Package: dad (via r-universe)

November 25, 2024

Type Package

Title Three-Way / Multigroup Data Analysis Through Densities

Version 4.1.5

Author Rachid Boumaza [aut], Pierre Santagostini [aut, cre], Smail Yousfi [aut], Gilles Hunault [ctb], Julie Bourbeillon [ctb], Besnik Pumo [ctb], Sabine Demotes-Mainard [aut]

Maintainer Pierre Santagostini

<pierre.santagostini@agrocampus-ouest.fr>

Description The data consist of a set of variables measured on several groups of individuals. To each group is associated an estimated probability density function. The package provides tools to create or manage such data and functional methods (principal component analysis, multidimensional scaling, cluster analysis, discriminant analysis...) for such probability densities.

URL https://forgemia.inra.fr/dad/dad

BugReports https://forgemia.inra.fr/dad/dad/-/issues

Depends R (>= 3.6.0)

- **Imports** methods, stats, graphics, grDevices, utils, ggplot2, e1071, DescTools
- Suggests MASS, knitr, markdown, rmarkdown

Encoding UTF-8

License GPL (≥ 2)

VignetteBuilder knitr

RoxygenNote 7.3.2

NeedsCompilation no

Repository CRAN

Date/Publication 2024-11-22 14:20:13 UTC

Config/pak/sysreqs make libssl-dev libx11-dev zlib1g-dev

Contents

dad-package	5
appendtofolderh	7
as.data.frame.folder	8
as.data.frame.folderh	9
as.data.frame.foldert	11
as.folder	12
as.folder.data.frame	13
as.folder.folderh	14
as.folderh	16
as.folderh.foldermtg	17
as.foldert	18
as.foldert.array	19
as.foldert.data.frame	20
association measures	22
association measures for folder	23
bandwidth.parameter	24
castles	25
castles.dated	26
castles.nondated	27
cor.folder	
cut.data.frame	
cut.folder	
ddchisqsym	32
ddchisqsympar	
ddhellinger	
ddhellingerpar	
ddjeffreys	37
ddjeffreyspar	38
ddjensen	39
ddjensenpar	40
ddlp	42
ddlppar	43
departments	44
discdd.misclass	45
discdd.predict	48
distl2d	51
distl2dnorm	52
distl2dnormpar	54
distl2dpar	55
dspg	56
dspgd2015	57
dstatis.inter	58
fdiscd.misclass	60
fdiscd.predict	63
fhclustd	66
floribundity	69

Contents

fmdsd	70
folder	74
folderh	
foldermtg	
foldert	
fpcad	81
fpcat	
getcol.folder	
getcol.foldert	
getrow.folder	
getrow.foldert	
hclustdd	
hellinger	
hellingerpar	
interpret	
interpret.dstatis	
interpret.fmdsd	
interpret.fpcad	
interpret.fpcat	
1 1	
interpret.mdsdd	
is.discdd.misclass	
is.discdd.predict	
is.dstatis	
is.fdiscd.misclass	
is.fdiscd.predict	
is.fhclustd	
is.fmdsd	
is.folder	
is.folderh	
is.foldermtg	
is.foldert	
is.fpcad	
is.mdsdd	
jeffreys	
jeffreyspar	115
kurtosis.folder	
12d	
12dpar	
matddchisqsym	
matddchisqsympar	
matddhellinger	
matddhellingerpar	
matddjeffreys	
matddjeffreyspar	
matddjensen	
matddjensenpar	
matddjp	
matddlppar	
mutuapput	

matdistl2d	. 131
matdistl2dnorm	. 132
matdistl2dnormpar	. 134
matdistl2dpar	
mathellinger	
mathellingerpar	
matipl2d	
matipl2dpar	
matjeffreys	
matjeffreyspar	
matwasserstein	
matwassersteinpar	
mdsdd	
mean.folder	
mtgcomponents	
mtgorder	
mtgplant1	
mtgplant2	
mtgrank	
plot.dstatis	
plot.fhclustd	
plot.fmdsd	
plot.foldert	
plot.fpcad	
plot.fpcat	
plot.hclustdd	
plot.mdsdd	
plotframes	
print.discdd.misclass	
print.discdd.predict	
print.disedd.predict	
print.discd.misclass	
print.fdiscd.predict	
print.fulustd	
print.fmdsd	
print.foldermtg	
print.foldert	
print.fpcad	
print.fpcat	
print.hclustdd	
print.mdsdd	
read.mtg	
rmcol.folder	
rmcol.foldert	
rmrow.folder	
rmrow.foldert	
roseflowers	
roseleaves	. 187

dad-package

rosephytomer		•			•						•			•		•	•			•	•	•		•		188
roses																										189
skewness.folder														•												190
sqrtmatrix														•												191
summary.folder														•		•	•									192
summary.folderh .														•		•	•									193
summary.foldermtg		•						•		•				•		•	•			•	•	•				194
summary.foldert		•						•		•				•		•	•			•	•	•				195
var.folder				•	•			•		•				•		•	•	•		•	•	•				196
varietyleaves				•	•			•		•				•		•	•	•		•	•	•			•	197
wasserstein				•				•		•				•		•	•	•		•	•	•			•	197
wassersteinpar	 •	•							•	•		•	•	•		•	•	•	•	•						199
																										201

Index

dad-package

Three-Way Data Analysis Through Densities

Description

The three-way data consists of a set of variables measured on several groups of individuals. To each group is associated an estimated probability density function. The package provides functional methods (principal component analysis, multidimensional scaling, cluster analysis, discriminant analysis...) for such probability densities.

Details

Package:	dad
Туре:	Package
Version:	4.1.2
Date:	2023-08-28
License:	GPL-2
URL: https://forgemia.inra.fr/dad/dad BugReports: https://forgemia.inra.fr/dad/dad/issues	

To cite dad, use citation("dad").

The main functions applying to the probability densities are:

- fpcad: functional principal component analysis,
- fpcat: functional principal component analysis applied to data indexed according to time,
- fmdsd: multidimensional scaling,
- fhclustd: hierarchical clustering,
- fdiscd.misclass: functional discriminant analysis in order to compute the misclassification ratio with the one-leave-out method,
- fdiscd.predict: discriminant analysis in order to predict the class (synonymous with cluster, not to be confused with the class attribute of an R object) of each probability density whose class is unknown,

- mdsdd: multidimensional scaling of discrete probability distributions,
- discdd.misclass: functional discriminant analysis of discrete probability distributions, in order to compute the misclassification ratio with the one-leave-out method,
- discdd.predict: discriminant analysis of discrete probability distributions, in order to predict the class of each probability distribution whose class is unknown,

The above functions are completed by:

- A print() method for objects of class fpcad, fmdsd, fdiscd.misclass, fdiscd.predict or mdsdd, in order to display the results of the corresponding function,
- A plot() method for objects of class fpcad, fmdsd, fhclustd or mdsdd, in order to display some useful graphics attached to the corresponding function,
- A generic function interpret that applies to objects of class fpcad fmdsd or mdsdd, helps the user to interpret the scores returned by the corresponding function, in terms of moments (fpcad or fmdsd) or in terms of marginal probability distributions (mdsdd).

We also introduce classes of objects and tools in order to handle collections of data frames:

• folder creates an object of class folder, that is a list of data frames which have in common the same columns.

The following functions apply to a folder and compute some statistics on the columns of its elements: mean.folder, var.folder, cor.folder, skewness.folder or kurtosis.folder.

- folderh creates an object of class folderh, that is a list of data frames with a hierarchic relation between each pair of consecutive data frames.
- foldert creates an object of class foldert, that is a list of data frames indexed according to time, concerning the same individuals and variables or not.
- read.mtg creates an object of class foldermtg from an MTG (Multiscale Tree Graph) file containing plant architecture data.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard with the contributions from Gilles Hunault, Julie Bourbeillon and Besnik Pumo

References

Boumaza, R. (1998). Analyse en composantes principales de distributions gaussiennes multidimensionnelles. Revue de Statistique Appliqu?e, XLVI (2), 5-20.

Boumaza, R., Yousfi, S., Demotes-Mainard, S. (2015). Interpreting the principal component analysis of multivariate density functions. Communications in Statistics - Theory and Methods, 44 (16), 3321-3339.

Boumaza, R. (2004). Discriminant analysis with independently repeated multivariate measurements: an L^2 approach. Computational Statistics & Data Analysis, 47, 823-843.

Delicado, P. (2011). Dimensionality reduction when data are density functions. Computational Statistics & Data Analysis, 55, 401-420.

Deza, M.M. and Deza E. (2013). Encyclopedia of distances. Springer.

Pradal, C., Godin, C. and Cokelaer, T. (2023). MTG user guide

Rudrauf, J.M., Boumaza, R. (2001). Contribution à l'étude de l'architecture médiévale: les caractéristiques des pierres à bossage des châteaux forts alsaciens. Centre de Recherches Archéologiques Médiévales de Saverne, 5, 5-38.

Rachev, S.T., Klebanov, L.B., Stoyanov, S.V. and Fabozzi, F.J. (2013). The methods of distances in the theory of probability and statistics. Springer.

Yousfi, S., Boumaza, R., Aissani, D., Adjabi, S. (2014). Optimal bandwith matrices in functional principal component analysis of density functions. Journal of Statistical Computation and Simulation, 85 (11), 2315-2330.

appendtofolderh *Adds a data frame to a* folderh.

Description

Creates an object of class folderh by appending a data frame to an object of class folderh. The appended data frame will be the first or last element of the returned folderh.

Usage

appendtofolderh(fh, df, key, after = FALSE)

Arguments

fh	object of class folderh.
df	data frame to be appended to fh.
key	character string. The key defining the relation $1toN$ between df and the first (if after = FALSE, the default value) or last (if after = TRUE) data frame of fh.
after	logical. If FALSE (default), the data frame df is related to the first data frame of fh, and is appended as the first element of the returned folderh. If TRUE, df is related to the last data frame of fh and becomes the last element of the returned folderh.

Value

Returns an object of class folderh, that is a list of n + 1 data frames where n is the number of data frames of fh. The value of the attribute attr(, "keys") is c(key, attr(fh, "keys")) if after = FALSE), c(attr(fh, "keys"), key) otherwise.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

folderh.

as.data.frame.folder Folder to data frame

Description

Builds a data frame from an object of class folder.

Usage

```
## S3 method for class 'folder'
as.data.frame(x, row.names = NULL, optional = FALSE, ..., group.name = "group")
```

Arguments

х	object of class folder that is a list of data frames with the same column names.					
row.names,optional						
	for consistency with as.data.frame. as.data.frame.folder does not take them into account.					
	further arguments passed to or from other methods.					
group.name	the name of the grouping variable. It is the name of the last column of the returned data frame.					

Details

The data frame is simply obtained by row binding the data frames of the folder and adding a factor (as last column). The name of this column is given by group.name argument. The levels of this factor are the names of the elements of the folder.

Value

as.data.frame.folder returns a data frame.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

folder: object of class folder. as.folder.data.frame: build an object of class folder from a data frame.

as.data.frame.folderh

data(iris)

Examples

```
iris.fold <- as.folder(iris, "Species")
print(iris.fold)
iris.df <- as.data.frame(iris.fold)
print(iris.df)</pre>
```

as.data.frame.folderh Hierarchic folder to data frame

Description

Builds a data frame from a folderh.

Usage

Arguments

x	object of class folderh containing N (N>1) data frames: x[[1]],, x[[N]], related by (N-1) keys: keys[1],, keys[N-1].
row.names,optic	onal
	for consistency with as.data.frame. Not taken into account.
	further arguments passed to or from other methods.
elt	string. The name of one element of x, that is the data frame, say the j-th, whose rows are the rows of the returned data frame. See details.
key	string. The name of an element of $attr(x, "keys")$, that is the key, say the k-th with k <j, column="" data="" designating="" details.<="" factor="" frame.="" is="" last="" of="" returned="" see="" td="" the="" which=""></j,>

Value

as.data.frame.folderh returns a data frame whose row names are those of x[[elt]] (that is x[[j]]). The data frame contains the values of x[[elt]] and the corresponding values of the data frames x[[k]], these correspondances being defined by the keys of the hierarchic folder.

The column names of the returned data frame are organized in three parts.

- 1. The first part consists in the key names keys[k],..., keys[j-1].
- 2. The second part consists in the values of x[[j]].
- 3. The third part consists in the values of x[[k]] except the key keys[k].

See the examples to view these details.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

folder, folderh, as.folder.folderh.

```
# First example: rose flowers
data(roseflowers)
flg <- roseflowers$variety</pre>
flx <- roseflowers$flower</pre>
flfh <- folderh(flg, "rose", flx)</pre>
print(flfh)
fldf <- as.data.frame(flfh)</pre>
print(fldf)
# Second example: castles
data(castles.dated)
cag <- castles.dated$periods</pre>
cax <- castles.dated$stones</pre>
cafh <- folderh(cag, "castle", cax)</pre>
print(cafh)
cadf <- as.data.frame(cafh)</pre>
print(summary(cadf))
# Third example: leaves (example of a folderh with more than two data frames)
data(roseleaves)
lvr <- roseleaves$rose</pre>
lvs <- roseleaves$stem</pre>
lvl <- roseleaves$leaf</pre>
lvll <- roseleaves$leaflet</pre>
lfh <- folderh(lvr, "rose", lvs, "stem", lvl, "leaf", lvll)</pre>
lf1 <- as.data.frame(lfh, elt = "lvs", key = "rose")</pre>
print(lf1)
lf2 <- as.data.frame(lfh, elt = "lvl", key = "rose")</pre>
print(lf2)
lf3 <- as.data.frame(lfh, elt = "lvll", key = "rose")</pre>
print(lf3)
lf4 <- as.data.frame(lfh, elt = "lvll", key = "stem")</pre>
print(lf4)
```

as.data.frame.foldert *foldert to data frame*

Description

Builds a data frame from an object of class foldert.

Usage

```
## S3 method for class 'foldert'
as.data.frame(x, row.names = NULL, optional = FALSE, ..., group.name = "time")
```

Arguments

х	object of class foldert with the same row names. An object of class foldert is a list of data frames with the same column names, each of them corresponding to a time of observation.						
row.names,optional							
	for consistency with as.data.frame. as.data.frame.foldert does not take them into account.						
	further arguments passed to or from other methods.						
group.name	the name of the grouping variable. It is the name of the last column of the returned data frame.						
	As the observations are indexed by time, the default value is group.name = "time".						

Details

as.data.frame.foldert uses as.data.frame.folder.

Value

as.data.frame.foldert returns a data frame.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

foldert: object of class foldert. as.foldert.data.frame: build an object of class foldert from a data frame. as.foldert.array: build an object of class foldert from a 3*d*-array.

Examples

```
data(floribundity)
ftflor <- foldert(floribundity, cols.select = "union", rows.select = "union")
print(ftflor)
dfflor <- as.data.frame(ftflor)
summary(dfflor)</pre>
```

as.folder

Coerce to a folder

Description

Coerces a data frame or an object of class "folderh" to an object of class "folder".

Usage

as.folder(x, ...)

Arguments

х	an object of class data.frame or folderh.
	• data.frame: see as.folder.data.frame
	 folderh: see as.folder.folderh
	further arguments passed to or from other methods.

Value

an object of class folder.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

folder: objects of class folder. as.data.frame.folder: build a data frame from an object of class folder. as.folder.data.frame: build an object of class folder from a data frame. as.folder.folderh: build an object of class folder from an object of class folderh.

12

as.folder.data.frame Data frame to folder

Description

Builds an object of class folder from a data frame.

Usage

```
## S3 method for class 'data.frame'
as.folder(x, groups = tail(colnames(x), 1), ...)
```

Arguments

х	data frame.
groups	string. The name of the column of x containing the grouping variable. x[, groups] must be a factor, otherwise, there is an error.
	If omitted, the last column of x is used as grouping variable.
	further arguments passed to or from other methods.

Value

as.folder.data.frame returns an object of class folder that is a list of data frames with the same column names.

Each element of the folder contains the data corresponding to one level of x[, groups].

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

folder: objects of class folder. as.data.frame.folder: build a data frame from an object of class folder. as.folder.folderh: build an object of class folder from an object of class folderh.

```
# First example: iris (Fisher)
data(iris)
iris.fold <- as.folder(iris, "Species")
print(iris.fold)
# Second example: roses
data(roses)
roses.fold <- as.folder(roses, "rose")
print(roses.fold)</pre>
```

as.folder.folderh Hierarchic folder to folder

Description

Creates an object of class folder, that is a list of data frames with the same column names, from a folderh.

Usage

```
## S3 method for class 'folderh'
as.folder(x, elt = names(x)[2], key = attr(x, "keys")[1], ...)
```

Arguments

x	object of class folderh containing N (N>1) data frames: x[[1]],, x[[N]], related by (N-1) keys: keys[1],, keys[N-1].
elt	string. The name of one element of x, that is data frame, say the j-th, whose rows are distributed among the data frames of the returned folder. See details.
key	string. The name of an element of $attr(x, "keys")$, that is the key, say the k-th with k <j, are="" data="" details.<="" factor="" folder.="" frames="" is="" levels="" names="" of="" returned="" see="" td="" the="" which="" whose=""></j,>
	further arguments passed to or from other methods.

Value

as.folder.folderh returns an object of class folder, a list of data frames with the same columns. These data frames contain the values of x[[elt]] (or x[[j]]) and the corresponding values of the data frames x[[j-1]], ..., x[[k]], these correspondances being defined by the keys of the hierarchic folder. The names of these data frames are given by the levels of the key attr(x, "keys")[k]).

The rows of the data frame x[[elt]] (or x[[j]]) are distributed among the data frames of the returned folder accordingly to the levels of the key attr(x, "keys")[k]. So the row names of the 1-th data frame of the returned folder consist in the rows of x[[j]] corresponding to the 1-th level of the key attr(x, "keys")[k].

The column names of the data frames of the returned folder are the union of the column names of the data frames x[[k]],..., x[[j]] and are organized in two parts.

- The first part consists in the columns of x[[k]] except the column corresponding to the key attr(x, "keys")[k].
- For each i=k+1,..., j the column names of the data frame x[[i]] are reorganized so that the key attr(x, "keys")[i] is its first column. The columns of the reorganized data frames x[[k+1]],..., x[[j]] are concatenated. The result forms the second part.

Notice that if:

• the folderh has two data frames df1 and df2, where the factor corresponding to the key has T levels, and one column of df2, say df2[, "Fa"], is a factor with levels "a1", ..., "ap"

• and the folder returned by as.folder includes T data frames dat1, ..., datT,

then each of dat1, ..., datT has a column named "Fa" which is a factor **with the same levels** "a1", ..., "ap" **as** df2[, "Fa"].

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

folder, folderh. as.folder.folderh to build an object of class folder from an object of class folderh. as.data.frame.folder to build a data frame from an object of class folder. as.data.frame.folderh to build a data frame from an object of class folderh.

```
# First example: flowers
data(roseflowers)
flg <- roseflowers$variety</pre>
flx <- roseflowers$flower</pre>
flfh <- folderh(flg, "rose", flx)</pre>
print(flfh)
flf <- as.folder(flfh)</pre>
print(flf)
# Second example: castles
data(castles.dated)
cag <- castles.dated$periods</pre>
cax <- castles.dated$stones</pre>
cafh <- folderh(cag, "castle", cax)</pre>
print(cafh)
caf <- as.folder(cafh)</pre>
print(caf)
# Third example: leaves (example of a folderh of more than two data frames)
data(roseleaves)
lvr <- roseleaves$rose</pre>
lvs <- roseleaves$stem</pre>
lvl <- roseleaves$leaf</pre>
lvll <- roseleaves$leaflet</pre>
lfh <- folderh(lvr, "rose", lvs, "stem", lvl, "leaf", lvll)</pre>
lf1 <- as.folder(lfh, elt = "lvs", key = "rose")</pre>
print(lf1)
lf2 <- as.folder(lfh, elt = "lvl", key = "rose")</pre>
```

as.folderh

```
print(lf2)
lf3 <- as.folder(lfh, elt = "lvll", key = "rose")
print(lf3)
lf4 <- as.folder(lfh, elt = "lvll", key = "stem")
print(lf4)</pre>
```

as.folderh

Coerce to a folderh

Description

Coerces an object to an object of class folderh.

Usage

as.folderh(x, classes)

Arguments

х	an object to be coerced to an object of class folderh. In the current version, it
	is an object of class "foldermtg" (see as.folderh.foldermtg).
classes	argument useful for as.folderh.foldermtg.

Value

an object of class folderh.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

as.folderh.foldermtg: build an object of class folderh from an object of class foldermtg.

16

as.folderh.foldermtg Build a hierarchic folder from an object of class foldermtg

Description

Creates an object of class folderh from an object of class foldermtg.

Usage

```
## S3 method for class 'foldermtg'
as.folderh(x, classes)
```

Arguments

	х	object of class foldermtg.
classes		character vector. Codes of the vertex classes in the returned folderh. These codes are the names of the elements (data frames) of x containing the features on the vertices corresponding to the codes.
		These codes must be distinct, and the corresponding classes must have distinct scales (see foldermtg). Otherwise, there is an error.
		These codes, except the one with the highest scale, are the keys of the returned folderh.

Details

This function uses folderh.

Value

An object of class folderh. Its elements are the data frames of x containing the features on vertices. Hence, each data frame matches with a class of vertex, and a scale. These data frames are in increasing order of the scale.

A column (factor) is added to the first data frame, containing the identifier of the vertex. Two columns are added to the second data frame:

- 1. the first one is a factor which gives, for each vertex, the name of the vertex of the first data frame which is its "parent",
- 2. and the second one is also a factor and contains the vertex's identifier.

And so on for the third and following data frames, if relevant.

The column containing the vertex identifiers is redundant with the row names; anyway, it is necessary for folderh.

The key of the relationship between the two first data frame is given by the first column of each of these data frames. If there are more than two data frames, the key of the relationship between the n-th and (n + 1)-th data frames (n > 1) is given by the second column of the n\$th data frame and the first column of the (n + 1)-th data frame.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

read.mtg: reads a MTG file and creates an object of class "foldermtg". folderh : object of class folderh.

Examples

```
mtgfile <- system.file("extdata/plant1.mtg", package = "dad")
x <- read.mtg(mtgfile)
# folderh containing the plant ("P") and the stems ("A")
as.folderh(x, classes = c("P", "A"))
# folderh containing the plant ("P"), axes ("A") and phytomers ("M")
as.folderh(x, classes = c("P", "A", "M"))
# folderh containing the plant ("P") and the phytomers ("M")
as.folderh(x, classes = c("P", "M"))
# folderh containing the axes and phytomers
fhPM <- as.folderh(x, classes = c("A", "M"))
# coerce this folderh into a folder, and compute statistics on this folder
fPM <- as.folder(fhPM)
mean(fPM)</pre>
```

as.foldert

Description

Coerces a data frame or array to an object of class foldert.

Coerce to a foldert

Usage

as.foldert(x, ...)

Arguments

```
х
```

an object of class data. frame or array.

- data.frame: see as.foldert.data.frame
- array: see as.foldert.array
- . . .
- arguments passed to as.foldert.data.frame or as.foldert.array, further arguments passed to or from other methods.

as.foldert.array

Value

an object of class foldert.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

as.foldert.array Data frame to foldert

Description

Builds an object of class foldert from a 3*d*-array.

Usage

S3 method for class 'array'
as.foldert(x, ind = 1, var = 2, time = 3, ...)

Arguments

х	a 3 <i>d</i> -array.
ind, var, time	three distinct integers among 1, 2 and 3.
	ind gives the dimension of the observations, var gives the dimension of the variables and ind gives the dimension of the times.
	further arguments passed to or from other methods.

Value

an object ft of class foldert that is a list of data frames, each of them corresponding to a time of observation; these data frames have the same column names.

They necessarily have the same row names (attr(ft, "same.rows")=TRUE). The "times" attribute of ft: attr(ft, "times") is a numeric vector, an ordered factor or an object of class Date, and contains the values of the dimension of x given by time argument.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

foldert: objects of class foldert.

as.foldert.data.frame: build an object of class foldert from a data frame.

Examples

as.foldert.data.frame Data frame to foldert

Description

Builds an object of class foldert from a data frame.

Usage

```
## S3 method for class 'data.frame'
as.foldert(x, method = 1, ind = 1, timecol = 2, nvar = NULL, same.rows = TRUE, ...)
```

Arguments

х	data frame.
method	1 or 2. Indicates the layout of the data frame x and, therefore, the method used to extract the data and build the foldert.
	• If method = 1, there is a column containing the identifiers of the measured objects and a column containing the times. The other columns contain the observations.
	• If method = 2, there is a column containing the identifiers of the measured objects, and the observations are organized as follows:
	 the observations corresponding to the 1st time are on columns timecol (timecol + nvar - 1)
	- the observations corresponding to the 2nd time are on columns (timecol + nvar) : (timecol + 2 * nvar - 1)
	– and so on.
ind	string or numeric. The name of the column of x containing the indentifiers of the measured objects, or the number of this column.
timecol	string or numeric.
	 If method = 1, timecol is the name or the number of the column of x containing the times of observation, or the number of this column. x[, timecol] must be of class "numeric", "ordered", "Date", "POSIXlt" or "POSIXct", otherwise, there is an error.

20

	• If method=2, timecol is the name or the number of the first column corresponding to the first observation. If there are duplicated column names and several columns are named by timecol, the first one is considered.
nvar	integer. If method=2, indicates the number of variables observed at each time. Omitted if method=1.
same.rows	logical. If TRUE (default), the elements of the returned foldert are data frames with the same row names. Necessarily TRUE if method = 2.
	further arguments passed to or from other methods.

Value

an object ft of class foldert, that is a list of data frames organised according to time; these data frames have the same column names.

If method = 1, they can have the same row names (attr(ft, "same.rows") = TRUE) or not (attr(ft, "same.rows") = FALSE). The time attribute attr(ft, "times") has the same class as x[, timecol] (numeric vector, ordered factor or object of class "Date", "POSIXlt" or "POSIXct") and contains the values of x[, timecol].

If method = 2, they necessarily have the same row names: attr(ft, "same.rows") = TRUE and attr(ft, "times") is 1:length(ft).

The rownames of each data frame are the identifiers of the individuals, as given by x[, ind].

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

foldert: objects of class foldert.

as.data.frame.foldert: build a data frame from an object of class foldert.

as.foldert.array: build an object of class foldert from a 3*d*-array.

```
ft1 <- as.foldert(x, method = 1, ind = "ind", timecol = "t", same.rows = TRUE)</pre>
print(ft1)
ft2 <- as.foldert(x, method = 1, ind = "ind", timecol = "t", same.rows = FALSE)</pre>
print(ft2)
data(castles.dated)
periods <- castles.dated$periods</pre>
stones <- castles.dated$stones</pre>
stones$stone <- rownames(stones)</pre>
castledf <- merge(periods, stones, by = "castle")</pre>
castledf$period <- as.numeric(castledf$period)</pre>
castledf$stone <- as.factor(paste(as.character(castledf$castle),</pre>
                              as.character(castledf$stone), sep = "_"))
castfoldt1 <- as.foldert(castledf, method = 1, ind = "stone", timecol = "period",</pre>
                           same.rows = FALSE)
summary(castfoldt1)
# Second example: method = 2
times <- as.Date(c("2017-03-01", "2017-04-01", "2017-05-01"))
y1 <- data.frame(z1=rep(0,6), z2=rep(0,6))</pre>
y2 <- data.frame(z1=rnorm(6,1,1), z2=rnorm(6,3,2))</pre>
y3 <- data.frame(z1=rnorm(6,3,2), z2=rnorm(6,6,3))</pre>
y <- cbind(ind = 1:6, y1, y2, y3)
ft3 <- as.foldert(y, method = 2, ind = "ind", timecol = 2, nvar = 2)</pre>
print(ft3)
```

association measures Association measures between several categorical variables of a data frame

Description

Computes pairwise association measures (Cramer's V, Pearson's contingency coefficient, phi, Tschuprow's T) between the categorical variables of a data frame, using functions of the package DescTools (see Assocs).

Usage

```
cramer.data.frame(x, check = TRUE)
pearson.data.frame(x, check = TRUE)
phi.data.frame(x, check = TRUE)
tschuprow.data.frame(x, check = TRUE)
```

22

Arguments

х	a data frame (can also be a tibble). Its columns should be factors.
check	logical. If TRUE (default) the function checks if each column of x is a factor, and
	there is a warning if it is not.

Value

A square matrix whose elements are the pairwise association measures.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

Examples

```
data(roses)
xr = roses[,c("Sha", "Den", "Sym", "rose")]
xr$Sha = cut(xr$Sha, breaks = c(0, 5, 7, 10))
xr$Den = cut(xr$Den, breaks = c(0, 4, 6, 10))
xr$Sym = cut(xr$Sym, breaks = c(0, 6, 8, 10))
cramer.data.frame(xr)
pearson.data.frame(xr)
phi.data.frame(xr)
tschuprow.data.frame(xr)
```

```
association measures for folder
```

Association measures between categorical variables of the data frames of a folder

Description

Computes the pairwise association measures (Cramer's V, Pearson's contingency coefficient, phi, Tschuprow's T) between the categorical variables of an object of class folder. The computation is carried out using the functions cramer.data.frame, tschuprow.data.frame, pearson.data.frame or phi.data.frame. These functions are built from corresponding functions of the package DescTools (see Assocs)

Usage

```
cramer.folder(xf)
tschuprow.folder(xf)
pearson.folder(xf)
phi.folder(xf)
```

Arguments

xf

an object of class folder that is a list of data frames with the same column names. Its columns should be factors, otherwise there is a warning.

Value

A list the length of which is equal to the number of data frames of the folder. Each element of the list is a square matrice giving the pairwise association measures of the variables of the corresponding data frame.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

Examples

```
data(roses)
xr = roses[,c("Sha", "Den", "Sym", "rose")]
xr$Sha = cut(xr$Sha, breaks = c(0, 5, 7, 10))
xr$Den = cut(xr$Den, breaks = c(0, 4, 6, 10))
xr$Sym = cut(xr$Sym, breaks = c(0, 6, 8, 10))
xfolder = as.folder(xr, groups = "rose")
cramer.folder(xfolder)
pearson.folder(xfolder)
phi.folder(xfolder)
tschuprow.folder(xfolder)
```

bandwidth.parameter *Parameter of the normal reference rule*

Description

Computation of the parameter of the normal reference rule in order to estimate the (matrix) bandwidth.

Usage

```
bandwidth.parameter(p, n)
```

Arguments

р	sample dimension.
n	sample size.

Details

The parameter is equal to:

$$h = \left(\frac{4}{n(p+2)}\right)^{\frac{1}{p+4}}$$

It is based on the minimisation of the asymptotic mean integrated square error in density estimation when using the Gaussian kernel method (Wand and Jones, 1995).

castles

Value

Returns the value required by the functions fpcad, fmdsd, fdiscd.misclass and fdiscd.predict when their argument windowh is set to NULL.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Boumaza, R., Yousfi, S., Demotes-Mainard, S. (2015). Interpreting the principal component analysis of multivariate density functions. Communications in Statistics - Theory and Methods, 44 (16), 3321-3339.

Wand, M. P., Jones, M. C. (1995). Kernel Smoothing. Boca Raton, FL: Chapman and Hall.

Examples

```
# Sample size :
n <- 20
# Number of variables :
p <- 3
bandwidth.parameter(p, n)</pre>
```

castles

Alsacian castles by year of building

Description

The data were collected by J.M. Rudrauf on Alsacian castles whose building year is known (even approximatively). On each castle, he measured 4 structural parameters on a sample of building stones.

These data are about the same castles as in castles.dated data set.

Usage

```
data(castles)
```

Format

castles is a list of 46 data frames. Each of these data frames matches with one year (between 1136 and 1510) and contains measures on one or several castles which have been built since that year.

Each data frame has 5 to 101 rows (stones) and 5 columns: height, width, edging, boss (numeric) and castle (factor).

Source

Rudrauf, J.M., Boumaza, R. (2001). Contribution a l'etude de l'architecture medievale: les caracteristiques des pierres a bossage des chateaux forts alsaciens. Centre de Recherches Archeologiques Medievales de Saverne, 5, 5-38.

Examples

data(castles)
foldert(castles)

castles.dated Dated Alsacian castles

Description

The data were collected by J.M. Rudrauf on Alsacian castles whose building period is known (even approximately). On each castle, he measured 4 structural parameters on a sample of building stones.

Usage

data(castles.dated)

Format

castles.dated is a list of two data frames:

- castles.dated\$stones: this first data frame has 1262 cases (rows) and 5 variables (columns) that are named height, width, edging, boss (numeric) and castle (factor).
- castles.dated\$periods: this second data frame has 68 cases and 2 variables named castle and period; the column castle corresponds to the levels of the factor castle of the first data frame; the column period is a factor with 6 levels indicating the approximative building period. Thus this factor defines 6 classes of castles.

Source

Rudrauf, J.M., Boumaza, R. (2001). Contribution a l'etude de l'architecture medievale: les caracteristiques des pierres a bossage des chateaux forts alsaciens. Centre de Recherches Archeologiques Medievales de Saverne, 5, 5-38.

```
data(castles.dated)
summary(castles.dated$stones)
summary(castles.dated$periods)
```

Description

The data were collected by J.M. Rudrauf on Alsacian castles whose building period is unknown. On each castle, he measured 4 structural parameters on a sample of building stones.

Usage

```
data(castles.nondated)
```

Format

castles.nondated is a list of two data frames:

- castles.nondated\$stones: this first data frame has 1280 cases (rows) and 5 variables (columns) that are named height, width, edging, boss (numeric) and castle (factor).
- castles.nondated\$periods: this second data frame has 67 cases and 2 variables named castle and period; the column castle corresponds to the levels of the factor castle of the first data frame; the column period is a factor indicating NA as the building period is unknown.

Notice that the data frames corresponding to the castles whose building period is known are those in castles.dated.

Source

Rudrauf, J.M., Boumaza, R. (2001). Contribution a l'etude de l'architecture medievale: les caracteristiques des pierres a bossage des chateaux forts alsaciens. Centre de Recherches Archeologiques Medievales de Saverne, 5, 5-38.

```
data(castles.nondated)
summary(castles.nondated$stones)
summary(castles.nondated$periods)
```

cor.folder

Description

Computes the correlation matrices of the elements of an object of class folder.

Usage

cor.folder(x, use = "everything", method = "pearson")

Arguments

x	an object of class folder that is a list of data frames with the same column names.
use	an optional character string giving a method for computing covariances in the presence of missing values. This must be (an abbreviation of) one of the strings "everything", "all.obs", "complete.obs", "na.or.complete", or "pairwise.complete.obs" (see var).
method	a character string indicating which correlation coefficient (or covariance) is to be computed. One of "pearson" (default), "kendall", or "spearman": can be abbreviated.

Details

It uses cor to compute the variance matrix of the numeric columns of each element of the folder. If some columns of the data frames are not numeric, there is a warning, and the variances are computed on the numeric columns only.

Value

A list whose elements are the correlation matrices of the elements of the folder.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

folder to create an object is of class folder. mean.folder, var.folder, skewness.folder, kurtosis.folder for other statistics for folder objects.

cut.data.frame

Examples

```
# First example: iris (Fisher)
data(iris)
iris.fold <- as.folder(iris, "Species")
iris.cor <- cor.folder(iris.fold)
print(iris.cor)
# Second example: roses
data(roses)
roses.fold <- as.folder(roses, "rose")
roses.cor <- cor.folder(roses.fold)
print(roses.cor)</pre>
```

cut.data.frame Change numeric variables into factors

Description

This function changes numerical columns of a data frame x into factors. For each of these columns, its range is divided into intervals and the values of this column is recoded according to which interval they fall.

For that, **cut** is applied to each column of x.

Usage

```
## S3 method for class 'data.frame'
cut(x, breaks, labels = NULL, include.lowest = FALSE, right = TRUE, dig.lab = 3L,
        ordered_result = FALSE, cutcol = NULL, ...)
```

Arguments

х	data frame (can also be a tibble).
breaks	list or numeric.
	• If breaks is a list, its length is equal to the number of columns in the data frame. It can be:
	 a list of numeric vectors. The jth element corresponds to the column x[, j], and is a vector of two or more unique cut points
	 or a list of single numbers (each greater or equal to 2). breaks[[j]] element gives the number of intervals into which th <i>j</i>th variable of the folder is to be cut. The elements breaks[[j]] corresponding to non-numeric columns must be NULL; if not, there is a warning.
	• If breaks is a numeric vector, it gives the number of intervals into which every column x[, j] is to be cut (see cut).

labels	list of character vectors. If given, its length is equal to the number of columns of x. labels[[j]] gives the labels for the intervals of the j^{th} columns of the data frame. By default, the labels are constructed using "(a,b]" interval notation. If labels = FALSE, simple integer codes are returned instead of a factor.	
	See cut.	
include.lowest	logical, indicating if, for each column x[, j], an x[i, j] equal to the lowest (or highest, for right = FALSE) 'breaks' value should be included (see cut).	
right	logical, indicating if the intervals should be closed on the right (and open on the left) or vice versa (see cut).	
dig.lab	integer or integer vector, which is used when labels are not given. It determines the number of digits used in formatting the break numbers.	
	• If it is a single value, it gives the number of digits for all variables of the folder (see cut).	
	• If it is a list of integers, its length is equal to the number of variables, and the j^{th} element gives the number of digits for the j^{th} variable of the folder.	
ordered_result	logical: should the results be ordered factors? (see cut)	
cutcol	numeric vector: indices of the columns to be converted into factors. These columns must all be numeric. Otherwise, there is a warning.	
	further arguments passed to or from other methods.	

Value

A data frame with the same column and row names as x.

If cutcol is given, each numeric column x[, j] whose number is contained in cutcol is replaced by a factor. The other columns are unmodified.

If any column x[, j] whose number is in cutcol is not numeric, it is unmodified.

If cutcol is omitted, every numerical columns are replaced by factors.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

```
data("roses")
x <- roses[roses$rose %in% c("A", "B"), c("Sha", "Sym", "Den", "rose")]
cut(x, breaks = 3)
cut(x, breaks = 5)
cut(x, breaks = c(0, 4, 6, 10))
cut(x, breaks = list(c(0, 6, 8, 10), c(0, 5, 7, 10), c(0, 6, 7, 10)))
cut(x, breaks = list(c(0, 6, 8, 10), c(0, 5, 7, 10)), cutcol = 1:2)</pre>
```

Description

This function applies to a folder. For each elements (data frames) of this folder, it changes its numerical columns into factors, using cut.data.frame.

Usage

```
## S3 method for class 'folder'
cut(x, breaks, labels = NULL, include.lowest = FALSE, right = TRUE, dig.lab = 3L,
        ordered_result = FALSE, cutcol = NULL, ...)
```

Arguments

х	an object of class folder.
breaks	list or numeric, defining the intervals into which the variables of each element of the folder is to be cut. See cut.folder.
labels	list of character vectors. If not omitted, it gives the labels for the intervals of each column of the elements of x . See cut.folder.
include.lowest	logical, indicating if a value equal to the lowest (or highest, for right = FALSE) 'breaks' value should be included (see cut.folder).
right	logical, indicating if the intervals should be closed on the right (and open on the left) or vice versa (see cut.folder).
dig.lab	integer or integer vector, which is used when labels are not given. It determines the number of digits used in formatting the break numbers. See cut.folder.
ordered_result	logical: should the results be ordered factors? (see cut.folder)
cutcol	numeric vector: indices of the columns of the elements of x to be converted into factors. These columns must all be numeric. Otherwise, there is a warning. See cut.folder.
	further arguments passed to or from other methods.

Value

An object of class folder with the same length and names as x. Its elements (data frames) have the same column and row names as the elements of x.

For more details, see cut.data.frame

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

Examples

```
data("roses")
x <- as.folder(roses[, c("Sha", "Den", "Sym", "rose")], groups = "rose")
summary(x)
x3 <- cut(x, breaks = 3)
summary(x3)
x7 <- cut(x, breaks = 7)
summary(x7)</pre>
```

ddchisqsym	Distance between probability distributions of discrete variables given
	samples

Description

Symmetrized chi-squared distance between two multivariate (q > 1) or univariate (q = 1) discrete probability distributions, estimated from samples.

Usage

ddchisqsym(x1, x2)

Arguments

x1, x2 vectors or data frames of q columns (can also be a tibble).If they are data frames and have not the same column names, there is a warning.

Details

Let p_1 and p_2 denote the estimated probability distributions of the discrete samples x_1 and x_2 . The symmetrized chi-squared distance between the discrete probability distributions of the samples are computed using the ddchisqsympar function.

Value

The distance between the two probability distributions.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

References

Deza, M.M. and Deza E. (2013). Encyclopedia of distances. Springer.

32

ddchisqsympar

See Also

ddchisqsympar: chi-squared distance between two discrete distributions, given the probabilities on their common support.

Other distances: ddhellinger, ddjeffreys, ddjensen, ddlp.

Examples

```
ddchisqsympar
```

Distance between discrete probability distributions given the probabilities on their common support

Description

Symmetrized chi-squared distance between two discrete probability distributions on the same support (which can be a Cartesian product of q sets), given the probabilities of the states (which are q-tuples) of the support.

Usage

ddchisqsympar(p1, p2)

Arguments

p1	array (or table) the dimension of which is q . The first probability distribution on the support.
p2	array (or table) the dimension of which is q . The second probability distribution on the support.

Details

The chi-squared distance between two discrete distributions p_1 and p_2 is given by:

$$\sum_{x} (p_1(x) - p_2(x))^2 / p_2(x)$$

Then the symmetrized chi-squared distance is given by the formula:

$$||p_1 - p_2|| = \sum_x (p_1(x) - p_2(x))^2 / (p_1(x) + p_2(x))$$

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

References

Deza, M.M. and Deza E. (2013). Encyclopedia of distances. Springer.

See Also

ddchisqsym: chi-squared distance between two estimated discrete distributions, given samples.

Other distances: ddhellingerpar, ddjeffreyspar, ddjensenpar, ddlppar.

Examples

ddhellinger	Distance between probability distributions of discrete variables given
	samples

Description

Hellinger (or Matusita) distance between two multivariate (q > 1) or univariate (q = 1) discrete probability distributions, estimated from samples.

Usage

ddhellinger(x1, x2)

Arguments

x1, x2	data frames of q columns or vectors (can also be tibbles).
	If they are data frames and have not the same column names, there is a warning.

ddhellingerpar

Details

Let p_1 and p_2 denote the estimated probability distributions of the discrete samples x_1 and x_2 . The Matusita distance between the discrete probability distributions of the samples are computed using the ddhellingerpar function.

Value

The distance between the two probability distributions.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

References

Deza, M.M. and Deza E. (2013). Encyclopedia of distances. Springer.

See Also

ddhellingerpar: Hellinger metric (Matusita distance) between two discrete distributions, given the on their common support probabilities.

Other distances: ddchisqsym, ddjeffreys, ddjensen, ddlp.

Examples

ddhellingerpar

Distance between discrete probability distributions given the probabilities on their common support

Description

Hellinger (or Matusita) distance between two discrete probability distributions on the same support (which can be a Cartesian product of q sets), given the probabilities of the states (which are q-tuples) of the support.

Usage

ddhellingerpar(p1, p2)

Arguments

р1	array (or table) the dimension of which is q . The first probability distribution on the support.
p2	array (or table) the dimension of which is q . The second probability distribution on the support.

Details

The Hellinger distance between two discrete distributions p_1 and p_2 is given by: $\sqrt{\sum_x (\sqrt{p_1(x)} - \sqrt{p_2(x)})^2}$ Notice that some authors divide this expression by $\sqrt{2}$.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

References

Deza, M.M. and Deza E. (2013). Encyclopedia of distances. Springer.

See Also

ddhellinger: Hellinger distance between two estimated discrete distributions, given samples. Other distances: ddchisqsympar, ddjeffreyspar, ddjensenpar, ddlppar.

ddjeffreys

Divergence between probability distributions of discrete variables given samples

Description

jeffreys's divergence (symmetrized Kullback-Leibler divergence) between two multivariate (q > 1) or univariate (q = 1) discrete probability distributions, estimated from samples.

Usage

ddjeffreys(x1, x2)

Arguments

x1, x2	vectors or data frames of q columns (can also be a tibble).
	If they are data frames and have not the same column names, there is a warning.

Details

Let p_1 and p_2 denote the estimated probability distributions of the discrete samples x_1 and x_2 . The jeffreys's divergence between the discrete probability distributions of the samples are computed using the ddjeffreyspar function.

Value

The divergence between the two probability distributions.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

References

Deza, M.M. and Deza E. (2013). Encyclopedia of distances. Springer.

See Also

ddjeffreyspar: Jeffrey's distances between two discrete distributions, given the probabilities on their common support.

Other distances: ddchisqsym, ddhellinger, ddjensen, ddlp.

Examples

```
ddjeffreyspar
```

Distance between discrete probability distributions given the probabilities on their common support

Description

Jeffreys divergence (symmetrized Kullback-Leibler divergence) between two discrete probability distributions on the same support (which can be a Cartesian product of q sets), given the probabilities of the states (which are q-tuples) of the support.

Usage

ddjeffreyspar(p1, p2)

Arguments

p1	array (or table) the dimension of which is q . The first probability distribution on the support.
p2	array (or table) the dimension of which is q . The second probability distribution on the support.

Details

Jeffreys divergence $||p_1 - p_2||$ between two discrete distributions p_1 and p_2 is given by the formula:

$$||p_1 - p_2|| = \sum_x (p_1(x) - p_2(x))log(p_1(x)/p_2(x))$$

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

38

ddjensen

References

Deza, M.M. and Deza E. (2013). Encyclopedia of distances. Springer.

See Also

ddjeffreys: Jeffreys distance between two estimated discrete distributions, given samples.

Other distances: ddchisqsympar, ddhellingerpar, ddjensenpar, ddlppar.

Examples

ddjensen	Divergence between	probability	distributions	of	discrete	variables
	given samples					

Description

Jensen-Shannon divergence between two multivariate (q > 1) or univariate (q = 1) discrete probability distributions, estimated from samples.

Usage

```
ddjensen(x1, x2)
```

Arguments

x1, x2	vectors or data frames of q columns (can also be tibbles).
	If they are data frames and have not the same column names, there is a warning.

Details

Let p_1 and p_2 denote the estimated probability distributions of the discrete samples x_1 and x_2 . The Jensen-Shannon divergence between the discrete probability distributions of the samples are computed using the ddjensenpar function.

ddjensenpar

Value

The distance between the two probability distributions.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

References

Deza, M.M. and Deza E. (2013). Encyclopedia of distances. Springer.

See Also

ddjensenpar: Jensen-Shannon distance between two discrete distributions, given the probabilities on their common support.

Other distances: ddchisqsym, ddhellinger, ddjeffreys, ddlp.

Examples

do	lje	nse	enp	ar

Divergence between discrete probability distributions given the probabilities on their common support

Description

Jensen-Shannon divergence between two discrete probability distributions on the same support (which can be a Cartesian product of q sets), given the probabilities of the states (which are q-tuples) of the support.

Usage

ddjensenpar(p1, p2)

ddjensenpar

Arguments

p1	array (or table) the dimension of which is q . The first probability distribution on the support.
p2	array (or table) the dimension of which is q . The second probability distribution on the support.

Details

The Jensen-Shannon divergence $||p_1 - p_2||$ between two discrete distributions p_1 and p_2 is given by the formula:

$$||p_1 - p_2|| = \sum_x \left(p_1(x) \log(2p_1(x) / (p_1(x) + p_2(x))) \right) + \left(p_2(x) \log(2p_2(x) / (p_1(x) + p_2(x))) \right)$$

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

References

Deza, M.M. and Deza E. (2013). Encyclopedia of distances. Springer.

See Also

ddjensen: Jensen-Shannon distance between two estimated discrete distributions, given samples.

Other distances: ddchisqsympar, ddhellingerpar, ddjeffreyspar, ddlppar.

Examples

ddlp

Distance between probability distributions of discrete variables given samples

Description

 L^p distance between two multivariate (q > 1) or univariate (q = 1) discrete probability distributions, estimated from samples.

Usage

ddlp(x1, x2, p = 1)

Arguments

x1, x2	vectors or data frames of q columns (can also be tibbles).
	If they are data frames and have not the same column names, there is a warning.
р	integer. Parameter of the distance.

Details

Let p_1 and p_2 denote the estimated probability distributions of the discrete samples x_1 and x_2 . The L^p distance between the discrete probability distributions of the samples are computed using the ddlppar function.

Value

The distance between the two discrete probability distributions.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

References

Deza, M.M. and Deza E. (2013). Encyclopedia of distances. Springer.

See Also

ddlppar: L^p distance between two discrete distributions, given the probabilities on their common support.

Other distances: ddchisqsym, ddhellinger, ddjeffreys, ddjensen.

ddlppar

Examples

ddlppar

Distance between discrete probability distributions given the probabilities on their common support

Description

 L^p distance between two discrete probability distributions on the same support (which can be a Cartesian product of q sets), given the probabilities of the states (which are q-tuples) of the support.

Usage

ddlppar(p1, p2, p = 1)

Arguments

p1	array (or table) the dimension of which is q . The first probability distribution on the support.
p2	array (or table) the dimension of which is q . The second probability distribution on the support.
р	integer. Parameter of the distance.

Details

The L^p distance $||p_1 - p_2||$ between two discrete distributions p_1 and p_2 is given by the formula:

$$||p_1 - p_2||^p = \sum_{x} |p_1(x) - p_2(x)|^p$$

If p = 1, it is the variational distance.

If p = 2, it is the Patrick-Fisher distance.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

References

Deza, M.M. and Deza E. (2013). Encyclopedia of distances. Springer.

See Also

ddlp: L^p distance between two estimated discrete distributions, given samples.

Other distances: ddchisqsympar, ddhellingerpar, ddjeffreyspar, ddjensenpar.

Examples

departments French departments and regions

Description

Departments and regions of metropolitan France.

Usage

data(departments)

Format

departments is a data frame with 96 rows and 4 columns (factors):

- coded: departments: numbers
- named: departments: names
- coder: regions: ISO code
- namer: region: names

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

discdd.misclass

Source

INSEE. Code officiel g\'eographique au 1er janvier 2018.

Examples

data(departments)
print(departments)

discdd.misclass

Misclassification ratio in functional discriminant analysis of discrete probability distributions.

Description

Computes the one-leave-out misclassification ratio of the rule assigning T groups of individuals, one group after another, to the class of groups (among K classes of groups) which achieves the minimum of the distances or divergences between the probability distribution associated to the group to assign and the K probability distributions associated to the K classes.

Usage

Arguments

xf

object of class folderh with two data frames or list of arrays (or tables).

• If it is a folderh:

- The first data.frame has at least two columns. One column contains the names of the T groups (all the names must be different). An other column is a factor with K levels partitionning the T groups into K classes.
- The second one has (q + 1) columns. The first q columns are factors (otherwise, they are coerced into factors). The last column is a factor with T levels defining T groups. Each group, say t, consists of n_t individuals.
- If it is a list of arrays or tables, the t^{th} element (t = 1, ..., T) is the table of the joint distribution (absolute or relative frequencies) of the t^{th} group. These arrays have the same shape:

Each array (or table) xf[[i]] has:

- the same dimension(s). If q = 1 (univariate), dim(xf[[i]]) is an integer. If q > 1 (multivariate), dim(xf[[i]]) is an integer vector of length q.
- the same dimension names dimnames(xf[[i]]) (is non NULL). These dimnames are the names of the variables.

class.var	string (if xf is an object of class "folderh") or data.frame with two columns (if xf is a list of arrays).
	 If xf is of class "folder", class.var is the name of the class variable. If xf is a list of arrays or a list of tables, class.var is a data.frame with at least two columns named "group" and "class". The "group" column contains the names of the <i>T</i> groups (all the names must be different). The "class" column is a factor with <i>K</i> levels partitioning the <i>T</i> groups into <i>K</i> classes.
distance	The distance or dissimilarity used to compute the distance matrix between the densities. It can be:
	• "11" (default) the L^p distance with $p = 1$
	• "12" the L^p distance with $p = 2$
	 "chisqsym" the symmetric Chi-squared distance
	 "hellinger" the Hellinger metric (Matusita distance)
	• "jeffreys" Jeffreys distance (symmetrised Kullback-Leibler divergence)
	 "jensen" the Jensen-Shannon distance
	• "lp" the L^p distance with p given by the argument p of the function.
crit	1 or 2. In order to select the densities associated to the classes. See Details.
р	integer. Optional. When distance = "lp" (L^p distance with $p > 2$), p is the parameter of the distance.

Details

• If xf is an object of class "folderh" containing the data:

The T probability distributions f_t corresponding to the T groups of individuals are estimated by frequency distributions within each group.

To the class k consisting of T_k groups is associated the probability distribution g_k , knowing that when using the one-leave-out method, we do not include the group to assign in its class k. The crit argument selects the estimation method of the g_k 's.

- crit=1 The probability distribution g_k is estimated using the whole data of this class, that is the rows of x corresponding to the T_k groups of the class k.
 - The estimation of the g_k 's uses the same method as the estimation of the f_t 's.
- crit=2 The T_k probability distributions f_t are estimated using the corresponding data from xf. Then they are averaged to obtain an estimation of the density g_k , that is $g_k = \frac{1}{T_k} \sum f_t$.
- If xf is a list of arrays (or list of tables):

The t^{th} array is the joint frequency distribution of the t^{th} group. The frequencies can be absolute or relative.

To the class k consisting of T_k groups is associated the probability distribution g_k , knowing that when using the one-leave-out method, we do not include the group to assign in its class k. The crit argument selects the estimation method of the g_k 's.

- crit=1 $g_k = \frac{1}{\sum n_t} \sum n_t f_t$, where n_t is the total of xf[[t]]. Notice that when xf[[t]] contains relative frequencies, its total is 1. That is equivalent to crit=2.
- crit=2 $g_k = \frac{1}{T_k} \sum f_t$.

discdd.misclass

Value

Returns an object of class discdd.misclass, that is a list including:

classification data frame with 4 columns:

- factor giving the group name. The column name is the same as that of the column (q + 1) of x,
- the prior class of the group if it is available, or NA if not,
- alloc: the class allocation computed by the discriminant analysis method,
- misclassed: boolean. TRUE if the group is misclassed, FALSE if it is wellclassed, NA if the prior class of the group is unknown.

```
confusion.mat confusion matrix,
```

misalloc.per.class		
	the misclassification ratio per class,	
misclassed	the misclassification ratio,	
distances	matrix with T rows and K columns, of the distances (d_{tk}) : d_{tk} is the distance between the group t and the class k,	
proximities	matrix of the proximity indices (in percents) between the groups and the classes. The proximity between the group t and the class k is: $(1/d_{tk})/\sum_{l=1}^{l=K} (1/d_{tl})$.	

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Rudrauf, J.M., Boumaza, R. (2001). Contribution à l'étude de l'architecture médiévale: les caractéristiques des pierres à bossage des châteaux forts alsaciens, Centre de Recherches Archéologiques médiévales de Saverne, 5, 5-38.

Examples

```
# Example 1 with a folderh obtained by converting numeric variables
data("castles.dated")
stones <- castles.dated$periods
stones$height <- cut(stones$height, breaks = c(19, 27, 40, 71), include.lowest = TRUE)
stones$width <- cut(stones$width, breaks = c(24, 45, 62, 144), include.lowest = TRUE)
stones$edging <- cut(stones$edging, breaks = c(0, 3, 4, 8), include.lowest = TRUE)
stones$boss <- cut(stones$boss, breaks = c(0, 6, 9, 20), include.lowest = TRUE )
castlefh <- folderh(periods, "castle", stones)
# Default: dist="11", crit=1
discdd.misclass(castlefh, "period")
# Hellinger distance, crit=2
discdd.misclass(castlefh, "period", distance = "hellinger", crit = 2)
```

```
# Example 2 with a list of 96 arrays
data("dspgd2015")
data("departments")
classes <- departments[, c("coded", "namer")]
names(classes) <- c("group", "class")
# Default: dist="11", crit=1
discdd.misclass(dspgd2015, classes)
# Hellinger distance, crit=2
discdd.misclass(dspgd2015, classes, distance = "hellinger", crit = 2)
```

discdd.predict *Predicting the class of a group of individuals with discriminant analysis of probability distributions.*

Description

Assigns several groups of individuals, one group after another, to the class of groups (among K classes of groups) which achieves the minimum of the distances or divergences between the probability distribution associated to the group to assign and the K probability distributions associated to the K classes.

Usage

Arguments

xf

object of class folderh with two data frames or list of arrays (or tables).

- If it is a folderh:
 - The first data.frame has at least two columns. One column contains the names of the T groups (all the names must be different). An other column is a factor with K levels partitionning the T groups into K classes.
 - The second one has (q + 1) columns. The first q columns are factors (otherwise, they are coerced into factors). The last column is a factor with T levels defining T groups. Each group, say t, consists of n_t individuals.
- If it is a list of arrays or tables, the t^{th} element (t = 1, ..., T) is the table of the joint distribution (absolute or relative frequencies) of the t^{th} group. These arrays have the same shape:

Each array (or table) xf[[i]] has:

the same dimension(s). If q = 1 (univariate), dim(xf[[i]]) is an integer. If q > 1 (multivariate), dim(xf[[i]]) is an integer vector of length q.

class.var string (if xf is an object of class "folderh") or data.frame with two columns (if xf is a list of arrays).

- If xf is of class "folder", class.var is the name of the class variable.
- If xf is a list of arrays or a list of tables, class.var is a data.frame with at least two columns named "group" and "class". The "group" column contains the names of the T groups (all the names must be different). The "class" column is a factor with K levels partitioning the T groups into K classes.
- distance The distance or dissimilarity used to compute the distance matrix between the densities. It can be:
 - "11" (default) the L^p distance with p = 1
 - "12" the L^p distance with p = 2
 - "chisqsym" the symmetric Chi-squared distance
 - "hellinger" the Hellinger metric (Matusita distance)
 - "jeffreys" Jeffreys distance (symmetrised Kullback-Leibler divergence)
 - "jensen" the Jensen-Shannon distance
 - "lp" the L^p distance with p given by the argument p of the function.
 - 1 or 2. In order to select the densities associated to the classes. See Details.
- misclass.ratio logical (default FALSE). If TRUE, the confusion matrix and misclassification ratio are computed on the groups whose prior class is known. In order to compute the misclassification ratio by the one-leave-out method, use the discdd.misclass function.
- p integer. Optional. When distance = "lp" (L^p distance with p > 2), p is the parameter of the distance.

Details

crit

• If xf is an object of class "folderh" containing the data:

The T probability distributions f_t corresponding to the T groups of individuals are estimated by frequency distributions within each group.

To the class k consisting of T_k groups is associated the probability distribution g_k . The crit argument selects the estimation method of the g_k 's.

- crit=1 The probability distribution g_k is estimated using the whole data of this class, that is the rows of x corresponding to the T_k groups of the class k.
 - The estimation of the g_k 's uses the same method as the estimation of the f_t 's.
- crit=2 The T_k probability distributions f_t are estimated using the corresponding data from xf. Then they are averaged to obtain an estimation of the density g_k , that is $g_k = \frac{1}{T_k} \sum f_t$.
- If xf is a list of arrays (or list of tables):

The t^{th} array is the joint frequency distribution of the t^{th} group. The frequencies can be absolute or relative.

To the class k consisting of T_k groups is associated the probability distribution g_k . The crit argument selects the estimation method of the g_k 's.

- crit=1 $g_k = \frac{1}{\sum n_t} \sum n_t f_t$, where n_t is the total of xf[[t]]. Notice that when xf[[t]] contains relative frequencies, its total is 1. That is equivalent to crit=2.
- crit=2 $g_k = \frac{1}{T_k} \sum f_t$.

Value

Returns an object of class discdd.predict, that is a list including:

prediction	data frame with 3 columns:
	• factor giving the group name. The column name is the same as that of the column (q + 1) of x,
	• class.known: the prior class of the group if it is available, or NA if not,
	• class.predict: the class allocation predicted by the discriminant analysis method. If misclass.ratio = TRUE, the class allocations are computed for all groups. Otherwise (default), they are computed only for the groups whose class is unknown.
distances	matrix with T rows and K columns, of the distances (d_{tk}) : d_{tk} is the distance between the group t and the class k, computed with the measure given by argument,
proximities	matrix of the proximities (in percents). The proximity of a group t to the class k is computed as so: $(1/d_{tk})/\sum_{l=1}^{l=K} (1/d_{tl})$.
confusion.mat	the confusion matrix (if misclass.ratio = TRUE)
misclassed	the misclassification ratio (if misclass.ratio = TRUE)

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Rudrauf, J.M., Boumaza, R. (2001). Contribution à l'étude de l'architecture médiévale: les caractéristiques des pierres à bossage des châteaux forts alsaciens, Centre de Recherches Archéologiques médiévales de Saverne, 5, 5-38.

Examples

```
data(castles.dated)
data(castles.nondated)
stones <- rbind(castles.dated$stones, castles.nondated$stones)
periods <- rbind(castles.dated$periods, castles.nondated$periods)
stones$height <- cut(stones$height, breaks = c(19, 27, 40, 71), include.lowest = TRUE)
stones$width <- cut(stones$width, breaks = c(24, 45, 62, 144), include.lowest = TRUE)
stones$edging <- cut(stones$edging, breaks = c(0, 3, 4, 8), include.lowest = TRUE)
stones$boss <- cut(stones$boss, breaks = c(0, 6, 9, 20), include.lowest = TRUE )</pre>
```

castlesfh <- folderh(periods, "castle", stones)</pre>

distl2d

```
# Default: dist="11", crit=1
discdd.predict(castlesfh, "period")
# With the calculation of the confusion matrix and misclassification ratio
discdd.predict(castlesfh, "period", misclass.ratio = TRUE)
# Hellinger distance
discdd.predict(castlesfh, "period", distance = "hellinger")
# crit=2
discdd.predict(castlesfh, "period", crit = 2)
```

distl2d	L^2 distance between probability densities
---------	--

Description

 L^2 distance between two multivariate (p > 1) or univariate (dimension: p = 1) probability densities, estimated from samples.

Usage

distl2d(x1, x2, method = "gaussiand", check = FALSE, varw1 = NULL, varw2 = NULL)

Arguments

x1, x2	the samples from the probability densities (see 12d).
method	string. It can be:
	• "gaussiand" if the densities are considered to be Gaussian.
	• "kern" if they are estimated using the Gaussian kernel method.
check	logical. When TRUE (the default is FALSE) the function checks if the covari- ance matrices (if method = "gaussiand") or smoothing bandwidth matrices (if method = "kern") are not degenerate, before computing the inner product.
	Notice that if $p = 1$, it checks if the variances or smoothing parameters are not zero.
varw1,varw2	the bandwidths when the densities are estimated by the kernel method (see 12d).

Details

The function distl2d computes the distance between f_1 and f_2 from the formula

 $||f_1 - f_2||^2 = \langle f_1, f_1 \rangle + \langle f_2, f_2 \rangle - 2 \langle f_1, f_2 \rangle$

For some information about the method used to compute the L^2 inner product or about the arguments, see 12d.

Value

The L^2 distance between the two densities.

Be careful! If check = FALSE and one smoothing bandwidth matrix is degenerate, the result returned can not be considered.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

matdistl2d in order to compute pairwise distances between several densities.

Examples

```
require(MASS)
m1 <- c(0,0)
v1 <- matrix(c(1,0,0,1),ncol = 2)
m2 <- c(0,1)
v2 <- matrix(c(4,1,1,9),ncol = 2)
x1 <- mvrnorm(n = 3,mu = m1,Sigma = v1)
x2 <- mvrnorm(n = 5, mu = m2, Sigma = v2)
distl2d(x1, x2, method = "gaussiand")
distl2d(x1, x2, method = "kern")
distl2d(x1, x2, method = "kern", varw1 = v1, varw2 = v2)
```

```
distl2dnorm
```

 L^2 distance between L^2 -normed probability densities

Description

 L^2 distance between two multivariate (p > 1) or univariate (dimension: p = 1) L^2 -normed probability densities, estimated from samples, where a L^2 -normed probability density is the original probability density function divided by its L^2 -norm.

Usage

```
distl2dnorm(x1, x2, method = "gaussiand", check = FALSE, varw1 = NULL, varw2 = NULL)
```

Arguments

x1, x2	the samples from the probability densities (see 12d.
method	string. It can be:
	• "gaussiand" if the densities are considered to be Gaussian.
	• "kern" if they are estimated using the Gaussian kernel method.

distl2dnorm

check	logical. When TRUE (the default is FALSE) the function checks if the covari- ance matrices (if method = "gaussiand") or smoothing bandwidth matrices (if method = "kern") are not degenerate, before computing the inner product. Notice that if $p = 1$, it checks if the variances or smoothing parameters are not zero.
varw1,varw2	the bandwidths when the densities are estimated by the kernel method (see 12d.

Details

Given densities f_1 and f_2 , the function distl2dnormpar computes the distance between the L^2 -normed densities $f_1/||f_1||$ and $f_2/||f_2||$:

$$2 - 2 < f_1, f_2 > /(||f_1||||f_2||)$$

For some information about the method used to compute the L^2 inner product or about the arguments, see 12d.

Value

The L^2 distance between the two L^2 -normed densities.

Be careful! If check = FALSE and one smoothing bandwidth matrix is degenerate, the result returned can not be considered.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

distl2d for the distance between two probability densities.

matdistl2dnorm in order to compute pairwise distances between several L^2 -normed densities.

Examples

```
require(MASS)
m1 <- c(0,0)
v1 <- matrix(c(1,0,0,1),ncol = 2)
m2 <- c(0,1)
v2 <- matrix(c(4,1,1,9),ncol = 2)
x1 <- mvrnorm(n = 3,mu = m1,Sigma = v1)
x2 <- mvrnorm(n = 5, mu = m2, Sigma = v2)
distl2dnorm(x1, x2, method = "gaussiand")
distl2dnorm(x1, x2, method = "kern")
distl2dnorm(x1, x2, method = "kern", varw1 = v1, varw2 = v2)</pre>
```

distl2dnormpar

Description

 L^2 distance between two multivariate (p > 1) or univariate (dimension: p = 1) L^2 -normed Gaussian densities, given their parameters (mean vectors and covariance matrices if the densities are multivariate, or means and variances if univariate) where a L^2 -normed probability density is the original probability density function divided by its L^2 -norm.

Usage

```
distl2dnormpar(mean1, var1, mean2, var2, check = FALSE)
```

Arguments

mean1, mean2	means of the probability densities.
var1, var2	variances $(p = 1)$ or covariance matrices $(p > 1)$ of the probability densities.
check	logical. When TRUE (the default is FALSE) the function checks if the covariance matrices are not degenerate, before computing the inner product.
	If the variables are univariate, it checks if the variances are not zero.

Details

Given densities f_1 and f_2 , the function distl2dnormpar computes the distance between the L^2 -normed densities $f_1/||f_1||$ and $f_2/||f_2||$:

$$2-2 < f_1, f_2 > /(||f_1||||f_2||)$$

For some information about the method used to compute the L^2 inner product or about the arguments, see 12dpar; the norm ||f|| of the multivariate Gaussian density f is equal to $(4\pi)^{-p/4} det(var)^{-1/4}$.

Value

The L^2 distance between the two L^2 -normed Gaussian densities.

Be careful! If check = FALSE and one variance matrix is degenerated (or one variance is zero if the densities are univariate), the result returned must not be considered.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

distl2dpar

See Also

distl2dpar for the distance between two probability densities.

matdistl2d in order to compute pairwise distances between several densities.

Examples

```
u1 <- c(1,1,1);
v1 <- matrix(c(4,0,0,0,16,0,0,0,25),ncol = 3);
u2 <- c(0,1,0);
v2 <- matrix(c(1,0,0,0,1,0,0,0,1),ncol = 3);
distl2dnormpar(u1,v1,u2,v2)
```

distl2dpar

```
L^2 distance between Gaussian densities given their parameters
```

Description

 L^2 distance between two multivariate (p > 1) or univariate (dimension: p = 1) Gaussian densities, given their parameters (mean vectors and covariance matrices if the densities are multivariate, or means and variances if univariate).

Usage

distl2dpar(mean1, var1, mean2, var2, check = FALSE)

Arguments

mean1, mean2	means of the probability densities.
var1, var2	variances $(p = 1)$ or covariance matrices $(p > 1)$ of the probability densities.
check	logical. When TRUE (the default is FALSE) the function checks if the covariance matrices are not degenerate, before computing the inner product.
	If the variables are univariate, it checks if the variances are not zero.

Details

The function distl2dpar computes the distance between two densities, say f_1 and f_2 , from the formula:

$$||f_1 - f_2||^2 = \langle f_1, f_1 \rangle + \langle f_2, f_2 \rangle - 2 \langle f_1, f_2 \rangle$$

For some information about the method used to compute the L^2 inner product or about the arguments, see 12dpar.

Value

The L^2 distance between the two densities.

Be careful! If check = FALSE and one variance matrix is degenerated (or one variance is zero if the densities are univariate), the result returned must not be considered.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

matdistl2d in order to compute pairwise distances between several densities.

Examples

```
u1 <- c(1,1,1);
v1 <- matrix(c(4,0,0,0,16,0,0,0,25),ncol = 3);
u2 <- c(0,1,0);
v2 <- matrix(c(1,0,0,0,1,0,0,0,1),ncol = 3);
distl2dpar(u1,v1,u2,v2)
```

dspg

Diploma x Socio professional group

Description

Contingency tables of the counts of Diploma x Socio professional group of France

Usage

data(dspg)

Format

dspg is a list of 7 arrays (each one corresponding to a year: 1968, 1975, 1982, 1990, 1999, 2010, 2015) of 4 rows (each one corresponding to a level of diploma) and 6 columns (each one corresponding to a socio professional group).

csp: Socio professional group

diplome: Diploma

- agri: farmer (agriculteur)
- arti: craftsperson (artisan)
- cadr: senior manager (cadre sup\'erieur)
- pint: middle manager (profession interm\'ediaire)
- empl: employee (employ\'e)
- ouvr: worker (ouvrier)

dspgd2015

bepc:	brevet
cap:	NVQ (cap)
bac:	baccalaureate
sup:	higher education (sup\'erieur)

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

Source

INSEE. Population active de 25 à 54 ans ayant un emploi et chômeurs par catégorie socioprofessionnelle et diplôme par commune et département (1968 à 2015).

Examples

data(dspg)
names(dspg)
print(dspg[[1]])

dspgd2015

Diploma x Socio professional group by departement in 2015

Description

Contingency tables of the counts of Diploma x Socio professional group by metroplitan France departement in year 2015.

Usage

data(dspgd2015)

Format

dspgd2015 is a list of 96 arrays (each one corresponding to a department, designated by its official geographical code) of 4 rows (each one corresponding to a level of diploma) and 6 columns (each one corresponding to a socio professional group).

csp: Socio professional group

diplome: Diploma

- agri: farmer (agriculteur)
- arti: craftsperson (artisan)
- cadr: senior manager (cadre sup\'erieur)
- pint: middle manager (profession interm\'ediaire)
- empl: employee (employ\'e)

dstatis.inter

- ouvr: worker (ouvrier) bepc: brevet
- cap: NVQ (cap)
- bac: baccalaureate
- sup: higher education (sup\'erieur)

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

Source

INSEE. Population active de 25 à 54 ans ayant un emploi et chômeurs par catégorie socioprofessionnelle et diplôme par commune et département (1968 à 2015).

Examples

```
data(dspgd2015)
names(dspgd2015)
print(dspgd2015[[1]])
```

dstatis.inter Dual STATIS method (interstructure stage)

Description

Performs the first stage (interstructure) of the dual STATIS method in order to describe a data folder, consisting of T groups of individuals on which are observed p variables. It returns an object of class dstatis.

Usage

```
dstatis.inter(xf, normed = TRUE, centered = TRUE, data.scaled = FALSE, nb.factors = 3,
    nb.values = 10, sub.title = "", plot.eigen = TRUE, plot.score = FALSE,
    nscore = 1:3, group.name = "group", filename = NULL)
```

Arguments

xf	object of class folder. Its elements are data frames with p numeric columns. If there are non numeric columns, there is an error. The t^{th} element $(t = 1,, T)$ matches with the t^{th} group.
normed	logical. If TRUE (default), the scalar products are normed.
centered	logical. If TRUE (default), the scalar products are centered.
data.scaled	logical. If TRUE, the data of each group are centered and scaled. The analysis is then performed on the correlation matrices. If FALSE (default), the analysis is performed on the covariance matrices.

58

dstatis.inter

nb.factors	numeric. Number of returned principal scores (default nb.factors = 3).
nb.values	numerical. Number of returned eigenvalues (default nb.values = 10).
<pre>sub.title</pre>	string. If provided, the subtitle for the graphs.
plot.eigen	logical. If TRUE (default), the barplot of the eigenvalues is plotted.
plot.score	logical. If TRUE, the graphs of principal scores are plotted. A new graphic device is opened for each pair of principal scores defined by nscore argument.
nscore	numeric vector. If plot.score = TRUE, the numbers of the principal scores which are plotted. By default it is equal to nscore = 1:3. Its components cannot be greater than nb.factors.
group.name	string. Name of the grouping variable. Default: groupname = "group".
filename	string. Name of the file in which the results are saved. By default (filename = NULL) the results are not saved.

Details

The covariance matrices (if data.scale is FALSE) or correlation matrices (if TRUE) per group are computed. The matrix W of the scalar products between these covariance matrices is then computed.

To perform the STATIS method, see the function DSTATIS of the multigroup package.

Value

Returns an object of class dstatis, that is a list including:

inertia	data frame of the eigenvalues and percentages of inertia.
contributions	data frame of the contributions to the first nb.factors principal components.
qualities	data frame of the qualities on the first nb.factors principal factors.
scores	data frame of the first nb.factors scores of the spectral decomposition of W .
norm	vector of the L^2 norms of the densities.
means	list of the means.
variances	list of the covariance matrices.
correlations	list of the correlation matrices.
skewness	list of the skewness coefficients.
kurtosis	list of the kurtosis coefficients.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Lavit, C., Escoufier, Y., Sabatier, R., Traissac, P. (1994). The ACT (STATIS method). Computational Statistics & Data Analysis, 18 (1994), 97-119.

See Also

print.dstatis, plot.dstatis, interpret.dstatis.

Examples

```
data(roses)
rosesf <- as.folder(roses[,c("Sha", "Den", "Sym", "rose")])
# Dual STATIS on the covariance matrices
result1 <- dstatis.inter(rosesf, data.scaled = FALSE, group.name = "rose")
print(result1)
# Dual STATIS on the correlation matrices
result2 <- dstatis.inter(rosesf, data.scaled = FALSE, group.name = "rose")
print(result2)
plot(result2)</pre>
```

fdiscd.misclass	Misclassification ratio in functional discriminant analysis of probabil-
	ity densities.

Description

Computes the one-leave-out misclassification ratio of the rule assigning T groups of individuals, one group after another, to the class of groups (among K classes of groups) which achieves the minimum of the distances or divergences between the density function associated to the group to assign and the K density functions associated to the K classes.

Usage

Arguments

xf	object of class folderh with two data frames:
	• The first one has at least two columns. One column contains the names of the T groups (all the names must be different). An other column is a factor with K levels partitionning the T groups into K classes.
	• The second one has $(p + 1)$ columns. The first p columns are numeric (otherwise, there is an error). The last column is a factor with T levels defining T groups. Each group, say t , consists of n_t individuals.
class.var	string. The name of the class variable.
distance	The distance or dissimilarity used to compute the distance matrix between the densities. It can be:

60

	• "jeffreys" (default) the Jeffreys measure (symmetrised Kullback-Leibler divergence),
	• "hellinger" the Hellinger (Matusita) distance,
	 "wasserstein" the Wasserstein distance,
	• "12" the L^2 distance,
	• "12norm" (only available when crit = 1) the densities are normed and the L^2 distance between these normed densities is used;
	If gaussiand = FALSE, the densities are estimated by the Gaussian kernel method and the distance is "12" or "12norm".
crit	1, 2 or 3. In order to select the densities associated to the classes. See Details.
	If distance is "hellinger", "jeffreys" or "wasserstein", crit is neces- sarily 1 (see Details).
gaussiand	logical. If TRUE (default), the probability densities are supposed Gaussian. If FALSE, densities are estimated using the Gaussian kernel method.
	If distance is "hellinger", "jeffreys" or "wasserstein", gaussiand is necessarily TRUE.
windowh	strictly positive numeric value. If windowh = NULL (default), the bandwidths are computed using the bandwidth.parameter function.
	Omitted when distance is "hellinger", "jeffreys" or "wasserstein" (see Details).

Details

The T probability densities f_t corresponding to the T groups of individuals are either parametrically estimated (gaussiand = TRUE) or estimated using the Gaussian kernel method (gaussiand = FALSE). In the latter case, the windowh argument provides the list of the bandwidths to be used. Notice that in the multivariate case (p>1), the bandwidths are positive-definite matrices.

The argument windowh is a numerical value, the matrix bandwidth is of the form hS, where S is either the square root of the covariance matrix (p>1) or the standard deviation of the estimated density.

If windowh = NULL (default), h in the above formula is computed using the bandwidth.parameter function.

To the class k consisting of T_k groups is associated the density denoted g_k . The crit argument selects the estimation method of the K densities g_k .

1. The density g_k is estimated using the whole data of this class, that is the rows of x corresponding to the T_k groups of the class k.

The estimation of the densities g_k uses the same method as the estimation of the f_t .

- 2. The T_k densities f_t are estimated using the corresponding data from x. Then they are averaged to obtain an estimation of the density g_k , that is $g_k = \frac{1}{T_k} \sum f_t$.
- 3. Each previous density f_t is weighted by n_t (the number of rows of x corresponding to f_t). Then they are averaged, that is $g_k = \frac{1}{\sum n_t} \sum n_t f_t$.

The last two methods are only available for the L^2 -distance. If the divergences between densities are computed using the Hellinger or Wasserstein distance or Jeffreys measure, only the first of these methods is available.

The distance or dissimilarity between the estimated densities is either the L^2 distance, the Hellinger distance, Jeffreys measure (symmetrised Kullback-Leibler divergence) or the Wasserstein distance.

- If it is the L^2 distance (distance="12" or distance="12norm"), the densities can be either parametrically estimated or estimated using the Gaussian kernel.
- If it is the Hellinger distance (distance="hellinger"), Jeffreys measure (distance="jeffreys") or the Wasserstein distance (distance="wasserstein"), the densities are considered Gaussian and necessarily parametrically estimated.

Value

Returns an object of class fdiscd.misclass, that is a list including:

classification data frame with 4 columns:

- factor giving the group name. The column name is the same as that of the column (*p* + 1) of x,
- the prior class of the group if it is available, or NA if not,
- alloc: the class allocation computed by the discriminant analysis method,
- misclassed: boolean. TRUE if the group is misclassed, FALSE if it is wellclassed, NA if the prior class of the group is unknown.

confusion.mat	confusion matrix,
misalloc.per.c	lass
	the misclassification ratio per class,
misclassed	the misclassification ratio,
distances	matrix with T rows and K columns, of the distances (d_{tk}) : d_{tk} is the distance between the group t and the class k, computed with the measure given by argu- ment distance (L^2 -distance, Hellinger distance or Jeffreys measure),
proximities	matrix of the proximity indices (in percents) between the groups and the classes. The proximity of the group t to the class k is computed as so: $(1/d_{tk})/\sum_{l=1}^{l=K} (1/d_{tl})$

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Boumaza, R. (2004). Discriminant analysis with independently repeated multivariate measurements: an L^2 approach. Computational Statistics & Data Analysis, 47, 823-843.

Rudrauf, J.M., Boumaza, R. (2001). Contribution à l'étude de l'architecture médiévale: les caractéristiques des pierres à bossage des châteaux forts alsaciens. Centre de Recherches Archéologiques Médiévales de Saverne, 5, 5-38.

Examples

```
data(castles.dated)
castles.stones <- castles.dated$stones
castles.periods <- castles.dated$periods</pre>
```

```
castlesfh <- folderh(castles.periods, "castle", castles.stones)
result <- fdiscd.misclass(castlesfh, "period")
print(result)</pre>
```

fdiscd.predict

Predicting the class of a group of individuals with discriminant analysis of probability densities.

Description

Assigns several groups of individuals, one group after another, to the class of groups (among K classes of groups) which achieves the minimum of the distances or divergences between the density function associated to the group to assign and the K density functions associated to the K classes.

Usage

Arguments

xf	object of class folderh with two data frames:
	• The first one has at least two columns. One column contains the names of the T groups (all the names must be different). An other column is a factor with K levels partitionning the T groups into K classes
	• The second one has $(p + 1)$ columns. The first p columns are numeric (otherwise, there is an error). The last column is a factor with T levels defining T groups. Each group, say t , consists of n_t individuals.
	Notice that for the versions earlier than 2.0, fdiscd.predict applied to two data frames.
class.var	string. The name of the class variable.
distance	The distance or divergence used to compute the distance matrix between the densities. It can be:
	• "jeffreys" (default) Jeffreys measure (symmetrised Kullback-Leibler divergence),
	 "hellinger" the Hellinger (Matusita) distance,
	 "wasserstein" the Wasserstein distance,
	• "12" the L^2 distance,
	• "l2norm" the densities are normed and the L ² distance between these normed densities is used;
	If gaussiand = FALSE, the densities are estimated by the Gaussian kernel method and the distance is "12" or "12norm".

crit	1, 2 or 3. In order to select the densities associated to the classes. See Details.
	If distance is "hellinger", "jeffreys" or "wasserstein", crit is necessarily 1 (see Details).
gaussiand	logical. If TRUE (default), the probability densities are supposed Gaussian. If FALSE, densities are estimated using the Gaussian kernel method.
	If distance is "hellinger", "jeffreys" or "wasserstein", gaussiand is necessarily TRUE.
windowh	strictly positive number. If windowh = NULL (default), the bandwidths are computed using the bandwidth.parameter function.
	Omitted when distance is "hellinger", "jeffreys" or "wasserstein" (see Details).
misclass.ratio	logical (default FALSE). If TRUE, the confusion matrix and misclassification ratio are computed on the groups whose prior class is known. In order to compute the misclassification ratio by the one-leave-out method, use the fdiscd.misclass function.

Details

To the group t is associated the density denoted f_t . To the class k consisting of T_k groups is associated the density denoted g_k . The crit argument selects the estimation method of the K densities g_k .

- 1. The density g_k is estimated using the whole data of this class, that is the rows of x corresponding to the T_k groups of the class k.
- 2. The T_k densities f_t are estimated using the corresponding data from x. Then they are averaged to obtain an estimation of the density g_k , that is $g_k = (1/T_k) \sum f_t$.
- 3. Each previous density f_t is weighted by n_t (the number of rows of x corresponding to f_t). Then they are averaged, that is $g_k = (1/\sum n_t) \sum n_t f_t$.

The last two methods are available only for the L^2 -distance. If the divergences between densities are computed using the Hellinger or Wasserstein distance or Jeffreys measure, only the first of these methods is available.

Value

Returns an object of class fdiscd.predict, that is a list including:

prediction	data frame with 3 columns:
	• factor giving the group name. The column name is the same as that of the column $(p + 1)$ of x,
	• class.known: the prior class of the group if it is available, or NA if not,
	• class.predict: the class allocation predicted by the discriminant analysis method. If misclass.ratio = TRUE, the class allocations are computed for all groups. Otherwise (default), they are computed only for the groups whose class is unknown.
distances	matrix with T rows and K columns, of the distances (d_{tk}) : d_{tk} is the distance between the group t and the class k, computed with the measure given by argu- ment distance (L^2 -distance, Hellinger distance or jeffreys measure),

fdiscd.predict

proximities	matrix of the proximities (in percents). The proximity of a group t to the class
	k is computed as so: $(1/d_{tk}) / \sum_{l=1}^{l=K} (1/d_{tl})$.
confusion.mat	the confusion matrix (if misclass.ratio = TRUE)
misclassed	the misclassification ratio (if misclass.ratio = TRUE)

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Boumaza, R. (2004). Discriminant analysis with independently repeated multivariate measurements: an L^2 approach. Computational Statistics & Data Analysis, 47, 823-843.

Rudrauf, J.M., Boumaza, R. (2001). Contribution à l'étude de l'architecture médiévale: les caractéristiques des pierres à bossage des châteaux forts alsaciens. Centre de Recherches Archéologiques Médiévales de Saverne, 5, 5-38.

Examples

```
data(castles.dated)
data(castles.nondated)
castles.stones <- rbind(castles.dated$stones, castles.nondated$stones)</pre>
castles.periods <- rbind(castles.dated$periods, castles.nondated$periods)</pre>
castlesfh <- folderh(castles.periods, "castle", castles.stones)</pre>
# With the L^2-distance
# - crit=1
result12.1 <- fdiscd.predict(castlesfh, "period", distance="12", crit=1)</pre>
print(result12.1)
# - crit=2
## Not run:
result12.2 <- fdiscd.predict(castlesfh, "period", distance="12", crit=2)</pre>
print(result12.2)
## End(Not run)
# - crit=3
result12.3 <- fdiscd.predict(castlesfh, "period", distance="12", crit=3)</pre>
print(result12.3)
# With the Hellinger distance
resulthelling <- fdiscd.predict(castlesfh, "period", distance="hellinger")</pre>
print(resulthelling)
# With jeffreys measure
resultjeff <- fdiscd.predict(castlesfh, "period", distance="jeffreys")</pre>
print(resultjeff)
```

fhclustd

Description

Performs functional hierarchic cluster analysis of probability densities. It returns an object of class fhclustd. It applies hclust to the distance matrix between the T densities.

Usage

Arguments

xf	object of class "folder" or data.frame.
	• If it is an object of class "folder", its elements are data frames with p numeric columns. If there are non numeric columns, there is an error. The t^{th} element $(t = 1,, T)$ matches with the t^{th} group.
	• If it is a data frame, the column with name given by the group.name argument is a factor giving the groups. The other columns are all numeric; otherwise, there is an error.
group.name	string.
	• If xf is an object of class "folder", it is the name of the grouping variable in the returned results. The default is groupname = "group".
	• If xf is a data frame, it is the name of the column of xf containing the groups.
gaussiand	logical. If TRUE (default), the probability densities are supposed Gaussian. If FALSE, densities are estimated using the Gaussian kernel method.
	If distance is "hellinger", "jeffreys" or "wasserstein", gaussiand is necessarily TRUE (see Details).
distance	The distance or divergence used to compute the distance matrix between the densities. It can be:
	• "jeffreys" (default) Jeffreys measure (symmetrised Kullback-Leibler divergence),
	 "hellinger" the Hellinger (Matusita) distance,
	 "wasserstein" the Wasserstein distance,
	• "12" the L^2 distance,
	• "12norm" the densities are normed and the L ² distance between these normed densities is used;
	If gaussiand = FALSE, the densities are estimated by the Gaussian kernel method and the distance can be "12" (default) or "12norm".

fhclustd

windowh	either a list of T bandwidths (one per density associated to a group), or a strictly positive number. If windowh = NULL (default), the bandwidths are automatically computed. See Details.	
	Omitted when distance is "hellinger", "jeffreys" or "wasserstein" (see Details).	
data.centered	logical. If TRUE (default is FALSE), the data of each group are centered.	
data.scaled	logical. If TRUE (default is FALSE), the data of each group are centered (even if data.centered = FALSE) and scaled.	
common.variance		
	logical. If TRUE (default is FALSE), a common covariance matrix (or correlation matrix if data.scaled = TRUE), computed on the whole data, is used. If FALSE (default), a covariance (or correlation) matrix per group is used.	
<pre>sub.title</pre>	string. If provided, the subtitle for the graphs.	
filename	string. Name of the file in which the results are saved. By default (filename = NULL) the results are not saved.	
method.hclust	the agglomeration method to be used for the clustering. See the method argument of the hclust function.	

Details

In order to compute the distances/dissimilarities between the groups, the T probability densities f_t corresponding to the T groups of individuals are either parametrically estimated (gaussiand = TRUE) or estimated using the Gaussian kernel method (gaussiand = FALSE). In the latter case, the windowh argument provides the list of the bandwidths to be used. Notice that in the multivariate case (p>1), the bandwidths are positive-definite matrices. The distances between the T groups of individuals are given by the L^2 -distances between the T probability densities f_t corresponding to these groups. The hclust function is then applied to the distance matrix to perform the hierarchical clustering on the T groups.

If windowh is a numerical value, the matrix bandwidth is of the form hS, where S is either the square root of the covariance matrix (p>1) or the standard deviation of the estimated density.

If windowh = NULL (default), h in the above formula is computed using the bandwidth.parameter function.

The distance or dissimilarity between the estimated densities is either the L^2 distance, the Hellinger distance, Jeffreys measure (symmetrised Kullback-Leibler divergence) or the Wasserstein distance.

- If it is the L^2 distance (distance="12" or distance="12norm"), the densities can be either parametrically estimated or estimated using the Gaussian kernel.
- If it is the Hellinger distance (distance="hellinger"), Jeffreys measure (distance="jeffreys") or the Wasserstein distance (distance="wasserstein"), the densities are considered Gaussian and necessarily parametrically estimated.

Value

Returns an object of class fhclustd, that is a list including:

distances	matrix of the L^2 -distances between the estimated densities.
clust	an object of class hclust.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

fdiscd.predict, fdiscd.misclass

Examples

```
data(castles.dated)
stones <- castles.dated$stones</pre>
periods <- castles.dated$periods</pre>
periods123 <- periods[periods$period %in% 1:3, "castle"]</pre>
stones123 <- stones[stones$castle %in% periods123, ]</pre>
stones123$castle <- as.factor(as.character(stones123$castle))</pre>
yf <- as.folder(stones123)</pre>
# Jeffreys measure (default):
resultjef <- fhclustd(yf)</pre>
print(resultjef)
print(resultjef, dist.print = TRUE)
plot(resultjef)
plot(resultjef, hang = -1)
# Use cutree (stats package) to get the partition
cutree(resultjef$clust, k = 1:4)
cutree(resultjef$clust, k = 5)
cutree(resultjef$clust, h = 0.041)
# Applied to a data frame (Jeffreys measure):
fhclustd(stones123, group.name = "castle")
# Use cutree (stats package) to get the partition
cutree(resultjef$clust, k = 1:4)
cutree(resultjef clust, k = 5)
cutree(resultjef$clust, h = 0.041)
# Hellinger distance:
resulthel <- fhclustd(yf, distance = "hellinger")
print(resulthel)
print(resulthel, dist.print = TRUE)
plot(resulthel)
plot(resulthel, hang = -1)
# Use cutree (stats package) to get the partition
```

floribundity

```
cutree(resulthel$clust, k = 1:4)
cutree(resulthelsclust, k = 5)
cutree(resulthel$clust, h = 0.041)
## Not run:
# L2-distance:
xf <- as.folder(stones)</pre>
result <- fhclustd(xf, distance = "12")</pre>
print(result)
print(result, dist.print = TRUE)
plot(result)
plot(result, hang = -1)
# Use cutree (stats package) to get the partition
cutree(result$clust, k = 1:5)
cutree(resultsclust, k = 5)
cutree(result$clust, h = 0.18)
## End(Not run)
periods123 <- periods[periods$period %in% 1:3, "castle"]</pre>
stones123 <- stones[stones$castle %in% periods123, ]</pre>
stones123$castle <- as.factor(as.character(stones123$castle))</pre>
yf <- as.folder(stones123)</pre>
result123 <- fhclustd(yf, distance = "12")</pre>
print(result123)
print(result123, dist.print = TRUE)
plot(result123)
plot(result123, hang = -1)
# Use cutree (stats package) to get the partition
cutree(result123$clust, k = 1:4)
cutree(result123$clust, k = 5)
cutree(result123$clust, h = 0.041)
```

floribundity Rose flowering

Description

These data are collected on eight rosebushes from four varieties, during summer 2010 in Angers, France. They give measures of the flowering.

Usage

data("floribundity")

Format

floribundity is a list of 16 data frames, each corresponding to an observation date. Each one of these data frames has 3 or 4 columns:

- rose: the number of the rosebush, that is an identifier.
- variety: factor. The variety of the rosebush.
- area (when available): numeric. The ratio of flowering area to the whole plant area, measured on the photograph of the rosebush.
- nflowers (when available): integer. The number of flowers on the rosebush.

The row names of these data frames are the rose identifiers.

Examples

```
data(floribundity)
foldt <- foldert(floribundity, times = as.Date(names(floribundity)), rows.select = "union")
summary(foldt)</pre>
```

fmdsd

Multidimensional scaling of probability densities

Description

Applies the multidimensional scaling (MDS) method to probability densities in order to describe a data folder, consisting of T groups of individuals on which are observed p variables. It returns an object of class fmdsd. It applies cmdscale to the distance matrix between the T densities.

Usage

```
fmdsd(xf, group.name = "group", gaussiand = TRUE, distance = c("jeffreys", "hellinger",
    "wasserstein", "l2", "l2norm"), windowh=NULL, data.centered = FALSE,
    data.scaled = FALSE, common.variance = FALSE, add = TRUE, nb.factors = 3,
    nb.values = 10, sub.title = "", plot.eigen = TRUE, plot.score = FALSE, nscore = 1:3,
    filename = NULL)
```

Arguments

object of class "folder" or data.frame.

- If it is an object of class "folder", its elements are data frames with p numeric columns. If there are non numeric columns, there is an error. The t^{th} element (t = 1, ..., T) matches with the t^{th} group.
- If it is a data frame, the column with name given by the group.name argument is a factor giving the groups. The other columns are all numeric; otherwise, there is an error.

group.name string.

	• If xf is an object of class "folder", it is the name of the grouping variable in the returned results. The default is groupname = "group".
	• If xf is a data frame, it is the name of the column of xf containing the groups.
gaussiand	logical. If TRUE (default), the probability densities are supposed Gaussian. If FALSE, densities are estimated using the Gaussian kernel method.
distance	The distance or divergence used to compute the distance matrix between the densities.
	If gaussiand = TRUE, the densities are parametrically estimated and the distance can be:
	• "jeffreys" (default) Jeffreys measure (symmetrised Kullback-Leibler divergence),
	 "hellinger" the Hellinger (Matusita) distance,
	• "wasserstein" the Wasserstein distance,
	• "12" the L^2 distance,
	• "12norm" the densities are normed and the L ² distance between these normed densities is used;
	If gaussiand = FALSE, the densities are estimated by the Gaussian kernel method and the distance can be "12" (default) or "12norm".
windowh	either a list of T bandwidths (one per density associated to a group), or a strictly positive number. If windowh = NULL (default), the bandwidths are automatically computed. See Details.
	Omitted when distance is "hellinger", "jeffreys" or "wasserstein" (see Details).
data.centered	logical. If TRUE (default is FALSE), the data of each group are centered.
data.scaled	logical. If TRUE (default is FALSE), the data of each group are centered (even if data.centered = FALSE) and scaled.
common.varianc	e
	logical. If TRUE (default is FALSE), a common covariance matrix (or correlation matrix if data.scaled = TRUE), computed on the whole data, is used. If FALSE (default), a covariance (or correlation) matrix per group is used.
add	logical indicating if an additive constant should be computed and added to the non diagonal dissimilarities such that the modified dissimilarities are Euclidean (default TRUE; see add argument of cmdscale).
nb.factors	numeric. Number of returned principal coordinates (default nb.factors = 3). Warning: The plot.fmdsd and interpret.fmdsd functions cannot take into account more than nb.factors principal factors.
nb.values	numeric. Number of returned eigenvalues (default nb.values = 10).
<pre>sub.title</pre>	string. Subtitle for the graphs (default NULL).
plot.eigen	logical. If TRUE (default), the barplot of the eigenvalues is plotted.
plot.score	logical. If TRUE, the graphs of new coordinates are plotted. A new graphic device is opened for each pair of coordinates defined by nscore argument.

nscore	numeric vector. If plot.score = TRUE, the numbers of the principal coordinates which are plotted. By default it is equal to nscore = 1:3. Its components cannot be greater than nb.factors.
filename	string. Name of the file in which the results are saved. By default (filename = NULL) they are not saved.

Details

In order to compute the distances/dissimilarities between the groups, the T probability densities f_t corresponding to the T groups of individuals are either parametrically estimated (gaussiand = TRUE) or estimated using the Gaussian kernel method (gaussiand = FALSE). In the latter case, the windowh argument provides the list of the bandwidths to be used. Notice that in the multivariate case (p>1), the bandwidths are positive-definite matrices.

If windowh is a numerical value, the matrix bandwidth is of the form hS, where S is either the square root of the covariance matrix (p>1) or the standard deviation of the estimated density.

If windowh = NULL (default), h in the above formula is computed using the bandwidth.parameter function.

The distance or dissimilarity between the estimated densities is either the L^2 distance, the Hellinger distance, Jeffreys measure (symmetrised Kullback-Leibler divergence) or the Wasserstein distance.

- If it is the L^2 distance (distance="12" or distance="12norm"), the densities can be either parametrically estimated or estimated using the Gaussian kernel.
- If it is the Hellinger distance (distance="hellinger"), Jeffreys measure (distance="jeffreys") or the Wasserstein distance (distance="wasserstein"), the densities are considered Gaussian and necessarily parametrically estimated.

Value

Returns an object of class fmdsd, i.e. a list including:

inertia	data frame of the eigenvalues and percentages of inertia.
scores	data frame of the nb.factors first principal coordinates.
means	list of the means.
variances	list of the covariance matrices.
correlations	list of the correlation matrices.
skewness	list of the skewness coefficients.
kurtosis	list of the kurtosis coefficients.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

fmdsd

References

Boumaza, R., Yousfi, S., Demotes-Mainard, S. (2015). Interpreting the principal component analysis of multivariate density functions. Communications in Statistics - Theory and Methods, 44 (16), 3321-3339.

Delicado, P. (2011). Dimensionality reduction when data are density functions. Computational Statistics & Data Analysis, 55, 401-420.

Yousfi, S., Boumaza, R., Aissani, D., Adjabi, S. (2014). Optimal bandwith matrices in functional principal component analysis of density function. Journal of Statistical Computation and Simulation, 85 (11), 2315-2330.

Cox, T.F., Cox, M.A.A. (2001). Multimensional Scaling, second ed. Chapman & Hall/CRC.

See Also

fpcad print.fmdsd, plot.fmdsd, interpret.fmdsd, bandwidth.parameter

Examples

```
data(roses)
rosesf <- as.folder(roses[,c("Sha","Den","Sym","rose")])</pre>
# MDS on Gaussian densities (on sensory data)
# using jeffreys measure (default):
resultjeff <- fmdsd(rosesf, distance = "jeffreys")</pre>
print(resultjeff)
plot(resultjeff)
## Not run:
# Applied to a data frame:
resultjeffdf <- fmdsd(roses[,c("Sha","Den","Sym","rose")],</pre>
                       distance = "jeffreys", group.name = "rose")
print(resultjeffdf)
plot(resultjeffdf)
## End(Not run)
# using the Hellinger distance:
resulthellin <- fmdsd(rosesf, distance = "hellinger")</pre>
print(resulthellin)
plot(resulthellin)
# using the Wasserstein distance:
resultwass <- fmdsd(rosesf, distance = "wasserstein")</pre>
print(resultwass)
plot(resultwass)
# Gaussian case, using the L2-distance:
resultl2 <- fmdsd(rosesf, distance = "12")</pre>
print(result12)
plot(result12)
```

```
# Gaussian case, using the L2-distance between normed densities:
resultl2norm <- fmdsd(rosesf, distance = "l2norm")
print(resultl2norm)
plot(resultl2norm)
## Not run:
# Non Gaussian case, using the L2-distance,
# the densities are estimated using the Gaussian kernel method:
result <- fmdsd(rosesf, distance = "l2", gaussiand = FALSE, group.name = "rose")
print(result)
plot(result)
```

End(Not run)

folder

Folder of data sets

Description

Creates an object of class "folder" (called folder below), that is a list of data frames with the same column names. Thus, these data sets are on the same variables. They can be on the same individuals or not.

Usage

```
folder(x1, x2 = NULL, ..., cols.select = "intersect", rows.select = "")
```

Arguments

x1	data frame (can also be a tibble) or list of data frames.
	• If x1 is a data frame, x2 must be provided.
	• If x1 is a list of data frames, its elements are the datasets of the folder. In this case, there is no x2 argument.
x2	data frame. Must be provided if x1 is a data frame.
	optional. One or several data frames. When $x1$ and $x2$ are data frames, these are the other data frames.
cols.select	string. Gives the method used to choose the column names of the data frames of the folder. This argument can be:
	"intersect" (default) the column names of the data frames in the folder are the intersection of the column names of all the data frames given as arguments.
	"union" the column names of the data frames in the folder are the union of the column names of all the data frames given as arguments. When necessary, the rows of the returned data frames are completed by NA. If cols.select is a character vector, it gives the column names selected in the data frames given as arguments. The corresponding columns constitute the columns of

	the elements of the returned folder. Notice that when a column name is not present in all data frames (given as arguments), the data are completed by NA.
rows.select	string. Gives the method used to choose the row names of the data frames of the folder. This argument can be:
	"" (default) the data frames of the folder have the same rows as those which were passed as arguments.
	"intersect" the row names of the data frames in the folder are the intersection of the row names of all the data frames given as arguments.
	"union" the row names of the data frames in the folder are the union of the row names of all the data frames given as arguments. When necessary, the

The class folder has a logical attributes attr(, "same.rows").

The data frames in the returned folder all have the same column names. That means that the same variables are observed in every data sets.

columns of the data frames returned are completed by NA.

If the rows.select argument is "union" or "intersect", the elements of the returned folder have the same rows. That means that the same individuals are present in every data sets. This allows to consider the evolution of each individual among time.

If rows.select is "", every rows of this folder are different, and the row names are made unique by adding the name of the data frame to the row names. In this case, The individuals of the data sets are assumed to be all different. Or, at least, the user does not mind if they are the same or not.

Value

Returns an object of class "folder", that is a list of data frames.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

is.folder to test if an object is of class folder. folderh to build a folder of several data frames with a hierarchic relation between each pair of consecutive data frames.

Examples

```
# First example
x1 <- data.frame(x = rnorm(10), y = 1:10)
x2 <- data.frame(x = rnorm(10), z = runif(10, 1, 10))
f1 <- folder(x1, x2)
print(f1)
f2 <- folder(x1, x2, cols.select = "union")
print(f2)</pre>
```

```
#Second example
data(iris)
iris.set <- iris[iris$Species == "setosa", 1:4]
iris.ver <- iris[iris$Species == "versicolor", 1:4]
iris.vir <- iris[iris$Species == "virginica", 1:4]
irisf1 <- folder(iris.set, iris.ver, iris.vir)
print(irisf1)
listofdf <- list(df1 = iris.set,df2 = iris.ver,df3 = iris.vir)
irisf2 <- folder(listofdf,x2 = NULL)
print(irisf2)
```

```
folderh
```

Hierarchic folder of n data frames related in pairs by (n-1) keys

Description

Creates an object of class folderh, that is a list of n > 1 data frames whose rows are related by (n-1) keys, each key defining a relation "1 to N" between the two adjacent data frames passed as arguments of the function.

Usage

folderh(df1, key1, df2, ..., na.rm = TRUE)

Arguments

df1	data frame (can also be a tibble) with at least two columns. It contains a factor (whose name is given by key1 argument) whose levels are taken exactly once.
key1	character string. The name of the factor of the data frames df1 and df2 which contains the key of the relations "1 to N" between the two datasets.
df2	data frame (or tibble) with at least two columns. It contains a factor column (named by keys argument) with the same levels as df1[, key1] (see Details).
	optional. One or several supplementary character strings and data frames, or- dered as follows: key2, df3, The argument key2 indicates the key defin- ing the relation "1 to N" between the data frames df2 and df3, and so on.
na.rm	logical. If TRUE, the rows of each data frame for which the key is NA are removed.

Details

The object of class folder h is a list of $n \ge 2$ data frames.

• If no optional arguments are given via ..., that is n = 2, the two data frames of the list have a column named by the attribute attr(, "keys") (argument key1), which is a factor with the same levels. Each one of these levels occur exactly once in the first data frame of the list.

foldermtg

• If some supplementary data frames and supplementary strings key2, df3, ... are given as optional arguments, n is the number of data frames given as arguments. Then, the attribute attr(, "keys") is a vector of n - 1 character strings. For i = 1, ..., N - 1, its *i*-th element is the name of a column of the *i*-th and (i + 1)-th data frames of the folderh, which are factors with the same levels. Each one of these levels occur exactly once in the *i*-th data frame.

If there are more than two data frames, folderh computes a folderh with the two last data frames, and then uses the function appendtofolderh to append each one of the other data frames to the folderh.

Value

Returns an object of class folderh. Its elements are the data frames passed as arguments, and the attribute attr(, "keys") contains the character arguments.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

is.folderh to test if an object is of class folderh. folder for a folder of data frames with no hierarchic relation between them. as.folder.folderh (or as.data.frame.folderh) to build an object of class folder (or a data frame) from an object of class folderh,

Examples

```
# First example: rose flowers
data(roseflowers)
df1 <- roseflowers$variety
df2 <- roseflowers$flower
fh1 <- folderh(df1, "rose", df2)
print(fh1)
# Second example
data(roseleaves)
roses <- roseleaves$rose
stems <- roseleaves$rose
stems <- roseleaves$tem
leaves <- roseleaves$leaf
leaflets <- roseleaves$leaflet
fh2 <- folderh(roses, "rose", stems, "stem", leaves, "leaf", leaflets)
print(fh2)</pre>
```

foldermtg

Description

An object of S3 class "foldermtg" is built and returned by the function read.mtg.

foldermtg

Value

An object of this S3 class is a list of at least 5 data frames (see the Value section in read.mtg): classes, description, features, topology, coordinates...

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Pradal, C., Godin, C. and Cokelaer, T. (2023). MTG user guide

See Also

read.mtg print.foldermtg mtgorder

Examples

```
mtgfile1 <- system.file("extdata/plant1.mtg", package = "dad")
x1 <- read.mtg(mtgfile1)
print(x1)
mtgfile2 <- system.file("extdata/plant2.mtg", package = "dad")
x2 <- read.mtg(mtgfile2)
print(x2)</pre>
```

foldert

Folder of data sets among time

Description

Creates an object of class "foldert" (called foldert below), that is a list of data frames, each of them corresponding to a time of observation. These data sets are on the same variables. They can be on the same individuals or not.

Usage

```
foldert(x1, x2 = NULL, ..., times = NULL, cols.select = "intersect", rows.select = "")
```

Arguments

x1	data frame (can also be a tibble) or list of data frames.
	• If x1 is a data frame, x2 must be provided.
	• If x1 is a list of data frames, its elements are the datasets of the folder. In this case, there is no x2 argument.
x2	data frame. Must be provided if x1 is a data frame. Omitted if x1 is a list of data frames.

	optional. One or several data frames when x1 is a data frame. These supplementary data frames are added to the list of data frames constituting the returned foldert.
times	Vector of the "times" of observations. It can be either numeric, or an ordered factor or an object of class "Date", "POSIXlt" or "POSIXct". If omitted, it is 1:N where N is the number of data frame arguments (if x1 is a data frame) or the length of x1 (if it is a list).
	So there is an order relationship between these times.
cols.select	string or character vector. Gives the method used to choose the column names of the data frames of the foldert. This argument can be:
	"intersect" (default) the column names of the data frames in the foldert are the intersection of the column names of all the data frames given as argu- ments.
	"union" the column names of the data frames in the foldert are the union of the column names of all the data frames given as arguments. When necessary, the rows of the returned data frames are completed by NA.
	If cols.select is a character vector, it gives the column names selected in the data frames given as arguments. The corresponding columns constitute the columns of the elements of the returned foldert. Notice that when a column name is not present in all data frames (given as arguments), the data are com- pleted by NA.
rows.select	string. Gives the method used to choose the row names of the data frames of the foldert. This argument can be:
	"" (default) the data frames of the foldert have the same rows as those which were passed as arguments.
	"intersect" the row names of the data frames in the foldert are the intersec- tion of the row names of all the data frames given as arguments.
	"union" the row names of the data frames in the foldert are the union of the row names of all the data frames given as arguments. When necessary, the columns of the data frames returned are completed by NA.

The class "foldert" has an attribute attr(, "times") (the times argument, when provided) and a logical attributes attr(, "same.rows").

The data frames in the returned foldert all have the same column names. That means that the same variables are observed in every data sets.

If the rows.select argument is "union" or "intersect", the elements of the returned foldert have the same rows. That means that the same individuals are present in every data sets. This allows to consider the evolution of each individual among time.

If rows.select is "", every rows of this foldert are different, and the row names are made unique by adding the name of the data frame to the row names. In this case, The individuals of the data sets are assumed to be all different. Or, at least, the user does not mind if they are the same or not.

Value

Returns an object of class "foldert", that is a list of data frames. The elements of this list are ordered according to time.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

is.foldert to test if an object is of class foldert. as.foldert.data.frame: build an object of class foldert from a data frame. as.foldert.array: build an object of class foldert from a 3*d*-array.

Examples

```
x <- data.frame(xyz = rep(c("A", "B", "C"), each = 2),</pre>
                xy = letters[1:6],
                x1 = rnorm(6),
                x^{2} = rnorm(6, 2, 1),
                 row.names = paste0("i", 1:6),
                 stringsAsFactors = TRUE)
y <- data.frame(xyz = c("A", "A", "B", "C"),</pre>
                xy = c("a", "b", "a", "c"),
                 y1 = rnorm(4, 4, 2),
                 row.names = c(paste0("i", c(1, 2, 4, 6))),
                stringsAsFactors = TRUE)
z <- data.frame(xyz = c("A", "B", "C"),</pre>
                z1 = rnorm(3),
                 row.names = c("i1", "i2", "i5"),
                 stringsAsFactors = TRUE)
# Columns selected by the user
ftc. <- foldert(x, y, z, cols.select = c("xyz", "x1", "y1", "z1"))</pre>
print(ftc.)
# cols.select = "union": all the variables (columns) of each data frame are kept
ftcun <- foldert(x, y, z, cols.select = "union")</pre>
print(ftcun)
# cols.select = "intersect": only variables common to all data frames
ftcint <- foldert(x, y, z, cols.select = "intersect")</pre>
print(ftcint)
# rows.select = "": the rows of the data frames are unchanged
# and the rownames are made unique
ftr. <- foldert(x, y, z, rows.select = "")</pre>
print(ftr.)
# rows.select = "union": all the individuals (rows) of each data frame are kept
ftrun <- foldert(x, y, z, rows.select = "union")</pre>
print(ftrun)
```

80

fpcad

```
# rows.select = "intersect": only individuals common to all data frames
ftrint <- foldert(x, y, z, rows.select = "intersect")
print(ftrint)
# Define the times (times argument)
ftimes <- foldert(x, y, z, times = as.Date(c("2018-03-01", "2018-04-01", "2018-05-01")))
print(ftimes)</pre>
```

fpcad

Functional PCA of probability densities

Description

Performs functional principal component analysis of probability densities in order to describe a data folder, consisting of T groups of individuals on which are observed p variables. It returns an object of class fpcad.

Usage

```
fpcad(xf, group.name = "group", gaussiand = TRUE, windowh = NULL, normed = TRUE,
    centered = TRUE, data.centered = FALSE, data.scaled = FALSE,
    common.variance = FALSE, nb.factors = 3, nb.values = 10, sub.title = "",
    plot.eigen = TRUE, plot.score = FALSE, nscore = 1:3,
    filename = NULL)
```

Arguments

xf	object of class "folder" or data.frame.
	• If it is an object of class "folder", its elements are data frames with p numeric columns. If there are non numeric columns, there is an error. The t^{th} element $(t = 1,, T)$ matches with the t^{th} group.
	• If it is a data frame, the column with name given by the group.name argument is a factor giving the groups. The other columns are all numeric; otherwise, there is an error.
group.name	string.
	• If xf is an object of class "folder", name of the grouping variable in the returned results. The default is groupname = "group".
	• If xf is a data frame, group.name is the name of the column of xf containing the groups.
gaussiand	logical. If TRUE (default), the probability densities are supposed Gaussian. If FALSE, densities are estimated using the Gaussian kernel method.
windowh	either a list of T bandwidths (one per density associated to a group), or a strictly positive number. If windowh = NULL (default), the bandwidths are automatically computed. See Details.

normed	logical. If TRUE (default), the densities are normed before computing the distances.
centered	logical. If TRUE (default), the densities are centered.
data.centered	logical. If TRUE (default is FALSE), the data of each group are centered.
data.scaled	logical. If TRUE (default is FALSE), the data of each group are centered (even if data.centered = FALSE) and scaled.
common.variance	9
	logical. If TRUE (default is FALSE), a common covariance matrix (or correlation matrix if data.scaled = TRUE), computed on the whole data, is used. If FALSE (default), a covariance (or correlation) matrix per group is used.
nb.factors	numeric. Number of returned principal scores (default nb.factors = 3).
	Warning: The plot.fpcad and interpret.fpcad functions cannot take into account more than nb.factors principal factors.
nb.values	numerical. Number of returned eigenvalues (default nb.values = 10).
<pre>sub.title</pre>	string. If provided, the subtitle for the graphs.
plot.eigen	logical. If TRUE (default), the barplot of the eigenvalues is plotted.
plot.score	logical. If TRUE, the graphs of principal scores are plotted. A new graphic device is opened for each pair of principal scores defined by nscore argument.
nscore	numeric vector. If plot.score = TRUE, the numbers of the principal scores which are plotted. By default it is equal to nscore = 1:3. Its components cannot be greater than nb.factors.
filename	string. Name of the file in which the results are saved. By default (filename = NULL) the results are not saved.

The *T* probability densities f_t corresponding to the *T* groups of individuals are either parametrically estimated (gaussiand = TRUE) or estimated using the Gaussian kernel method (gaussiand = FALSE). In the latter case, the windowh argument provides the list of the bandwidths to use. Notice that in the multivariate case (p>1) the bandwidths are positive-definite matrices.

If windowh is a numerical value, the matrix bandwidth is of the form hS, where S is either the square root of the covariance matrix (p>1) or the standard deviation of the estimated density.

If windowh = NULL (default), h in the above formula is computed using the bandwidth.parameter function.

Value

Returns an object of class fpcad, that is a list including:

inertia	data frame of the eigenvalues and percentages of inertia.
contributions	data frame of the contributions to the first nb . factors principal components.
qualities	data frame of the qualities on the first nb.factors principal factors.
scores	data frame of the first nb.factors principal scores.
norm	vector of the L^2 norms of the densities.

fpcad

means	list of the means.
variances	list of the covariance matrices.
correlations	list of the correlation matrices.
skewness	list of the skewness coefficients.
kurtosis	list of the kurtosis coefficients.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Boumaza, R. (1998). Analyse en composantes principales de distributions gaussiennes multidimensionnelles. Revue de Statistique Appliqu?e, XLVI (2), 5-20.

Boumaza, R., Yousfi, S., Demotes-Mainard, S. (2015). Interpreting the principal component analysis of multivariate density functions. Communications in Statistics - Theory and Methods, 44 (16), 3321-3339.

Delicado, P. (2011). Dimensionality reduction when data are density functions. Computational Statistics & Data Analysis, 55, 401-420.

Yousfi, S., Boumaza, R., Aissani, D., Adjabi, S. (2014). Optimal bandwith matrices in functional principal component analysis of density functions. Journal of Statistical Computation and Simulation, 85 (11), 2315-2330.

See Also

print.fpcad, plot.fpcad, interpret.fpcad, bandwidth.parameter

Examples

```
data(roses)
# Case of a normed non-centred PCA of Gaussian densities (on 3 architectural
# characteristics of roses: shape (Sha), foliage density (Den) and symmetry (Sym))
rosesf <- as.folder(roses[,c("Sha","Den","Sym","rose")])</pre>
result3 <- fpcad(rosesf, group.name = "rose")</pre>
print(result3)
plot(result3)
# Applied to a data frame:
result3df <- fpcad(roses[,c("Sha", "Den", "Sym", "rose")], group.name = "rose")</pre>
print(result3df)
plot(result3df)
# Flower colors of the roses
scores <- result3$scores</pre>
scores <- data.frame(scores, color = scores$rose, stringsAsFactors = TRUE)</pre>
colours <- scores$rose
colours <- factor(c(A = "yellow", B = "yellow", C = "pink", D = "yellow", E = "red",</pre>
                   F = "yellow", G = "pink", H = "pink", I = "yellow", J = "yellow"))
levels(scores$color) <- c(A = "yellow", B = "yellow", C = "pink", D = "yellow", E = "red",</pre>
```

```
F = "yellow", G = "pink", H = "pink", I = "yellow", J = "yellow")
# Scores according to the first two principal components, per color
plot(result3, nscore = 1:2, color = colours)
```

fpcat

Functional PCA of probability densities among time

Description

Performs functional principal component analysis of probability densities in order to describe a data "foldert", consisting of individuals on which are observed p variables on T times. It returns an object of class fpcat.

Usage

```
fpcat(xf, group.name="time", method = 1, ind = 1, nvar = NULL, gaussiand = TRUE,
  windowh = NULL, normed=TRUE, centered=TRUE, data.centered = FALSE,
  data.scaled = FALSE, common.variance = FALSE, nb.factors = 3, nb.values = 10,
  sub.title = "", plot.eigen = TRUE, plot.score = FALSE, nscore = 1:3,
  filename = NULL)
```

Arguments

xf

object of class "foldert" or data.frame.

- An object of class "foldert" is a list of data frames with the same column names, each of them corresponding to a time of observation. Its elements are data frames with p numeric columns. If there are non numeric columns, there is an error. The t^{th} element (t = 1, ..., T) matches with the t^{th} time of observation.
- If it is a data frame:
 - If method=1: the column with name given by the group.name argument is a factor giving the groups. The other columns are all numeric; otherwise, there is an error.
 - If method=2: the column named after the ind argument contains the identifiers of the measured objects, and the observations are organized as follows:

Given timecol the number of the column named by the group.name argument,

the observations corresponding to the 1st time are on columns timecol : (timecol + nvar - 1)

the observations corresponding to the 2nd time are on columns (timecol + nvar) : (timecol + 2 * nvar - 1)

and so on.

group.name string or numeric.

• If xf is an object of class "foldert", string. Name of the grouping variable, that is the observation times. The default is groupname = "time".

	 If xf is a data frame, string or numeric, as the ind argument of as.foldert.data.frame. If method = 1, timecol is the name or the number of the column of x containing the times of observation, or the number of this column. x[, timecol] must be of class "numeric", "ordered", "Date", "POSIXlt" or "POSIXct", otherwise, there is an error. If method=2, timecol is the name or the number of the first column
	corresponding to the first observation. If there are duplicated column names and several columns are named by timecol, the first one is considered.
method	if xf is a data frame, 1 or 2. Omitted if xf is an object of class "foldert".
	If xf is a data frame, method indicates the layout of this data frame and, there- fore, the method used to extract the data and build the foldert.
	• If method = 1, there is a column containing the identifiers of the measured objects and a column containing the times. The other columns contain the observations.
	• If method = 2, there is a column containing the identifiers of the measured objects, and the observations are organized as follows:
	 the observations corresponding to the 1st time are on columns timecol : (timecol + nvar - 1)
	- the observations corresponding to the 2nd time are on columns (timecol + nvar) : (timecol + 2 * nvar - 1)
	– and so on.
ind	if xf is a data frame, string or numeric. Omitted if xf is an object of class "foldert".
	The name of the column of x containing the indentifiers of the measured objects, or the number of this column. See the ind argument of as.foldert.data.frame.
nvar	if xf is a data frame and mathod=2, string or numeric. Omitted if xf is an object of class "foldert" or if method=1.
	The number of variable measured at each observation time. See the ind argument of as.foldert.data.frame.
All other argume	nts are the same as for fpcad.
gaussiand	logical. If TRUE (default), the probability densities are supposed Gaussian. If FALSE, densities are estimated using the Gaussian kernel method (as fpcad).
windowh	either a list of T bandwidths (one per density associated to a group), or a strictly positive number. If windowh = NULL (default), the bandwidths are automatically computed (as fpcad). See Details.
normed	logical. If TRUE (default), the densities are normed before computing the dis- tances (as fpcad).
centered	logical. If TRUE (default), the densities are centered (as fpcad).
data.centered	logical. If TRUE (default is FALSE), the data of each group are centered (as fpcad).
data.scaled	logical. If TRUE (default is FALSE), the data of each group are centered (even if data.centered = FALSE) and scaled (as fpcad).

common.variance		
	logical. If TRUE (default is FALSE), a common covariance matrix (or correlation matrix if data.scaled = TRUE), computed on the whole data, is used. If FALSE (default), a covariance (or correlation) matrix per group is used (as fpcad).	
nb.factors	numeric. Number of returned principal scores (default nb.factors = 3) (as fpcad).	
	Warning: The plot.fpcad and interpret.fpcad functions cannot take into account more than nb.factors principal factors (as fpcad).	
nb.values	numerical. Number of returned eigenvalues (default nb.values = 10) (as fpcad).	
<pre>sub.title</pre>	string. Subtitle for the graphs (default NULL) (as fpcad).	
plot.eigen	logical. If TRUE (default), the barplot of the eigenvalues is plotted (as fpcad).	
plot.score	logical. If TRUE, the graphs of principal scores are plotted. A new graphic device is opened for each pair of principal scores defined by nscore argument (as fpcad).	
nscore	numeric vector. If plot.score = TRUE, the numbers of the principal scores which are plotted. By default it is equal to nscore = $1:3$. Its components cannot be greater than nb.factors (as fpcad).	
filename	string. Name of the file in which the results are saved. By default (filename = NULL) the results are not saved (as fpcad).	

The T probability densities f_t corresponding to the T times of observation are either parametrically estimated or estimated using the Gaussian kernel method (see fpcad for the use of the arguments indicating the method used to estimate these densities).

Value

Returns an object of class fpcat, that is a list including:

times	vector of the times of observation.
inertia	data frame of the eigenvalues and percentages of inertia.
contributions	data frame of the contributions to the first nb.factors principal components.
qualities	data frame of the qualities on the first nb.factors principal factors.
scores	data frame of the first nb.factors principal scores.
norm	vector of the L^2 norms of the densities.
means	list of the means.
variances	list of the covariance matrices.
correlations	list of the correlation matrices.
skewness	list of the skewness coefficients.
kurtosis	list of the kurtosis coefficients.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

getcol.folder

References

Boumaza, R. (1998). Analyse en composantes principales de distributions gaussiennes multidimensionnelles. Revue de Statistique Appliqu?e, XLVI (2), 5-20.

Boumaza, R., Yousfi, S., Demotes-Mainard, S. (2015). Interpreting the principal component analysis of multivariate density functions. Communications in Statistics - Theory and Methods, 44 (16), 3321-3339.

Delicado, P. (2011). Dimensionality reduction when data are density functions. Computational Statistics & Data Analysis, 55, 401-420.

Yousfi, S., Boumaza, R., Aissani, D., Adjabi, S. (2014). Optimal bandwith matrices in functional principal component analysis of density functions. Journal of Statistical Computation and Simulation, 85 (11), 2315-2330.

See Also

print.fpcat, plot.fpcat, bandwidth.parameter

Examples

```
times <- as.Date(c("2017-03-01", "2017-04-01", "2017-05-01", "2017-06-01"))
x1 <- data.frame(z1=rnorm(6,1,5), z2=rnorm(6,3,3))
x2 <- data.frame(z1=rnorm(6,4,6), z2=rnorm(6,5,2))
x3 <- data.frame(z1=rnorm(6,7,2), z2=rnorm(6,8,4))
x4 <- data.frame(z1=rnorm(6,9,3), z2=rnorm(6,10,2))
ft <- foldert(x1, x2, x3, x4, times = times, rows.select="intersect")
print(ft)
result <- fpcat(ft)
print(result)
plot(result)</pre>
```

getcol.folder Select columns in all elements of a folder

Description

Select columns in all data frames of a folder.

Usage

```
getcol.folder(object, name)
```

Arguments

object	object of class folder that is a list of data frames with the same column names.
name	character vector. The names of the columns to be selected in each data frame of
	the folder.

Value

A folder with the same number of elements as object. Its k^{th} element is a data frame, and its columns are the columns of object[[k]] given by name.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

folder: object of class folder.

rmcol.folder: remove columns in all elements of a folder.

getrow. folder: select rows in all elements of a folder.

rmrow.folder: remove rows in all elements of a folder.

Examples

data(iris)

```
iris.fold <- as.folder(iris, "Species")
getcol.folder(iris.fold, "Sepal.Length")
getcol.folder(iris.fold, c("Petal.Length", "Petal.Width"))</pre>
```

getcol.foldert Select columns in all elements of a foldert

Description

Select columns in all data frames of a foldert.

Usage

getcol.foldert(object, name)

Arguments

object	object of class foldert that is a list of data frames with the same column names, each of them corresponding to a time of observation.
name	character vector. The names of the columns to be selected in each data frame of the foldert.

Value

A foldert with the same number of elements as object. Its k^{th} element is a data frame, and its columns are the columns of object[[k]] given by name.

getrow.folder

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

foldert: object of class foldert.

rmcol.foldert: remove columns in all elements of a foldert.

getrow. foldert: select rows in all elements of a foldert.

rmrow.foldert: remove rows in all elements of a foldert.

Examples

data(floribundity)

ft0 <- foldert(floribundity, cols.select = "union")
getcol.foldert(ft0, c("rose", "variety"))</pre>

getrow.folder Select rows in all elements of a folder

Description

Select rows in all data frames of a folder.

Usage

getrow.folder(object, name)

Arguments

object	object of class folder that is a list of data frames with the same column names.
name	character vector. The names of the rows to be selected in each data frame of the
Hame	folder.

Value

A folder with the same number of elements as object. Its k^{th} element is a data frame, and its rows are the rows of object[[k]] given by name.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

folder: object of class folder.

rmrow.folder: remove rows in all elements of a folder.

getcol.folder: select rows in all elements of a folder.

rmcol.folder: remove rows in all elements of a folder.

Examples

```
data(iris)
iris.fold <- as.folder(iris, "Species")
getrow.folder(iris.fold, c(1:5, 51:55, 101:105))</pre>
```

getrow.foldert Select rows in all elements of a foldert

Description

Select rows in all data frames of a foldert.

Usage

getrow.foldert(object, name)

Arguments

object	object of class foldert that is a list of data frames with the same column names, each of them corresponding to a time of observation.
name	character vector. The names of the rows to be selected in each data frame of the foldert.

Value

A foldert with the same number of elements as object. Its k^{th} element is a data frame, and its rows are the rows of object[[k]] given by name.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

foldert: object of class foldert.
rmrow.foldert: remove rows in all elements of a foldert.
getcol.foldert: select columns in all elements of a foldert.
rmcol.foldert: remove columns in all elements of a foldert.

90

hclustdd

Examples

data(floribundity)

```
ft0 <- foldert(floribundity, cols.select = "union", rows.select = "union")
getrow.foldert(ft0, c("16", "51"))</pre>
```

hclustdd

Hierarchic cluster analysis of discrete probability distributions

Description

Performs functional hierarchic cluster analysis of discrete probability distributions. It returns an object of class hclustdd. It applies hclust to the distance matrix between the T distributions.

Usage

```
hclustdd(xf, group.name = "group", distance = c("l1", "l2", "chisqsym", "hellinger",
        "jeffreys", "jensen", "lp"),
        sub.title = "", filename = NULL,
        method.hclust = "complete")
```

Arguments

•	,	1
2	٢.	т
٠	•	

object of class folder, or list of arrays (or tables).

- If it is a folder, its elements are data frames with q columns (considered as factors). The t^{th} element (t = 1, ..., T) matches with the t^{th} group.
- If it is a data frame, the columns with name given by the group.name argument is a factor giving the groups. The other columns are all considered as factors.
- If it is a list of arrays (or tables), the t^{th} element (t = 1, ..., T) is the table of the joint frequency distribution of q variables within the t^{th} group. The frequency distribution is expressed with relative or absolute frequencies. These arrays have the same shape.

Each array (or table) xf[[i]] has:

- the same dimension(s). If q = 1 (univariate), dim(xf[[i]]) is an integer. If q > 1 (multivariate), dim(xf[[i]]) is an integer vector of length q.
- the same dimension names dimnames(xf[[i]]) (is non NULL). These dimnames are the names of the variables.

The elements of the arrays are non-negative numbers (if they are not, there is an error).

group.namestring. Name of the grouping variable. Default: group.name = "group".distanceThe distance or divergence used to compute the distance matrix between the
discrete distributions (see Details). It can be:

• "11" (default) the L^p distance with p = 1

	• "12" the L^p distance with $p = 2$
	 "chisqsym" the symmetric Chi-squared distance
	• "hellinger" the Hellinger metric (Matusita distance)
	• "jeffreys" Jeffreys distance (symmetrised Kullback-Leibler divergence)
	• "jensen" the Jensen-Shannon distance
	• "lp" the L^p distance with p given by the argument p of the function.
sub.title	string. If provided, the subtitle for the graphs.
filename	string. Name of the file in which the results are saved. By default (filename = NULL) the results are not saved.
method.hclust	the agglomeration method to be used for the clustering. See the method argument of the hclust function.

In order to compute the distances/dissimilarities between the groups, the T probability distributions f_t corresponding to the T groups of individuals are estimated from observations. Then the distances/dissimilarities between the estimated distributions are computed, using the distance or divergence defined by the distance argument:

If the distance is "11", "12" or "1p", the distances are computed by the function matddlppar. Otherwise, it can be computed by matddchisqsympar ("chisqsym"), matddhellingerpar ("hellinger"), matddjeffreyspar ("jeffreys") or matddjensenpar ("jensen").

Value

Returns an object of class hclustdd, that is a list including:

distances	matrix of the L^2 -distances between the estimated densities.
clust	an object of class hclust.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

hclustdd

Examples

```
# Example 1 with a folder (10 groups) of 3 factors
# obtained by converting numeric variables
data(roses)
xr = roses[,c("Sha", "Den", "Sym", "rose")]
xr = cut(xr, breaks = list(c(0, 5, 7, 10), c(0, 4, 6, 10), c(0, 6, 8, 10)))
xf = as.folder(xr, groups = "rose")
af = hclustdd(xf)
print(af)
print(af, dist.print = TRUE)
```

hellinger

```
plot(af)
plot(af, hang = -1)
# Example 2 with a data frame obtained by converting numeric variables
ar = hclustdd(xr, group.name = "rose")
print(ar)
print(ar, dist.print = TRUE)
plot(ar)
plot(ar, hang = -1)
# Example 3 with a list of 7 arrays
data(dspg)
xl = dspg
hclustdd(xl)
```

hellinger

Hellinger distance between Gaussian densities

Description

Hellinger distance between two multivariate (p > 1) or univariate (p = 1) Gaussian densities (see Details).

Usage

hellinger(x1, x2, check = FALSE)

Arguments

x1	a matrix or data frame of n_1 rows (observations) and p columns (variables) (can also be a tibble) or a vector of length n_1 .
x2	matrix or data frame (or tibble) of n_2 rows and p columns or vector of length n_2 .
check	logical. When TRUE (the default is FALSE) the function checks if the covariance matrices are not degenerate (multivariate case) or if the variances are not zero (univariate case).

Details

The Hellinger distance between the two Gaussian densities is computed by using the hellingerpar function and the density parameters estimated from samples.

Value

Returns the Hellinger distance between the two probability densities.

Be careful! If check = FALSE and one smoothing bandwidth matrix is degenerate, the result returned can not be considered.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

McLachlan, G.J. (1992). Discriminant analysis and statistical pattern recognition. John Wiley & Sons, New York .

See Also

hellingerpar: Hellinger distance between Gaussian densities, given their parameters.

Examples

```
require(MASS)
m1 <- c(0,0)
v1 <- matrix(c(1,0,0,1),ncol = 2)
m2 <- c(0,1)
v2 <- matrix(c(4,1,1,9),ncol = 2)
x1 <- mvrnorm(n = 3,mu = m1,Sigma = v1)
x2 <- mvrnorm(n = 5, mu = m2, Sigma = v2)
hellinger(x1, x2)</pre>
```

```
hellingerpar
```

Hellinger distance between Gaussian densities given their parameters

Description

Hellinger distance between two multivariate (p > 1) or univariate (p = 1) Gaussian densities given their parameters (mean vectors and covariance matrices if the densities are multivariate, or means and variances if univariate) (see Details).

Usage

```
hellingerpar(mean1, var1, mean2, var2, check = FALSE)
```

Arguments

mean1	p-length numeric vector: the mean of the first Gaussian density.
var1	$p \ge p$ symmetric numeric matrix $(p > 1)$ or numeric $(p = 1)$: the covariance matrix $(p > 1)$ or the variance $(p = 1)$ of the first Gaussian density.
mean2	p-length numeric vector: the mean of the second Gaussian density.
var2	$p \ge p$ symmetric numeric matrix $(p > 1)$ or numeric $(p = 1)$: the covariance matrix $(p > 1)$ or the variance $(p = 1)$ of the second Gaussian density.
check	logical. When TRUE (the default is FALSE) the function checks if the covariance matrices are not degenerate (multivariate case) or if the variances are not zero (univariate case).

interpret

Details

The mean vectors (m1 and m2) and variance matrices (v1 and v2) given as arguments (mean1, mean2, var1 and var2) are used to compute the Hellinger distance between the two Gaussian densities, equal to:

$$(2(1-2^{p/2}det(v1v2)^{1/4}det(v1+v2)^{-1/2}exp((-1/4)t(m1-m2)(v1+v2)^{-1}(m1-m2))))^{1/2}exp((-1/4)t(m1-m2)(v1+v2)^{-1}(m1-m2))))^{1/2}exp((-1/4)t(m1-m2)(v1+v2)^{-1}(m1-m2))))^{1/2}exp((-1/4)t(m1-m2)(v1+v2)^{-1}(m1-m2))))^{1/2}exp((-1/4)t(m1-m2)(v1+v2)^{-1}(m1-m2))))^{1/2}exp((-1/4)t(m1-m2)(v1+v2)^{-1}(m1-m2))))^{1/2}exp((-1/4)t(m1-m2)(v1+v2)^{-1}(m1-m2))))^{1/2}exp((-1/4)t(m1-m2)(v1+v2)^{-1}(m1-m2))))^{1/2}exp((-1/4)t(m1-m2)(v1+v2)^{-1}(m1-m2))))^{1/2}exp((-1/4)t(m1-m2)(v1+v2)^{-1}(m1-m2))))^{1/2}exp((-1/4)t(m1-m2)(v1+v2)^{-1}(m1-m2))))^{1/2}exp((-1/4)t(m1-m2)(v1+v2)^{-1}(m1-m2))))^{1/2}exp((-1/4)t(m1-m2)(v1+v2)^{-1}(m1-m2))))^{1/2}exp((-1/4)t(m1-m2)(v1+v2)^{-1}(m1-m2))))^{1/2}exp((-1/4)t(m1-m2)(v1+v2)^{-1}(m1-m2)))))^{1/2}exp((-1/4)t(m1-m2)(v1+v2)^{-1}(m1-m2)))))^{1/2}exp((-1/4)t(m1-m2)(v1+v2)^{-1}(m1-m2))))))$$

If p = 1 the means and variances are numbers, the formula is the same ignoring the following operators: t (transpose of a matrix or vector) and det (determinant of a square matrix).

Value

The Hellinger distance between two Gaussian densities.

Be careful! If check = FALSE and one covariance matrix is degenerated (multivariate case) or one variance is zero (univariate case), the result returned must not be considered.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

McLachlan, G.J. (1992). Discriminant analysis and statistical pattern recognition. John Wiley & Sons, New York .

See Also

hellinger: Hellinger distance between Gaussian densities estimated from samples.

Examples

```
m1 <- c(1,1)
v1 <- matrix(c(4,1,1,9),ncol = 2)
m2 <- c(0,1)
v2 <- matrix(c(1,0,0,1),ncol = 2)
hellingerpar(m1,v1,m2,v2)</pre>
```

interpret	Scores of fmdsd, dstatis, fpcad, or fpcat vs. moments, or scores of
	mdsdd vs. marginal distributions or association measures

Description

This generic function provides a tool for the interpretation of the results of fmdsd, dstatis, fpcad, fpcat or mdsdd function.

interpret

Usage

interpret(x, nscore = 1:3, ...)

Arguments

x	object of class fmdsd, dstatis, fpcad, fpcat or mdsdd.
	• fmdsd: see interpret.fmdsd
	 dstatis: see interpret.dstatis
	• fpcad: see interpret.fpcad
	• fpcat: see interpret.fpcat
	• mdsdd: see interpret.mdsdd
nscore	numeric vector. Selects the columns of the data frame x\$scores to be interpreted.
	Warning: Its components cannot be greater than the nb.factors argument in the call of the fpcad or fpcat function.
	Arguments to be passed to the methods, such as moment (for interpret.fmdsd, interpret.dstatis, interpret.fpcad and interpret.fpcat), or mma (for interpret.mdsdd).

Value

Returns a list including:

pearson	matrix of Pearson correlations between selected scores and moments, probabil- ities or associations.
spearman	matrix of Spearman correlations between selected scores and moments, probabilities or associations.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

References

Boumaza, R., Yousfi, S., Demotes-Mainard, S. (2015). Interpreting the principal component analysis of multivariate density functions. Communications in Statistics - Theory and Methods, 44 (16), 3321-3339.

See Also

interpret.fmdsd; interpret.dstatis; interpret.fpcad; interpret.fpcat; interpret.mdsdd.

96

interpret.dstatis Scores of the dstatis function vs. moments of the densities

Description

Applies to an object of class "dstatis", plots the principal scores vs. the moments of the densities (means, standard deviations, variances, correlations, skewness and kurtosis coefficients), and computes the correlations between these scores and moments.

Usage

Arguments

х	object of class "dstatis" (returned by the dstatis.inter function).
nscore	numeric. Selects the column of the data frame x\$scores consisting of a score vector.
	Note that since dad-4, nscore can only be a single value (in earlier versions, it could be a vector of length > 1).
	Warning: nscore cannot be greater than the nb.factors argument in the call of the dstatis.inter function.
moment	characters string. Selects the moments to cross with scores:
	• "mean" (means)
	• "sd" (standard deviations)
	 "cov" (covariances)
	 "cor" (correlation coefficients)
	 "skewness" (skewness coefficients)
	 "kurtosis" (kurtosis coefficients)
	Arguments to be passed to methods.

Details

A graphics device can contain up to 9 graphs. If there are too many (more than 36) graphs for each score, one can display the graphs in a multipage PDF file.

The number of principal scores to be interpreted cannot be greater than nb.factors of the data frame x\$scores returned by the function dstatis.inter.

Value

Returns a list including:

pearson	matrix of Pearson correlations between selected scores and moments.
spearman	matrix of Spearman correlations between selected scores and moments.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Lavit, C., Escoufier, Y., Sabatier, R., Traissac, P. (1994). The ACT (STATIS method). Computational Statistics & Data Analysis, 18 (1994), 97-119.

See Also

dstatis.inter; plot.dstatis.

Examples

```
data(roses)
rosesf <- as.folder(roses[,c("Sha","Den","Sym","rose")])</pre>
```

```
# Dual STATIS on the covariance matrices
## Not run:
result <- dstatis.inter(rosesf, group.name = "rose")
interpret(result)
interpret(result, moment = "var")
interpret(result, moment = "cor")
interpret(result, nscore = 2)</pre>
```

End(Not run)

interpret.fmdsd Scores of the fmdsd function vs. moments of the densities

Description

Applies to an object of class "fmdsd", plots the scores vs. the moments of the densities (means, standard deviations, variances, correlations, skewness and kurtosis coefficients), and computes the correlations between these scores and moments.

Usage

Arguments

object of class "fmdsd" (returned by the fmdsd function).

Х

nscore	numeric. Selects the column of the data frame x\$scores consisting of a score vector.
	Note that since dad-4, nscore can only be a single value (in earlier versions, it could be a vector of length > 1).
	Warning: nscore cannot be greater than the nb.factors argument in the call of the fmdsd function.
moment	character string. Selects the moments to cross with scores:
	• "mean" (means, which is the default value)
	• "sd" (standard deviations)
	• "cov" (covariances)
	 "cor" (correlation coefficients)
	 "skewness" (skewness coefficients)
	 "kurtosis" (kurtosis coefficients)
	Arguments to be passed to methods.

A graphics device can contain up to 9 graphs. If there are too many (more than 36) graphs for each score, one can display the graphs in a multipage PDF file.

The number of principal scores to be interpreted cannot be greater than nb.factors of the data frame x\$scores returned by the function fmdsd.

Value

Returns a list including:

pearson	matrix of Pearson correlations between selected scores and moments.
spearman	matrix of Spearman correlations between selected scores and moments.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Boumaza, R., Yousfi, S., Demotes-Mainard, S. (2015). Interpreting the principal component analysis of multivariate density functions. Communications in Statistics - Theory and Methods, 44 (16), 3321-3339.

Delicado, P. (2011). Dimensionality reduction when data are density functions. Computational Statistics & Data Analysis, 55, 401-420.

See Also

fmdsd; plot.fmdsd.

Examples

```
data(roses)
x <- roses[,c("Sha", "Den", "Sym", "rose")]
rosesfold <- as.folder(x)
result1 <- fmdsd(rosesfold)
interpret(result1)
## Not run:
interpret(result1, moment = "var")
## End(Not run)
interpret(result1, nscore = 2)</pre>
```

interpret.fpcad Scores of the fpcad function vs. moments of the densities

Description

Applies to an object of class "fpcad", plots the principal scores vs. the moments of the densities (means, standard deviations, variances, correlations, skewness and kurtosis coefficients), and computes the correlations between these scores and moments.

Usage

Arguments

х	object of class "fpcad" (returned by the fpcad function).
nscore	numeric. Selects the column of the data frame x\$scores consisting of a score vector.
	Note that since dad-4, nscore can only be a single value (in earlier versions, it could be a vector of length > 1).
	Warning: nscore cannot be greater than the nb.factors argument in the call of the fpcad function.
moment	characters string. Selects the moments to cross with scores:
	• "mean" (means)
	• "sd" (standard deviations)
	• "cov" (covariances)
	"cor" (correlation coefficients)
	"skewness" (skewness coefficients)
	 "kurtosis" (kurtosis coefficients)
	Arguments to be passed to methods.

100

interpret.fpcad

Details

A graphics device can contain up to 9 graphs. If there are too many (more than 36) graphs for each score, one can display the graphs in a multipage PDF file.

The number of principal scores to be interpreted cannot be greater than nb.factors of the data frame x\$scores returned by the function fpcad.

Value

Returns a list including:

pearson	matrix of Pearson correlations between selected scores and moments.
spearman	matrix of Spearman correlations between selected scores and moments.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Boumaza, R., Yousfi, S., Demotes-Mainard, S. (2015). Interpreting the principal component analysis of multivariate density functions. Communications in Statistics - Theory and Methods, 44 (16), 3321-3339.

See Also

fpcad; plot.fpcad.

Examples

```
data(roses)
rosefold <- as.folder(roses[,c("Sha","Den","Sym","rose")])
result1 <- fpcad(rosefold)
interpret(result1)
## Not run:
interpret(result1, moment = "var")
## End(Not run)
interpret(result1, moment = "cor")
interpret(result1, nscore = 2)</pre>
```

interpret.fpcat

Description

This function applies to an object of class "fpcat" and does the same as for an object of class "fpcad": it plots the principal scores vs. the moments of the densities (means, standard deviations, variances, correlations, skewness and kurtosis coefficients), and computes the correlations between these scores and moments.

Usage

Arguments

x nscore	object of class "fpcat" (returned by the fpcat function). numeric. Selects the column of the data frame x\$scores consisting of a score vector.
	Note that since dad-4, nscore can only be a single value (in earlier versions, it could be a vector of length > 1).
	Warning: nscore cannot be greater than the nb.factors argument in the call of the fpcat function.
moment	characters string. Selects the moments to cross with scores:
	• "mean" (means)
	• "sd" (standard deviations)
	 "cov" (covariances)
	 "cor" (correlation coefficients)
	 "skewness" (skewness coefficients)
	 "kurtosis" (kurtosis coefficients)
	Arguments to be passed to methods.

Details

A graphics device can contain up to 9 graphs. If there are too many (more than 36) graphs for each score, one can display the graphs in a multipage PDF file.

The number of principal scores to be interpreted cannot be greater than nb.factors of the data frame x\$scores returned by the function fpcat.

Value

Returns a list including:

pearson	matrix of Pearson correlations between selected scores and moments.
spearman	matrix of Spearman correlations between selected scores and moments.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Boumaza, R., Yousfi, S., Demotes-Mainard, S. (2015). Interpreting the principal component analysis of multivariate density functions. Communications in Statistics - Theory and Methods, 44 (16), 3321-3339.

See Also

fpcat; plot.fpcat.

Examples

```
# Alsacian castles with their building year
data(castles)
castyear <- foldert(lapply(castles, "[", 1:4))
fpcayear <- fpcat(castyear, group.name = "year")
interpret(fpcayear)
## Not run:
interpret(fpcayear, moment="var")
```

End(Not run)

interpret.mdsdd	Scores of the mdsdd function vs. marginal probability distributions or
	association measures

Description

Applies to an object of class "mdsdd", plots the scores vs. the marginal probability distributions or pairwise association measures of the discrete variables, and computes the correlations between these scores and probabilities or association measures (see Details).

Usage

```
## S3 method for class 'mdsdd'
interpret(x, nscore = 1, mma = c("marg1", "marg2", "assoc"), ...)
```

Arguments

х	object of class "mdsdd" (returned by the mdsdd function).
nscore	numeric. Selects the column of the data frame x\$scores consisting of a score vector.
	Note that since dad-4, nscore can only be a single value (in earlier versions, it could be a vector of length > 1). Warning: nscore cannot be greater than the nb.factors argument in the call
	of the mdsdd function.

mma	character. Indicates which measures will be considered:
	• "marg1": the probability distribution of each variable.
	• "marg2": the joint probability distribution of each pair of variables.
	• "assoc": the pairwise association measures of the variables.
	Arguments to be passed to methods.

A graphics device can contain up to 9 graphs. If there are too many (more than 36) graphs for each score, one can display the graphs in a multipage PDF file.

The number of principal scores to be interpreted cannot be greater than nb.factors of the data frame x\$scores returned by the function mdsdd.

Value

Returns a list including:

pearson	matrix of Pearson correlations between selected scores and probabilities or as- sociation measures.
spearman	matrix of Spearman correlations between selected scores and probabilities or association measures.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

See Also

mdsdd; plot.mdsdd.

Examples

```
# INSEE (France): Diploma x Socio professional group, seven years.
data(dspg)
xlista = dspg
a <- mdsdd(xlista)</pre>
interpret(a)
# Example 3 with a list of 96 arrays (departments)
## Not run:
data(dspgd2015)
xd = dspgd2015
res = mdsdd(xd, group.name = "coded")
interpret(res)
plot(res, fontsize.points = 0.7)
# Each department is represented by its name
data(departments)
coor = merge(res$scores, departments, by = "coded")
dev.new()
```

is.discdd.misclass

```
plot(coor$PC.1, coor$PC.2, type ="n")
text(coor$PC.1, coor$PC.2, coor$named, cex = 0.5)
# Each department is represented by its region
dev.new()
plot(coor$PC.1, coor$PC.2, type ="n")
text(coor$PC.1, coor$PC.2, coor$coder, cex = 0.7)
## End(Not run)
```

is.discdd.misclass Class discdd.misclass

Description

Tests if its argument is an object of class discdd.misclass (see Details of the function discdd.misclass).

Usage

```
is.discdd.misclass(x)
```

Arguments

x object to be tested.

Value

TRUE if its argument is of class discdd.misclass, and FALSE otherwise.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

discdd.misclass.

is.discdd.predict Class discdd.predict

Description

Tests if its argument is an object of class discdd.predict (see Details of the function discdd.predict).

Usage

is.discdd.predict(x)

Arguments

х

object to be tested.

Value

TRUE if its argument is of class discdd.predict, and FALSE otherwise.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

discdd.predict.

is.dstatis Class dstatis

Description

Tests if its argument is an object of class dstatis (see Details of the function dstatis.inter).

Usage

is.dstatis(x)

Arguments ×

object to be tested.

Value

TRUE if its argument is of class dstatis, and FALSE otherwise.

is.fdiscd.misclass

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

dstatis.inter.

is.fdiscd.misclass Class fdiscd.misclass

Description

Tests if its argument is an object of class fdiscd.misclass (see Details of the function fdiscd.misclass).

Usage

```
is.fdiscd.misclass(x)
```

Arguments

x object to be tested.

Value

TRUE if its argument is of class fdiscd.misclass, and FALSE otherwise.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

fdiscd.misclass.

Description

Tests if its argument is an object of class fdiscd.predict (see Details of the function fdiscd.predict)...

Usage

is.fdiscd.predict(x)

Arguments

х

object to be tested.

Value

TRUE if its argument is of class fdiscd.predict, and FALSE otherwise.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

fdiscd.predict.

is.fhclustd Class fhclustd

Description

Tests if its argument is an object of class fhclustd (see Details of the function fhclustd).

Usage

is.fhclustd(x)

Arguments ×

object to be tested.

Value

TRUE if its argument is of class fhclustd, and FALSE otherwise.

is.fmdsd

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

fhclustd.

d Class fmdsd
d Class fmdsd

Description

Tests if its argument is an object of class fmdsd (see Details of the function fmdsd).

Usage

is.fmdsd(x)

Arguments

x object to be tested.

Value

TRUE if its argument is of class fmdsd, and FALSE otherwise.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

fmdsd.

is.folder

Description

Tests if its argument is an object of class folder (see folder).

Usage

is.folder(x)

Arguments ×

object to be tested.

Value

TRUE if its argument is of class folder, and FALSE otherwise.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

folder to create an object of class folder.

is.folderh Class folderh

Description

Tests if its argument is an object of class folderh (see folderh).

Usage

is.folderh(x)

Arguments ×

object to be tested.

Value

TRUE if its argument is of class folderh, and FALSE otherwise.

is.foldermtg

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

folderh to create an object of class folderh.

is.foldermtg	Class foldermtg

Description

Tests if its argument is an object of class foldermtg (see read.mtg).

Usage

is.foldermtg(x)

Arguments

x object to be tested.

Value

TRUE if its argument is of class foldermtg, and FALSE otherwise.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

read.mtg to read a MTG file and create an object of class foldermtg.

is.foldert

Description

Tests if its argument is an object of class foldert (see foldert).

Usage

is.foldert(x)

Arguments ×

object to be tested.

Value

TRUE if its argument is of class foldert, and FALSE otherwise.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

foldert to create an object of class foldert.

is.fpcad Class fpcad

Description

Tests if its argument is an object of class fpcad (see Details of the function fpcad).

Usage

is.fpcad(x)

Arguments ×

object to be tested.

Value

TRUE if its argument is of class fpcad, and FALSE otherwise.

is.mdsdd

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

fpcad.

is.mdsdd	Class mdsdd	

Description

Tests if its argument is an object of class mdsdd (see Details of the function mdsdd).

Usage

is.mdsdd(x)

Arguments

x object to be tested.

Value

TRUE if its argument is of class mdsdd, and FALSE otherwise.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

mdsdd.

jeffreys

Description

Jeffreys measure (or symmetrised Kullback-Leibler divergence) between two multivariate (p > 1) or univariate (p = 1) Gaussian densities given samples (see Details).

Usage

jeffreys(x1, x2, check = FALSE)

Arguments

x1	a matrix or data frame of n_1 rows (observations) and p columns (variables) (can also be a tibble) or a vector of length n_1 .
x2	matrix or data frame (or tibble) of n_2 rows and p columns or vector of length n_2 .
check	logical. When TRUE (the default is FALSE) the function checks if the covariance matrices are not degenerate (multivariate case) or if the variances are not zero (univariate case).

Details

The Jeffreys measure between the two Gaussian densities is computed by using the jeffreyspar function and the density parameters estimated from samples.

Value

Returns the Jeffrey's measure between the two probability densities.

Be careful! If check = FALSE and one smoothing bandwidth matrix is degenerate, the result returned must not be considered.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Thabane, L., Safiul Haq, M. (1999). On Bayesian selection of the best population using the Kullback-Leibler divergence measure. Statistica Neerlandica, 53(3): 342-360.

See Also

jeffreyspar: Jeffreys measure between Gaussian densities, given their parameters.

jeffreyspar

Examples

```
require(MASS)
m1 <- c(0,0)
v1 <- matrix(c(1,0,0,1),ncol = 2)
m2 <- c(0,1)
v2 <- matrix(c(4,1,1,9),ncol = 2)
x1 <- mvrnorm(n = 3,mu = m1,Sigma = v1)
x2 <- mvrnorm(n = 5, mu = m2, Sigma = v2)
jeffreys(x1, x2)</pre>
```

```
jeffreyspar
```

Jeffreys measure between Gaussian densities given their parameters

Description

Jeffreys measure (or symmetrised Kullback-Leibler divergence) between two multivariate (p > 1) or univariate (p = 1) Gaussian densities, given their parameters (mean vectors and covariance matrices if they are multivariate, means and variances if univariate) (see Details).

Usage

jeffreyspar(mean1, var1, mean2, var2, check = FALSE)

Arguments

mean1	p-length numeric vector: the mean of the first Gaussian density.
var1	$p \ge p$ symmetric numeric matrix $(p > 1)$ or numeric $(p = 1)$: the covariance matrix $(p > 1)$ or the variance $(p = 1)$ of the first Gaussian density.
mean2	p-length numeric vector: the mean of the second Gaussian density.
var2	$p \ge p$ symmetric numeric matrix $(p > 1)$ or numeric $(p = 1)$: the covariance matrix $(p > 1)$ or the variance $(p = 1)$ of the second Gaussian density.
check	logical. When TRUE (the default is FALSE) the function checks if the covariance matrices are not degenerate (multivariate case) or if the variances are not zero (univariate case).

Details

.

Let m1 and m2 the mean vectors, v1 and v2 the covariance matrices, Jeffreys measure of the two Gaussian densities is equal to:

$$(1/2)t(m1 - m2)(v1^{-1} + v2^{-1})(m1 - m2) - (1/2)tr((v1 - v2)(v1^{-1} - v2^{-1}))$$

If p = 1 the means and variances are numbers, the formula is the same ignoring the following operators: t (transpose of a matrix or vector) and tr (trace of a square matrix).

Value

Jeffreys measure between two Gaussian densities.

Be careful! If check = FALSE and one covariance matrix is degenerated (multivariate case) or one variance is zero (univariate case), the result returned must not be considered.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

McLachlan, G.J. (1992). Discriminant analysis and statistical pattern recognition. John Wiley & Sons, New York .

Thabane, L., Safiul Haq, M. (1999). On Bayesian selection of the best population using the Kullback-Leibler divergence measure. Statistica Neerlandica, 53(3): 342-360.

See Also

jeffreys: Jeffreys measure of two parametrically estimated Gaussian densities, given samples.

Examples

m1 <- c(1,1)
v1 <- matrix(c(4,1,1,9),ncol = 2)
m2 <- c(0,1)
v2 <- matrix(c(1,0,0,1),ncol = 2)
jeffreyspar(m1,v1,m2,v2)</pre>

kurtosis.folder Kurtosis coefficients of a folder of data sets

Description

Computes the kurtosis coefficient by column of the elements of an object of class folder.

Usage

kurtosis.folder(x, na.rm = FALSE, type = 3)

Arguments

x	an object of class folder.
na.rm	logical. Should missing values be omitted from the calculations? (see ${\tt kurtosis})$
type	an integer between 1 and 3 (see kurtosis).

Details

It uses kurtosis to compute the mean by numeric column of each element of the folder. If some columns of the data frames are not numeric, there is a warning, and the means are computed on the numeric columns only.

Value

A list whose elements are the kurtosis coefficients by column of the elements of the folder.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

folder to create an object is of class folder. mean.folder, var.folder, cor.folder, skewness.folder for other statistics for folder objects.

Examples

```
# First example: iris (Fisher)
data(iris)
iris.fold <- as.folder(iris, "Species")
iris.kurtosis <- kurtosis.folder(iris.fold)
print(iris.kurtosis)
# Second example: roses
data(roses)
roses.fold <- as.folder(roses, "rose")
roses.kurtosis <- kurtosis.folder(roses.fold)
print(roses.kurtosis)</pre>
```

12d

 L^2 inner product of probability densities

Description

 L^2 inner product of two multivariate (p > 1) or univariate (p = 1) probability densities, estimated from samples.

Usage

```
l2d(x1, x2, method = "gaussiand", check = FALSE, varw1 = NULL, varw2 = NULL)
```

Arguments

x1	a matrix or data frame of n_1 rows (observations) and p columns (variables) (can also be a tibble) or a vector of length n_1 .
x2	matrix or data frame (or tibble) of n_2 rows and p columns or vector of length n_2 .
method	string. It can be:
	• "gaussiand" if the densities are considered to be Gaussian.
	• "kern" if they are estimated using the Gaussian kernel method.
check	logical. When TRUE (the default is FALSE) the function checks if the covari- ance matrices (if method = "gaussiand") or smoothing bandwidth matrices (if method = "kern") are not degenerate, before computing the inner product.
	Notice that if $p = 1$, it checks if the variances or smoothing parameters are not zero.
varw1, varw2	$p \ge p$ symmetric matrices: the smoothing bandwidths for the estimation of the probability densities. If they are omitted, the smoothing bandwidths are computed using the normal reference rule matrix bandwidth (see details).

Details

- If method = "gaussiand", the mean vectors and the variance matrices (v1 and v2) of the two samples are computed, and they are used to compute the inner product using the l2dpar function.
- If method = "kern", the densities of both samples are estimated using the Gaussian kernel method. These estimations are then used to compute the inner product. if varw1 and varw2 arguments are omitted, the smoothing bandwidths are computed using the normal reference rule matrix bandwidth:

$$h_1 v_1^{1/2}$$

where

$$h_1 = (4/(n_1(p+2)))^{1/(p+4)}$$

for the first density. Idem for the second density after making the necessary changes.

Value

The L^2 inner product of the two probability densities.

Be careful! If check = FALSE and one smoothing bandwidth matrix is degenerate, the result returned can not be considered.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

12dpar

References

Boumaza, R., Yousfi, S., Demotes-Mainard, S. (2015). Interpreting the principal component analysis of multivariate density functions. Communications in Statistics - Theory and Methods, 44 (16), 3321-3339.

Wand, M., Jones, M. (1995). Kernel smoothing. Chapman and Hall/CRC, London.

Yousfi, S., Boumaza R., Aissani, D., Adjabi, S. (2014). Optimal bandwith matrices in functional principal component analysis of density functions. Journal of Statistical Computational and Simulation, 85 (11), 2315-2330.

See Also

12dpar for Gaussian densities whose parameters are given.

Examples

```
require(MASS)
m1 <- c(0,0)
v1 <- matrix(c(1,0,0,1),ncol = 2)
m2 <- c(0,1)
v2 <- matrix(c(4,1,1,9),ncol = 2)
x1 <- mvrnorm(n = 3,mu = m1,Sigma = v1)
x2 <- mvrnorm(n = 5, mu = m2, Sigma = v2)
l2d(x1, x2, method = "gaussiand")
l2d(x1, x2, method = "kern")
l2d(x1, x2, method = "kern", varw1 = v1, varw2 = v2)</pre>
```

12dpar

 L^2 inner product of Gaussian densities given their parameters

Description

 L^2 inner product of multivariate (p > 1) or univariate (p = 1) Gaussian densities, given their parameters (mean vectors and covariance matrices if the densities are multivariate, or means and variances if univariate).

Usage

```
l2dpar(mean1, var1, mean2, var2, check = FALSE)
```

Arguments

mean1	<i>p</i> -length numeric vector: the mean of the first Gaussian density.
var1	$p \ge p$ symmetric numeric matrix $(p > 1)$ or numeric $(p = 1)$: the covariance matrix $(p > 1)$ or the variance $(p = 1)$ of the first Gaussian density.
mean2	p-length numeric vector: the mean of the second Gaussian density.
var2	$p \ge p$ symmetric numeric matrix $(p > 1)$ or numeric $(p = 1)$: the covariance matrix $(p > 1)$ or the variance $(p = 1)$ of the second Gaussian density.

check logical. When TRUE (the default is FALSE) the function checks if the covariance matrices are not degenerate (multivariate case) or if the variances are not zero (univariate case).

Details

Computes the inner product of two Gaussian densities, equal to:

 $(2\pi)^{-p/2}det(var1+var2)^{-1/2}exp(-(1/2)t(mean1-mean2)(var1+var2)^{-1}(mean1-mean2))$

If p = 1 the means and variances are numbers, the formula is the same ignoring the following operators: t (transpose of a matrix or vector) and det (determinant of a square matrix).

Value

The L^2 inner product between two Gaussian densities.

Be careful! If check = FALSE and one covariance matrix is degenerated (multivariate case) or one variance is zero (univariate case), the result returned must not be considered.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

M. Wand and M. Jones (1995). Kernel Smoothing. Chapman and Hall, London.

See Also

12d for parametrically estimated Gaussian densities or nonparametrically estimated densities, given samples;

```
m1 <- c(1,1)
v1 <- matrix(c(4,1,1,9),ncol = 2)
m2 <- c(0,1)
v2 <- matrix(c(1,0,0,1),ncol = 2)
l2dpar(m1,v1,m2,v2)</pre>
```

matddchisqsym

Description

Computes the matrix of the symmetric Chi-squared distances between several multivariate or univariate discrete probability distributions, estimated from samples.

Usage

```
matddchisqsym(x)
```

Arguments

х

object of class "folder" containing the data. Its elements are data frames (one data frame per distribution) whose columns are factors.

Value

Positive symmetric matrix whose order is equal to the number of data frames (or distributions), consisting of the pairwise symmetric chi-squared distances between the distributions.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

References

Deza, M.M. and Deza E. (2013). Encyclopedia of distances. Springer.

See Also

ddchisqsym.

matddchisqsympar for discrete probability densities, given the probabilities on the same support.

matddchisqsympar

Matrix of distances between discrete probability densities given the probabilities on their common support

Description

Computes the matrix of the symmetric Chi-squared distances between several multivariate or univariate discrete probability distributions on the same support (which can be a Cartesian product of q sets), given the probabilities of the states (which are q-tuples) of the support.

Usage

```
matddchisqsympar(freq)
```

Arguments

freq

list of arrays. Their dim attribute is a vector with length q, its elements containing the numbers of levels of the *sets*. Each array contains the probabilities of the discrete distribution on the same support.

Value

Positive symmetric matrix whose order is equal to the number of distributions, consisting of the pairwise symmetric chi-squared distances between these distributions.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

References

Deza, M.M. and Deza E. (2013). Encyclopedia of distances. Springer.

See Also

ddchisqsympar.

matddchisqsym for discrete probability densities which are estimated from the data.

matddhellinger

Description

Computes the matrix of the Hellinger (or Matusita) distances between several multivariate or univariate discrete probability distributions, estimated from samples.

Usage

```
matddhellinger(x)
```

Arguments

х

object of class "folder" containing the data. Its elements are data frames (one data frame per distribution) whose columns are factors.

Value

Positive symmetric matrix whose order is equal to the number of data frames (or distributions), consisting of the pairwise Hellinger distances between the distributions.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

References

Deza, M.M. and Deza E. (2013). Encyclopedia of distances. Springer.

See Also

ddhellinger.

matddhellingerpar for discrete probability densities, given the probabilities on the same support.

matddhellingerpar Matrix of distances between discrete probability densities given the probabilities on their common support

Description

Computes the matrix of the Hellinger (or Matusita) distances between several multivariate or univariate discrete probability distributions on the same support (which can be a Cartesian product of q sets), given the probabilities of the states (which are q-tuples) of the support.

Usage

```
matddhellingerpar(freq)
```

Arguments

freq

list of arrays. Their dim attribute is a vector with length q, its elements containing the numbers of levels of the *sets*. Each array contains the probabilities of the discrete distribution on the same support.

Value

Positive symmetric matrix whose order is equal to the number of distributions, consisting of the pairwise Hellinger distances between these distributions.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

References

Deza, M.M. and Deza E. (2013). Encyclopedia of distances. Springer.

See Also

ddhellingerpar.

matddhellinger for discrete probability densities which are estimated from the data.

matddjeffreys

Description

Computes the matrix of Jeffreys divergences between several multivariate or univariate discrete probability distributions, estimated from samples.

Usage

```
matddjeffreys(x)
```

Arguments

х

object of class "folder" containing the data. Its elements are data frames (one data frame per distribution) whose columns are factors.

Value

Positive symmetric matrix whose order is equal to the number of data frames (or distributions), consisting of the pairwise Jeffreys divergences between the distributions.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

References

Deza, M.M. and Dezaz E. (2013). Encyclopedia of distances. Springer.

See Also

ddjeffreys.

matddjeffreyspar for discrete probability densities, given the probabilities on the same support.

matddjeffreyspar

Matrix of divergences between discrete probability densities given the probabilities on their common support

Description

Computes the matrix of Jeffreys divergences between several multivariate or univariate discrete probability distributions on the same support (which can be a Cartesian product of q sets), given the probabilities of the states (which are q-tuples) of the support.

Usage

```
matddjeffreyspar(freq)
```

Arguments

freq

list of arrays. Their dim attribute is a vector with length q, its elements containing the numbers of levels of the *sets*. Each array contains the probabilities of the discrete distribution on the same support.

Value

Positive symmetric matrix whose order is equal to the number of distributions, consisting of the pairwise Jeffreys divergences between these distributions.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

References

Deza, M.M. and Deza E. (2013). Encyclopedia of distances. Springer.

See Also

ddjeffreyspar.

matddjeffreys for discrete probability densities which are estimated from the data.

matddjensen

Description

Computes the matrix of the Jensen-Shannon divergences between several multivariate or univariate discrete probability distributions, estimated from samples.

Usage

```
matddjensen(x)
```

Arguments

х

object of class "folder" containing the data. Its elements are data frames (one data frame per distribution) whose columns are factors.

Value

Positive symmetric matrix whose order is equal to the number of data frames (or distributions), consisting of the pairwise Jensen-Shannon divergences between the distributions.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

References

Deza, M.M. and Deza E. (2013). Encyclopedia of distances. Springer.

See Also

ddjensen.

matddjensenpar for discrete probability densities, given the probabilities on the same support.

matddjensenpar

Matrix of divergences between discrete probability densities given the probabilities on their common support

Description

Computes the matrix of the Jensen-Shannon divergences between several multivariate or univariate discrete probability distributions on the same support (which can be a Cartesian product of q sets), given the probabilities of the states (which are q-tuples) of the support.

Usage

```
matddjensenpar(freq)
```

Arguments

freq

list of arrays. Their dim attribute is a vector with length q, its elements containing the numbers of levels of the *sets*. Each array contains the probabilities of the discrete distribution on the same support.

Value

Positive symmetric matrix whose order is equal to the number of densities, consisting of the pairwise Jensen-Shannon divergences between the discrete probability densities.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

References

Deza, M.M. and Deza E. (2013). Encyclopedia of distances. Springer.

See Also

ddjensenpar.

matddjensen for discrete probability densities which are estimated from the data.

matddlp

Description

Computes the matrix of the L^p distances between several multivariate or univariate discrete probability distributions, estimated from samples.

Usage

matddlp(x, p = 1)

Arguments

х	object of class "folder" containing the data. Its elements are data frames (one
	data frame per distribution) whose columns are factors.
р	integer. Parameter of the distance.

Value

Positive symmetric matrix whose order is equal to the number of data frames (or distributions), consisting of the pairwise L^p distances between the distributions.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

References

Deza, M.M. and Deza E. (2013). Encyclopedia of distances. Springer.

See Also

ddlp.

matddlppar for discrete probability distributions, given the probabilities on the same support.

```
# Example 1
x1 <- data.frame(x = factor(c("A", "A", "B", "B")))
x2 <- data.frame(x = factor(c("A", "A", "A", "B", "B")))
x3 <- data.frame(x = factor(c("A", "A", "B", "B", "B", "B")))
xf <- folder(x1, x2, x3)
matddlp(xf)
matddlp(xf, p = 2)
# Example 2</pre>
```

```
matddlppar
```

Matrix of distances between discrete probability densities given the probabilities on their common support

Description

Computes the matrix of the L^p distances between several multivariate or univariate discrete probability distributions on the same support (which can be a Cartesian product of q sets), given the probabilities of the states (which are q-tuples) of the support.

Usage

matddlppar(freq, p = 1)

Arguments

freq	list of arrays. Their dim attribute is a vector with length q , its elements contain-
	ing the numbers of levels of the sets. Each array contains the probabilities of
	the discrete distribution on the same support.
р	integer. Parameter of the distance.

Value

Positive symmetric matrix whose order is equal to the number of distributions, consisting of the pairwise L^p distances between these distributions.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

References

Deza, M.M. and Deza E. (2013). Encyclopedia of distances. Springer.

See Also

ddlppar.

matddlp for discrete probability distributions which are estimated from samples.

matdistl2d

Description

Computes the matrix of the L^2 distances between several multivariate (p > 1) or univariate (p = 1) probability densities, estimated from samples.

Usage

matdistl2d(x, method = "gaussiand", varwL = NULL)

Arguments

x	object of class "folder" containing the data. Its elements have only numeric variables (observations of the probability densities). If there are non numeric variables, there is an error.
method	string. It can be:
	 "gaussiand" if the densities are considered to be Gaussian. "kern" if they are estimated using the Gaussian kernel method.
varwL	list of matrices. The smoothing bandwidths for the estimation of each probabil- ity density. If they are omitted, the smoothing bandwidths are computed using the normal reference rule matrix bandwidth (see details of the 12d function).

Value

Positive symmetric matrix whose order is equal to the number of densities, consisting of the pairwise distances between the probability densities.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

distl2d.

matdistl2dpar when the probability densities are Gaussian, given the parameters (means and variances).

```
data(roses)
```

```
# Multivariate:
X <- as.folder(roses[,c("Sha","Den","Sym","rose")], groups = "rose")
summary(X)
mean.X <- mean(X)</pre>
```

```
var.X <- var.folder(X)</pre>
    # Parametrically estimated Gaussian densities:
    matdistl2d(X)
    ## Not run:
   # Estimated densities using the Gaussian kernel method ()normal reference rule bandwidth):
    matdistl2d(X, method = "kern")
    # Estimated densities using the Gaussian kernel method (bandwidth provided):
   matdistl2d(X, method = "kern", varwL = var.X)
## End(Not run)
    # Univariate :
    X1 <- as.folder(roses[,c("Sha", "rose")], groups = "rose")</pre>
    summary(X1)
   mean.X1 <- mean(X1)</pre>
    var.X1 <- var.folder(X1)</pre>
    # Parametrically estimated Gaussian densities:
    matdistl2d(X1)
  # Estimated densities using the Gaussian kernel method (normal reference rule bandwidth):
    matdistl2d(X1, method = "kern")
```

```
# Estimated densities using the Gaussian kernel method (normal reference rule bandwidth):
matdistl2d(X1, method = "kern", varwL = var.X1)
```

matdistl2dnorm $Matrix of L^2 distances between L^2-normed probability densities$

Description

Computes the matrix of the L^2 distances between several multivariate (p > 1) or univariate (p = 1) L^2 -normed probability densities, estimated from samples, where a L^2 -normed probability density is the original probability density function divided by its L^2 -norm.

Usage

```
matdistl2dnorm(x, method = "gaussiand", varwL = NULL)
```

Arguments

x	object of class "folder" containing the data. Its elements have only numeric variables (observations of the probability densities). If there are non numeric variables, there is an error.
method	string. It can be:
	• "gaussiand" if the densities are considered to be Gaussian.

	• "kern" if they are estimated using the Gaussian kernel method.
varwL	list of matrices. The smoothing bandwidths for the estimation of each probabil-
	ity density. If they are omitted, the smoothing bandwidths are computed using
	the normal reference rule matrix bandwidth (see details of the 12d function).

Value

Positive symmetric matrix whose order is equal to the number of densities, consisting of the pairwise distances between the L^2 -normed probability densities.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

distl2dnorm.

matdistl2d for the distance matrix between probability densities.

matdistl2dnormpar when the probability densities are Gaussian, given the parameters (means and variances).

Examples

data(roses)

```
# Multivariate:
X <- as.folder(roses[,c("Sha","Den","Sym","rose")], groups = "rose")
summary(X)
mean.X <- mean(X)
var.X <- var.folder(X)</pre>
```

Parametrically estimated Gaussian densities: matdistl2dnorm(X)

Not run: # Estimated densities using the Gaussian kernel method ()normal reference rule bandwidth): matdistl2dnorm(X, method = "kern")

Estimated densities using the Gaussian kernel method (bandwidth provided):
matdistl2dnorm(X, method = "kern", varwL = var.X)

```
## End(Not run)
```

```
# Univariate :
X1 <- as.folder(roses[,c("Sha","rose")], groups = "rose")
summary(X1)
mean.X1 <- mean(X1)
var.X1 <- var.folder(X1)</pre>
```

```
# Parametrically estimated Gaussian densities:
matdistl2dnorm(X1)
```

Estimated densities using the Gaussian kernel method (normal reference rule bandwidth):
 matdistl2dnorm(X1, method = "kern")

```
# Estimated densities using the Gaussian kernel method (normal reference rule bandwidth):
    matdistl2dnorm(X1, method = "kern", varwL = var.X1)
```

matdistl2dnormpar Matrix of L^2 distances between L^2 -normed Gaussian densities given their parameters

Description

Computes the matrix of the L^2 distances between several multivariate (p > 1) or univariate (p = 1) L^2 -normed Gaussian densities, given their parameters (mean vectors and covariance matrices if the densities are multivariate, or means and variances if univariate), where a L^2 -normed Gaussian density is the original probability density function divided by its L^2 -norm.

Usage

```
matdistl2dnormpar(meanL, varL)
```

Arguments

meanL	list of the means $(p = 1)$ or vector means $(p > 1)$ of the Gaussian densities.
varL	list of the variances $(p = 1)$ or covariance matrices $(p > 1)$ of the Gaussian densities.

Value

Positive symmetric matrix whose order is equal to the number of densities, consisting of the pairwise distances between the L^2 -normed probability densities.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

distl2dnormpar.

matdistl2dpar for the distance matrix between Gaussian densities, given their parameters.

matdistl2dnorm for the distance matrix between normed probability densities which are estimated from the data.

matdistl2dpar

Examples

data(roses)

```
# Multivariate:
X <- roses[,c("Sha","Den","Sym","rose")]
summary(X)
mean.X <- as.list(by(X[, 1:3], X$rose, colMeans))
var.X <- as.list(by(X[, 1:3], X$rose, var))
# Gaussian densities, given parameters
matdistl2dnormpar(mean.X, var.X)
# Univariate :
X1 <- roses[,c("Sha","rose")]
summary(X1)
mean.X1 <- by(X1$Sha, X1$rose, mean)
var.X1 <- by(X1$Sha, X1$rose, var)
# Gaussian densities, given parameters
matdistl2dnormpar(mean.X1, var.X1)
```

matdistl2dpar

Matrix of L^2 distances between Gaussian densities given their parameters

Description

Computes the matrix of the L^2 distances between several multivariate (p > 1) or univariate (p = 1) Gaussian densities, given their parameters (mean vectors and covariance matrices if the densities are multivariate, or means and variances if univariate).

Usage

```
matdistl2dpar(meanL, varL)
```

Arguments

meanL	list of the means $(p = 1)$ or vector means $(p > 1)$ of the Gaussian densities.
varL	list of the variances $(p = 1)$ or covariance matrices $(p > 1)$ of the Gaussian densities.

Value

Positive symmetric matrix whose order is equal to the number of densities, consisting of the pairwise distances between the probability densities.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

distl2dpar.

matdistl2d for the distance matrix between probability densities which are estimated from the data.

Examples

data(roses)

```
# Multivariate:
X <- roses[,c("Sha","Den","Sym","rose")]
summary(X)
mean.X <- as.list(by(X[, 1:3], X$rose, colMeans))
var.X <- as.list(by(X[, 1:3], X$rose, var))
# Gaussian densities, given parameters
matdistl2dpar(mean.X, var.X)
# Univariate :
X1 <- roses[,c("Sha","rose")]
summary(X1)
mean.X1 <- by(X1$Sha, X1$rose, mean)
var.X1 <- by(X1$Sha, X1$rose, var)
# Gaussian densities, given parameters
matdistl2dpar(mean.X1, var.X1)
```

mathellinger Matrix of Hellinger distances between Gaussian densities

Description

Computes the matrix of the Hellinger distances between several multivariate (p > 1) or univariate (p = 1) Gaussian densities given samples and using hellinger.

Usage

```
mathellinger(x)
```

Arguments

Х

object of class "folder" containing the data. Its elements have only numeric variables (observations of the probability densities). If there are non numeric variables, there is an error.

Value

Positive symmetric matrix whose order is equal to the number of densities, consisting of the pairwise Hellinger distances between the probability densities.

```
mathellingerpar
```

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

hellinger.

mathellingerpar when the probability densities are Gaussian, given the parameters (means and variances).

Examples

```
data(roses)
```

```
# Multivariate:
X <- as.folder(roses[,c("Sha","Den","Sym","rose")], groups = "rose")
summary(X)
mathellinger(X)
# Univariate :
X1 <- as.folder(roses[,c("Sha","rose")], groups = "rose")
summary(X1)
mathellinger(X1)
```

mathellingerpar	Matrix of Hellinger distances between Gaussian densities given their
	parameters

Description

Computes the matrix of the Hellinger distances between several multivariate (p > 1) or univariate (p = 1) Gaussian densities, given their means and variances, using hellingerpar.

Usage

```
mathellingerpar(meanL, varL)
```

Arguments

meanL	list of the means $(p = 1)$ or vector means $(p > 1)$ of the Gaussian densities.
varL	list of the variances $(p = 1)$ or covariance matrices $(p > 1)$ of the Gaussian densities.

Value

Positive symmetric matrix whose order is equal to the number of densities, consisting of the pairwise distances between the Gaussian densities.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

hellingerpar.

mathellinger for the distance matrix between probability densities which are estimated from the data.

Examples

data(roses)

```
# Multivariate:
X <- roses[,c("Sha","Den","Sym","rose")]
summary(X)
mean.X <- as.list(by(X[, 1:3], X$rose, colMeans))
var.X <- as.list(by(X[, 1:3], X$rose, var))
mathellingerpar(mean.X, var.X)
# Univariate :
```

```
X1 <- roses[,c("Sha","rose")]
summary(X1)
mean.X1 <- by(X1$Sha, X1$rose, mean)
var.X1 <- by(X1$Sha, X1$rose, var)
mathellingerpar(mean.X1, var.X1)</pre>
```

```
matipl2d
```

Matrix of L^2 inner products of probability densities

Description

Computes the matrix of the L^2 inner products between several multivariate (p > 1) or univariate (p = 1) probability densities, estimated from samples, using 12d.

Usage

```
matipl2d(x, method = "gaussiand", varwL = NULL)
```

Arguments

X	object of class "folder" containing the data. Its elements have only numeric variables (observations of the probability densities). If there are non numeric variables, there is an error.
method	string. It can be:
	• "gaussiand" if the densities are considered to be Gaussian.
	• "kern" if they are estimated using the Gaussian kernel method.

matipl2d

Value

Positive symmetric matrix whose order is equal to the number of densities, consisting of the pairwise inner products between the probability densities.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

12d.

matipl2dpar when the probability densities are Gaussian, given the parameters (means and variances).

Examples

data(roses)

```
# Multivariate:
 X <- as.folder(roses[,c("Sha", "Den", "Sym", "rose")], groups = "rose")</pre>
 summary(X)
 mean.X < - mean(X)
 var.X <- var.folder(X)</pre>
 # Parametrically estimated Gaussian densities:
matipl2d(X)
# Estimated densities using the Gaussian kernel method (normal reference rule bandwidth):
 matipl2d(X, method = "kern")
 # Estimated densities using the Gaussian kernel method (bandwidth provided):
matipl2d(X, method = "kern", varwL = var.X)
 # Univariate :
 X1 <- as.folder(roses[,c("Sha", "rose")], groups = "rose")</pre>
 summary(X1)
mean.X1 <- mean(X1)</pre>
 var.X1 <- var.folder(X1)</pre>
 # Parametrically estimated Gaussian densities:
 matipl2d(X1)
# Estimated densities using the Gaussian kernel method (normal reference rule bandwidth):
 matipl2d(X1, method = "kern")
```

```
# Estimated densities using the Gaussian kernel method (bandwidth provided):
matipl2d(X1, method = "kern", varwL = var.X1)
```

Description

Computes the matrix of the L^2 inner products between several multivariate (p > 1) or univariate (p = 1) Gaussian densities, given their parameters (mean vectors and covariance matrices if the densities are multivariate, or means and variances if univariate).

Usage

```
matipl2dpar(meanL, varL)
```

Arguments

meanL	list of the means $(p = 1)$ or vector means $(p > 1)$ of the Gaussian densities.
varL	list of the variances $(p = 1)$ or covariance matrices $(p > 1)$ of the Gaussian densities.

Value

Positive symmetric matrix whose order is equal to the number of densities, consisting of the pairwise inner products between the Gaussian densities.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

12dpar.

matipl2d for the distance matrix between probability densities which are estimated from the data.

```
data(roses)
```

```
# Multivariate:
X <- roses[,c("Sha","Den","Sym","rose")]
summary(X)
mean.X <- as.list(by(X[, 1:3], X$rose, colMeans))
var.X <- as.list(by(X[, 1:3], X$rose, var))
# Gaussian densities, given parameters
matipl2dpar(mean.X, var.X)
# Univariate :
X1 <- roses[,c("Sha","rose")]</pre>
```

matjeffreys

```
summary(X1)
mean.X1 <- by(X1$Sha, X1$rose, mean)
var.X1 <- by(X1$Sha, X1$rose, var)
# Gaussian densities, given parameters
matipl2dpar(mean.X1, var.X1)</pre>
```

```
matjeffreys
```

Matrix of the Jeffreys measures (symmetrised Kullback-Leibler divergences) between Gaussian densities

Description

Computes the matrix of Jeffreys measures between several multivariate (p > 1) or univariate (p = 1) Gaussian densities, given samples.

Usage

matjeffreys(x)

Arguments

```
х
```

object of class "folder" containing the data. Its elements have only numeric variables (observations of the probability densities). If there are non numeric variables, there is an error.

Value

Positive symmetric matrix whose order is equal to the number of densities, consisting of pairwise Jeffreys measures between the Gaussian densities.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

matjeffreyspar if the parameters of the Gaussian densities are known.

Examples

data(roses)

```
# Multivariate:
X <- as.folder(roses[,c("Sha","Den","Sym","rose")], groups = "rose")
summary(X)
matjeffreys(X)
# Univariate :
```

```
X1 <- as.folder(roses[,c("Sha","rose")], groups = "rose")
summary(X1)
matjeffreys(X1)</pre>
```

matjeffreyspar

Matrix of Jeffreys measures (symmetrised Kullback-Leibler divergences) between Gaussian densities

Description

Computes the matrix of Jeffreys measures between several multivariate (p > 1) or univariate (p = 1) Gaussian densities, given their parameters (mean vectors and covariance matrices if the densities are multivariate, or means and variances if univariate), using jeffreyspar.

Usage

```
matjeffreyspar(meanL, varL)
```

Arguments

meanL	list of the means $(p = 1)$ or vector means $(p > 1)$ of the Gaussian densities.
varL	list of the variances $(p = 1)$ or covariance matrices $(p > 1)$ of the probability
	densities.

Value

Positive symmetric matrix whose order is equal to the number of densities, consisting of pairwise Jeffreys measures between the Gaussian densities.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

jeffreyspar.

matjeffreys for the matrix of Jeffreys divergences between probability densities which are estimated from the data.

Examples

```
data(roses)
```

```
# Multivariate:
X <- roses[,c("Sha","Den","Sym","rose")]
summary(X)
mean.X <- as.list(by(X[, 1:3], X$rose, colMeans))
var.X <- as.list(by(X[, 1:3], X$rose, var))</pre>
```

matwasserstein

```
matjeffreyspar(mean.X, var.X)
# Univariate :
X1 <- roses[,c("Sha","rose")]
summary(X1)
mean.X1 <- by(X1$Sha, X1$rose, mean)
var.X1 <- by(X1$Sha, X1$rose, var)
matjeffreyspar(mean.X1, var.X1)</pre>
```

matwasserstein Matrix of 2-Wassterstein distance between Gaussian densities

Description

Computes the matrix of the 2-Wassterstein distances between several multivariate (p > 1) or univariate (p = 1) Gaussian densities, given samples.

Usage

matwasserstein(x)

Arguments

х

object of class "folder" containing the data. Its elements have only numeric variables (observations of the probability densities). If there are non numeric variables, there is an error.

Value

Positive symmetric matrix whose order is equal to the number of densities, consisting of the pairwise 2-Wassterstein distance between the Gaussian densities.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

matwassersteinpar if the parameters of the Gaussian densities are known.

```
data(roses)
```

```
# Multivariate:
X <- as.folder(roses[,c("Sha","Den","Sym","rose")], groups = "rose")
summary(X)
matwasserstein(X)
```

```
# Univariate :
X1 <- as.folder(roses[,c("Sha","rose")], groups = "rose")
summary(X1)
matwasserstein(X1)
```

matwassersteinpar Matrix of 2-Wasserstein distances between Gaussian densities

Description

Computes the matrix of the 2-Wasserstein distances between several multivariate (p > 1) or univariate (p = 1) Gaussian densities, given their parameters (mean vectors and covariance matrices if the densities are multivariate, or means and variances if univariate), using wassersteinpar.

Usage

```
matwassersteinpar(meanL, varL)
```

Arguments

meanL	list of the means $(p = 1)$ or vector means $(p > 1)$ of the Gaussian densities.
varL	list of the variances $(p = 1)$ or covariance matrices $(p > 1)$ of the probability densities.

Value

Positive symmetric matrix whose order is equal to the number of densities, consisting of the pairwise 2-Wasserstein distances between the Gaussian densities.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

wasserstein.

matwasserstein for the matrix of 2-Wasserstein distances between probability densities which are estimated from the data.

Examples

```
data(roses)
```

```
# Multivariate:
X <- roses[,c("Sha","Den","Sym","rose")]
summary(X)
mean.X <- as.list(by(X[, 1:3], X$rose, colMeans))
var.X <- as.list(by(X[, 1:3], X$rose, var))</pre>
```

mdsdd

```
matwassersteinpar(mean.X, var.X)
# Univariate :
X1 <- roses[,c("Sha","rose")]
summary(X1)
mean.X1 <- by(X1$Sha, X1$rose, mean)
var.X1 <- by(X1$Sha, X1$rose, var)
matwassersteinpar(mean.X1, var.X1)</pre>
```

```
\mathsf{mdsdd}
```

Multidimensional scaling of discrete probability distributions

Description

Applies the multidimensional scaling (MDS) method to discrete probability distributions in order to describe T groups of individuals on which are observed q categorical variables. It returns an object of class mdsdd. It applies cmdscale to the distance matrix between the T distributions.

Usage

```
mdsdd(xf, group.name = "group", distance = c("l1", "l2", "chisqsym", "hellinger",
  "jeffreys", "jensen", "lp"), nb.factors = 3, nb.values = 10, association = c("cramer",
    "tschuprow", "pearson", "phi"), sub.title = "", plot.eigen = TRUE,
    plot.score = FALSE, nscore = 1:3, filename = NULL, add = TRUE, p)
```

Arguments

xf

object of class folder, list of arrays (or tables) or data frame.

- If it is a folder, its elements are data frames with q columns (considered as factors). The t^{th} element (t = 1, ..., T) matches with the t^{th} group.
- If it is a data frame, the columns with name given by the group.name argument is a factor giving the groups. The other columns are all considered as factors.
- If it is a list of arrays (or tables), the t^{th} element (t = 1, ..., T) is the table of the joint frequency distribution of q variables within the t^{th} group. The frequency distribution is expressed with relative or absolute frequencies. These arrays have the same shape.

Each array (or table) xf[[i]] has:

- the same dimension(s). If q = 1 (univariate), dim(xf[[i]]) is an integer. If q > 1 (multivariate), dim(xf[[i]]) is an integer vector of length q.
- the same dimension names dimnames(xf[[i]]) (is non NULL). These dimnames are the names of the variables.

The elements of the arrays are non-negative numbers (if they are not, there is an error).

group.name string. Name of the grouping variable. Default: groupname = "group".

distance	The distance or divergence used to compute the distance matrix between the discrete distributions (see Details). It can be:
	• "11" (default) the L^p distance with $p = 1$
	• "12" the L^p distance with $p = 2$
	 "chisqsym" the symmetric Chi-squared distance
	• "hellinger" the Hellinger metric (Matusita distance)
	• "jeffreys" Jeffreys distance (symmetrised Kullback-Leibler divergence)
	 "jensen" the Jensen-Shannon distance
	• "lp" the L^p distance with p given by the argument p of the function.
nb.factors	numeric. Number of returned principal coordinates (default nb.factors = 3). This number must be less than $T - 1$.
	Warning: The plot.mdsdd and interpret.mdsdd functions cannot take into account more than nb.factors principal factors.
nb.values	numeric. Number of returned eigenvalues (default nb.values = 10).
association	The association measure between two discrete distributions to be used (see De- tails). It can be:
	• "cramer" (default) Cramer's V (see cramer.folder).
	• "tschuprow" Tschuprow's T (tschuprow.folder).
	 "pearson" Pearson's contingency coefficient (pearson.folder).
	• "phi" phi (phi.folder).
<pre>sub.title</pre>	string. Subtitle for the graphs (default NULL).
plot.eigen	logical. If TRUE (default), the barplot of the eigenvalues is plotted.
plot.score	logical. If TRUE, the graphs of new coordinates are plotted. A new graphic device is opened for each pair of coordinates defined by nscore argument.
nscore	numeric vector. If plot.score = TRUE, the numbers of the principal coordinates which are plotted. By default, nscore = 1:3. Its components cannot be greater than nb.factors.
filename	string. Name of the file in which the results are saved. By default (filename = NULL) they are not saved.
add	logical indicating if an additive constant should be computed and added to the non diagonal dissimilarities such that the modified dissimilarities are Euclidean (default TRUE; see add argument of cmdscale).
р	integer. Optional. When distance = "lp" (L^p distance with $p > 2$), p is the parameter of the distance.

Details

If a folder is given as argument, the T discrete probability distributions f_t corresponding to the T groups of individuals are estimated from observations. Then the distances/dissimilarities between the estimated distributions are computed, using the distance or divergence defined by the distance argument:

If the distance is "11", "12" or "1p", the distances are computed by the function matddlppar. Otherwise, it can be computed by matddchisqsympar ("chisqsym"), matddhellingerpar ("hellinger"), matddjeffreyspar ("jeffreys") or matddjensenpar ("jensen").

mdsdd

The association measures are computed accordingly to the value of the parameter associationThe computation uses the corresponding function of the package DescTools (see Assocs). Notice that an association measure between a constant variable with and other variable is set to zero. The association measure between each variable with itself is not computed and the diagonal of the returned association matrices is set to NA.

Value

Returns an object of class mdsdd, that is a list including:

inertia	data frame of the eigenvalues and the percentages of their sum.
scores	data frame of the coordinates along the nb.factors first principal coordinates.
jointp	list of arrays. The joint probability distribution for each group.
margins	list of two data frames giving respectively:
	 The probability distribution of each variable for each group. Each column of the data frame corresponds to one level of one categorical variable and contains the probabilities of this level in each group. The joint probability distribution of each pair of variables for each group. Each column of the data frame corresponds to one pair of levels of two categorical variables (one level per variable) and contains the probabilities of this pair of levels in each group.
associations	list of T matrices. Each matrix corresponds to a group and gives the pairwise association measures between the q categorical variables.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

References

Cox, T.F., Cox, M.A.A. (2001). Multidimensional Scaling, second ed. Chapman & Hall/CRC. Saporta, G. (2006). Probabilit\'es, Analyse des donn\'ees et Statistique. Editions Technip, Paris.

See Also

print.mdsdd, plot.mdsdd, interpret.mdsdd

```
# Example 1 with a folder (10 groups) of 3 factors
# obtained by converting numeric variables
data(roses)
xr = roses[,c("Sha", "Den", "Sym", "rose")]
xf = as.folder(xr, groups = "rose")
xf = cut(xf, breaks = list(c(0, 5, 7, 10), c(0, 4, 6, 10), c(0, 6, 8, 10)), cutcol = 1:3)
af = mdsdd(xf)
print(af)
print(af$
print(af$piointp)
print(af$margins[[1]]) # equivalent to print(af$margins$margin1)
```

```
print(af$margins[[2]])
print(af$associations)
# Example 2 with a data frame obtained by converting numeric variables
data(roses)
xr = roses[,c("Sha", "Den", "Sym", "rose")]
xr = cut(xr, breaks = list(c(0, 5, 7, 10), c(0, 4, 6, 10), c(0, 6, 8, 10)), cutcol = 1:3)
ar = mdsdd(xr, group.name = "rose")
print(ar)
print(ar$jointp)
print(ar$margins[[1]]) # equivalent to print(ar$margins$margin1)
print(ar$margins[[2]])
print(ar$associations)
# Example 3 with a list of 7 arrays
data(dspg)
x1 = dspg
mdsdd(x1)
```

```
mean.folder
```

Means of a folder of data sets

Description

Computes the means by column of the elements of an object of class folder.

Usage

S3 method for class 'folder'
mean(x, ..., na.rm = FALSE)

Arguments

x	an object of class folder that is a list of data frames with the same column names.
	further arguments passed to or from other methods.
na.rm	logical. Should missing values (including NaN) be omitted from the calcula- tions? (see mean or colMeans)

Details

It uses colMeans to compute the mean by numeric column of each element of the folder. If some columns of the data frames are not numeric, there is a warning, and the means are computed on the numeric columns only.

Value

A list whose elements are the mean by column of the elements of the folder.

mtgcomponents

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

folder to create an object of class folder. var.folder, cor.folder, skewness.folder, kurtosis.folder for other statistics for folder objects.

Examples

```
# First example: iris (Fisher)
data(iris)
iris.fold <- as.folder(iris, "Species")
iris.means <- mean(iris.fold)
print(iris.means)
# Second example: roses
data(roses)
roses.fold <- as.folder(roses, "rose")
roses.means <- mean(roses.fold)
print(roses.means)</pre>
```

mtgcomponents Components of upper scale of a vertex

Description

For a vertex in an object of class foldermtg, computes its decomposition into vertices of an upper scale.

Usage

```
mtgcomponents(x, vertex, scale)
```

Arguments

х	an object of class foldermtg.
vertex	character. The identifier of a vertex. These identifiers are the rownames of the data frame x\$topology.
scale	integer. The scale of the components of vertex which will be returned.

Details

If vertex is a vertex of scale i, then scale (the scale of the returned components of vertex) must be higher than i. For example, if vertex is a vertex of scale 2, then scale > 2, for instance scale = 3. The returned components are then vertices of scale 3 which have a decomposition relationship with vertex.

A character vector, containing the idendifiers of the components of vertex.

If there is no component, then the returned vector is empty.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Pradal, C., Godin, C. and Cokelaer, T. (2023). MTG user guide

See Also

read.mtg: reads a MTG file and builds an object of class foldermtg. mtgorder, mtgrank.

Examples

```
mtgfile <- system.file("extdata/plant1.mtg", package = "dad")
xmtg <- read.mtg(mtgfile)
# Vertex of class "P" (plant, of scale 1), components of class 2 (axes: "A")
mtgcomponents(xmtg, vertex = "v01", scale = 2)
# Vertex of class "P" (plant, of scale 1), components of class 3 ("0", "M" and "I")
mtgcomponents(xmtg, vertex = "v01", scale = 3)
# Vertex of class "A" (stem, of scale 2), components of class 3 ("0", "M" and "I")
mtgcomponents(xmtg, vertex = "v12", scale = 3)</pre>
```

mtgorder

Branching order of vertices

Description

Computes the branching order of vertices contained in an object of class foldermtg. The order of a vertex is the number of the column of topology, which contains this vertex.

Usage

mtgorder(x, classes = "all", display = FALSE)

mtgorder

Arguments

x	an object of class foldermtg.
classes	character vector. The classes of entities for which the branching order is com- puted. If omitted, the branching orders are computed for all entities.
display	logical. If TRUE, the data frames of x corresponding to classes are displayed. Default: FALSE.

Details

Returns x after appending the branching orders of the vertices of the classes given in the argument classes. The branching orders are appended to the data frames containing the vertices (one data frame per class) and the values of their corresponding features.

Value

Returns an object of class foldermtg, that is a list of data frames.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Pradal, C., Godin, C. and Cokelaer, T. (2023). MTG user guide

See Also

read.mtg: reads a MTG file and builds an object of class foldermtg.

mtgorder.

```
mtgfile <- system.file("extdata/plant1.mtg", package = "dad")
xmtg <- read.mtg(mtgfile)
# The branching orders
ymtg <- mtgorder(xmtg)
print(ymtg)</pre>
```

```
# Add the branching orders to the 'foldermtg'
zmtg <- mtgorder(xmtg, display = TRUE)
print(zmtg)</pre>
```

mtgplant1

Description

These data produced by the SAGAH team (Sciences Agronomiques Appliquées à l'Horticulture, now Research Institute on Horticulture and Seeds), provide the topological structure of a rosebush.

Usage

data("mtgplant1")

Format

This object of class foldermtg is a list of 10 data frames:

mtgplant1\$classes: data frame with 6 rows and 5 columns named SYMBOL (factor: the classes of the vertices), SCALE (integer: the scale at which they appear), DECOMPOSITION (factor), INDEXATION (factor) and DEFINITION (factor).

The vertex classes are:

- P: the whole plant (scale 1)
- A: the axes (scale 2)
- 0, M, I: the ..., metamers (phytomers) and inflorescences (scale 3)
- mtgplant1\$description: data frame with 8 rows and 4 columns (factors) named LEFT, RIGHT, RELTYPE and MAX.

mtgplant1\$features: data frame with 13 rows and 2 columns (factors) named NAME and TYPE.

mtgplant1\$topology: data frame with 88 rows and 4 columns:

- order1, order2 and order3 (factors): the codes of the vertices, as they are found in the MTG table of the MTG file. The column on which a code appears gives the branching order of the corresponding vertex.
- vertex (character): the same codes of vertices, on a single column.
- mtgplant1\$coordinates: data frame with 86 rows and 6 columns (numeric) named XX, YY and 22: cartesian coordinates of the vertices, and AA, BB and CC: an other coordinates system.
- mtgplant1\$P, mtgplant1\$A, mtgplant1\$M, mtgplant1\$I: data frames of the features on the vertices (all numeric).

Details

This object of class foldermtg can be built by reading the data in a MTG file (see examples).

References

Pradal, C., Godin, C. and Cokelaer, T. (2023). MTG user guide

mtgplant2

See Also

read.mtg: to read an MTG file and build an object of class MTG.

mtgplant2: an other example of such data.

Examples

```
data(mtgplant1)
print(mtgplant1)
```

```
# To read these data from a MTG file:
mtgfile1 <- system.file("extdata/plant1.mtg", package = "dad")
mtgplant1 <- read.mtg(mtgfile1)
print(mtgplant1)
```

mtgplant2 Class foldermtg

Description

These data provides the topology of a bushy plant.

Usage

data("mtgplant2")

Format

This object of class foldermtg is a list of 9 data frames:

mtgplant2\$classes: data frame with 6 rows and 5 columns named SYMBOL (factor: the classes of the vertices), SCALE (integer: the scale at which they appear), DECOMPOSITION (factor), INDEXATION (factor) and DEFINITION (factor).

The vertex classes are:

- P: the whole plant (scale 1)
- A: the axes (scale 2)
- F, I: the flower and internodes (scale 3)
- mtgplant2\$description: data frame with 4 rows and 4 columns (factors) named LEFT, RIGHT, RELTYPE and MAX.

mtgplant2\$features: data frame with 9 rows and 2 columns (factors) named NAME and TYPE. mtgplant2\$topology: data frame with 14 rows and 3 columns:

- order1 and order2 (factors): the codes of the vertices, as they are found in the MTG table of the MTG file. The column on which a code appears gives the branching order of the corresponding vertex.
- vertex (character): the same codes of vertices, on a single column.
- mtgplant2\$coordinates: data frame with 0 rows and 0 columns (there are no spatial coordinates in these MTG data).
- mtgplant2\$P, mtgplant2\$A, mtgplant2\$F and mtgplant2\$I: data frames of the features on the vertices (all numeric).

Details

This object of class foldermtg can be built by reading the data in a MTG file (see examples).

References

Pradal, C., Godin, C. and Cokelaer, T. (2023). MTG user guide

See Also

read.mtg: to read an MTG file and build an object of class MTG.

mtgplant1: an other example of such data.

Examples

```
data(mtgplant2)
print(mtgplant2)
```

```
# To read these data from a MTG file:
mtgfile2 <- system.file("extdata/plant2.mtg", package = "dad")
mtgplant2 <- read.mtg(mtgfile2)
print(mtgplant2)
```

mtgrank

Ranks of vertices in a decomposition

Description

Computes the rank of the vertices contained in an object of class foldermtg. The vertex sequences resulting from a decomposition of other vertices, the rank of the vertices making up the sequences are computed from the beginning of the sequence or from its end. These ranks can be absolute or relative.

For example: ranks of the phytomeres and inflorescences in each stem.

Usage

```
mtgrank(x, classe, parent.class = NULL, sibling.classes = NULL,
relative = FALSE, from = c("origin", "end"), rank.name = "Rank",
display = FALSE)
```

Arguments

х	an object of class foldermtg.
classe	character. The class of the vertices for which the ranks are computed.
parent.class	character. The class of the parent entities of those for which the ranks are computed. If omitted, the entities of scale maxscal -1 , where maxscal is the highest scale in x data.

mtgrank

sibling.classes		
	character vector. The classes of vertices appearing at the same scale as classe, which are used in the computing of the ranks.	
	If omitted, only the vertices of class classe are used to compute the ranks.	
relative	logical. If TRUE, the relative ranks are computed, i.e. ranks from 0 to 1. Default: FALSE.	
from	character. It can be "origin" (default) or "end".	
	If from = "origin", the ranks are computed from the origin to the end, i.e. from 1 to its maximum (from 0 to 1 if relative = TRUE). If from = "end", they are computed from the end to the origin, i.e. from the maximum to 1 (from 1 to 0 if relative = TRUE).	
rank.name	character. Name of the rank column that is appended to x[[classe]]. The default is "Rank".	
display	logical. If TRUE, the data frames of ${\sf x}$ corresponding to classes are displayed. Default: FALSE.	

Details

If the branching orders of the entities given by classe, parent.class and, if relevant, sibling.classes are not contained in x, mtgrank() uses mtgorder to compute them. The ranks are appended to the data frames containing the vertices (one data frame per class) and the values of their corresponding features.

Value

Returns an object of class foldermtg, that is a list of data frames.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Pradal, C., Godin, C. and Cokelaer, T. (2023). MTG user guide

See Also

read.mtg: reads a MTG file and builds an object of class foldermtg. mtgorder.

```
mtgfile <- system.file("extdata/plant1.mtg", package = "dad")
xmtg <- read.mtg(mtgfile)
ymtg <- mtgrank(xmtg, "M")
print(ymtg)
mtgrank(xmtg, "M", display = TRUE)</pre>
```

```
mtgrank(xmtg, "M", parent.class = "A", display = TRUE)
mtgrank(xmtg, "M", parent.class = "A", sibling.classes = c("0", "I"), display = TRUE)
mtgrank(xmtg, "M", relative = TRUE, display = TRUE)
mtgrank(xmtg, "M", from = "origin", display = TRUE)
mtgrank(xmtg, "M", from = "end", display = TRUE)
```

plot.dstatis

	Pl	otting scores	s of STATIS	S method	(interstructure) analysi	is
--	----	---------------	-------------	----------	-----------------	-----------	----

Description

Applies to an object of class "dstatis" (see details of the dstatis.inter function). Plots the scores.

Usage

S3 method for class 'dstatis'
plot(x, nscore = c(1, 2), sub.title = NULL, color = NULL, fontsize.points = 1.5, ...)

Arguments

х	object of class "dstatis" (returned by dstatis.inter).
nscore	a length 2 numeric vector. The numbers of the score vectors to be plotted.
	Warning: Its components cannot be greater than the nb.factors argument in the call of the dstatis.inter function.
<pre>sub.title</pre>	string. Subtitle to be added to each graph.
color	When provided, the colour of the symbols of each group. Can be a vector with length equal to the number of groups.
fontsize.points	
	Numeric. Expansion of the characters (or symbols) of the groups on the graph. This works as a multiple of par("cex") (see points).
	optional arguments to plot methods.

Details

Plots the principal scores returned by the dstatis.inter function. A new graphics window is opened for each pair of principal axes defined by the nscore argument.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Lavit, C., Escoufier, Y., Sabatier, R., Traissac, P. (1994). The ACT (STATIS method). Computational Statistics & Data Analysis, 18 (1994), 97-119.

plot.fhclustd

See Also

dstatis.inter; print.dstatis; interpret.dstatis.

Examples

```
data(roses)
rosesf <- as.folder(roses[,c("Sha","Den","Sym","rose")])</pre>
```

```
# Dual STATIS on the covariance matrices
result <- dstatis.inter(rosesf, data.scaled = FALSE, group.name = "rose")
plot(result)</pre>
```

plot.fhclustd *Plotting a hierarchical clustering*

Description

Applies to an object of class fhclustd (see details of the fhclustd function). Plots the dendogram.

Usage

Arguments

Х	object of class fhclustd (returned by fhclustd).
labels, hang, ch	eck, axes, frame.plot, ann, main, sub, xlab, ylab
	Arguments concerning the graphical representation of the dendogram. See plot.hclust.
	Further graphical arguments.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

fhclustd; print.fhclustd.

Examples

```
data(castles.dated)
xf <- as.folder(castles.dated$stones)
## Not run:
result <- fhclustd(xf)
plot(result)
plot(result, hang = -1)</pre>
```

End(Not run)

plot.fmdsd

Plotting scores of multidimensional scaling of density functions

Description

Applies to an object of class "fmdsd" (see the details section of the fmdsd function). Plots the scores.

Usage

```
## S3 method for class 'fmdsd'
plot(x, nscore = c(1, 2), main="MDS of probability density functions",
        sub.title = NULL, color = NULL, fontsize.points = 1.5, ...)
```

Arguments

х	object of class "fmdsd".	
nscore	a length 2 numeric vector. The numbers of the score vectors to be plotted.	
	Warning: Its components cannot be greater than the nb.factors argument in the call of the fmdsd function.	
main	this argument to title has an useful default here.	
<pre>sub.title</pre>	string. Subtitle to be added to each graph.	
color	When provided, the colour of the symbols of each group. Can be a vector with length equal to the number of groups.	
fontsize.point	points	
	Numeric. Expansion of the characters (or symbols) of the groups on the graph.	
	This works as a multiple of par("cex") (see points).	
	optional arguments to plot methods.	

Details

Plots the principal scores returned by the function fmdsd. A new graphics window is opened for each pair of principal score vectors defined by the nscore argument.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

plot.foldert

References

Boumaza, R., Yousfi, S., Demotes-Mainard, S. (2015). Interpreting the principal component analysis of multivariate density functions. Communications in Statistics - Theory and Methods, 44 (16), 3321-3339.

See Also

fmdsd; print.fmdsd; interpret.fmdsd.

Examples

```
data(roses)
x <- roses[,c("Sha","Den","Sym","rose")]
rosesfold <- as.folder(x)
result <- fmdsd(rosesfold)
plot(result)</pre>
```

plot.foldert

Plotting data of a foldert

Description

Applies to an object of class foldert (called foldert below) that is a list. Plots the longitudinal evolution of a numeric variable for every individuals.

Usage

Arguments

x	object of class foldert that is a list of data frames with the same column names, each of them corresponding to a time of observation.
which	character. Name of a column of the data frames of x. It gives the name of the variable to be plotted.
	For each element x[[k]] of x, x[[k]] must be numeric. Otherwise, there is an error
na.inter	logical. If TRUE (default), for each individual, the missing values are deleted before plotting its evolution. If FALSE, the line corresponding to each individual is interrupted if there is a missing value, as for matplot.
type	character string (length 1 vector) or vector of 1-character strings (default "1") indicating the type of plot for each of the individuals followed among time, that is for each line of the data frames in the foldert. For further information about this argument, see matplot.

plot.fpcad

ylim	ranges of y axis. xlim is as in matplot. See details.
ylab	a label for the y axis. Default: the name of the plotted variable (which argument).
main	an overall title for the plot: see title.
	optional arguments to plot methods.

Details

Internally, plot.foldert builds a matrix mdata containing the data of the variable given by which argument. The element mdata[ind, t] of this matrix is the value of the variable which for the individual ind: x[[t]][ind, which].

If the ylim argument is omitted, the range of y axis is given by range(mdata, na.rm = TRUE)*c(0, 1.2).

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Boumaza, R., Yousfi, S., Demotes-Mainard, S. (2015). Interpreting the principal component analysis of multivariate density functions. Communications in Statistics - Theory and Methods, 44 (16), 3321-3339.

See Also

foldert: object of class foldert. as.foldert.data.frame: build an object of class foldert from a data frame. as.foldert.array: build an object of class foldert from a 3*d*-array.

Examples

plot.fpcad

Plotting scores of principal component analysis of density functions

Description

Applies to an object of class "fpcad" (see details of the fpcad function). Plots the scores.

Usage

```
## S3 method for class 'fpcad'
plot(x, nscore = c(1, 2), main = "PCA of probability density functions",
    sub.title = NULL, color = NULL, fontsize.points = 1.5, ...)
```

plot.fpcad

Arguments

x	object of class "fpcad" (returned by fpcad).	
nscore	a length 2 numeric vector. The numbers of the score vectors to be plotted.	
	Warning: Its components cannot be greater than the nb.factors argument in the call of the fpcad function.	
main	this argument to title has an useful default here.	
<pre>sub.title</pre>	string. Subtitle to be added to each graph.	
color	When provided, the colour of the symbols of each group. Can be a vector with length equal to the number of groups.	
fontsize.points		
	Numeric. Expansion of the characters (or symbols) of the groups on the graph. This works as a multiple of par("cex") (see points).	
	optional arguments to plot methods.	

Details

Plots the principal scores returned by the fpcad function. A new graphics window is opened for each pair of principal axes defined by the nscore argument.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Boumaza, R., Yousfi, S., Demotes-Mainard, S. (2015). Interpreting the principal component analysis of multivariate density functions. Communications in Statistics - Theory and Methods, 44 (16), 3321-3339.

See Also

fpcad; print.fpcad; interpret.fpcad.

```
data(roses)
rosefold <- as.folder(roses[,c("Sha","Den","Sym","rose")])
result <- fpcad(rosefold)
plot(result)</pre>
```

plot.fpcat

Description

Applies to an object of class "fpcat" (see details of the fpcat function). Plots the scores.

Usage

```
## S3 method for class 'fpcat'
plot(x, nscore=c(1, 2), main = "PCA of probability density functions",
    sub.title = NULL, ...)
```

Arguments

х	object of class "fpcat" (returned by fpcat).
nscore	numeric or length 2 numeric vector. If it is a length 2 numeric vector (default), it contains the numbers of the score vectors to be plotted. If it is a single value, it is the number of the score which is plotted among time.
	Warning: The components of nscore cannot be greater than the nb.factors argument in the call of the fpcat function.
main	this argument to title has an useful default here.
<pre>sub.title</pre>	string. Subtitle to be added to each graph.
	optional arguments to plot methods.

Details

Plots:

- if nscore is a length 2 vector (default): the principal scores returned by the fpcat function with arrows from the point corresponding to each time to the next one.
- if nscore is a single value, the principal scores among time with arrows from each time to the next one.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Boumaza, R., Yousfi, S., Demotes-Mainard, S. (2015). Interpreting the principal component analysis of multivariate density functions. Communications in Statistics - Theory and Methods, 44 (16), 3321-3339.

plot.hclustdd

See Also

fpcat; print.fpcat

Examples

```
times <- as.Date(c("2017-03-01", "2017-04-01", "2017-05-01", "2017-06-01"))
x1 <- data.frame(z1=rnorm(6,1,5), z2=rnorm(6,3,3))
x2 <- data.frame(z1=rnorm(6,4,6), z2=rnorm(6,5,2))
x3 <- data.frame(z1=rnorm(6,7,2), z2=rnorm(6,10,2))
ft <- foldert(x1, x2, x3, x4, times = times, rows.select="intersect")
print(ft)
result <- fpcat(ft)
plot(result)
plot(result, nscore = c(1, 2))
plot(result, nscore = 1)
plot(result)</pre>
```

plot.hclustdd

Plotting a hierarchical clustering of discrete distributions

Description

Applies to an object of class hclustdd (see details of the hclustdd function). Plots the dendogram.

Usage

Arguments

object of class hclustdd (returned by hclustdd).	х	
labels, hang, check, axes, frame.plot, ann, main, sub, xlab, ylab		
Arguments concerning the graphical representation of the dendogram. See plot.hclust.		
Further graphical arguments.		

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

hclustdd; print.hclustdd.

Examples

```
data(dspg)
xl = dspg
result <- hclustdd(xl)
plot(result)
plot(result, hang = -1)</pre>
```

plot.mdsdd	Plotting scores of multidimensional scaling analysis of discrete distri-
	butions

Description

Applies to an object of class "mdsdd" (see the details section of the mdsdd function). Plots the scores.

Usage

```
## S3 method for class 'mdsdd'
plot(x, nscore = c(1, 2), main="MDS of probability density functions",
    sub.title = NULL, color = NULL, fontsize.points = 1.5, ...)
```

Arguments

х	object of class "mdsdd".	
nscore	a length 2 numeric vector. The numbers of the score vectors to be plotted.	
	Warning: Its components cannot be greater than the nb.factors argument in the call of the fmdsd function.	
main	this argument to title has an useful default here.	
<pre>sub.title</pre>	string. Subtitle to be added to each graph.	
color	When provided, the colour of the symbols of each group. Can be a vector with length equal to the number of groups.	
fontsize.points		
	Numeric. Expansion of the characters (or symbols) of the groups on the graph. This works as a multiple of par("cex") (see points).	
	optional arguments to plot methods.	

Details

Plots the principal scores returned by the function mdsdd. A new graphics window is opened for each pair of principal score vectors defined by the nscore argument.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

plotframes

See Also

mdsdd; print.mdsdd; interpret.mdsdd.

Examples

```
# INSEE (France): Diploma x Socio professional group, seven years.
data(dspg)
xlista = dspg
a <- mdsdd(xlista)
plot(a)
```

plotframes

Plotting of two sets of variables

Description

Plots a set of numeric variables vs. another set and prints the pairwise correlations. It uses the ggplot2 package.

Usage

plotframes(x, y, xlab = NULL, ylab = NULL, font.size = 12, layout = NULL)

Arguments

х	data frame (can also be a tibble). Variables on x coordinates.
У	data frame (or tibble). Variables on y coordinates.
xlab	a label for the x axis, by default the column names of y.
ylab	a label for the y axis (by default there is no label).
font.size	integer. Size of the characters in the strips.
layout	numeric vector of length 2 or 3 giving the number of columns, rows, and option- ally pages of the lattice. If omitted, the graphs will be displayed on 3 lines and 3 columns, with a number of pages set to the required number.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

```
require(MASS)
mx <- c(0,0)
vx <- matrix(c(1,0,0,1),ncol = 2)
my <- c(0,1)
vy <- matrix(c(4,1,1,9),ncol = 2)
x <- as.data.frame(mvrnorm(n = 10, mu = mx, Sigma = vx))
y <- as.data.frame(mvrnorm(n = 10, mu = my, Sigma = vy))</pre>
```

colnames(x) <- c("x1", "x2")
colnames(y) <- c("y1", "y2")
plotframes(x, y)</pre>

print.discdd.misclass Printing results of discriminant analysis of discrete probability distributions

Description

Applies to an object of class "discdd.misclass". Prints the numerical results of discdd.misclass.

Usage

S3 method for class 'discdd.misclass'
print(x, dist.print=FALSE, prox.print=FALSE, digits=2, ...)

Arguments

x	object of class "discdd.misclass", returned by discdd.misclass.
dist.print	logical. Its default value is FALSE. If TRUE, prints the matrix of distances be- tween, on one side, the groups (densities) and, on the other side, the classes (of groups or densities).
prox.print	logical. Its default value is FALSE. If TRUE, prints the matrix of proximity indices (in percent))between, on one side, the groups (densities) and, on the other side, the classes (of groups or densities).
digits	numeric. Number of significant digits for the display of numerical results.
	optional arguments to print methods.

Details

By default, are printed the whole misallocation ratio, the confusion matrix (allocations versus origins) with the misallocation ratios per class, and the data frame whose rows are the groups, and whose columns are the origin classes and allocation classes, and a logical variable indicating misclassification.

If dist.print = TRUE or prox.print = TRUE, the distances or proximity indices (in percent) between groups and classes, are displayed.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

discdd.misclass; print.

print.discdd.predict

Examples

```
data("castles.dated")
stones <- castles.dated$stones
periods <- castles.dated$periods
stones$height <- cut(stones$height, breaks = c(19, 27, 40, 71), include.lowest = TRUE)
stones$width <- cut(stones$width, breaks = c(24, 45, 62, 144), include.lowest = TRUE)
stones$edging <- cut(stones$edging, breaks = c(0, 3, 4, 8), include.lowest = TRUE)
stones$boss <- cut(stones$boss, breaks = c(0, 6, 9, 20), include.lowest = TRUE )
castlefh <- folderh(periods, "castle", stones)
res <- discdd.misclass(castlefh, "period")
print(res)</pre>
```

print.discdd.predict Printing results of discriminant analysis of discrete probability distributions

Description

print function, applied to an object of class "discdd.predict", prints numerical results of discdd.predict.

Usage

```
## S3 method for class 'discdd.predict'
print(x, dist.print=TRUE, prox.print=FALSE, digits=2, ...)
```

Arguments

x	object of class "discdd.predict", returned by discdd.predict.
dist.print	logical. If TRUE (the default), prints the matrix of distances between, on one side, the groups (densities) and, on the other side, the classes (of groups or densities).
prox.print	logical. Its default value is FALSE. If TRUE, prints the matrix of proximity indices between, on one side, the groups (densities) and, on the other side, the classes (of groups or densities).
digits	numerical. Number of significant digits for the display of numerical results.
	optional arguments to print methods.

Details

By default, are printed:

• if available (if misclass.ratio argument of discdd.predict was TRUE), the whole misallocation ratio, the confusion matrix (allocations versus origins) and the misallocation ratio per class are printed. • the data frame the rows of which are the groups, and the columns of which are of the origin (NA if not available) and allocation classes.

If dist.print = TRUE or prox.print = TRUE, the distances or proximity indices between groups and classes, are displayed.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

discdd.predict; print.

Examples

```
data(castles.dated)
data(castles.nondated)
stones <- rbind(castles.dated$stones, castles.nondated$stones)
periods <- rbind(castles.dated$periods, castles.nondated$periods)
stones$height <- cut(stones$height, breaks = c(19, 27, 40, 71), include.lowest = TRUE)
stones$width <- cut(stones$width, breaks = c(24, 45, 62, 144), include.lowest = TRUE)
stones$edging <- cut(stones$edging, breaks = c(0, 3, 4, 8), include.lowest = TRUE)
stones$boss <- cut(stones$boss, breaks = c(0, 6, 9, 20), include.lowest = TRUE )
castlesfh <- folderh(periods, "castle", stones)
result <- discdd.predict(castlesfh, "period")
print(result)
print(result, prox.print=TRUE)</pre>
```

print.dstatis Printing results of STATIS method (interstructure) analysis

Description

Applies to an object of class "dstatis". Prints the numeric results returned by the dstatis.inter function.

Usage

```
## S3 method for class 'dstatis'
print(x, mean.print = FALSE, var.print = FALSE,
    cor.print = FALSE, skewness.print = FALSE, kurtosis.print = FALSE,
    digits = 2, ...)
```

print.dstatis

Arguments

x	object of class "dstatis", returned by the dstatis.inter function.
mean.print	logical. If TRUE, prints for each group the means and standard deviations of the variables and the norm of the density.
var.print	logical. If TRUE, prints for each group the variances and covariances of the variables.
cor.print	logical. If TRUE, prints for each group the correlations between the variables.
skewness.print	logical. If TRUE, prints for each group the skewness coefficients of the variables.
kurtosis.print	logical. If TRUE, prints for each group the kurtosis coefficients of the variables.
digits	numeric. Number of significant digits for the display of numeric results.
	optional arguments to print methods.

Details

By default, are printed the inertia explained by the nb.values (see dstatis.inter) first principal components, the contributions, the qualities of representation of the densities along the nb.factors (see dstatis.inter) first principal components, and the principal scores.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Lavit, C., Escoufier, Y., Sabatier, R., Traissac, P. (1994). The ACT (STATIS method). Computational Statistics & Data Analysis, 18 (1994), 97-119.

See Also

dstatis.inter; plot.dstatis; interpret.dstatis; print.dstatis.

```
data(roses)
rosesf <- as.folder(roses[,c("Sha","Den","Sym","rose")])
# Dual STATIS on the covariance matrices
result <- dstatis.inter(rosesf, data.scaled = FALSE, group.name = "rose")
print(result)</pre>
```

print.fdiscd.misclass Printing results of discriminant analysis of probability density functions

Description

Applies to an object of class "fdiscd.misclass". Prints the numerical results of fdiscd.misclass.

Usage

```
## S3 method for class 'fdiscd.misclass'
print(x, dist.print=FALSE, prox.print=FALSE, digits=2, ...)
```

Arguments

х	object of class "fdiscd.misclass", returned by fdiscd.misclass.
dist.print	logical. Its default value is FALSE. If TRUE, prints the matrix of distances be- tween, on one side, the groups (densities) and, on the other side, the classes (of groups or densities).
prox.print	logical. Its default value is FALSE. If TRUE, prints the matrix of proximity indices (in percent))between, on one side, the groups (densities) and, on the other side, the classes (of groups or densities).
digits	numeric. Number of significant digits for the display of numerical results.
	optional arguments to print methods.

Details

By default, are printed the whole misallocation ratio, the confusion matrix (allocations versus origins) with the misallocation ratios per class, and the data frame whose rows are the groups, and whose columns are the origin classes and allocation classes, and a logical variable indicating misclassification.

If dist.print = TRUE or prox.print = TRUE, the distances or proximity indices (in percent) between groups and classes, are displayed.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Boumaza, R. (2004). Discriminant analysis with independently repeated multivariate measurements: an L^2 approach. Computational Statistics & Data Analysis, 47, 823-843.

Rudrauf, J.M., Boumaza, R. (2001). Contribution à l'étude de l'architecture médiévale: les caractéristiques des pierres à bossage des châteaux forts alsaciens, Centre de Recherches Archéologiques Médiévales de Saverne, 5, 5-38.

print.fdiscd.predict

See Also

fdiscd.misclass; print.

Examples

```
data(castles.dated)
castlesfh <- folderh(castles.dated$periods, "castle", castles.dated$stones)
result <- fdiscd.misclass(castlesfh, "period")
print(result)
print(result, dist.print=TRUE)
print(result, prox.print=TRUE)</pre>
```

print.fdiscd.predict Printing results of discriminant analysis of probability density functions

Description

print function, applied to an object of class "fdiscd.predict", prints numerical results of fdiscd.predict .

Usage

```
## S3 method for class 'fdiscd.predict'
print(x, dist.print=TRUE, prox.print=FALSE, digits=2, ...)
```

Arguments

х	object of class "fdiscd.predict", returned by fdiscd.predict.
dist.print	logical. If TRUE (the default), prints the matrix of distances between, on one side, the groups (densities) and, on the other side, the classes (of groups or densities).
prox.print	logical. Its default value is FALSE. If TRUE, prints the matrix of proximity indices between, on one side, the groups (densities) and, on the other side, the classes (of groups or densities).
digits	numerical. Number of significant digits for the display of numerical results.
	optional arguments to print methods.

Details

By default, are printed:

- if available (if misclass.ratio argument of fdiscd.predict was TRUE), the whole misallocation ratio, the confusion matrix (allocations versus origins) and the misallocation ratio per class are printed.
- the data frame the rows of which are the groups, and the columns of which are of the origin (NA if not available) and allocation classes.

If dist.print = TRUE or prox.print = TRUE, the distances or proximity indices between groups and classes, are displayed.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Boumaza, R. (2004). Discriminant analysis with independently repeated multivariate measurements: an L^2 approach. Computational Statistics & Data Analysis, 47, 823-843.

Rudrauf, J.M., Boumaza, R. (2001). Contribution à l'étude de l'architecture médiévale: les caractéristiques des pierres à bossage des châteaux forts alsaciens, Centre de Recherches Archéologiques médiévales de Saverne, 5, 5-38.

See Also

fdiscd.predict; print.

Examples

```
data(castles.dated)
data(castles.nondated)
castles.stones <- rbind(castles.dated$stones, castles.nondated$stones)
castles.periods <- rbind(castles.dated$periods, castles.nondated$periods)
castlesfh <- folderh(castles.periods, "castle", castles.stones)
result <- fdiscd.predict(castlesfh, "period")
print(result)
print(result, prox.print=TRUE)</pre>
```

print.fhclustd	Printing results of a hierarchical clustering of probability density func-
	tions

Description

print function, applied to an object of class "fhclustd", prints numerical results of fhclustd .

Usage

```
## S3 method for class 'fhclustd'
print(x, dist.print=FALSE, digits=2, ...)
```

Arguments

х	object of class "fhclustd", returned by fhclustd.
dist.print	logical. If TRUE (default: FALSE), prints the matrix of distances between the groups (densities).
digits	numerical. Number of significant digits for the display of numerical results.
	optional arguments to print methods.

print.fmdsd

Details

If dist.print = TRUE, the distances between groups are displayed.

By default, the result of the clustering is printed. The display is the same as that of the print.hclust function.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

fhclustd; print.

Examples

```
data(castles.dated)
xf <- as.folder(castles.dated$stones)
## Not run:
result <- fhclustd(xf)
print(result)
print(result, dist.print = TRUE)</pre>
```

End(Not run)

print.fmdsd	Printing results of a multidimensional scaling analysis of probability
	densities

Description

Applies to an object of class "fmdsd". Prints the numeric results returned by the fmdsd function.

Usage

```
## S3 method for class 'fmdsd'
print(x, mean.print = FALSE, var.print = FALSE,
    cor.print = FALSE, skewness.print = FALSE, kurtosis.print = FALSE,
    digits = 2, ...)
```

Arguments

x	object of class "fmdsd", returned by the fmdsd function.
mean.print	logical. If TRUE, prints for each group the means and standard deviations of the variables and the norm of the density.
var.print	logical. If TRUE, prints for each group the variances and covariances of the variables.
cor.print	logical. If TRUE, prints for each group the correlations between the variables.

skewness.print	logical. If TRUE, prints for each group the skewness coefficients of the variables.
kurtosis.print	logical. If TRUE, prints for each group the kurtosis coefficients of the variables.
digits	numeric. Number of significant digits for the display of numeric results.
	optional arguments to print methods.

Details

By default, are printed the inertia explained by the nb.values (see fmdsd) first coordinates and the nb.factors (see fmdsd) coordinates of the densities.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Boumaza, R., Yousfi, S., Demotes-Mainard, S. (2015). Interpreting the principal component analysis of multivariate density functions. Communications in Statistics - Theory and Methods, 44 (16), 3321-3339.

See Also

fmdsd; plot.fmdsd; interpret.fmdsd; print.

Examples

```
data(roses)
x <- roses[,c("Sha","Den","Sym","rose")]
rosesfold <- as.folder(x)
result <- fmdsd(rosesfold)
print(result)
print(result, mean.print = TRUE)</pre>
```

print.foldermtg Printing an object of class foldermtg

Description

print function, applied to an object of class "foldermtg", prints an MTG (Multiscale Tree Graph) folder, as returned by foldermtg function.

Usage

```
## S3 method for class 'foldermtg'
print(x, classes = TRUE, description = FALSE, features = TRUE,
    topology = FALSE, coordinates = FALSE, ...)
```

print.foldermtg

Arguments

x	an object of class foldermtg.
classes	logical. If TRUE (default), prints the data frame describing the classes (CLASSES: table in the MTG file).
description	logical. If TRUE (default: FALSE), prints the description data frame (DESCRIPTION: table in the MTG file).
features	logical. If TRUE (default), prints the data frame of the features and their types (FEATURES: table in the MTG file).
topology	logical. If TRUE (default: FALSE), prints the data frame of the plant topology.
coordinates	logical. If TRUE (default: FALSE), prints the spatial coordinates of the entities of the plant.
	optional arguments to print methods.

Details

If classes, description or features are TRUE, the corresponding data frames are displayed.

If topology = TRUE, the plant structure is displayed; and if coordinates = TRUE, the spatial coordinates are displayed.

By default, the data frames containing the features on the vertices per class are printed.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Pradal, C., Godin, C. and Cokelaer, T. (2023). MTG user guide

See Also

read.mtg: reads a MTG file and creates an object of class "foldermtg".

```
mtgfile1 <- system.file("extdata/plant1.mtg", package = "dad")
xmtg1 <- read.mtg(mtgfile1)
print(xmtg1)
print(xmtg1, topology = TRUE)
print(xmtg1, coordinates = TRUE)
mtgfile2 <- system.file("extdata/plant2.mtg", package = "dad")
xmtg2 <- read.mtg(mtgfile2)
print(xmtg2)
print(xmtg2, topology = TRUE)
print(xmtg2, coordinates = TRUE)</pre>
```

print.foldert

Description

print function, applied to an object of class "foldert", prints a foldert, as returned by foldert or as.foldert function.

Usage

S3 method for class 'foldert'
print(x, ...)

Arguments

х	an object of class foldert.
	optional arguments to print methods.

Details

The foldert is printed. In any data frame x[[t]] of this foldert, if a row is entirely NA (which means that the corresponding individual was not observed at time t), this row are not printed.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

foldert: object of class foldert. as.foldert.data.frame: build an object of class foldert from a data frame. as.foldert.array: build an object of class foldert from a 3*d*-array.

```
data(floribundity)
```

```
ft <- foldert(floribundity, cols.select = "union", rows.select = "union")
print(ft)</pre>
```

print.fpcad

Description

Applies to an object of class "fpcad". Prints the numeric results returned by the fpcad function.

Usage

```
## S3 method for class 'fpcad'
print(x, mean.print = FALSE, var.print = FALSE,
    cor.print = FALSE, skewness.print = FALSE, kurtosis.print = FALSE,
    digits = 2, ...)
```

Arguments

х	object of class "fpcad", returned by the fpcad function.
mean.print	logical. If TRUE, prints for each group the means and standard deviations of the variables and the norm of the density.
var.print	logical. If TRUE, prints for each group the variances and covariances of the variables.
cor.print	logical. If TRUE, prints for each group the correlations between the variables.
skewness.print	logical. If TRUE, prints for each group the skewness coefficients of the variables.
kurtosis.print	logical. If TRUE, prints for each group the kurtosis coefficients of the variables.
digits	numeric. Number of significant digits for the display of numeric results.
	optional arguments to print methods.

Details

By default, are printed the inertia explained by the nb.values (see fpcad) first principal components, the contributions, the qualities of representation of the densities along the nb.factors (see fpcad) first principal components, and the principal scores.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Boumaza, R., Yousfi, S., Demotes-Mainard, S. (2015). Interpreting the principal component analysis of multivariate density functions. Communications in Statistics - Theory and Methods, 44 (16), 3321-3339.

See Also

fpcad; plot.fpcad; interpret.fpcad; print.

Examples

```
data(roses)
rosefold <- as.folder(roses[,c("Sha","Den","Sym","rose")])
result <- fpcad(rosefold)
print(result)
print(result, mean.print = TRUE)</pre>
```

print.fpcat	Printing results of a functional PCA of probability densities among
	time

Description

Applies to an object of class "fpcat". Prints the numeric results returned by the fpcat function.

Usage

```
## S3 method for class 'fpcat'
print(x, mean.print = FALSE, var.print = FALSE,
    cor.print = FALSE, skewness.print = FALSE, kurtosis.print = FALSE,
    digits = 2, ...)
```

Arguments

x	object of class "fpcat", returned by the fpcat function.
mean.print	logical. If TRUE, prints for each observation time the means and standard devia- tions of the variables and the norm of the density.
var.print	logical. If TRUE, prints for each observation time the variances and covariances of the variables.
cor.print	logical. If TRUE, prints for each observation time the correlations between the variables.
skewness.print	logical. If TRUE, prints for each observation time the skewness coefficients of the variables.
kurtosis.print	logical. If TRUE, prints for each observation time the kurtosis coefficients of the variables.
digits	numeric. Number of significant digits for the display of numeric results.
	optional arguments to print methods.

Details

By default, are printed the vector of observation times (numeric, ordered factor or object of class "Date"), the inertia explained by the nb.values (see fpcat) first principal components, the contributions, the qualities of representation of the densities along the nb.factors (see fpcat) first principal components, and the principal scores.

print.hclustdd

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Boumaza, R., Yousfi, S., Demotes-Mainard, S. (2015). Interpreting the principal component analysis of multivariate density functions. Communications in Statistics - Theory and Methods, 44 (16), 3321-3339.

See Also

fpcat; plot.fpcat; print.

Examples

```
times <- as.Date(c("2017-03-01", "2017-04-01", "2017-05-01", "2017-06-01"))
x1 <- data.frame(z1=rnorm(6,1,5), z2=rnorm(6,3,3))
x2 <- data.frame(z1=rnorm(6,4,6), z2=rnorm(6,5,2))
x3 <- data.frame(z1=rnorm(6,7,2), z2=rnorm(6,8,4))
x4 <- data.frame(z1=rnorm(6,9,3), z2=rnorm(6,10,2))
ft <- foldert(x1, x2, x3, x4, times = times, rows.select="intersect")
print(ft)
result <- fpcat(ft)
print(result)
print(result, mean.print = TRUE, var.print = TRUE)</pre>
```

print.hclustdd Printing results of a hierarchical clustering of discrete distributions

Description

print function, applied to an object of class "hclustdd", prints numerical results of hclustdd .

Usage

```
## S3 method for class 'hclustdd'
print(x, dist.print=FALSE, digits=2, ...)
```

Arguments

х	object of class "hclustdd", returned by hclustdd.
dist.print	logical. If TRUE (default: FALSE), prints the matrix of distances between the groups (densities).
digits	numerical. Number of significant digits for the display of numerical results.
	optional arguments to print methods.

Details

If dist.print = TRUE, the distances between groups are displayed.

By default, the result of the clustering is printed. The display is the same as that of the print.hclust function.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

hclustdd; plot.hclustdd.

Examples

```
data(dspg)
xl = dspg
result <- hclustdd(xl)
print(result)
print(result, dist.print = TRUE)</pre>
```

print.mdsdd	Printing results of a multidimensional scaling analysis of discrete dis-
	tributions

Description

Applies to an object of class "mdsdd". Prints the numeric results returned by the mdsdd function.

Usage

Arguments

х	object of class "mdsdd", returned by the mdsdd function.
joint	logical. If TRUE, prints for each group the table of estimated joint distribution.
margin1	logical. If TRUE, prints for each group the data frame of estimated marginal distributions.
margin2	logical. If TRUE, prints for each group the data frame of the estimated marginal distributions per combination of two variables.
association	logical. If TRUE, prints for each group the matrix of the pairwise association measures of the variables.
	optional arguments to print methods.

read.mtg

Details

By default, are printed the inertia explained by the nb.values (see mdsdd) first coordinates and the nb.factors (see mdsdd) coordinates of the densities.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Sabine Demotes-Mainard

See Also

mdsdd; plot.mdsdd; interpret.mdsdd

Examples

```
# INSEE (France): Diploma x Socio professional group, seven years.
data(dspg)
xlista = dspg
a <- mdsdd(xlista)
print(a, joint = TRUE, margin1 = TRUE, margin2 = TRUE)
```

```
read.mtg
```

Read a MTG (Multiscale Tree Graph) file

Description

Reads an MTG (Multiscale Tree Graph) file and returns an object of class foldermtg, that is a list of data frames (see Details).

Usage

read.mtg(file, ...)

Arguments

file	character. Path of the MTG file.
	optional arguments to print methods.

Details

Recalling that a MTG file is a text file that can be opened with a spreadsheet (Excel, LibreOffice-Calc...). Its 4 tables are:

- **CLASSES:** In this table the first column, named SYMBOL, contains the symbolic character denoting each botanical entity (or vertex class, plant component...) used in the MTG (for example, P for plant, A for axis...). The second column, named SCALE, represents the scale at which each entity appears in the MTG (for example 1 for P, 2 for axis...).
- **DESCRIPTION:** This table displays the relations between the vertices: + (branching relationship) or < (successor relationship).

- **FEATURES:** This table contains the features that can be attached to the vertices and their types: INT (integer), REAL (real numbers), STRING (character)...
- **MTG:** This table describes the plant topology, that is the vertices (one vertex per row) and their relations, the spatial coordinates of each vertex and the values taken by each vertex on the above listed features.

Each vertex is labelled by its class, designating its botanical entity, and its index, designating its position among its immediate neighbours having the same scale. Each vertex label is preceded by + or <, seen above, or by the symbol / (decomposition relationship) that means that the corresponding vertex is the first vertex of the decomposition of the vertex which precedes /.

Notice that the column number of a vertex matches with its branching order. The vertices of scale k resulting from the decomposition of a vertex of scale k-1, named parent vertex, have the same order as that of the parent vertex.

See the example below.

Value

read.mtg returns an object, say x, of class fodermtg, that is a list of at least 6 data frames:

classes	the table CLASSES: in the MTG file.
description	the table DESCRIPTION: in the MTG file.
features	the table FEATURES: in the MTG file.
topology	data frame containing the first columns of the "MTG:" table of the MTG file. If the maximum branching order of the elements of the MTG is p , then x\$topology has p columns.
	If the i-th vertex appears on the j-th column, it means that its branching order is j, that is it belongs to a vertex of the j-th order.
coordinates	data frame of the spatial coordinates of the entities. It has six columns: XX, YY, ZZ (cartesian coordinates), AA, BB, CC (angle coordinates). If there are no coordinates in the MTG file, this data frame has 0 row.

The sixth and following elements are nclass data frames, nclass being the number of classes in the MTG file. Each data frame matches with a vertex class, such as "P" (plant), "A" (axes), "M" (metamers or phytomers), and contains the features on the corresponing vertices.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Pradal, C., Godin, C. and Cokelaer, T. (2023). MTG user guide

See Also

print.foldermtg mtgorder

rmcol.folder

Examples

```
mtgfile1 <- system.file("extdata/plant1.mtg", package = "dad")
x1 <- read.mtg(mtgfile1)
print(x1)
mtgfile2 <- system.file("extdata/plant2.mtg", package = "dad")
x2 <- read.mtg(mtgfile2)
print(x2)</pre>
```

rmcol.folder Remove columns in all elements of a folder

Description

Remove some columns in all data frames of a folder.

Usage

rmcol.folder(object, name)

Arguments

object	object of class folder that is a list of data frames with the same column names.
name	character vector. The names of the columns to be removed in each data frame
	of the folder.

Value

A folder with the same number of elements as object. Its k^{th} element is a data frame, and its columns are the columns of object[[k]], except those given by name.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

folder: object of class folder.

getcol.folder: select columns in all elements of a folder.

getrow.folder: select rows in all elements of a folder.

rmrow.folder: remove rows in all elements of a folder.

```
data(iris)
```

```
iris.fold <- as.folder(iris, "Species")
rmcol.folder(iris.fold, c("Petal.Length", "Petal.Width"))</pre>
```

rmcol.foldert

Description

Remove some columns in all data frames of a foldert.

Usage

rmcol.foldert(object, name)

Arguments

object	object of class foldert that is a list of data frames with the same column names, each of them corresponding to a time of observation.
name	character vector. The names of the columns to be removed in each data frame of the foldert.

Value

A foldert with the same number of elements as object. Its k^{th} element is a data frame, and its columns are the columns of object[[k]], except those given by name.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

foldert: object of class foldert.

getcol.foldert: select columns in all elements of a foldert.

getrow.foldert: get rows in all elements of a foldert.

rmrow.foldert: remove rows in all elements of a foldert.

```
data(floribundity)
```

```
ft0 <- foldert(floribundity, cols.select = "union", rows.select = "union")
ft0
rmcol.foldert(ft0, c("area"))</pre>
```

rmrow.folder

Description

Remove some rows in all data frames of a folder.

Usage

```
rmrow.folder(object, name)
```

Arguments

object	object of class folder that is a list of data frames with the same column names.
name	character vector. The names of the rows to be removed in each data frame of the folder.

Value

A folder with the same number of elements as object. Its k^{th} element is a data frame, and its rows are the rows of object[[k]], except those given by name.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

folder: object of class folder.

getrow. folder: select rows in all elements of a folder.

getcol.folder: select columns in all elements of a folder.

rmcol.folder: remove columns in all elements of a folder.

```
data(iris)
```

```
iris.fold <- as.folder(iris, "Species")
rmrow.folder(iris.fold, as.character(seq(1, 150, by = 2)))</pre>
```

rmrow.foldert

Description

Remove some rows in all data frames of a foldert.

Usage

rmrow.foldert(object, name)

Arguments

object	object of class foldert that is a list of data frames with the same column names, each of them corresponding to a time of observation.
name	character vector. The names of the rows to be removed in each data frame of the foldert.

Value

A foldert with the same number of elements as object. Its k^{th} element is a data frame, and its rows are the rows of object[[k]], except those given by name.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

foldert: object of class foldert.

getrow. foldert: select rows in all elements of a foldert.

getcol.foldert: select columns in all elements of a foldert.

rmcol.foldert: remove columns in all elements of a foldert.

```
data(floribundity)
```

```
ft0 <- foldert(floribundity, cols.select = "union", rows.select = "union")
ft0
rmrow.foldert(ft0, c("rose", c("16", "51")))</pre>
```

roseflowers

Rose flowers

Description

The data are extracted from measures on roses from an agronomic experiment in a greenhouse and outdoors.

Usage

data(roseflowers)

Format

roseflowers is a list of two data frames:

- roseflowers\$variety: this first data frame has 5 rows and 3 columns (factors) named place, rose and variety.
- roseflowers\$flower: this second data frame has 11 cases and 5 columns named numflower (the order number of the flower), rose, diameter and height (the diameter and height of the flower), and nleaves (the number of the leaves of the axis).

Examples

```
data(roseflowers)
summary(roseflowers$variety)
summary(roseflowers$flower)
```

roseleaves

Rose leaves

Description

The data are extracted from measures on roses from an agronomic experiment in a greenhouse and outdoors.

Usage

data("roseleaves")

Format

roseleaves is a list of four data frames:

- roseflowers\$rose: data frame with 7 rows and 3 columns (factors) named rose, place and variety.
- roseflowers\$stem: data frame with 12 rows and 5 columns named rose, stem, date, order (the ramification order of the stem) and nleaves (the number of leaves of the stem).
- roseflowers\$leaf: data frame with 35 rows and 5 columns named stem, leaf, rank (the rank of the leaf on the stem), nleaflets and lrachis (the number of leaflets of the leaf and the length of its rachis).
- roseflowers\$leaflet: data frame with 221 rows and 4 columns named leaf, leaflet, lleaflet and wleaflet (the length and width of the leaflet).

Each row (rose) in roseleaves\$rose pertains to several rows (stems) in roseleaves\$stem.

Each row (stem) in roseleaves\$rose pertains to several rows (leaves) in roseleaves\$leaf.

Each row (leaf) in roseleaves\$rose pertains to several rows (leaflets) in roseleaves\$leaflet.

Examples

```
data(roseleaves)
summary(roseleaves$rose)
summary(roseleaves$stem)
summary(roseleaves$leaf)
summary(roseleaves$leaflet)
```

rosephytomer

Rose leaf and internode dynamics

Description

These data are extracted from measures on rosebushes during a study on leaf and internode expansion dynamics. For four rosebushes, on each metamer, the length of the terminal leaflet and the length of the internode were measured on several days, from the 24 april 2010 to the 19 july 2010.

The metamers which have no leaflets are omitted.

Usage

```
data("rosephytomer")
```

Format

A data frame with 643 rows (4 plants, 7, 8 or 9 metamers per plant, 37 days of observation) and 6 columns:

date a POSIXct

nplant a factor with levels 113 114 118 121. Numbers of the plants.

rank numeric. Rank of the metamer on the stem.

lleaflet, linternode numeric. Length of the terminal leaflet, length of the internode.

phytomer factor. Identifiers of the metamers.

Source

Demotes-Mainard, S., Bertheloot, J., Boumaza, R., Huché-Thélier, L., Guéritaine, G., Guérin, V. and Andrieu, B. (2013). Rose bush leaf and internode expansion dynamics: analysis and development of a model capturing interplant variability. Frontiers in Plant Science 4: 418. Doi: 10.3389/fpls.2013.00418

Examples

```
data(rosephytomer)
as.foldert(rosephytomer, method = 1, ind = "phytomer", timecol = "date", same.rows = TRUE)
```

roses

Roses data

Description

Sensory data characterising the visual aspect of 10 rosebushes

Usage

data(roses)

Format

roses is a data frame of sensory data with 420 rows (10 products, 14 assessors, 3 sessions) and 17 columns. The first 16 columns are numeric and correspond to 16 visual characteristics of rosebushes. The last column is a factor giving the name of the corresponding rosebush.

- Sha: top sided shape
- Den: foliage thickness
- Sym: plant symmetry
- Vgr: stem vigour
- Qrm: quantity of stems
- Htr: branching level
- Qf1: quantity of flowers
- Ef1: staggering of flowering
- Mvfl: flower enhancement
- Difl: flower size
- Qfr: quantity of faded flowers/fruits

- Qbt: quantity of floral buds
- Def1: density of flower petals
- Vcfl: intensity of flower colour
- Tfe: leaf size
- Vfe: darkness of leaf colour
- rose: factor with 10 levels: A, B, C, D, E, F, G, H, I and J

Source

Boumaza, R., Huché-Thélier, L., Demotes-Mainard, S., Le Coz, E., Leduc, N., Pelleschi-Travier, S., Qannari, E.M., Sakr, S., Santagostini, P., Symoneaux, R., Guérin, V. (2010). Sensory profile and preference analysis in ornamental horticulture: The case of rosebush. Food Quality and Preference, 21, 987-997.

Examples

data(roses)
summary(roses)

skewness.folder Skewness coefficients of a folder of data sets

Description

Computes the skewness coefficient by column of the elements of an object of class folder.

Usage

```
skewness.folder(x, na.rm = FALSE, type = 3)
```

Arguments

Х	an object of class folder that is a list of data frames with the same column
	names.
na.rm	logical. Should missing values be omitted from the calculations? (see skewness)
type	an integer between 1 and 3 (see skewness).

Details

It uses skewness to compute the mean by numeric column of each element of the folder. If some columns of the data frames are not numeric, there is a warning, and the means are computed on the numeric columns only.

Value

A list whose elements are the skewness coefficients by column of the elements of the folder.

190

sqrtmatrix

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

folder to create an object is of class folder. mean. folder, var. folder, cor. folder, kurtosis. folder for other statistics for folder objects.

Examples

```
# First example: iris (Fisher)
data(iris)
iris.fold <- as.folder(iris, "Species")
iris.skewness <- skewness.folder(iris.fold)
print(iris.skewness)
# Second example: roses
data(roses)
roses.fold <- as.folder(roses, "rose")
roses.skewness <- skewness.folder(roses.fold)
print(roses.skewness)</pre>
```

sqrtmatrix Square root of a symmetric, positive semi-definite matrix

Description

Calculation of the square root of a positive semi-definite matrix (see Details for the definition of such a matrix).

Usage

sqrtmatrix(mat)

Arguments

mat numeric matrix.

Details

The matrix mat must be symmetric and positive semi-definite. Otherwise, there is an error.

The square root of the matrix mat is the positive semi-definite matrix M such as t(M) %% M = mat. Do not confuse with sqrt(mat), which returns the square root of the elements of mat.

The computation is based on the diagonalisation of mat. The eigenvalues smaller than 10⁻¹⁶ are identified as null values.

Matrix: the square root of the matrix mat.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

Examples

```
M2 <- matrix(c(5, 4, 4, 5), nrow = 2)
M <- sqrtmatrix(M2)
M
```

summary.folder Summarize a folder

Description

Summarize an object of class folder.

Usage

S3 method for class 'folder'
summary(object, ...)

Arguments

object	object of class folder that is a list of data frames with the same column names.
	further arguments passed to or from other methods.

Value

A list, each element of it contains the summary of the corresponding element of object. This list has an attribute attr(, "same.rows").

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

folder: object of class folder. as.folder.data.frame: build an object of class folder from a data frame.

Examples

```
data(iris)
iris.fold <- as.folder(iris, "Species")
summary(iris.fold)</pre>
```

192

summary.folderh Summarize a folderh

Description

Summarize an object of class folderh.

Usage

S3 method for class 'folderh'
summary(object, ...)

Arguments

object	object of class folderh that is a list of data frames.
	further arguments passed to or from other methods.

Value

A list, each element of it containing the summary of the corresponding element of object. This list has an attribute attr(, "keys") (see folderh).

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

folderh: object of class folderh.

```
# First example
mtgfile <- system.file("extdata/plant1.mtg", package = "dad")
x <- read.mtg(mtgfile)
fh1 <- as.folderh(x, classes = c("P", "A", "M"))
summary(fh1)
# Second example
data(roseleaves)
roses <- roseleaves$rose
stems <- roseleaves$rose
stems <- roseleaves$tem
leaves <- roseleaves$leaf
leaflets <- roseleaves$leaflet
fh2 <- folderh(roses, "rose", stems, "stem", leaves, "leaf", leaflets)</pre>
```

summary.foldermtg Summary of an object of class foldermtg

Description

Summary method for S3 class foldermtg.

Usage

```
## S3 method for class 'foldermtg'
summary(object, ...)
```

Arguments

object	an object of class foldermtg.
	optional arguments to summary methods.

Value

The summary of the data frames containing the vertices of each class and the values of the features on these vertices.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Pradal, C., Godin, C. and Cokelaer, T. (2023). MTG user guide

See Also

read.mtg: reads a MTG file and creates an object of class "foldermtg".

```
mtgfile1 <- system.file("extdata/plant1.mtg", package = "dad")
x1 <- read.mtg(mtgfile1)
summary(x1)
mtgfile2 <- system.file("extdata/plant2.mtg", package = "dad")
x2 <- read.mtg(mtgfile2)
summary(x2)</pre>
```

Description

Summarize an object of class foldert.

Usage

```
## S3 method for class 'foldert'
summary(object, ...)
```

Arguments

object	object of class foldert that is a list of data frames organised according to time
	further arguments passed to or from other methods.

Value

A list, each element of it contains the summary of the corresponding element of object. This list has two attributes attr(, "times") and attr(, "same.rows").

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

foldert: object of class foldert. as.foldert.data.frame: build an object of class foldert from a data frame. as.foldert.array: build an object of class foldert from a 3*d*-array.

```
# 1st example
data(floribundity)
ftflor <- foldert(floribundity, cols.select = "union", rows.select = "union")
summary(ftflor)</pre>
```

var.folder

Description

Computes the variance matrices of the elements of an object of class folder.

Usage

var.folder(x, na.rm = FALSE, use = "everything")

Arguments

х	an object of class folder that is a list of data frames with the same column names.
na.rm	logical. Should missing values be removed? (see var)
use	an optional character string giving a method for computing covariances in the presence of missing values. This must be (an abbreviation of) one of the strings "everything", "all.obs", "complete.obs", "na.or.complete", or "pairwise.complete.obs" (see var).

Details

It uses var to compute the variance matrix of the numeric columns of each element of the folder. If some columns of the data frames are not numeric, there is a warning, and the variances are computed on the numeric columns only.

Value

A list whose elements are the variance matrices of the elements of the folder.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

See Also

folder to create an object is of class folder. mean.folder, cor.folder, skewness.folder, kurtosis.folder for other statistics for folder objects.

```
# First example: iris (Fisher)
data(iris)
iris.fold <- as.folder(iris, "Species")
iris.vars <- var.folder(iris.fold)
print(iris.vars)</pre>
```

varietyleaves

```
# Second example: roses
data(roses)
roses.fold <- as.folder(roses, "rose")
roses.vars <- var.folder(roses.fold)
print(roses.vars)</pre>
```

varietyleaves Rose variety leaves

Description

The data are extracted from measures on roses from an agronomic experiment in a greenhouse and outdoors.

Usage

```
data("varietyleaves")
```

Format

varietyleaves is an object of class "folderh", that is a list of two data frames:

- varietyleaves\$variety: data frame with 31 rows and 2 columns (factors) named rose and variety.
- varietyleaves\$leaves: data frame with 581 rows and 5 columns named rose, nleaflet (number of leaflets), lrachis (length of the rachis), lleaflet (length of the principal leaflet) and wleaflet (width of the principal leaflet).

Examples

```
data(varietyleaves)
summary(varietyleaves)
```

wasserstein

2-Wasserstein distance between Gaussian densities

Description

The 2-Wasserstein distance between two multivariate (p > 1) or univariate (p = 1) Gaussian densities (see Details).

Usage

wasserstein(x1, x2, check = FALSE)

Arguments

x1	a matrix or data frame of n_1 rows (observations) and p columns (variables) (can also be a tibble) or a vector of length n_1 .
x2	matrix or data frame (or tibble) of n_2 rows and p columns or vector of length n_2 .
check	logical. When TRUE (the default is FALSE) the function checks if the covariance matrices are not degenerate (multivariate case) or if the variances are not zero (univariate case).

Details

The Wasserstein distance between the two Gaussian densities is computed by using the wassersteinpar function and the density parameters estimated from samples.

Value

Returns the 2-Wasserstein distance between the two probability densities.

Be careful! If check = FALSE and one smoothing bandwidth matrix is degenerate, the result returned can not be considered.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Peterson, A., Mueller, H.G. (2016). Functional Data Analysis for Density Functions by Transformation to a Hilbert Space. The annals of Statistics, 44 (1), 183-218. DOI: 10.1214/15-AOS1363

Dowson, D.C., Ladau, B.V. (1982). The Fréchet Distance between Multivariate Normal Distributions. Journal of Multivariate Analysis, 12, 450-455.

See Also

wassersteinpar: 2-Wasserstein distance between Gaussian densities, given their parameters.

```
require(MASS)
m1 <- c(0,0)
v1 <- matrix(c(1,0,0,1),ncol = 2)
m2 <- c(0,1)
v2 <- matrix(c(4,1,1,9),ncol = 2)
x1 <- mvrnorm(n = 3,mu = m1,Sigma = v1)
x2 <- mvrnorm(n = 5, mu = m2, Sigma = v2)
wasserstein(x1, x2)</pre>
```

wassersteinpar

2-Wasserstein distance between Gaussian densities given their parameters

Description

The 2-Wasserstein distance between two multivariate (p > 1) or univariate (p = 1) Gaussian densities given their parameters (mean vectors and covariance matrices if the densities are multivariate, or means and variances if univariate) (see Details).

Usage

```
wassersteinpar(mean1, var1, mean2, var2, check = FALSE)
```

Arguments

mean1	p-length numeric vector: the mean of the first Gaussian density.
var1	$p \ge p$ symmetric numeric matrix $(p > 1)$ or numeric $(p = 1)$: the covariance matrix $(p > 1)$ or the variance $(p = 1)$ of the first Gaussian density.
mean2	p-length numeric vector: the mean of the second Gaussian density.
var2	$p \ge p$ symmetric numeric matrix $(p > 1)$ or numeric $(p = 1)$: the covariance matrix $(p > 1)$ or the variance $(p = 1)$ of the second Gaussian density.
check	logical. When TRUE (the default is FALSE) the function checks if the covariance matrices are not degenerate (multivariate case) or if the variances are not zero (univariate case).

Details

The mean vectors (m1 and m2) and variance matrices (v1 and v2) given as arguments (mean1, mean2, var1 and var2) are used to compute the 2-Wasserstein distance between the two Gaussian densities, equal to:

$$(||m1 - m2||_{2}^{2} + trace((v1 + v2) - 2 * (v2^{1/2}v1v2^{1/2})^{1/2}))^{1/2})$$

If p = 1:

$$((m1 - m2)^2 + v1 + v2 - 2 * (v1 * v2)^{1/2})^{1/2}$$

Value

The 2-Wasserstein distance between two Gaussian densities.

Be careful! If check = FALSE and one covariance matrix is degenerated (multivariate case) or one variance is zero (univariate case), the result returned must not be considered.

Author(s)

Rachid Boumaza, Pierre Santagostini, Smail Yousfi, Gilles Hunault, Sabine Demotes-Mainard

References

Peterson, A., Mueller, H.G (2016). Functional Data Analysis for Density Functions by Transformation to a Hilbert Space. The annals of Statistics, 44 (1), 183-218. DOI: 10.1214/15-AOS1363

Dowson, D.C., Ladau, B.V. (1982). The Fréchet Distance between Multivariate Normal Distributions. Journal of Multivariate Analysis, 12, 450-455.

See Also

wasserstein: 2-Wasserstein distance between Gaussian densities estimated from samples.

```
m1 <- c(1,1)
v1 <- matrix(c(4,1,1,9),ncol = 2)
m2 <- c(0,1)
v2 <- matrix(c(1,0,0,1),ncol = 2)
wassersteinpar(m1,v1,m2,v2)</pre>
```

Index

* datasets castles. 25 castles.dated, 26 castles.nondated, 27 departments, 44 dspg, 56 dspgd2015, 57 floribundity, 69 mtgplant1, 152 mtgplant2, 153 roseflowers, 187 roseleaves, 187 rosephytomer, 188 roses, 189 varietyleaves, 197 appendtofolderh, 7, 77 as.data.frame, 8, 9, 11 as.data.frame.folder, 8, 11-13, 15 as.data.frame.folderh, 9, 15, 77 as.data.frame.foldert, 11, 21 as.folder, 12 as.folder.data.frame, 8, 12, 13, 192 as.folder.folderh, 10, 12, 13, 14, 15, 77 as.folderh.16 as.folderh.foldermtg, 16, 17 as.foldert, 18, 176 as.foldert.array, 11, 18, 19, 21, 80, 160, 176.195 as.foldert.data.frame, 11, 18, 19, 20, 80, 85, 160, 176, 195 association measures, 22 association measures for folder, 23 Assocs, 22, 23, 147 bandwidth.parameter, 24, 61, 64, 67, 72, 73, 82, 83, 87 castles, 25 castles.dated, 25, 26, 27

castles.nondated, 27 cmdscale, 70, 71, 145, 146 colMeans, 148 cor, 28 cor.folder, 6, 28, 117, 149, 191, 196 cramer.data.frame, 23 cramer.data.frame(association measures), 22 cramer.folder, 146 cramer.folder (association measures for folder), 23 cut, 29, 30 cut.data.frame, 29, 31 cut.folder, 31, 31 dad (dad-package), 5 dad-package, 5 ddchisqsym, 32, 34, 35, 37, 40, 42, 121 ddchisqsympar, 32, 33, 33, 36, 39, 41, 44, 122 ddhellinger, 33, 34, 36, 37, 40, 42, 123 ddhellingerpar, 34, 35, 35, 39, 41, 44, 124 ddjeffreys, 33, 35, 37, 39, 40, 42, 125 ddjeffreyspar, 34, 36, 37, 38, 41, 44, 126 ddjensen, 33, 35, 37, 39, 41, 42, 127 ddjensenpar, 34, 36, 39, 40, 40, 44, 128 ddlp, 33, 35, 37, 40, 42, 44, 129 ddlppar, 34, 36, 39, 41, 42, 43, 130 departments, 44 discdd.misclass, 6, 45, 49, 105, 166 discdd.predict, 6, 48, 106, 167, 168 distl2d, 51, 53, 131 distl2dnorm, 52, 133 distl2dnormpar, 54, 134 distl2dpar, 55, 55, 136 dspg, 56 dspgd2015, 57 dstatis (dstatis.inter), 58 dstatis.inter, 58, 97, 98, 106, 107, 156, 157, 168, 169

fdiscd.misclass, 5, 25, 60, 64, 68, 107, 170, 171 fdiscd.predict, 5, 25, 63, 68, 108, 171, 172 fhclustd, 5, 66, 66, 108, 109, 157, 172, 173 floribundity, 69 fmdsd, 5, 25, 70, 98, 99, 109, 158, 159, 164, 173.174 folder, 6, 8, 10, 12–15, 23, 28, 31, 58, 66, 70, 71, 74, 77, 81, 87–91, 110, 116, 117, 145, 148, 149, 183, 185, 190–192, 196 folderh, 6, 7, 9, 10, 14-18, 45, 48, 60, 63, 75, 76, 110, 111, 193 foldermtg, 17, 77, 149–155, 174, 175, 194 foldert, 6, 11, 18-21, 78, 84, 88-90, 112, 159, 160, 176, 184, 186, 195 fpcad, 5, 25, 73, 81, 85, 86, 96, 100, 101, 112, 113, 160, 161, 177 fpcat, 5, 84, 96, 102, 103, 162, 163, 178, 179 getcol.folder, 87, 90, 183, 185 getcol.foldert, 88, 90, 184, 186 getrow.folder, 88, 89, 183, 185 getrow.foldert, 89, 90, 184, 186 ggplot2, 165 hclust, 66, 67, 91, 92 hclustdd, 91, 91, 92, 163, 179, 180 hellinger, 93, 95, 136, 137 hellingerpar, 93, 94, 94, 137, 138 interpret, 6, 95 interpret.dstatis, 60, 96, 97, 157, 169 interpret.fmdsd, 71, 73, 96, 98, 159, 174 interpret.fpcad, 82, 83, 86, 96, 100, 161, 177 interpret.fpcat, 96, 102 interpret.mdsdd, 96, 103, 146, 147, 165, 181 is.discdd.misclass, 105 is.discdd.predict, 106 is.dstatis.106 is.fdiscd.misclass, 107 is.fdiscd.predict, 108 is.fhclustd, 108 is.fmdsd.109 is.folder, 75, 110 is.folderh, 77, 110 is.foldermtg, 111 is.foldert, 80, 112

is.fpcad, 112 is.mdsdd, 113 jeffreys, 114, 116 jeffreyspar, 114, 115, 142 kurtosis, 116, 117 kurtosis.folder, 6, 28, 116, 149, 191, 196 12d, 51–53, 117, 120, 131, 133, 138, 139 12dpar, 54, 55, 118, 119, 119, 140 matddchisqsym, 121, 122 matddchisqsympar, 92, 121, 122, 146 matddhellinger, 123, 124 matddhellingerpar, 92, 123, 124, 146 matddjeffreys, 125, 126 matddjeffreyspar, 92, 125, 126, 146 matddjensen, 127, 128 matddjensenpar, 92, 127, 128, 146 matddlp, 129, 130 matddlppar, 92, 129, 130, 146 matdistl2d, 52, 55, 56, 131, 133, 136 matdistl2dnorm, 53, 132, 134 matdistl2dnormpar, 133, 134 matdistl2dpar, 131, 134, 135 mathellinger, 136, 138 mathellingerpar, 137, 137 matipl2d, 138, 140 matipl2dpar, *139*, 140 matjeffreys, 141, 142 matjeffreyspar, 141, 142 matplot, 159, 160 matwasserstein, 143, 144 matwassersteinpar, 143, 144 mdsdd, 6, 103, 104, 113, 145, 164, 165, 180, 181 mean, 148 mean.folder, 6, 28, 117, 148, 191, 196 mtgcomponents, 149 mtgorder, 78, 150, 150, 151, 155, 182 mtgplant1, 152, 154 mtgplant2, 153, 153 mtgrank, 150, 154 pearson.data.frame, 23 pearson.data.frame(association measures), 22 pearson.folder, 146

INDEX

pearson.folder(association measures for folder), 23 phi.data.frame, 23 phi.data.frame (association measures), 22 phi.folder, 146 phi.folder (association measures for folder), 23 plot.dstatis, 60, 98, 156, 169 plot.fhclustd, 157 plot.fmdsd, 71, 73, 99, 158, 174 plot.foldert, 159 plot.fpcad, 82, 83, 86, 101, 160, 177 plot.fpcat, 87, 103, 162, 179 plot.hclust, 157, 163 plot.hclustdd, 163, 180 plot.mdsdd, 104, 146, 147, 164, 181 plotframes, 165 points, 156, 158, 161, 164 print, 166, 168, 171-174, 177, 179 print.discdd.misclass, 166 print.discdd.predict, 167 print.dstatis, 60, 157, 168, 169 print.fdiscd.misclass, 170 print.fdiscd.predict, 171 print.fhclustd, 157, 172 print.fmdsd, 73, 159, 173 print.foldermtg, 78, 174, 182 print.foldert, 176 print.fpcad, 83, 161, 177 print.fpcat, 87, 163, 178 print.hclust, 173, 180 print.hclustdd, 163, 179 print.mdsdd, 147, 165, 180 read.mtg, 6, 18, 77, 78, 111, 150, 151, 153-155, 175, 181, 194 rmcol.folder, 88, 90, 183, 185 rmcol.foldert, 89, 90, 184, 186 rmrow.folder, 88, 90, 183, 185 rmrow.foldert, 89, 90, 184, 186 roseflowers, 187 roseleaves, 187 rosephytomer, 188 roses, 189 skewness, 190 skewness.folder, 6, 28, 117, 149, 190, 196 sqrtmatrix, 191

summary.folder, 192
summary.folderh, 193
summary.foldermtg, 194
summary.foldert, 195

var, 28, 196 var.folder, 6, 28, 117, 149, 191, 196 varietyleaves, 197

wasserstein, *144*, 197, *200* wassersteinpar, *144*, *198*, 199