Package: excursions (via r-universe)

October 28, 2026

Type Package

Title Excursion Sets and Contour Credibility Regions for Random Fields

Version 2.5.11

Description Functions that compute probabilistic excursion sets, contour credibility regions, contour avoiding regions, and simultaneous confidence bands for latent Gaussian random processes and fields. The package also contains functions that calculate these quantities for models estimated with the INLA package. The main references for excursions are Bolin and Lindgren (2015) <doi:10.1111/rssb.12055>, Bolin and Lindgren (2017) <doi:10.1080/10618600.2016.1228537>, and Bolin and Lindgren (2018) <doi:10.18637/jss.v086.i05>. These can be generated by the citation function in R.

Depends R (>= 3.5), Matrix

Imports fmesher (>= 0.5.0), graphics, methods, stats, withr, lifecycle

Suggests INLA (>= 21.08.31), testthat (>= 3.0.0), sf, sp, inlabru (>= 2.12.0), RColorBrewer, splancs, fields, rSPDE, knitr, rmarkdown

VignetteBuilder knitr

SystemRequirements Gnu Scientific Library version >= 2.1

Additional_repositories https://inla.r-inla-download.org/R/testing

BugReports https://github.com/davidbolin/excursions/issues

License GPL (>= 3)

URL https://github.com/davidbolin/excursions, https://davidbolin.github.io/excursions/

Copyright The R package and code, and the main programs, were written by and are Copyright by David Bolin and Finn Lindgren, and are redistributable under the GNU Public License, version 3 or later. The package also includes code from the libraries CAMD from the SuiteSparse collection of Tim Davis, and the RngStreams library by Pierre L'Ecuyer. For details see the COPYRIGHTS file.

NeedsCompilation yes

RoxygenNote 7.3.3

Encoding UTF-8

Config/testthat/parallel true

Config/testthat/edition 3

Author David Bolin [cre, aut] (ORCID:
<https://orcid.org/0000-0003-2361-5465>), Finn Lindgren [aut]
(ORCID: <https://orcid.org/0000-0002-5833-2011>), Suen Man Ho
[ctb]

Maintainer David Bolin <davidbolin@gmail.com>

Config/pak/sysreqs libgsl0-dev

Repository https://cran.r-universe.dev

Date/Publication 2025-12-15 10:50:02 UTC

RemoteUrl https://github.com/cran/excursions

RemoteRef HEAD

RemoteSha 0e4b7d8e6e1e262a14d118a0c15667a9f5d3eebc

Contents

excursions-package . . . 3
continuous . . . 4
contourmap . . . 7
contourmap.colors . . . 9
contourmap.inla . . . 10
contourmap.mc . . . 14
exc_safe_inla . . . 16
excursions . . . 17
excursions.inla . . . 20
excursions.mc . . . 24
excursions.variances . . . 26
gaussint . . . 27
require.nowarnings . . . 29
simconf . . . 30
simconf.inla . . . 32
simconf.mc . . . 35
simconf.mixture . . . 36
submesh.grid . . . 38
submesh.mesh . . . 39
summary.excurobj . . . 40
tricontour . . . 41

Index **45**

`excursions-package` *Excursions: Excursion Sets and Contour Credibility Regions for Random Fields*

Description

`excursions` contains functions that compute probabilistic excursion sets, contour credibility regions, contour avoiding regions, contour map quality measures, and simultaneous confidence bands for latent Gaussian random processes and fields. A detailed manual can be found in the paper Bolin, D and Lindgren, F (2018) *Calculating Probabilistic Excursion Sets and Related Quantities Using excursions*, Journal of Statistical Software, 86(5), 1–20.

Details

The main functions in the package fall into three different categories described below.

Excursion sets, contour credibility regions, and contour avoiding regions

The main functions for computing excursion sets, contour credibility regions, and contour avoiding regions are

`excursions()` The main function for Gaussian models.

`excursions.inla()` Interface for latent Gaussian models estimated using INLA.

`excursions.mc()` Function for analyzing models that have been estimated using Monte Carlo methods.

The output from the functions above provides a discrete domain estimate of the regions. Based on this estimate, the function `continuous()` computes a continuous domain estimate.

The main reference for these functions is Bolin, D. and Lindgren, F. (2015) *Excursion and contour uncertainty regions for latent Gaussian models*, JRSS-series B, vol 77, no 1, pp 85-106.

Contour map quality measures

The package provides several functions for computing contour maps and their quality measures. These quality measures can be used to decide on an appropriate number of contours to use for the contour map.

The main functions for computing contour maps and the corresponding quality measures are

`contourmap()` The main function for Gaussian models.

`contourmap.inla()` Interface for latent Gaussian models estimated using INLA.

`contourmap.mc()` Function for analyzing models that have been estimated using Monte Carlo methods.

Other noteworthy functions relating to contourmaps are `tricontour()` and `tricontourmap()`, which compute contour curves for functinos defined on triangulations, as well as `contourmap.colors()` which can be used to compute appropriate colors for displaying contour maps.

The main reference for these functions is Bolin, D. and Lindgren, F. (2017) *Quantifying the uncertainty of contour maps*, Journal of Computational and Graphical Statistics, 26:3, 513-524.

Simultaneous confidence bands

The main functions for computing simultaneous confidence bands are

`simconf()` Function for analyzing Gaussian models.

`simconf.inla()` Function for analyzing latent Gaussian models estimated using INLA.

`simconf.mc()` Function for analyzing models estimated using Monte Carlo methods.

`simconf.mixture()` Function for analyzing Gaussian mixture models.

The main reference for these functions is Bolin et al. (2015) *Statistical prediction of global sea level from global temperature*, Statistica Sinica, Vol 25, pp 351-367.

Author(s)

Maintainer: David Bolin <davidbolin@gmail.com> (ORCID)

Authors:

- Finn Lindgren <finn.lindgren@gmail.com> (ORCID)

Other contributors:

- Suen Man Ho <M.H.Suen@sms.ed.ac.uk> [contributor]

See Also

Useful links:

- https://github.com/davidbolin/excursions
- https://davidbolin.github.io/excursions/
- Report bugs at https://github.com/davidbolin/excursions/issues

---

`continuous` *Calculate continuous domain excursion and credible contour sets*

Description

Calculates continuous domain excursion and credible contour sets

Usage

```
continuous(
  ex,
  geometry,
  alpha,
  method = c("log", "linear", "step"),
  output = c("sp", "fm", "inla"),
  subdivisions = 1,
  calc.credible = TRUE
)
```

Arguments

ex	An excurobj object generated by a call to excursions() or contourmap().
geometry	Specification of the lattice or triangulation geometry of the input. One of list(x, y), list(loc, dims), fm_lattice_2d, inla.mesh.lattice, fm_mesh_2d, or inla.mesh, where x and y are vectors, loc is a two-column matrix of coordinates, and dims is the lattice size vector. The first three versions are all treated topologically as lattices, and the lattice boxes are assumed convex.
alpha	The target error probability. A warning is given if it is detected that the information ex isn't sufficient for the given alpha. Defaults to the value used when calculating ex.
method	The spatial probability interpolation transformation method to use. One of log, linear, or step. For log, the probabilities are interpolated linearly in the transformed scale. For step, a conservative step function is used.
output	Specifies what type of object should be generated. sp gives a SpatialPolygons object, and fm or inla gives a fm_segm object.
subdivisions	The number of mesh triangle subdivisions to perform for the interpolation of the excursions or contour function. 0 is no subdivision. The setting has a small effect on the evaluation of P0 for the log method (higher values giving higher accuracy) but the main effect is on the visual appearance of the interpolation. Default=1.
calc.credible	Logical, if TRUE (default), calculate credible contour region objects in addition to avoidance sets.

Value

A list with elements

M	SpatialPolygons or fm_segm object. The subsets are tagged, so that credible regions are tagged "-1", and regions between levels are tagged as.character(0:nlevels).
F	Interpolated F function.
G	Contour and inter-level set indices for the interpolation.
F.geometry	Mesh geometry for the interpolation.
P0	P0 measure based on interpolated F function (only for contourmap input).

Author(s)

Finn Lindgren <finn.lindgren@gmail.com>

References

Bolin, D. and Lindgren, F. (2017) *Quantifying the uncertainty of contour maps*, Journal of Computational and Graphical Statistics, vol 26, no 3, pp 513-524.

Bolin, D. and Lindgren, F. (2018), *Calculating Probabilistic Excursion Sets and Related Quantities Using excursions*, Journal of Statistical Software, vol 86, no 1, pp 1-20.

Examples

```
## Not run:
if (require("fmesher") &&
  require("sp")) {
  # Generate mesh and SPDE model
  n.lattice <- 10 # Increase for more interesting, but slower, examples
  x <- seq(from = 0, to = 10, length.out = n.lattice)
  lattice <- fm_lattice_2d(x = x, y = x)
  mesh <- fm_rcdt_2d_inla(lattice = lattice, extend = FALSE, refine = FALSE)

  # Generate an artificial sample
  sigma2.e <- 0.1
  n.obs <- 100
  obs.loc <- cbind(
    runif(n.obs) * diff(range(x)) + min(x),
    runif(n.obs) * diff(range(x)) + min(x)
  )
  Q <- fm_matern_precision(mesh, alpha = 2, rho = 3, sigma = 1)
  x <- fm_sample(n = 1, Q = Q)
  A <- fm_basis(mesh, loc = obs.loc)
  Y <- as.vector(A %*% x + rnorm(n.obs) * sqrt(sigma2.e))

  ## Calculate posterior
  Q.post <- (Q + (t(A) %*% A) / sigma2.e)
  mu.post <- as.vector(solve(Q.post, (t(A) %*% Y) / sigma2.e))
  vars.post <- excursions.variances(chol(Q.post), max.threads = 1)

  ## Calculate contour map with two levels
  map <- contourmap(
    n.levels = 2, mu = mu.post, Q = Q.post,
    alpha = 0.1, F.limit = 0.1, max.threads = 1
  )

  ## Calculate the continuous representation
  sets <- continuous(map, mesh, alpha = 0.1)

  ## Plot the results
  reo <- mesh$idx$lattice
  cols <- contourmap.colors(map,
    col = heat.colors(100, 1, rev = TRUE),
    credible.col = grey(0.5, 1)
  )
  names(cols) <- as.character(-1:2)

  par(mfrow = c(2, 2))
  image(matrix(mu.post[reo], n.lattice, n.lattice),
    main = "mean", axes = FALSE, asp = 1
  )
  image(matrix(sqrt(vars.post[reo]), n.lattice, n.lattice),
    main = "sd", axes = FALSE, asp = 1
  )
  image(matrix(map$M[reo], n.lattice, n.lattice),
```

```
    col = cols, axes = FALSE, asp = 1
  )
  idx.M <- setdiff(names(sets$M), "-1")
  plot(sets$M[idx.M], col = cols[idx.M])
}

## End(Not run)
```

`contourmap` *Contour maps and contour map quality measures for latent Gaussian models*

Description

`contourmap` is used for calculating contour maps and quality measures for contour maps for Gaussian models.

Usage

```
contourmap(
  mu,
  Q,
  vars,
  n.levels,
  ind,
  levels,
  type = c("standard", "pretty", "equalarea", "P0-optimal", "P1-optimal", "P2-optimal"),
  compute = list(F = TRUE, measures = NULL),
  use.marginals = TRUE,
  alpha,
  F.limit,
  n.iter = 10000,
  verbose = FALSE,
  max.threads = 0,
  seed = NULL
)
```

Arguments

`mu`	Expectation vector.
`Q`	Precision matrix.
`vars`	Precomputed marginal variances (optional).
`n.levels`	Number of levels in contour map.
`ind`	Indices of the nodes that should be analyzed (optional).
`levels`	Levels to use in contour map.

`type` Type of contour map. One of:

'standard' Equidistant levels between smallest and largest value of the posterior mean (default).

'pretty' Equally spaced 'round' values which cover the range of the values in the posterior mean.

'equalarea' Levels such that different spatial regions are approximately equal in size.

'P0-optimal' Levels chosen to maximize the P0 measure.

'P1-optimal' Levels chosen to maximize the P1 measure.

'P2-optimal' Levels chosen to maximize the P2 measure.

`compute` A list with quality indices to compute

'F': TRUE/FALSE indicating whether the contour map function should be computed (default TRUE).

'measures': A list with the quality measures to compute ("P0", "P1", "P2") or corresponding bounds based only on the marginal probabilities ("P0-bound", "P1-bound", "P2-bound").

`use.marginals` Only marginal distributions are used when finding P-optimal maps (default TRUE).

`alpha` Maximal error probability in contour map function (default=1).

`F.limit` The limit value for the computation of the F function. F is set to NA for all nodes where `F < 1-F.limit`. Default is `F.limit = alpha`.

`n.iter` Number or iterations in the MC sampler that is used for calculating the quantities in `compute`. The default value is 10000.

`verbose` Set to TRUE for verbose mode (optional).

`max.threads` Decides the number of threads the program can use. Set to 0 for using the maximum number of threads allowed by the system (default).

`seed` Random seed (optional).

Details

The Gaussian model is specified using the mean `mu` and the precision matrix `Q`. The contour map is then computed for the mean, using either the contour levels specified in `levels`, or `n.levels` contours that are placed according to the argument `type`.

A number of quality measures can be computed based based on the specified contour map and the Gaussian distribution. What should be computed is specified using the `compute` argument. For details on these quanties, see the reference below.

Value

`contourmap` returns an object of class "excurobj" with the following elements

`u` Contour levels used in the contour map.

`n.levels` The number of contours used.

`u.e` The values associated with the level sets G_k.

`G` A vector which shows which of the level sets G_k each node belongs to.

map	Representation of the contour map with map[i]=u.e[k] if i is in G_k.
F	The contour map function (if computed).
M	Contour avoiding sets (if F is computed). $M = -1$ for all non-significant nodes and $M = k$ for nodes that belong to M_k.
P0/P1/P2	Calculated quality measures (if computed).
P0bound/P1bound/P2bound	Calculated upper bounds quality measures (if computed).
meta	A list containing various information about the calculation.

Author(s)

David Bolin <davidbolin@gmail.com>

References

Bolin, D. and Lindgren, F. (2017) *Quantifying the uncertainty of contour maps*, Journal of Computational and Graphical Statistics, vol 26, no 3, pp 513-524.

Bolin, D. and Lindgren, F. (2018), *Calculating Probabilistic Excursion Sets and Related Quantities Using excursions*, Journal of Statistical Software, vol 86, no 1, pp 1-20.

See Also

contourmap.inla(), contourmap.mc(), contourmap.colors()

Examples

```
n <- 10
Q <- Matrix(toeplitz(c(1, -0.5, rep(0, n - 2))))
mu <- seq(-5, 5, length = n)
lp <- contourmap(mu, Q,
  n.levels = 2,
  compute = list(F = FALSE, measures = c("P1", "P2")),
  max.threads = 1
)
# Plot the contourmap
plot(lp$map)
# Display the quality measures
cat(c(lp$P1, lp$P2))
```

---

contourmap.colors *Define a color map for displaying contour maps.*

Description

contourmap.colors calculates suitable colours for displaying contour maps.

Usage

```
contourmap.colors(lp, zlim, col, credible.col)
```

Arguments

lp	A contourmap calculated by contourmap, contourmap.inla, or contourmap.mc
zlim	The range that should be used (optional). The default is the range of the mean value function used when creating the contourmap.
col	The colormap that the colours should be taken from.
credible.col	The color that should be used for displaying the credible regions for the contour curves (optional).

Value

A color map.

Author(s)

David Bolin <davidbolin@gmail.com>

Examples

```
n <- 10
Q <- Matrix(toeplitz(c(1, -0.5, rep(0, n - 2))))
map <- contourmap(
  mu = seq(-5, 5, length = n), Q, n.levels = 2,
  compute = list(F = FALSE), max.threads = 1
)
cols <- contourmap.colors(map,
  col = heat.colors(100, 1),
  credible.col = grey(0.5, 1)
)
```

---

contourmap.inla *Contour maps and contour map quality measures for latent Gaussian models*

Description

An interface to the contourmap function for latent Gaussian models calculated using the INLA method.

Usage

```
contourmap.inla(
  result.inla,
  stack,
  name = NULL,
  tag = NULL,
  method = "QC",
  n.levels,
  type = c("standard", "pretty", "equalarea"),
  compute = list(F = TRUE, measures = NULL),
  alpha,
  F.limit,
  n.iter = 10000,
  verbose = FALSE,
  max.threads = 0,
  compressed = TRUE,
  seed = NULL,
  ind,
  ...
)
```

Arguments

result.inla	Result object from INLA call.
stack	The stack object used in the INLA call.
name	The name of the component for which to do the calculation. This argument should only be used if a stack object is not provided, use the tag argument otherwise.
tag	The tag of the component in the stack for which to do the calculation. This argument should only be used if a stack object is provided, use the name argument otherwise.
method	Method for handeling the latent Gaussian structure. Currently only Empirical Bayes (EB) and Quantile corrections (QC) are supported.
n.levels	Number of levels in contour map.
type	Type of contour map. One of:
	'standard' Equidistant levels between smallest and largest value of the posterior mean (default).
	'pretty' Equally spaced 'round' values which cover the range of the values in the posterior mean.
	'equalarea' Levels such that different spatial regions are approximately equal in size.
compute	A list with quality indices to compute
	'F': TRUE/FALSE indicating whether the contour map function should be computed (default TRUE)

'measures': A list with the quality measures to compute ("P0", "P1", "P2") or corresponding bounds based only on the marginal probabilities ("P0-bound", "P1-bound", "P2-bound")

alpha	Maximal error probability in contour map function (default=1)
F.limit	The limit value for the computation of the F function. F is set to NA for all nodes where F<1-F.limit. Default is F.limit = alpha.
n.iter	Number or iterations in the MC sampler that is used for calculating the quantities in compute. The default value is 10000.
verbose	Set to TRUE for verbose mode (optional)
max.threads	Decides the number of threads the program can use. Set to 0 for using the maximum number of threads allowed by the system (default).
compressed	If INLA is run in compressed mode and a part of the linear predictor is to be used, then only add the relevant part. Otherwise the entire linear predictor is added internally (default TRUE).
seed	Random seed (optional).
ind	If only a part of a component should be used in the calculations, this argument specifies the indices for that part (optional).
...	Additional arguments to the contour map function. See the documentation for contourmap for details.

Details

The INLA approximation of the quantity of interest is in general a weighted sum of Gaussian distributions with different parameters. If method = 'EB' is used, then the contour map is computed for the mean of the component in the weighted sum that has parameters with the highest likelihood. If on the other hand method='QC', then the contour map is computed for the posterior mean reported by INLA. If the EB method also is used in INLA, then this reported posterior mean is equal to the mean of the component with the highest likelihood. Therefore, method='EB' is appropriate if the EB method also is used in INLA, but method='QC' should be used in general.

The n.levels contours in the contour map are are placed according to the argument type. A number of quality measures can be computed based based on the specified contour map and the distribution of the component of interest. What should be computed is specified using the compute argument. For details on these quanties, see the reference below.

Value

contourmap.inla returns an object of class "excurobj" with the same elements as returned by contourmap.

Note

This function requires the INLA package, which is not a CRAN package. See https://www.r-inla.org/download-install for easy installation instructions.

Author(s)

David Bolin <davidbolin@gmail.com>

References

Bolin, D. and Lindgren, F. (2017) *Quantifying the uncertainty of contour maps*, Journal of Computational and Graphical Statistics, 26:3, 513-524.

Bolin, D. and Lindgren, F. (2018), *Calculating Probabilistic Excursion Sets and Related Quantities Using excursions*, Journal of Statistical Software, vol 86, no 1, pp 1-20.

See Also

`contourmap()`, `contourmap.mc()`, `contourmap.colors()`

Examples

```
## Not run:
if (require.nowarnings("INLA")) {
  # Generate mesh and SPDE model
  n.lattice <- 10 # increase for more interesting, but slower, examples
  x <- seq(from = 0, to = 10, length.out = n.lattice)
  lattice <- fmesher::fm_lattice_2d(x = x, y = x)
  mesh <- fmesher::fm_rcdt_2d_inla(
    lattice = lattice,
    extend = FALSE,
    refine = FALSE
  )
  spde <- inla.spde2.matern(mesh, alpha = 2)

  # Generate an artificial sample
  sigma2.e <- 0.01
  n.obs <- 100
  obs.loc <- cbind(
    runif(n.obs) * diff(range(x)) + min(x),
    runif(n.obs) * diff(range(x)) + min(x)
  )
  Q <- inla.spde2.precision(spde, theta = c(log(sqrt(0.5)), log(sqrt(1))))
  x <- inla.qsample(Q = Q, num.threads = 1)
  A <- fmesher::fm_basis(mesh = mesh, loc = obs.loc)
  Y <- as.vector(A %*% x + rnorm(n.obs) * sqrt(sigma2.e))

  ## Estimate the parameters using INLA
  mesh.index <- inla.spde.make.index(name = "field", n.spde = spde$n.spde)
  ef <- list(c(mesh.index, list(Intercept = 1)))

  s.obs <- inla.stack(
    data = list(y = Y),
    A = list(A),
    effects = ef,
    tag = "obs"
  )
  s.pre <- inla.stack(
    data = list(y = NA),
    A = list(1),
    effects = ef,
```

```
  tag = "pred"
)
stack <- inla.stack(s.obs, s.pre)
formula <- y ~ -1 + Intercept + f(field, model = spde)
result <- inla(
  formula = formula, family = "normal", data = inla.stack.data(stack),
  control.predictor = list(
    A = inla.stack.A(stack),
    compute = TRUE
  ),
  control.compute = list(
    config = TRUE,
    return.marginals.predictor = TRUE
  ),
  num.threads = 1
)

## Calculate contour map with two levels
map <- contourmap.inla(result,
  stack = stack, tag = "pred",
  n.levels = 2, alpha = 0.1, F.limit = 0.1,
  max.threads = 1
)

## Plot the results
cols <- contourmap.colors(map,
  col = heat.colors(100, 1),
  credible.col = grey(0.5, 1)
)
image(matrix(map$M[mesh$idx$lattice], n.lattice, n.lattice), col = cols)
}

## End(Not run)
```

`contourmap.mc` *Contour maps and contour map quality measures using Monte Carlo samples*

Description

`contourmap.mc` is used for calculating contour maps and quality measures for contour maps based on Monte Carlo samples of a model.

Usage

```
contourmap.mc(
  samples,
  n.levels,
  ind,
  levels,
```

```
  type = c("standard", "equalarea", "P0-optimal", "P1-optimal", "P2-optimal"),
  compute = list(F = TRUE, measures = NULL),
  alpha,
  verbose = FALSE
)
```

Arguments

samples	Matrix with model Monte Carlo samples. Each column contains a sample of the model.
n.levels	Number of levels in contour map.
ind	Indices of the nodes that should be analyzed (optional).
levels	Levels to use in contour map.
type	Type of contour map. One of: **'standard'** Equidistant levels between smallest and largest value of the posterior mean (default). **'pretty'** Equally spaced 'round' values which cover the range of the values in the posterior mean. **'equalarea'** Levels such that different spatial regions are approximately equal in size. **'P0-optimal'** Levels chosen to maximize the P0 measure. **'P1-optimal'** Levels chosen to maximize the P1 measure. **'P2-optimal'** Levels chosen to maximize the P2 measure.
compute	A list with quality indices to compute **'F':** TRUE/FALSE indicating whether the contour map function should be computed (default TRUE). **'measures':** A list with the quality measures to compute ("P0", "P1", "P2") or corresponding bounds based only on the marginal probabilities ("P0-bound", "P1-bound", "P2-bound").
alpha	Maximal error probability in contour map function (default=0.1).
verbose	Set to TRUE for verbose mode (optional).

Details

The contour map is computed for the empirical mean of the samples. See `contourmap()` and `contourmap.inla()` for further details.

Value

`contourmap` returns an object of class "excurobj" with the following elements

u	Contour levels used in the contour map.
n.levels	The number of contours used.
u.e	The values associated with the level sets `G_k`.
G	A vector which shows which of the level sets `G_k` each node belongs to.

map	Representation of the contour map with map[i]=u.e[k] if i is in G_k.
F	The contour map function (if computed).
M	Contour avoiding sets (if F is computed). $M = -1$ for all non-significant nodes and $M = k$ for nodes that belong to M_k.
P0/P1/P2	Calculated quality measures (if computed).
P0bound/P1bound/P2bound	Calculated upper bounds quality measures (if computed).
meta	A list containing various information about the calculation.

Author(s)

David Bolin <davidbolin@gmail.com>

References

Bolin, D. and Lindgren, F. (2017) *Quantifying the uncertainty of contour maps*, Journal of Computational and Graphical Statistics, 26:3, 513-524.

Bolin, D. and Lindgren, F. (2018), *Calculating Probabilistic Excursion Sets and Related Quantities Using excursions*, Journal of Statistical Software, 86(5), 1–20.

See Also

contourmap(), contourmap.inla(), contourmap.colors()

Examples

```
n <- 100
Q <- Matrix(toeplitz(c(1, -0.5, rep(0, n - 2))))
mu <- seq(-5, 5, length = n)
## Sample the model 100 times (increase for better estimate)
X <- mu + solve(chol(Q), matrix(rnorm(n = n * 100), nrow = n, ncol = 100))

lp <- contourmap.mc(X, n.levels = 2, compute = list(F = FALSE, measures = c("P1", "P2")))

# plot contourmap
plot(lp$map)
# display quality measures
c(lp$P1, lp$P2)
```

---

exc_safe_inla *Load INLA safely for examples and tests*

Description

Loads the INLA package with requireNamespace("INLA", quietly = TRUE), and optionally checks and sets the multicore num.threads INLA option.

Usage

```
exc_safe_inla(multicore = NULL, quietly = FALSE)
```

Arguments

multicore	logical; if TRUE, multiple cores are allowed, and the INLA num.threads option is not checked or altered. If FALSE, forces num.threads="1:1". Default: NULL, checks if running in testthat or non-interactively, in which case sets multicore=FALSE, otherwise TRUE.
quietly	logical; if TRUE, prints diagnostic messages. Default: FALSE.

Value

logical; TRUE if INLA was loaded safely, otherwise FALSE

Examples

```
## Not run:
if (exc_safe_inla()) {
  # Run inla dependent calculations
}

## End(Not run)
```

---

excursions *Excursion Sets and Contour Credibility Regions for Random Fields*

Description

excursions is one of the main functions in the package with the same name. For an introduction to the package, see excursions-package(). The function is used for calculating excursion sets, contour credible regions, and contour avoiding sets for latent Gaussian models. Details on the function and the package are given in the sections below.

Usage

```
excursions(
  alpha,
  u,
  mu,
  Q,
  type,
  n.iter = 10000,
  Q.chol,
  F.limit,
  vars,
```

```
  rho,
  reo,
  method = "EB",
  ind,
  max.size,
  verbose = 0,
  max.threads = 0,
  seed,
  prune.ind = FALSE
)
```

Arguments

alpha	Error probability for the excursion set.
u	Excursion or contour level.
mu	Expectation vector.
Q	Precision matrix.
type	Type of region: **'>'** positive excursion region **'<'** negative excursion region **'!='** contour avoiding region **'='** contour credibility region
n.iter	Number or iterations in the MC sampler that is used for approximating probabilities. The default value is 10000.
Q.chol	The Cholesky factor of the precision matrix (optional).
F.limit	The limit value for the computation of the F function. F is set to NA for all nodes where F<1-F.limit. Default is F.limit = alpha.
vars	Precomputed marginal variances (optional).
rho	Marginal excursion probabilities (optional). For contour regions, provide $P(X > u)$.
reo	Reordering (optional).
method	Method for handeling the latent Gaussian structure: **'EB'** Empirical Bayes (default) **'QC'** Quantile correction, rho must be provided if QC is used.
ind	Indices of the nodes that should be analysed (optional).
max.size	Maximum number of nodes to include in the set of interest (optional).
verbose	Set to TRUE for verbose mode (optional).
max.threads	Decides the number of threads the program can use. Set to 0 for using the maximum number of threads allowed by the system (default).
seed	Random seed (optional).
prune.ind	If TRUE and ind is supplied, then the result object is pruned to contain only the active nodes specified by ind.

Details

The estimation of the region is done using sequential importance sampling with `n.iter` samples. The procedure requires computing the marginal variances of the field, which should be supplied if available. If not, they are computed using the Cholesky factor of the precision matrix. The cost of this step can therefore be reduced by supplying the Cholesky factor if it is available.

The latent structure in the latent Gaussian model can be handled in several different ways. The default strategy is the EB method, which is exact for problems with Gaussian posterior distributions. For problems with non-Gaussian posteriors, the QC method can be used for improved results. In order to use the QC method, the true marginal excursion probabilities must be supplied using the argument `rho`. Other more complicated methods for handling non-Gaussian posteriors must be implemented manually unless `INLA` is used to fit the model. If the model is fitted using `INLA`, the method `excursions.inla` can be used. See the Package section for further details about the different options.

Value

`excursions` returns an object of class "excurobj" with the following elements

`E`	Excursion set, contour credible region, or contour avoiding set
`G`	Contour map set. $G = 1$ for all nodes where the $mu > u$.
`M`	Contour avoiding set. $M = -1$ for all non-significant nodes. $M = 0$ for nodes where the process is significantly below `u` and $M = 1$ for all nodes where the field is significantly above `u`. Which values that should be present depends on what type of set that is calculated.
`F`	The excursion function corresponding to the set `E` calculated or values up to `F.limit`
`rho`	Marginal excursion probabilities
`mean`	The mean `mu`.
`vars`	Marginal variances.
`meta`	A list containing various information about the calculation.

Author(s)

David Bolin <davidbolin@gmail.com> and Finn Lindgren <finn.lindgren@gmail.com>

References

Bolin, D. and Lindgren, F. (2015) *Excursion and contour uncertainty regions for latent Gaussian models*, JRSS-series B, vol 77, no 1, pp 85-106.

Bolin, D. and Lindgren, F. (2018), *Calculating Probabilistic Excursion Sets and Related Quantities Using excursions*, Journal of Statistical Software, vol 86, no 1, pp 1-20.

See Also

`excursions-package()`, `excursions.inla()`, `excursions.mc()`

Examples

```
## Create a tridiagonal precision matrix
n <- 21
Q.x <- sparseMatrix(
  i = c(1:n, 2:n), j = c(1:n, 1:(n - 1)), x = c(rep(1, n), rep(-0.1, n - 1)),
  dims = c(n, n), symmetric = TRUE
)
## Set the mean value function
mu.x <- seq(-5, 5, length = n)

## calculate the level 0 positive excursion function
res.x <- excursions(
  alpha = 1, u = 0, mu = mu.x, Q = Q.x,
  type = ">", verbose = 1, max.threads = 2
)

## Plot the excursion function and the marginal excursion probabilities
plot(res.x$F,
  type = "l",
  main = "Excursion function (black) and marginal probabilites (red)"
)
lines(res.x$rho, col = 2)
```

`excursions.inla` *Excursion sets and contour credible regions for latent Gaussian models*

Description

Excursion sets and contour credible regions for latent Gaussian models calculated using the INLA method.

Usage

```
excursions.inla(
  result.inla,
  stack,
  name = NULL,
  tag = NULL,
  ind = NULL,
  method,
  alpha = 1,
  F.limit,
  u,
  u.link = FALSE,
  type,
  n.iter = 10000,
  verbose = 0,
```

```
  max.threads = 0,
  compressed = TRUE,
  seed = NULL,
  prune.ind = FALSE
)
```

Arguments

result.inla	Result object from INLA call.
stack	The stack object used in the INLA call.
name	The name of the component for which to do the calculation. This argument should only be used if a stack object is not provided, use the tag argument otherwise.
tag	The tag of the component in the stack for which to do the calculation. This argument should only be used if a stack object is provided, use the name argument otherwise.
ind	If only a part of a component should be used in the calculations, this argument specifies the indices for that part.
method	Method for handeling the latent Gaussian structure: **'EB'** Empirical Bayes **'QC'** Quantile correction **'NI'** Numerical integration **'NIQC'** Numerical integration with quantile correction **'iNIQC'** Improved integration with quantile correction
alpha	Error probability for the excursion set of interest. The default value is 1.
F.limit	Error probability for when to stop the calculation of the excursion function. The default value is alpha, and the value cannot be smaller than alpha. A smaller value of F.limit results in a smaller computation time.
u	Excursion or contour level.
u.link	If u.link is TRUE, u is assumed to be in the scale of the data and is then transformed to the scale of the linear predictor (default FALSE).
type	Type of region: **'>'** positive excursions **'<'** negative excursions **'!='** contour avoiding function **'='** contour credibility function
n.iter	Number or iterations in the MC sampler that is used for approximating probabilities. The default value is 10000.
verbose	Set to TRUE for verbose mode (optional).
max.threads	Decides the number of threads the program can use. Set to 0 for using the maximum number of threads allowed by the system (default).
compressed	If INLA is run in compressed mode and a part of the linear predictor is to be used, then only add the relevant part. Otherwise the entire linear predictor is added internally (default TRUE).

seed	Random seed (optional).
prune.ind	If TRUE and ind is supplied, then the result object is pruned to contain only the active nodes specified by ind.

Details

The different methods for handling the latent Gaussian structure are listed in order of accuracy and computational cost. The EB method is the simplest and is based on a Gaussian approximation of the posterior of the quantity of interest. The QC method uses the same Gaussian approximation but improves the accuracy by modifying the limits in the integrals that are computed in order to find the region. The other three methods are intended for Bayesian models where the posterior distribution for the quantity of interest is obtained by integrating over the parameters in the model. The NI method approximates this integration in the same way as is done in INLA, and the NIQC and iNIQC methods combine this apprximation with the QC method for improved accuracy.

If the main purpose of the analysis is to construct excursion or contour sets for low values of alpha, we recommend using QC for problems with Gaussian likelihoods and NIQC for problems with non-Gaussian likelihoods. The reason for this is that the more accurate methods also have higher computational costs.

Value

excursions.inla returns an object of class "excurobj" with the following elements

E	Excursion set, contour credible region, or contour avoiding set
F	The excursion function corresponding to the set E calculated for values up to F.limit
G	Contour map set. $G = 1$ for all nodes where the $mu > u$.
M	Contour avoiding set. $M = -1$ for all non-significant nodes. $M = 0$ for nodes where the process is significantly below u and $M = 1$ for all nodes where the field is significantly above u. Which values that should be present depends on what type of set that is calculated.
rho	Marginal excursion probabilities
mean	Posterior mean
vars	Marginal variances
meta	A list containing various information about the calculation.

Note

This function requires the INLA package, which is not a CRAN package. See https://www.r-inla.org/download-install for easy installation instructions.

Author(s)

David Bolin <davidbolin@gmail.com> and Finn Lindgren <finn.lindgren@gmail.com>

References

Bolin, D. and Lindgren, F. (2015) *Excursion and contour uncertainty regions for latent Gaussian models*, JRSS-series B, vol 77, no 1, pp 85-106.

Bolin, D. and Lindgren, F. (2018), *Calculating Probabilistic Excursion Sets and Related Quantities Using excursions*, Journal of Statistical Software, vol 86, no 1, pp 1-20.

See Also

excursions(), excursions.mc()

Examples

```
## In this example, we calculate the excursion function
## for a partially observed AR process.
## Not run:
if (require.nowarnings("INLA")) {
  ## Sample the process:
  rho <- 0.9
  tau <- 15
  tau.e <- 1
  n <- 100
  x <- 1:n
  mu <- 10 * ((x < n / 2) * (x - n / 2) + (x >= n / 2) * (n / 2 - x) + n / 4) / n
  Q <- tau * sparseMatrix(
    i = c(1:n, 2:n), j = c(1:n, 1:(n - 1)),
    x = c(1, rep(1 + rho^2, n - 2), 1, rep(-rho, n - 1)),
    dims = c(n, n), symmetric = TRUE
  )
  X <- mu + solve(chol(Q), rnorm(n))

  ## measure the sampled process at n.obs random locations
  ## under Gaussian measurement noise.
  n.obs <- 50
  obs.loc <- sample(1:n, n.obs)
  A <- sparseMatrix(
    i = 1:n.obs, j = obs.loc, x = rep(1, n.obs),
    dims = c(n.obs, n)
  )
  Y <- as.vector(A %*% X + rnorm(n.obs) / sqrt(tau.e))

  ## Estimate the parameters using INLA
  ef <- list(c(list(ar = x), list(cov = mu)))
  s.obs <- inla.stack(data = list(y = Y), A = list(A), effects = ef, tag = "obs")
  s.pre <- inla.stack(data = list(y = NA), A = list(1), effects = ef, tag = "pred")
  stack <- inla.stack(s.obs, s.pre)
  formula <- y ~ -1 + cov + f(ar, model = "ar1")
  result <- inla(
    formula = formula, family = "normal", data = inla.stack.data(stack),
    control.predictor = list(A = inla.stack.A(stack), compute = TRUE),
    control.compute = list(
      config = TRUE,
```

```
    return.marginals.predictor = TRUE
  )
)

## calculate the level 0 positive excursion function
res.qc <- excursions.inla(result,
  stack = stack, tag = "pred", alpha = 0.99, u = 0,
  method = "QC", type = ">", max.threads = 2
)
## plot the excursion function and marginal probabilities
plot(res.qc$rho,
  type = "l",
  main = "marginal probabilities (black) and excursion function (red)"
)
lines(res.qc$F, col = 2)
}

## End(Not run)
```

`excursions.mc` *Excursion sets and contour credible regions using Monte Carlo samples*

Description

`excursions.mc` is used for calculating excursion sets, contour credible regions, and contour avoiding sets based on Monte Carlo samples of models.

Usage

```
excursions.mc(
  samples,
  alpha,
  u,
  type,
  rho,
  reo,
  ind,
  max.size,
  verbose = FALSE,
  prune.ind = FALSE
)
```

Arguments

`samples`	Matrix with model Monte Carlo samples. Each column contains a sample of the model.

alpha	Error probability for the excursion set.
u	Excursion or contour level.
type	Type of region: **'>'** positive excursions **'<'** negative excursions **'!='** contour avoiding function **'='** contour credibility function
rho	Marginal excursion probabilities (optional). For contour regions, provide $P(X > u)$.
reo	Reordering (optional).
ind	Indices of the nodes that should be analysed (optional).
max.size	Maximum number of nodes to include in the set of interest (optional).
verbose	Set to TRUE for verbose mode (optional).
prune.ind	If TRUE and ind is supplied, then the result object is pruned to contain only the active nodes specified by ind.

Value

excursions.mc returns an object of class "excurobj" with the following elements

E	Excursion set, contour credible region, or contour avoiding set.
G	Contour map set. $G = 1$ for all nodes where the $mu > u$.
M	Contour avoiding set. $M = -1$ for all non-significant nodes. $M = 0$ for nodes where the process is significantly below u and $M = 1$ for all nodes where the field is significantly above u. Which values that should be present depends on what type of set that is calculated.
F	The excursion function corresponding to the set E calculated for values up to F.limit
rho	Marginal excursion probabilities
mean	The mean mu.
vars	Marginal variances.
meta	A list containing various information about the calculation.

Author(s)

David Bolin <davidbolin@gmail.com> and Finn Lindgren <finn.lindgren@gmail.com>

References

Bolin, D. and Lindgren, F. (2015) *Excursion and contour uncertainty regions for latent Gaussian models*, JRSS-series B, vol 77, no 1, pp 85-106.

Bolin, D. and Lindgren, F. (2018), *Calculating Probabilistic Excursion Sets and Related Quantities Using excursions*, Journal of Statistical Software, vol 86, no 1, pp 1-20.

See Also

excursions(), excursions.inla()

Examples

```
## Create mean and a tridiagonal precision matrix
n <- 101
mu.x <- seq(-5, 5, length = n)
Q.x <- Matrix(toeplitz(c(1, -0.1, rep(0, n - 2))))
## Sample the model 100 times (increase for better estimate)
X <- mu.x + solve(chol(Q.x), matrix(rnorm(n = n * 1000), nrow = n, ncol = 1000))
## calculate the positive excursion function
res.x <- excursions.mc(X, alpha = 0.05, type = ">", u = 0)
## Plot the excursion function and the marginal excursion probabilities
plot(res.x$F,
  type = "l",
  main = "Excursion function (black) and marginal probabilites (red)"
)
lines(res.x$rho, col = 2)
```

---

excursions.variances *Calculate variances from a sparse precision matrix*

Description

excursions.variances calculates the diagonal of the inverse of a sparse symmetric positive definite matrix Q.

Usage

```
excursions.variances(L, Q, max.threads = 0)
```

Arguments

L	Cholesky factor of precision matrix.
Q	Precision matrix.
max.threads	Decides the number of threads the program can use. Set to 0 for using the maximum number of threads allowed by the system (default).

Details

The method for calculating the diagonal requires the Cholesky factor, L, of Q, which should be supplied if available. If Q is provided, the cholesky factor is calculated and the variances are then returned in the same ordering as Q. If L is provided, the variances are returned in the same ordering as L, even if L@invpivot exists.

Value

A vector with the variances.

Author(s)

David Bolin <davidbolin@gmail.com>

Examples

```
## Create a tridiagonal precision matrix
n <- 21
Q <- Matrix(toeplitz(c(1, -0.1, rep(0, n - 2))))
v2 <- excursions.variances(Q = Q, max.threads = 2)
## var2 should be the same as:
v1 <- diag(solve(Q))
```

---

gaussint *Sequential estimation of Gaussian integrals*

Description

gaussint is used for calculating n-dimensional Gaussian integrals

$$\int_a^b \frac{|Q|^{1/2}}{(2\pi)^{n/2}} \exp(-\frac{1}{2}(x-\mu)^T Q(x-\mu))dx$$

A limit value lim can be used to stop the integration if the sequential estimate goes below the limit, which can result in substantial computational savings in cases when one only is interested in testing if the integral is above the limit value. The integral is calculated sequentially, and estimates for all subintegrals are also returned.

Usage

```
gaussint(
  mu,
  Q.chol,
  Q,
  a,
  b,
  lim = 0,
  n.iter = 10000,
  ind,
  use.reordering = c("natural", "sparsity", "limits"),
  max.size,
  max.threads = 0,
  seed
)
```

Arguments

`mu`	Expectation vector for the Gaussian distribution.
`Q.chol`	The Cholesky factor of the precision matrix (optional).
`Q`	Precision matrix for the Gaussian distribution. If Q is supplied but not Q.chol, the cholesky factor is computed before integrating.
`a`	Lower limit in integral.
`b`	Upper limit in integral.
`lim`	If this argument is used, the integration is stopped and 0 is returned if the estimated value goes below lim.
`n.iter`	Number or iterations in the MC sampler that is used for approximating probabilities. The default value is 10000.
`ind`	Indices of the nodes that should be analyzed (optional).
`use.reordering`	Determines what reordering to use: **"natural"** No reordering is performed. **"sparsity"** Reorder for sparsity in the cholesky factor (MMD reordering is used). **"limits"** Reorder by moving all nodes with a=-Inf and b=Inf first and then reordering for sparsity (CAMD reordering is used).
`max.size`	The largest number of sub-integrals to compute. Default is the total dimension of the distribution.
`max.threads`	Decides the number of threads the program can use. Set to 0 for using the maximum number of threads allowed by the system (default).
`seed`	The random seed to use (optional).

Details

The function uses sequential importance sampling to estimate the Gaussian integral, and returns all computed sub-integrals. This means that if, for example, the function is used to compute $P(x > 0)$ for an n-dimensional Gaussian variable x, then all integrals $P(x_1 > 0, \ldots, x_i > 0)$ for $i = 1, \ldots, n$ are computed.

If one is only interested in whether $P(x > 0) > \alpha$ or not, then one can stop the integration as soon as $P(x_1 > 0, \ldots, x_i > 0) < \alpha$. This can save a lot of computation time if $P(x_1 > 0, \ldots, x_i > 0) < \alpha$ for i much smaller than n. This limit value is specified by the `lim` argument.

Which reordering to use depends on what the purpose of the calculation is and what the integration limits are. However, in general the `limits` reordering is typically most appropriate since this combines sparisty (which improves accuracy and reduces computational cost) with automatic handling of dimensions with limits `a=-Inf` and `b=Inf`, which do not affect the probability but affect the computation time if they are not handled separately.

Value

A list with elements

`P`	Value of the integral.

E	Estimated error of the P estimate.
Pv	A vector with the estimates of all sub-integrals.
Ev	A vector with the estimated errors of the Pv estimates.

Author(s)

David Bolin <davidbolin@gmail.com>

References

Bolin, D. and Lindgren, F. (2015) *Excursion and contour uncertainty regions for latent Gaussian models*, JRSS-series B, vol 77, no 1, pp 85-106.

Bolin, D. and Lindgren, F. (2018), *Calculating Probabilistic Excursion Sets and Related Quantities Using excursions*, Journal of Statistical Software, vol 86, no 1, pp 1-20.

Examples

```
## Create mean and a tridiagonal precision matrix
n <- 11
mu.x <- seq(-5, 5, length = n)
Q.x <- Matrix(toeplitz(c(1, -0.1, rep(0, n - 2))))
## Calculate the probability that the variable is between mu-3 and mu+3
prob <- gaussint(mu = mu.x, Q = Q.x, a = mu.x - 3, b = mu.x + 3, max.threads = 2)
prob$P
```

---

require.nowarnings *Warnings free loading of add-on packages*

Description

Turn off all warnings for require(), to allow clean completion of examples that require unavailable Suggested packages.

Usage

```
require.nowarnings(package, lib.loc = NULL, character.only = FALSE)
```

Arguments

package	The name of a package, given as a character string.
lib.loc	a character vector describing the location of R library trees to search through, or NULL. The default value of NULL corresponds to all libraries currently known to .libPaths(). Non-existent library trees are silently ignored.
character.only	a logical indicating whether package can be assumed to be a character string.

Details

`require(package)` acts the same as `require(package, quietly = TRUE)` but with warnings turned off. In particular, no warning or error is given if the package is unavailable. Most cases should use `requireNamespace(package, quietly = TRUE)` instead, which doesn't produce warnings.

Value

`require.nowarnings` returns (invisibly) `TRUE` if it succeeds, otherwise `FALSE`

See Also

`require()`

Examples

```
## This should produce no output:
if (require.nowarnings(nonexistent)) {
  message("Package loaded successfully")
}
```

---

simconf *Simultaneous confidence regions for Gaussian models*

Description

`simconf` is used for calculating simultaneous confidence regions for Gaussian models x. The function returns upper and lower bounds a and b such that $P(a < x < b) = 1 - \alpha$.

Usage

```
simconf(
  alpha,
  mu,
  Q,
  n.iter = 10000,
  Q.chol,
  vars,
  ind = NULL,
  verbose = 0,
  max.threads = 0,
  seed = NULL
)
```

Arguments

alpha	Error probability for the region.
mu	Expectation vector for the Gaussian distribution.
Q	Precision matrix for the Gaussian distribution.
n.iter	Number or iterations in the MC sampler that is used for approximating probabilities. The default value is 10000.
Q.chol	The Cholesky factor of the precision matrix (optional).
vars	Precomputed marginal variances (optional).
ind	Indices of the nodes that should be analyzed (optional).
verbose	Set to TRUE for verbose mode (optional).
max.threads	Decides the number of threads the program can use. Set to 0 for using the maximum number of threads allowed by the system (default).
seed	Random seed (optional).

Details

The pointwise confidence bands are based on the marginal quantiles, meaning that a.marignal is a vector where the ith element equals $\mu_i + q_{\alpha,i}$ and b.marginal is a vector where the ith element equals $\mu_i + q_{1-\alpha,i}$, where μ_i is the expected value of the x_i and $q_{\alpha,i}$ is the α-quantile of $x_i - \mu_i$.

The simultaneous confidence band is defined by the lower limit vector a and the upper limit vector b, where $a_i = \mu_i + cq_\alpha$ and $b_i = \mu_i + cq_{1-\alpha}$, where c is a constant computed such that $P(a < x < b) = 1 - \alpha$.

Value

An object of class "excurobj" with elements

a	The lower bound.
b	The upper bound.
a.marginal	The lower bound for pointwise confidence bands.
b.marginal	The upper bound for pointwise confidence bands.

Author(s)

David Bolin <davidbolin@gmail.com> and Finn Lindgren <finn.lindgren@gmail.com>

References

Bolin et al. (2015) *Statistical prediction of global sea level from global temperature*, Statistica Sinica, vol 25, pp 351-367.

Bolin, D. and Lindgren, F. (2018), *Calculating Probabilistic Excursion Sets and Related Quantities Using excursions*, Journal of Statistical Software, vol 86, no 1, pp 1-20.

See Also

simconf.inla(), simconf.mc(), simconf.mixture()

Examples

```
## Create mean and a tridiagonal precision matrix
n <- 11
mu.x <- seq(-5, 5, length = n)
Q.x <- Matrix(toeplitz(c(1, -0.1, rep(0, n - 2))))
## calculate the confidence region
conf <- simconf(0.05, mu.x, Q.x, max.threads = 2)
## Plot the region
plot(mu.x,
  type = "l", ylim = c(-10, 10),
  main = "Mean (black) and confidence region (red)"
)
lines(conf$a, col = 2)
lines(conf$b, col = 2)
```

`simconf.inla` *Simultaneous confidence regions for latent Gaussian models*

Description

`simconf.inla` is used for calculating simultaneous confidence regions for latent Gaussian models estimated using `INLA`.

Usage

```
simconf.inla(
  result.inla,
  stack,
  name = NULL,
  tag = NULL,
  ind = NULL,
  alpha,
  method = "NI",
  n.iter = 10000,
  verbose = FALSE,
  link = FALSE,
  max.threads = 0,
  compressed = TRUE,
  seed = NULL,
  inla.sample = TRUE
)
```

Arguments

`result.inla`	Result object from INLA call.
`stack`	The stack object used in the INLA call.

name	The name of the component for which to do the calculation. This argument should only be used if a stack object is not provided, use the tag argument otherwise.
tag	The tag of the component in the stack for which to do the calculation. This argument should only be used if a stack object is provided, use the name argument otherwise.
ind	If only a part of a component should be used in the calculations, this argument specifies the indices for that part.
alpha	Error probability for the region.
method	Method for handling the latent Gaussian structure: **'EB'** Empirical Bayes (Gaussian approximation of posterior). **'NI'** Numerical integration (Calculation based on the Gaussian mixture approximation of the posterior, as calculated by INLA).
n.iter	Number or iterations in the MC sampler that is used for approximating probabilities. The default value is 10000.
verbose	Set to TRUE for verbose mode (optional).
link	Transform output to the scale of the data using the link function as defined in the model estimated with INLA (default FALSE).
max.threads	Decides the number of threads the program can use. Set to 0 for using the maximum number of threads allowed by the system (default).
compressed	If INLA is run in compressed mode and a part of the linear predictor is to be used, then only add the relevant part. Otherwise the entire linear predictor is added internally (default TRUE).
seed	Random seed (optional).
inla.sample	Set to TRUE if inla.posterior.sample should be used for the MC integration.

Details

See simconf() for details.

Value

An object of class "excurobj" with elements

a	The lower bound.
b	The upper bound.
a.marginal	The lower bound for pointwise confidence bands.
b.marginal	The upper bound for pointwise confidence bands.

Note

This function requires the INLA package, which is not a CRAN package. See https://www.r-inla.org/download-install for easy installation instructions.

Author(s)

David Bolin <davidbolin@gmail.com>

References

Bolin et al. (2015) *Statistical prediction of global sea level from global temperature*, Statistica Sinica, vol 25, pp 351-367.

Bolin, D. and Lindgren, F. (2018), *Calculating Probabilistic Excursion Sets and Related Quantities Using excursions*, Journal of Statistical Software, vol 86, no 1, pp 1-20.

See Also

simconf(), simconf.mc(), simconf.mixture()

Examples

```
## Not run:
if (require.nowarnings("INLA")) {
  n <- 10
  x <- seq(0, 6, length.out = n)
  y <- sin(x) + rnorm(n)
  mu <- 1:n
  result <- inla(y ~ 1 + f(mu, model = "rw2"),
    data = list(y = y, mu = mu), verbose = FALSE,
    control.compute = list(
      config = TRUE,
      return.marginals.predictor = TRUE
    ),
    num.threads = "1:1"
  )

  res <- simconf.inla(
    result,
    name = "mu", alpha = 0.05,
    max.threads = 1, num.threads = "1:1"
  )

  plot(result$summary.random$mu$mean, ylim = c(-2, 2))
  lines(res$a)
  lines(res$b)
  lines(res$a.marginal, col = "2")
  lines(res$b.marginal, col = "2")
}

## End(Not run)
```

simconf.mc *Simultaneous confidence regions using Monte Carlo samples*

Description

simconf.mc is used for calculating simultaneous confidence regions based on Monte Carlo samples. The function returns upper and lower bounds a and b such that $P(a < x < b) = 1 - \alpha$.

Usage

```
simconf.mc(samples, alpha, ind, verbose = FALSE)
```

Arguments

samples	Matrix with model Monte Carlo samples. Each column contains a sample of the model.
alpha	Error probability for the region.
ind	Indices of the nodes that should be analyzed (optional).
verbose	Set to TRUE for verbose mode (optional).

Details

See simconf() for details.

Value

An object of class "excurobj" with elements

a	The lower bound.
b	The upper bound.
a.marginal	The lower bound for pointwise confidence bands.
b.marginal	The upper bound for pointwise confidence bands.

Author(s)

David Bolin <davidbolin@gmail.com>

See Also

simconf(), simconf.inla()

Examples

```
## Create mean and a tridiagonal precision matrix
n <- 11
mu.x <- seq(-5, 5, length = n)
Q.x <- Matrix(toeplitz(c(1, -0.1, rep(0, n - 2))))
## Sample the model 100 times (increase for better estimate)
X <- mu.x + solve(chol(Q.x), matrix(rnorm(n = n * 100), nrow = n, ncol = 100))
## calculate the confidence region
conf <- simconf.mc(X, 0.2)
## Plot the region
plot(mu.x,
  type = "l", ylim = c(-10, 10),
  main = "Mean (black) and confidence region (red)"
)
lines(conf$a, col = 2)
lines(conf$b, col = 2)
```

`simconf.mixture` *Simultaneous confidence regions for Gaussian mixture models*

Description

`simconf.mixture` is used for calculating simultaneous confidence regions for Gaussian mixture models. The distribution for the process x is assumed to be

$$\pi(x) = \sum_{k=1}^{K} w_k N(\mu_k, Q_k^{-1}).$$

The function returns upper and lower bounds a and b such that $P(a < x < b) = 1 - \alpha$.

Usage

```
simconf.mixture(
  alpha,
  mu,
  Q,
  w,
  ind,
  n.iter = 10000,
  vars,
  verbose = FALSE,
  max.threads = 0,
  seed = NULL,
  mix.samp = TRUE
)
```

Arguments

alpha	Error probability for the region.
mu	A list with the k expectation vectors μ_k.
Q	A list with the k precision matrices Q_k.
w	A vector with the weights for each class in the mixture.
ind	Indices of the nodes that should be analyzed (optional).
n.iter	Number or iterations in the MC sampler that is used for approximating probabilities. The default value is 10000.
vars	A list with precomputed marginal variances for each class (optional).
verbose	Set to TRUE for verbose mode (optional).
max.threads	Decides the number of threads the program can use. Set to 0 for using the maximum number of threads allowed by the system (default).
seed	Random seed (optional).
mix.samp	If TRUE, the MC integration is done by directly sampling the mixture, otherwise sequential integration is used.

Details

See simconf() for details.

Value

An object of class "excurobj" with elements

a	The lower bound.
b	The upper bound.
a.marginal	The lower bound for pointwise confidence bands.
b.marginal	The upper bound for pointwise confidence bands.

Author(s)

David Bolin <davidbolin@gmail.com>

References

Bolin et al. (2015) *Statistical prediction of global sea level from global temperature*, Statistica Sinica, vol 25, pp 351-367.

Bolin, D. and Lindgren, F. (2018), *Calculating Probabilistic Excursion Sets and Related Quantities Using excursions*, Journal of Statistical Software, vol 86, no 1, pp 1-20.

See Also

simconf(), simconf.inla(), simconf.mc()

Examples

```
n <- 11
K <- 3
mu <- Q <- list()
for (k in 1:K) {
  mu[[k]] <- k * 0.1 + seq(-5, 5, length = n)
  Q[[k]] <- Matrix(toeplitz(c(1, -0.1, rep(0, n - 2))))
}
## calculate the confidence region
conf <- simconf.mixture(0.05, mu, Q, w = rep(1 / 3, 3), max.threads = 2)

## Plot the region
plot(mu[[1]], type = "l")
lines(mu[[2]])
lines(mu[[3]])
lines(conf$a, col = 2)
lines(conf$b, col = 2)
```

---

submesh.grid *Extract a part of a grid*

Description

Extracts a part of a grid.

Usage

```
submesh.grid(z, grid = NULL)
```

Arguments

z	A matrix with values indicating which nodes that should be present in the submesh.
grid	A list with locations and dimensions of the grid.

Value

An fm_mesh_2d object.

Author(s)

Finn Lindgren <finn.lindgren@gmail.com>

Examples

```
## Not run:
if (require("fmesher")) {
  nxy <- 40
  x <- seq(from = 0, to = 4, length.out = nxy)
  lattice <- fm_lattice_2d(x = x, y = x)
  mesh <- fm_rcdt_2d_inla(lattice = lattice, extend = FALSE, refine = FALSE)

  # extract a part of the mesh inside a circle
  xy.in <- rowSums((mesh$loc[, 1:2] - 2)^2) < 1
  submesh <- submesh.grid(
    matrix(xy.in, nxy, nxy),
    list(loc = mesh$loc, dim = c(nxy, nxy))
  )
  plot(mesh$loc[, 1:2])
 lines(2 + cos(seq(0, 2 * pi, length.out = 100)), 2 + sin(seq(0, 2 * pi, length.out = 100)))
  plot(submesh, add = TRUE)
  points(mesh$loc[xy.in, 1:2], col = "2")
}

## End(Not run)
```

`submesh.mesh` *Extract a part of a mesh*

Description

Extracts a part of a mesh

Usage

```
submesh.mesh(z, mesh)
```

Arguments

`z`	A matrix with values indicating which nodes that should be present in the submesh.
`mesh`	An `fm_mesh_2d` object.

Value

An `fm_mesh_2d` object.

Author(s)

Finn Lindgren <finn.lindgren@gmail.com>

Examples

```
## Not run:
if (require(fmesher)) {
  nxy <- 30
  x <- seq(from = 0, to = 4, length.out = nxy)
  lattice <- fm_lattice_2d(x = x, y = x)
  mesh <- fm_rcdt_2d_inla(lattice = lattice, extend = FALSE, refine = FALSE)

  # extract a part of the mesh inside a circle
  xy.in <- rowSums((mesh$loc[, 1:2] - 2)^2) < 1
  submesh <- submesh.mesh(matrix(xy.in, nxy, nxy), mesh)
  plot(mesh$loc[, 1:2], pch = 20)
 lines(2 + cos(seq(0, 2 * pi, length.out = 100)), 2 + sin(seq(0, 2 * pi, length.out = 100)))
  plot(submesh, add = TRUE)
  points(mesh$loc[xy.in, 1:2], col = "2")
}

## End(Not run)
```

`summary.excurobj` *Summarise excurobj objects*

Description

Summary method for class "excurobj"

Usage

```
## S3 method for class 'excurobj'
summary(object, ...)

## S3 method for class 'summary.excurobj'
print(x, ...)

## S3 method for class 'excurobj'
print(x, ...)
```

Arguments

`object`	an object of class "excurobj", usually, a result of a call to `excursions()`.
`...`	further arguments passed to or from other methods.
`x`	an object of class "summary.excurobj", usually, a result of a call to `summary.excurobj()`.

`tricontour` *Calculate contour curves on a triangulation*

Description

Calculates contour curves and/or regions between them, for functions defined on a triangulation

Usage

```
tricontour(
  x,
  z,
  nlevels = 10,
  levels = pretty(range(z, na.rm = TRUE), nlevels),
  ...
)

## S3 method for class 'fm_mesh_2d'
tricontour(
  x,
  z,
  nlevels = 10,
  levels = pretty(range(z, na.rm = TRUE), nlevels),
  ...
)

## S3 method for class 'matrix'
tricontour(
  x,
  z,
  nlevels = 10,
  levels = pretty(range(z, na.rm = TRUE), nlevels),
  loc,
  ...
)

## S3 method for class 'list'
tricontour(
  x,
  z,
  nlevels = 10,
  levels = pretty(range(z, na.rm = TRUE), nlevels),
  loc,
  type = c("+", "-"),
  tol = 1e-07,
  ...
)
```

```
tricontourmap(
  x,
  z,
  nlevels = 10,
  levels = pretty(range(z, na.rm = TRUE), nlevels),
  ...
)

## S3 method for class 'fm_mesh_2d'
tricontourmap(
  x,
  z,
  nlevels = 10,
  levels = pretty(range(z, na.rm = TRUE), nlevels),
  ...
)

## S3 method for class 'matrix'
tricontourmap(
  x,
  z,
  nlevels = 10,
  levels = pretty(range(z, na.rm = TRUE), nlevels),
  loc,
  ...
)

## S3 method for class 'list'
tricontourmap(
  x,
  z,
  nlevels = 10,
  levels = pretty(range(z, na.rm = TRUE), nlevels),
  loc,
  type = c("+", "-"),
  tol = 1e-07,
  output = c("sp", "fm", "inla.mesh.segment"),
  ...
)
```

Arguments

x	An object generated by a call to fm_mesh_2d or fm_rcdt_2d, a triangle-vertex index matrix, or a list of triangulation information, list(loc, graph=list(tv)).
z	A vector containing the values to be contoured (NAs are allowed).
nlevels	Number of contour levels desired, if and only if levels is not supplied.
levels	Numeric vector of levels at which to calculate contour lines.

...	Additional arguments passed to the other methods.
loc	coordinate matrix, to be supplied when x is given as a triangle-vertex index matrix only.
type	"+" or "-", indicating positive or negative association. For +, the generated contours enclose regions where $u_1 \leq z < u_2$, for - the regions fulfil $u_1 < z \leq u_2$.
tol	tolerance for determining if the value at a vertex lies on a level.
output	The format of the generated output. Implemented options are "sp" (default) and "fm" (and deprecated "inla.mesh.segment", converted to "fm").

Value

For tricontour, a list with some of the fields that fm_segm objects have:

loc	A coordinate matrix
idx	Contour segment indices, as a 2-column matrix, each row indexing a single segment
grp	A vector of group labels. Each segment has a label, in 1,...,nlevels*2+1, where even labels indicate interior on-level contour segments, and odd labels indicate boundary segments between levels.

For tricontourmap, a list:

contour	A list of sp or fm_segm objects defining countour curves (level sets)
map	A list of sp or fm_segm objects enclosing regions between level sets

Author(s)

Finn Lindgren <finn.lindgren@gmail.com>

Examples

```
## Not run:
if (require("fmesher") &&
  require("sp")) {
  ## Generate mesh and SPDE model
  n.lattice <- 20 # increase for more interesting, but slower, examples
  x <- seq(from = 0, to = 10, length.out = n.lattice)
  lattice <- fm_lattice_2d(x = x, y = x)
  mesh <- fm_rcdt_2d_inla(lattice = lattice, extend = FALSE, refine = FALSE)

  ## Generate an artificial sample
  sigma2.e <- 0.1
  n.obs <- 1000
  obs.loc <- cbind(
    runif(n.obs) * diff(range(x)) + min(x),
    runif(n.obs) * diff(range(x)) + min(x)
  )
  Q <- fm_matern_precision(mesh, alpha = 2, rho = 3, sigma = 1)
```

```
  x <- fm_sample(n = 1, Q = Q)
  A <- fm_basis(mesh, loc = obs.loc)
  Y <- as.vector(A %*% x + rnorm(n.obs) * sqrt(sigma2.e))

  ## Calculate posterior
  Q.post <- (Q + (t(A) %*% A) / sigma2.e)
  mu.post <- as.vector(solve(Q.post, (t(A) %*% Y) / sigma2.e))

  ## Calculate continuous contours
  tric <- tricontour(mesh,
    z = mu.post,
    levels = as.vector(quantile(x, c(0.25, 0.75)))
  )

  ## Discrete domain contours
  map <- contourmap(
    n.levels = 2, mu = mu.post, Q = Q.post,
    alpha = 0.1, compute = list(F = FALSE), max.threads = 1
  )

  ## Calculate continuous contour map
  setsc <- tricontourmap(mesh,
    z = mu.post,
    levels = as.vector(quantile(x, c(0.25, 0.75)))
  )

  ## Plot the results
  reo <- mesh$idx$lattice
  idx.setsc <- setdiff(names(setsc$map), "-1")
  cols2 <- contourmap.colors(map,
    col = heat.colors(100, 0.5, rev = TRUE),
    credible.col = grey(0.5, 0)
  )
  names(cols2) <- as.character(-1:2)

  par(mfrow = c(1, 2))
  image(matrix(mu.post[reo], n.lattice, n.lattice),
    main = "mean", axes = FALSE, asp = 1
  )
  plot(setsc$map[idx.setsc], col = cols2[idx.setsc])
  par(mfrow = c(1, 1))
}

## End(Not run)
```

Index

continuous, 4
continuous(), *3*
contourmap, 7
contourmap(), *3*, *5*, *13*, *15, 16*
contourmap.colors, 9
contourmap.colors(), *3*, *9*, *13*, *16*
contourmap.inla, 10
contourmap.inla(), *3*, *9*, *15, 16*
contourmap.mc, 14
contourmap.mc(), *3*, *9*, *13*

exc_safe_inla, 16
excursions, 17
excursions(), *3*, *5*, *23*, *26*, *40*
excursions-package, 3
excursions.inla, 20
excursions.inla(), *3*, *19*, *26*
excursions.mc, 24
excursions.mc(), *3*, *19*, *23*
excursions.variances, 26

gaussint, 27

print.excurobj *(*summary.excurobj*)*, 40
print.summary.excurobj
        *(*summary.excurobj*)*, 40

require(), *30*
require.nowarnings, 29

simconf, 30
simconf(), *4*, *33–35*, *37*
simconf.inla, 32
simconf.inla(), *4*, *31*, *35*, *37*
simconf.mc, 35
simconf.mc(), *4*, *31*, *34*, *37*
simconf.mixture, 36
simconf.mixture(), *4*, *31*, *34*
submesh.grid, 38
submesh.mesh, 39
summary.excurobj, 40
summary.excurobj(), *40*

tricontour, 41
tricontour(), *3*
tricontourmap *(*tricontour*)*, 41
tricontourmap(), *3*