 7, byrow = TRUE)

model3 <- eim(X = x_mat, W = w_mat)
```

`get_agg_opt` *Runs the EM algorithm* **over all possible group aggregating**, *returning the one with higher likelihood while constraining the standard deviation of the probabilities.*

Description

This function estimates the voting probabilities (computed using run_em) by trying all group aggregations (of adjacent groups), choosing the one that achieves the higher likelihood as long as the standard deviation (computed using bootstrap) of the estimated probabilities is below a given threshold. See **Details** for more informacion on adjacent groups.

Usage

```
get_agg_opt(
  object = NULL,
  X = NULL,
  W = NULL,
  json_path = NULL,
  sd_statistic = "maximum",
  sd_threshold = 0.05,
  method = "mult",
  nboot = 100,
  allow_mismatch = TRUE,
  seed = NULL,
  ...
)
```

Arguments

`object`	An object of class `eim`, which can be created using the eim function. This parameter should not be used if either (i) `X` and `W` matrices or (ii) `json_path` is supplied. See **Note** in run_em.
`X`	A `(b x c)` matrix representing candidate votes per ballot box.

`W`	A `(b x g)` matrix representing group votes per ballot box.
`json_path`	A path to a JSON file containing `X` and `W` fields, stored as nested arrays. It may contain additional fields with other attributes, which will be added to the returned object.
`sd_statistic`	String indicates the statistic for the standard deviation `(g x c)` matrix for the stopping condition, i.e., the algorithm stops when the statistic is below the threshold. It can take the value `maximum`, in which case computes the maximum over the standard deviation matrix, or `average`, in which case computes the average.
`sd_threshold`	Numeric with the value to use as a threshold for the statistic (`sc_statistic`) of the standard deviation of the estimated probabilities. Defaults to 0.05.
`method`	An optional string specifying the method used for estimating the E-step. Valid options are: • `mult`: The default method, using a single sum of Multinomial distributions. • `mvn_cdf`: Uses a Multivariate Normal CDF distribution to approximate the conditional probability. • `mvn_pdf`: Uses a Multivariate Normal PDF distribution to approximate the conditional probability. • `mcmc`: Uses MCMC to sample vote outcomes. This is used to estimate the conditional probability of the E-step. • `exact`: Solves the E-step using the Total Probability Law.
`nboot`	Integer specifying how many times to run the EM algorithm.
`allow_mismatch`	Boolean, if `TRUE`, allows a mismatch between the voters and votes for each ballot-box. If `FALSE`, throws an error if there is a mismatch. By default it is `TRUE`. See **Notes** in run_em for more details.
`seed`	An optional integer indicating the random seed for the randomized algorithms. This argument is only applicable if `initial_prob = "random"` or `method` is either `"mcmc"` or `"mvn_cdf"`. Aditionally, it sets the random draws of the ballot boxes.
`...`	Additional arguments passed to the run_em function that will execute the EM algorithm.

Details

Groups of consecutive column indices in the matrix `W` are considered adjacent. For example, consider the following seven groups defined by voters' age ranges: 20-29, 30-39, 40-49, 50-59, 60-69, 70-79, and 80+. A possible group aggregation can be a macro-group composed of the three following age ranges: 20-39, 40-59, and 60+. Since there are multiple group aggregations, the method evaluates all possible group aggregations (merging only adjacent groups).

Value

It returns an eim object with the same attributes as the output of run_em, plus the attributes:

- **sd**: A `(a x c)` matrix with the standard deviation of the estimated probabilities computed with bootstrapping. Note that `a` denotes the number of macro-groups of the resulting group aggregation, it should be between `1` and `g`.

- **nboot**: Number of samples used for the bootstrap method.
- **seed**: Random seed used (if specified).
- **sd_statistic**: The statistic used as input.
- **sd_threshold**: The threshold used as input.
- **group_agg**: Vector with the resulting group aggregation. See **Examples** for more details.

Additionally, it will create the `W_agg` attribute with the aggregated groups, along with the attributes corresponding to running run_em with the aggregated groups.

Examples

```
# Example 1: Using a simulated instance
simulations <- simulate_election(
    num_ballots = 20,
    num_candidates = 3,
    num_groups = 8,
    seed = 42
)

result <- get_agg_opt(
    X = simulations$X,
    W = simulations$W,
    sd_threshold = 0.05,
    seed = 42
)

result$group_agg # c(3,8)
# This means that the resulting group aggregation consists of
# two macro-groups: one that includes the original groups 1, 2, and 3;
# the remaining one with groups 4, 5, 6, 7 and 8.


# Example 2: Getting an unfeasible result
result2 <- get_agg_opt(
    X = simulations$X,
    W = simulations$W,
    sd_threshold = 0.001
)

result2$group_agg # Error
result2$X # Input candidates' vote matrix
result2$W # Input group-level voter matrix
```

`get_agg_proxy` *Runs the EM algorithm aggregating adjacent groups, maximizing the variability of macro-group allocation in ballot boxes.*

Description

This function estimates the voting probabilities (computed using run_em) aggregating adjacent groups so that the estimated probabilities' standard deviation (computed using bootstrap) is below a given threshold. See **Details** for more information.

Usage

```
get_agg_proxy(
  object = NULL,
  X = NULL,
  W = NULL,
  json_path = NULL,
  sd_statistic = "maximum",
  sd_threshold = 0.05,
  method = "mult",
  feasible = TRUE,
  nboot = 100,
  allow_mismatch = TRUE,
  seed = NULL,
  ...
)
```

Arguments

`object`	An object of class `eim`, which can be created using the eim function. This parameter should not be used if either (i) `X` and `W` matrices or (ii) `json_path` is supplied. See **Note** in run_em.
`X`	A `(b x c)` matrix representing candidate votes per ballot box.
`W`	A `(b x g)` matrix representing group votes per ballot box.
`json_path`	A path to a JSON file containing `X` and `W` fields, stored as nested arrays. It may contain additional fields with other attributes, which will be added to the returned object.
`sd_statistic`	String indicates the statistic for the standard deviation `(g x c)` matrix for the stopping condition, i.e., the algorithm stops when the statistic is below the threshold. It can take the value `maximum`, in which case computes the maximum over the standard deviation matrix, or `average`, in which case computes the average.
`sd_threshold`	Numeric with the value to use as a threshold for the statistic (`sc_statistic`) of the standard deviation of the estimated probabilities. Defaults to 0.05.
`method`	An optional string specifying the method used for estimating the E-step. Valid options are: • `mult`: The default method, using a single sum of Multinomial distributions. • `mvn_cdf`: Uses a Multivariate Normal CDF distribution to approximate the conditional probability. • `mvn_pdf`: Uses a Multivariate Normal PDF distribution to approximate the conditional probability.

- `mcmc`: Uses MCMC to sample vote outcomes. This is used to estimate the conditional probability of the E-step.
- `exact`: Solves the E-step using the Total Probability Law.

`feasible` Logical indicating whether the returned matrix must strictly satisfy the `sd_threshold`. If `TRUE`, no output is returned if the method does not find a group aggregation whose standard deviation statistic is below the threshold. If `FALSE` and the latter holds, it returns the group aggregation obtained from the DP with the the lowest standard deviation statistic. See **Details** for more information. Default is `TRUE`.

`nboot` Integer specifying how many times to run the EM algorithm.

`allow_mismatch` Boolean, if `TRUE`, allows a mismatch between the voters and votes for each ballot-box. If `FALSE`, throws an error if there is a mismatch. By default it is `TRUE`. See **Notes** in run_em for more details.

`seed` An optional integer indicating the random seed for the randomized algorithms. This argument is only applicable if `initial_prob = "random"` or `method` is either `"mcmc"` or `"mvn_cdf"`. Aditionally, it sets the random draws of the ballot boxes.

`...` Additional arguments passed to the run_em function that will execute the EM algorithm.

Details

Groups need to have an order relation so that adjacent groups can be merged. Groups of consecutive column indices in the matrix W are considered adjacent. For example, consider the following seven groups defined by voters' age ranges: 20-29, 30-39, 40-49, 50-59, 60-69, 70-79, and 80+. A possible group aggregation can be a macro-group composed of the three following age ranges: 20-39, 40-59, and 60+. Since there are multiple group aggregations, even for a fixed number of macro-groups, a Dynamic Program (DP) mechanism is used to find the group aggregation that maximizes the sum of the standard deviation of the macro-groups proportions among ballot boxes for a specific number of macro-groups. If no group aggregation standard deviation statistic meets the threshold condition, `NULL` is returned.

To find the best group aggregation, the function runs the DP iteratively, starting with all groups (this case is trivial since the group aggregation is such that all macro-groups match exactly the original groups). If the standard deviation statistic (`sd_statistic`) is below the threshold (`sd_threshold`), it stops. Otherwise, it runs the DP such that the number of macro-groups is one unit less than the original number of macro-groups. If the standard deviation statistic is below the threshold, it stops. This continues until either the algorithm stops, or until no group aggregation obtained by the DP satisfies the threshold condition. If the former holds, then the last group aggregation obtained (before stopping) is returned; while if the latter holds, then no output is returned unless the user sets the input parameter `feasible=FALSE`, in which case it returns the group aggregation that has the least standard deviation statistic, among the group-aggregations obtained from the DP.

Value

It returns an eim object with the same attributes as the output of run_em, plus the attributes:

- **sd**: A `(a x c)` matrix with the standard deviation of the estimated probabilities computed with bootstrapping. Note that `a` denotes the number of macro-groups of the resulting group aggregation, it should be between 1 and g.

- **nboot**: Number of samples used for the bootstrap method.
- **seed**: Random seed used (if specified).
- **sd_statistic**: The statistic used as input.
- **sd_threshold**: The threshold used as input.
- **is_feasible**: Boolean indicating whether the statistic of the standard deviation matrix is below the threshold.
- **group_agg**: Vector with the resulting group aggregation. See **Examples** for more details.

Additionally, it will create the `W_agg` attribute with the aggregated groups, along with the attributes corresponding to running run_em with the aggregated groups.

See Also

The eim object and run_em implementation.

Examples

```
# Example 1: Using a simulated instance
simulations <- simulate_election(
    num_ballots = 400,
    num_candidates = 3,
    num_groups = 6,
    group_proportions = c(0.4, 0.1, 0.1, 0.1, 0.2, 0.1),
    lambda = 0.7,
    seed = 42
)

result <- get_agg_proxy(
    X = simulations$X,
    W = simulations$W,
    sd_threshold = 0.015,
    seed = 42
)

result$group_agg # c(2 6)
# This means that the resulting group aggregation is conformed by
# two macro-groups: one that has the original groups 1 and 2; and
# a second that has the original groups 3, 4, 5, and 6.

# Example 2: Using the chilean election results
data(chile_election_2021)

niebla_df <- chile_election_2021[chile_election_2021$ELECTORAL.DISTRICT == "NIEBLA", ]

# Create the X matrix with selected columns
X <- as.matrix(niebla_df[, c("C1", "C2", "C3", "C4", "C5", "C6", "C7")])

# Create the W matrix with selected columns
W <- as.matrix(niebla_df[, c(
    "X18.19", "X20.29",
    "X30.39", "X40.49",
```

```
    "X50.59", "X60.69",
    "X70.79", "X80."
)])

solution <- get_agg_proxy(
    X = X, W = W,
    allow_mismatch = TRUE, sd_threshold = 0.03,
    sd_statistic = "average", seed = 42
)

solution$group_agg # c(3, 4, 5, 6, 8)
# This means that the resulting group aggregation consists of
# five macro-groups: one that includes the original groups 1, 2, and 3;
# three singleton groups (4, 5, and 6); and one macro-group that includes groups 7 and 8.
```

`get_eim_chile` *Extracts voting and demographic data matrices for a given electoral district in Chile.*

Description

This function retrieves the voting results and demographic group counts for a given electoral district from the 2021 Chilean election dataset included in this package. The function returns an `eim` object that can be directly used in `run_em` or other estimation functions.

Usage

```
get_eim_chile(
  elect_district = NULL,
  region = NULL,
  merge_blank_null = TRUE,
  remove_mismatch = FALSE,
  use_sex = FALSE
)
```

Arguments

`elect_district`	A string indicating the name of the electoral district to extract (e.g., "NIEBLA"). See **Note**.
`region`	A string indicating the name of the region to extract (e.g, "DE TARAPACA"). See **Note**.
`merge_blank_null`	Logical indicating whether blank and null votes should be merged into a single column. Defaults to `TRUE`.
`remove_mismatch`	Logical indicating whether to remove ballot boxes with mismatched vote totals (where `MISMATCH == TRUE`). Defaults to `FALSE`.
`use_sex`	Logical indicating whether to use the sex from the voters instead of the age ranges. Defaults to `FALSE`.

Details

The function builds the `X` matrix using the number of votes per candidate, and the `W` matrix using the number of voters in each demographic group (e.g., age ranges). Optionally, blank and null votes can be merged into a single additional column (considered as another candidate).

Additionally, ballot boxes where the number of votes does not match the number of registered voters (i.e., those where `MISMATCH == TRUE`) can be excluded from the dataset by setting `remove_mismatch = TRUE`.

Value

An `eim` object with the following attributes:

- **X**: A matrix `(b x c)` with the number of votes per candidate (including a column for blank + null votes if `merge_blank_null = TRUE`).
- **W**: A matrix `(b x g)` with the number of voters per group (e.g., age ranges) for each ballot box.

This object can be passed to functions like `run_em` or `get_agg_proxy` for estimation and group aggregation. See **Example**.

Only one parameter is accepted among `elect_district` and `region`. If either both parameters are given, it will return an error. If neither of these two inputs is supplied, it will return an `eim` object with an aggregation corresponding to the whole dataset. To see all electoral districts and regions names, see the function chile_election_2021.

See Also

chile_election_2021

Examples

```
# Load data and create an eim object for the electoral district of "NIEBLA"
eim_obj <- get_eim_chile(elect_district = "NIEBLA", remove_mismatch = FALSE)

# Use it to run the EM algorithm
result <- run_em(eim_obj, allow_mismatch = TRUE)

# Use it with group aggregation
agg_result <- get_agg_proxy(
    object = eim_obj,
    sd_threshold = 0.05,
    allow_mismatch = TRUE,
    seed = 123
)

agg_result$group_agg
```

plot.eim *Plot estimated probabilities*

Description

Plots the estimated probabilities as pie charts using ggplot2, one per row of the probability matrix. Each slice displays its percentage label.

Usage

```
## S3 method for class 'eim'
plot(
  x,
  title = "Estimated probabilities",
  legend_title = "Candidates",
  color_scale = NULL,
  min_pct = 3,
  pies_per_row = NULL,
  ...
)
```

Arguments

x	An "eim" object.
title	Title for the plot.
legend_title	Title for the legend.
color_scale	A vector of colors or a palette for the candidates.
min_pct	Minimum percentage required to display a label.
pies_per_row	Number of pie charts to display per row. Defaults to ceiling(sqrt(G)), where G is the number of groups.
...	Additional arguments that are ignored.

Value

Returns a ggplot2 object representing the pie charts.

Examples

```
sim <- simulate_election(
    num_ballots = 100,
    num_candidates = 4,
    num_groups = 5,
    ballot_voters = rep(40, 100),
    seed = 42
)
fit <- run_em(sim, maxiter = 5)
```

```
plot(fit, title = "Estimated probabilities", legend_title = "Candidates", min_pct = 7)
```

---

run_em *Compute the Expected-Maximization Algorithm*

Description

Executes the Expectation-Maximization (EM) algorithm indicating the approximation method to use in the E-step. Certain methods may require additional arguments, which can be passed through ... (see fastei-package for more details).

Usage

```
run_em(
  object = NULL,
  X = NULL,
  W = NULL,
  json_path = NULL,
  method = "mult",
  initial_prob = "group_proportional",
  allow_mismatch = TRUE,
  maxiter = 1000,
  miniter = 0,
  maxtime = 3600,
  param_threshold = 0.001,
  ll_threshold = as.double(-Inf),
  compute_ll = TRUE,
  seed = NULL,
  verbose = FALSE,
  group_agg = NULL,
  mcmc_samples = 1000,
  mcmc_stepsize = 3000,
  mvncdf_method = "genz",
  mvncdf_error = 0.001,
  mvncdf_samples = 5000,
  adjust_prob_cond_method = "project_lp",
  adjust_prob_cond_every = FALSE,
  scale_factor = 1,
  symmetric = FALSE,
  symmetric_weight_method = "joint",
  ...
)
```

Arguments

`object`	An object of class `eim`, which can be created using the eim function. This parameter should not be used if either (i) `X` and `W` matrices or (ii) `json_path` is supplied. See **Note**.
`X`	A `(b x c)` matrix representing candidate votes per ballot box.
`W`	A `(b x g)` matrix representing group votes per ballot box.
`json_path`	A path to a JSON file containing `X` and `W` fields, stored as nested arrays. It may contain additional fields with other attributes, which will be added to the returned object.
`method`	An optional string specifying the method used for estimating the E-step. Valid options are: • `mult`: The default method, using a single sum of Multinomial distributions. • `mvn_cdf`: Uses a Multivariate Normal CDF distribution to approximate the conditional probability. • `mvn_pdf`: Uses a Multivariate Normal PDF distribution to approximate the conditional probability. • `mcmc`: Uses MCMC to sample vote outcomes. This is used to estimate the conditional probability of the E-step. • `exact`: Solves the E-step using the Total Probability Law. For a detailed description of each method, see fastei-package and **References**.
`initial_prob`	An optional string specifying the method used to obtain the initial probability. Accepted values are: • `uniform`: Assigns equal probability to every candidate within each group. • `proportional`: Assigns probabilities to each group based on the proportion of candidates votes. • `group_proportional`: Computes the probability matrix by taking into account both group and candidate proportions. This is the default method. • `random`: Use randomized values to fill the probability matrix.
`allow_mismatch`	Boolean, if `TRUE`, allows a mismatch between the voters and votes for each ballot-box. If `FALSE`, throws an error if there is a mismatch. By default it is `TRUE`. See **Notes** for more details.
`maxiter`	An optional integer indicating the maximum number of EM iterations. The default value is `1000`.
`miniter`	An optional integer indicating the minimum number of EM iterations. The default value is `0`.
`maxtime`	An optional numeric specifying the maximum running time (in seconds) for the algorithm. This is checked at every iteration of the EM algorithm. The default value is `3600`, which corresponds to an hour.
`param_threshold`	An optional numeric value indicating the maximum Frobenius norm of the difference between consecutive probability matrices required to stop iterating. The default value is `0.001`. Note that the algorithm will stop if either `ll_threshold` **or** `param_threshold` is accomplished.

ll_threshold An optional numeric value indicating the minimum difference between consecutive log-likelihood values to stop iterating. The default value is inf, essentially deactivating the threshold. Note that the algorithm will stop if either ll_threshold **or** param_threshold is accomplished.

compute_ll An optional boolean indicating whether to compute the log-likelihood at each iteration. The default value is TRUE.

seed An optional integer indicating the random seed for the randomized algorithms. This argument is only applicable if initial_prob = "random" or method is either "mcmc" or "mvn_cdf".

verbose An optional boolean indicating whether to print informational messages during the EM iterations. The default value is FALSE.

group_agg An optional vector of increasing integers from 1 to the number of columns in W, specifying how to aggregate groups in W before running the EM algorithm. Each value represents the highest column index included in each aggregated group. For example, if W has four columns, group_agg = c(2, 4) indicates that columns 1 and 2 should be combined into one group, and columns 3 and 4 into another. Defaults to NULL, in which case no group aggregation is performed.

mcmc_samples An optional integer indicating the number of samples to generate for the **MCMC** method. This parameter is only relevant when method = "mcmc". The default value is 1000.

mcmc_stepsize An optional integer specifying the step size for the mcmc algorithm. This parameter is only applicable when method = "mcmc" and will be ignored otherwise. The default value is 3000.

mvncdf_method An optional string specifying the method used to estimate the mvn_cdf method via a Monte Carlo simulation. Accepted values are genz and genz2, with genz set as the default. This parameter is only applicable when method = "mvn_cdf". See **References** for more details.

mvncdf_error An optional numeric value defining the error threshold for the Monte Carlo simulation when estimating the mvn_cdf method. The default value is 1e-6. This parameter is only relevant when method = "mvn_cdf".

mvncdf_samples An optional integer specifying the number of Monte Carlo samples for the mvn_cdf method. The default value is 5000. This argument is only applicable when method = "mvn_cdf".

adjust_prob_cond_method
An optional string indicating the method used to adjust the conditional probabilities so that, for each candidate, the sum of the products of the number of voters and the conditional probabilities across groups equals the number of votes obtained by that candidate. It can take the following values: "" if no adjustment is made; "lp" if the adjustment is based on a linear program that penalizes using the L1 norm; "kl" if the estimated-count table is projected in KL divergence using iterative proportional fitting; or "project_lp" if it is projected onto the accounting-identity hyperplane and an LP is solved when a probability is negative. The default is "lp" for Joint-EM (symmetric = TRUE and symmetric_weight_method = "joint") and "project_lp" otherwise. "project_lp" is not supported in Joint-EM: requesting it issues a warning and runs "lp" instead. In the other modes, it retains the projection-plus-LP adjustment.

`adjust_prob_cond_every`
: An optional boolean indicating whether to adjust the conditional probability on every iteration (if `TRUE`), or only at the conditional probabilities obtained at the end of the EM algorithm (if `FALSE`, this is the default). This parameter applies only if `adjust_prob_conditional_method` is `lp`, `kl`, or `project_lp`.

`scale_factor`
: An optional numeric value used to scale down the `X` and `W` matrices before executing the EM algorithm. This scaling can help improve performance when dealing with large vote counts. For example if `scale_factor = 2` all elements of `X` and `W` are divided by two and rounded. The default value is `1`, which means no scaling is applied. In case the scaling results in mismatch between `W` and `X`, ensure that `allow_mismatch = TRUE`.

`symmetric`
: A boolean indicating whether to perform a symmetric estimation. If `TRUE`, the algorithm runs twice: first estimating the probabilities of candidates given groups, and then estimating the probabilities of groups given candidates. The final probabilities are obtained by combining both directions using `symmetric_weight_method` (`"joint"` by default). The default value is `FALSE`.

`symmetric_weight_method`
: Character string indicating how to combine both directions when `symmetric = TRUE`. Valid values are `"joint"` (default behavior: joint EM where forward/reverse E-steps are averaged each iteration using equal weights), `"average"`, `"delta_ll"` (weights based on the relative likelihood gaps), and `"mae_inverse"` (weights based on reconstruction errors).

`...`
: Added for compability

Value

The function returns an `eim` object with the function arguments and the following attributes:

prob The estimated global probability matrix `(g x c)`.

cond_prob A `(g x c x b)` 3d-array with the probability that at each ballot-box a voter of each group voted for each candidate, given the observed outcome at the particular ballot-box.

expected_outcome A `(g x c x b)` 3d-array with the expected votes cast for each ballot-box.

logLik The log-likelihood value from the last iteration.

iterations The total number of iterations performed by the EM algorithm.

time The total execution time of the algorithm in seconds.

status The final status ID of the algorithm upon completion:

- `0`: Converged
- `1`: Maximum time reached.
- `2`: Maximum iterations reached.

message The finishing status displayed as a message, matching the status ID value.

method The method for estimating the conditional probability in the E-step.

Aditionally, it will create `mcmc_samples` and `mcmc_stepsize` parameters if the specified `method = "mcmc"`, or `mvncdf_method`, `mvncdf_error` and `mvncdf_samples` if `method = "mvn_cdf"`.

Also, if the eim object supplied is created with the function simulate_election, it also returns the real probability and unobserved votes with the name `real_prob` and `outcome` respectively. See simulate_election.

If `group_agg` is different than `NULL`, two values are returned: `W_agg` a `(b x a)` matrix with the number of voters of each aggregated group o each ballot-box, and `group_agg` the same input vector.

Furthermore, if `symmetric = TRUE`, the following additional attributes are included:

prob_inv The estimated probability matrix `(c x g)`, obtained by swapping `X` and `W`, when the symmetric scheme performs an explicit reverse run (for example `"average"`, `"delta_ll"`, and `"mae_inverse"`).

cond_prob_inv A `(c x g x b)` 3d-array with the probability that at each ballot-box a voter of each candidate voted for each group, given the observed outcome at the particular ballot-box, when the symmetric scheme performs an explicit reverse run.

If `symmetric_weight_method = "delta_ll"` and both `logLik` values are available, the object also includes `LL_ind`, `LL_rev_ind`, `dLL`, `dLL_rev`, `nu`, `nu_rev`, and `symmetric_weights`. If `symmetric_weight_method = "mae_inverse"`, the object also includes `err_forward`, `err_inverse`, and `symmetric_weights`. Under this argument, the conditional probabilities will be obtained by dividing new expected outcomes by `W`. The probabilities will be calculated by performing an M-step.

Note

This function can be executed using one of three mutually exclusive approaches:

1. By providing an existing `eim` object.
2. By supplying both input matrices (`X` and `W`) directly.
3. By specifying a JSON file (`json_path`) containing the matrices.

These input methods are **mutually exclusive**, meaning that you must provide **exactly one** of these options. Attempting to provide more than one or none of these inputs will result in an error.

When called with an `eim` object, the function updates the object with the computed results. If an `eim` object is not provided, the function will create one internally using either the supplied matrices or the data from the JSON file before executing the algorithm.

If there are ballot-boxes with mismatch between `W` and `X`, and `allow_mismatch = TRUE`, then: if `method = "exact"`, at each ballot-box with mismatch D'Hont is applied to add or remove the necessary voters from (`W`) so that its total match the total number of votes (`X`); if method is `"mvn_pdf"`, `"mvn_cdf"` or `"mcmc"`, the number of voters (`W`) of the ballot-box with mismatch is scaled to match its total number of votes (`X`).

References

Ubilla Pavez, P., Hermosilla, D. and Thraves, C. (2026): *"An accurate, fast, and scalable ecological inference algorithm for the R×C case"*. Statistics and Computing, 36, Article 195.. Aditionally, the MVN CDF is computed by the methods introduced in Genz, A. (2000). Numerical computation of multivariate normal probabilities. *Journal of Computational and Graphical Statistics*

See Also

The eim object implementation.

Examples

```
# Example 1: Compute the Expected-Maximization with default settings
simulations <- simulate_election(
    num_ballots = 300,
    num_candidates = 5,
    num_groups = 3,
)
model <- eim(simulations$X, simulations$W)
model <- run_em(model) # Returns the object with updated attributes

# Example 2: Compute the Expected-Maximization using the mvn_pdf method
model <- run_em(
    object = model,
    method = "mvn_pdf",
)

# Example 3: Run the mvn_cdf method with default settings
model <- run_em(object = model, method = "mvn_cdf")

## Not run:
# Example 4: Perform an Exact estimation using user-defined parameters

run_em(
    json_path = "a/json/file.json",
    method = "exact",
    initial_prob = "uniform",
    maxiter = 10,
    maxtime = 600,
    param_threshold = 1e-3,
    ll_threshold = 1e-5,
    verbose = TRUE
)

## End(Not run)
```

---

save_eim *Save an* eim *object to a file*

Description

This function saves an `eim` object to a specified file format. Supported formats are **RDS**, **JSON**, and **CSV**. The function dynamically extracts and saves all available attributes when exporting to JSON. If the `prob` field exists, it is saved when using CSV; otherwise, it yields an error.

Usage

```
save_eim(object, filename, ...)
```

Arguments

`object`	An `eim` object.
`filename`	A character string specifying the file path, including the desired file extension (`.rds`, `.json`, or `.csv`).
`...`	Additional arguments (currently unused but included for compatibility).

Details

- If the file extension is **RDS**, the entire object is saved using `saveRDS()`.
- If the file extension is **JSON**, all available attributes of the object are stored in JSON format.
- If the file extension is **CSV**:
  - If the object contains a `prob` field, only that field is saved as a CSV.
  - Otherwise, returns an error.

Value

The function does not return anything explicitly but saves the object to the specified file.

See Also

The eim object implementation.

Examples

```
model <- eim(X = matrix(1:9, 3, 3), W = matrix(1:9, 3, 3))

model <- run_em(model)

td <- tempdir()
out_rds <- file.path(td, "model_results.rds")
out_json <- file.path(td, "model_results.json")
out_csv <- file.path(td, "model_results.csv")

# Save as RDS
save_eim(model, filename = out_rds)

# Save as JSON
save_eim(model, filename = out_json)

# Save as CSV
save_eim(model, filename = out_csv)

# Remove the files
files <- c(out_rds, out_json, out_csv)
file.remove(files)
```

`simulate_election` *Simulate an Election*

Description

This function simulates an election by creating matrices representing candidate votes (`X`) and voters' demographic group (`W`) across a specified number of ballot-boxes. It either (i) receives as input or (ii) generates a probability matrix (`prob`), indicating how likely each demographic group is to vote for each candidate.

By default, the number of voters per ballot box (`ballot_voters`) is set to a vector of 100 with length `num_ballots`. You can optionally override this by providing a custom vector.

Optional parameters are available to control the distribution of votes:

- `group_proportions`: A vector of length `num_groups` specifying the overall proportion of each demographic group. Entries must sum to one and be non-negative.
- `prob`: A user-supplied probability matrix of dimension (`num_groups` $\times$ `num_candidates`). If provided, this matrix is used directly. Otherwise, voting probabilities for each group are drawn from a Dirichlet distribution.

Usage

```
simulate_election(
  num_ballots,
  num_candidates,
  num_groups,
  ballot_voters = rep(100, num_ballots),
  lambda = 0.5,
  seed = NULL,
  group_proportions = rep(1/num_groups, num_groups),
  prob = NULL
)
```

Arguments

`num_ballots`	Number of ballot boxes (b).
`num_candidates`	Number of candidates (c).
`num_groups`	Number of demographic groups (g).
`ballot_voters`	A vector of length `num_ballots` representing the number of voters per ballot box. Defaults to `rep(100, num_ballots)`.
`lambda`	A numeric value between 0 and 1 that represents the fraction of voters that are randomly assigned to ballot-boxes. The remaining voters are assigned sequentially according to their demographic group. • `lambda = 0`: The assignment of voters to ballot-boxes is fully sequential in terms of their demographic group. This leads to a **high heterogeneity** of the voters' groups across ballot-boxes.

- `lambda = 1`: The assignment of voters to ballot-boxes is fully random. This leads to a **low heterogeneity** of the voters' group across ballot-boxes.

Default value is set to `0.5`. See **Shuffling Mechanish** for more details.

`seed` If provided, overrides the current global seed. Defaults to `NULL`.

`group_proportions`
Optional. A vector of length `num_groups` that indicates the fraction of voters that belong to each group. Default is that all groups are of the same size.

`prob` Optional. A user-supplied probability matrix of dimension `(g x c)`. If provided, this matrix is used as the underlying voting probability distribution. If not supplied, each row is sampled from a Dirichlet distribution with each parameter set to one.

Value

An eim object containing:

`X` A `(b x c)` matrix with candidates' votes for each ballot box.

`W` A `(b x g)` matrix with voters' groups for each ballot-box.

`real_prob` A `(g x c)` matrix with the probability that a voter from each group votes for each candidate. If prob is provided, it would equal such probability.

`outcome` A `(b x g x c)` array with the number of votes for each candidate in each ballot box, broken down by group.

Shuffling Mechanism

Without loss of generality, consider an order relation of groups and ballot-boxes. The shuffling step is controlled by the `lambda` parameter and operates as follows:

1. **Initial Assignment**: Voters are assigned to each ballot-box sequentially according to their demographic group. More specifically, the first ballot-boxes receive voters from the first group. Then, the next ballot-boxes receive voters from the second group. This continues until all voters have been assigned. Note that most ballot-boxes will contain voters from a single group (as long as the number of ballot-boxes exceeds the number of groups).
2. **Shuffling**: A fraction `lambda` of voters who have already been assigned is selected at random. Then, the ballot-box assignment of this sample is shuffled. Hence, different `lambda` values are interpreted as follows:
   - `lambda = 0` means no one is shuffled (the initial assignment remains).
   - `lambda = 1` means all individuals are shuffled.
   - Intermediate values like `lambda = 0.5` shuffle half the voters.

Using a high level of `lambda` (greater than 0.7) is not recommended, as this could make identification of the voting probabilities difficult. This is because higher values of lambda induce similar ballot-boxes in terms of voters' group.

References

The algorithm is fully explained in Ubilla Pavez, P., Hermosilla, D. and Thraves, C. (2026): *"An accurate, fast, and scalable ecological inference algorithm for the R×C case"*. Statistics and Computing, 36, Article 195..

Examples

```
# Example 1: Default usage with 200 ballot boxes, each having 100 voters
result1 <- simulate_election(
    num_ballots = 200,
    num_candidates = 3,
    num_groups = 5
)

# Example 2: Using a custom ballot_voters vector
result2 <- simulate_election(
    num_ballots = 340,
    num_candidates = 3,
    num_groups = 7,
    ballot_voters = rep(200, 340)
)

# Example 3: Supplying group_proportions
result3 <- simulate_election(
    num_ballots = 93,
    num_candidates = 3,
    num_groups = 4,
    group_proportions = c(0.3, 0.5, 0.1, 0.1)
)

# Example 4: Providing a user-defined prob matrix
custom_prob <- matrix(c(
    0.9,  0.1,
    0.4,  0.6,
    0.25, 0.75,
    0.32, 0.68,
    0.2,  0.8
), nrow = 5, byrow = TRUE)

result4 <- simulate_election(
    num_ballots = 200,
    num_candidates = 2,
    num_groups = 5,
    lambda = 0.3,
    prob = custom_prob
)

result4$real_prob == custom_prob
# The attribute of the output real_prob matches the input custom_prob.
```

`waldtest` *Performs a matrix-wise Wald test for two eim objects*

Description

This function compares two `eim` objects (or sets of matrices that can be converted to such objects) by computing a Wald test on each component of their estimated probability matrices. The Wald

test is applied using bootstrap-derived standard deviations, and the result is a matrix of p-values corresponding to each group-candidate combination.

Usage

```
waldtest(
  object1 = NULL,
  object2 = NULL,
  X1 = NULL,
  W1 = NULL,
  X2 = NULL,
  W2 = NULL,
  nboot = 100,
  seed = NULL,
  alternative = "two.sided",
  ...
)
```

Arguments

`object1`	An `eim` object, as returned by eim.
`object2`	A second `eim` object to compare with `object`.
`X1`	A `(b x c)` matrix representing candidate votes per ballot box.
`W1`	A `(b x g)` matrix representing group votes per ballot box.
`X2`	A second `(b x c)` matrix to compare with `X`.
`W2`	A second `(b x g)` matrix to compare with `W`.
`nboot`	Integer specifying how many times to run the EM algorithm per object.
`seed`	An optional integer indicating the random seed for the randomized algorithms. This argument is only applicable if `initial_prob = "random"` or `method` is either `"mcmc"` or `"mvn_cdf"`. Aditionally, it sets the random draws of the ballot boxes.
`alternative`	Character string specifying the type of alternative hypothesis to test. Must be one of `"two.sided"` (default), `"greater"`, or `"less"`. If `"two.sided"`, the test checks for any difference in estimated probabilities. If `"greater"`, it tests whether the first object has systematically higher probabilities than the second. If `"less"`, it tests whether the first has systematically lower probabilities.
`...`	Additional arguments passed to bootstrap and run_em.

Details

It uses Wald test to analyze if there is a significant difference between the estimated probabilities between a treatment and a control set. The test is performed independently for each component of the probability matrix.

The user must provide either of the following (but not both):

- Two `eim` objects via `object1` and `object2`, or

- Four matrices: `X1`, `W1`, `X2`, and `W2`, which will be converted into `eim` objects internally.

The Wald test is computed using the formula:

$$z_{ij} = \frac{p_{1,ij} - p_{2,ij}}{\sqrt{s_{1,ij}^2 + s_{2,ij}^2}}$$

In this expression, $s_{1,ij}^2$ and $s_{2,ij}^2$ represent the bootstrap sample variances for the treatment and control sets, respectively, while $p_{1,ij}$ and $p_{2,ij}$ are the corresponding estimated probability matrices obtained via the EM algorithm.

Value

A list with components:

- `pvals`: a numeric matrix of p-values with the same dimensions as the estimated probability matrices (`pvals`) from the input objects.
- `statistic`: a numeric matrix of z-statistics with the same dimensions as the estimated probability matrices (`pvals`).
- `eim1` and `eim2`: the original `eim` objects used for comparison.

Each entry in the pvals matrix is the p-value from Wald test between the corresponding entries of the two estimated probability matrices.

Examples

```
sim1 <- simulate_election(num_ballots = 100, num_candidates = 3, num_groups = 5, seed = 123)
sim2 <- simulate_election(num_ballots = 100, num_candidates = 3, num_groups = 5, seed = 124)

result <- waldtest(sim1, sim2, nboot = 100)

# Check which entries are significantly different
which(result$pvals < 0.05, arr.ind = TRUE)
```

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