

# Package: cusna (via r-universe)

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**Type** Package

**Title** Native GPU-Accelerated Simulation and Estimation of Network Models

**Version** 0.1.0

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**Description** A self-contained native engine (a C interface over 'CUDA' kernels and C++ host logic) for stochastic actor-oriented models (the model family of 'RSiena'), exponential random graph models (cross-sectional, temporal, and separable temporal), and models for binary actor attributes, callable from R without a Python runtime. Modelled on the 'torch' package: the CRAN build is CPU-only from source; the GPU path is compiled from source when a 'CUDA' toolkit is detected at configure time. The data preparation, host statistics ('RSiena' Appendix B conventions), and moment targets are validated bit-for-bit against the reference implementation and reproduce 'RSiena' targets on public datasets to machine precision; the estimators match 'RSiena', 'ergm', 'btergm', and 'tergm' on public benchmark models.

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**URL** <https://github.com/artemmaltsev74-techcom/cusna>

**BugReports** <https://github.com/artemmaltsev74-techcom/cusna/issues>

**Encoding** UTF-8

**SystemRequirements** C++17; optionally a CUDA 12.x toolkit (nvcc) for the GPU path

**LinkingTo** cpp11

**Imports** stats, utils

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|               |                                                                       |
|---------------|-----------------------------------------------------------------------|
| cusna-package | <i>cusna: native GPU-accelerated stochastic actor-oriented models</i> |
|---------------|-----------------------------------------------------------------------|

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Description

A self-contained native engine (C ABI over CUDA kernels and C++ host logic) for SAOM/RSiena and ERGM, callable from R without a Python runtime. Modelled on the **torch** package: the CRAN build is CPU-only from source, and the GPU path is compiled from source when a CUDA toolkit is detected at configure time.

## Details

The package covers four model families, all on the same compiled engine:

- **SAOM** (the RSiena model family): `saom_data` + `cusna_effect` + `mom_estimate` run the full Method-of-Moments (Robbins–Monro) estimator in R over the native simulator, including behavior co-evolution, composition change, and multi-network models (`mom_estimate_multinet`). The data preparation and moment targets are validated bit-for-bit against the reference implementation; the estimates agree within simulation standard errors.
- **ERGM**: `ergm_simulate` (native TNT sampler), `ergm_stats`, `ergm_mple`, and the `ergm_mcmc` maximum-likelihood estimator.
- **Temporal ERGM**: `tergm_mple` (pooled MPLE with block bootstrap), `tergm_simulate`, and the separable `stergm_cmle` (formation/persistence CMLE).
- **ALAAM** (autologistic actor attribute models): `alaam_mple`, `alaam_mcmc`, `alaam_simulate`.

The validated host statistics – the RSiena Appendix B convention carriers (`cusna_network_stats`, `cusna_behavior_stats`, `cusna_gof_distribution`) – reproduce RSiena targets on public datasets to machine precision and remain available as low-level entry points.

---

alaam\_mcmc

*Maximum likelihood estimate of an ALAAM (MCMC-MLE)*

---

## Description

Fits an ALAAM by MCMC maximum likelihood – an external moment-matching loop over the native Gibbs sampler, the attribute-DV twin of `ergm_mcmc`. The autologistic model is a canonical exponential family, so its Fisher information is the covariance of the sufficient statistics (density, contagion, covariate products); each iteration simulates the attribute at the current parameters, forms their mean and covariance, and takes a damped Newton step until the observed statistics are matched. Unlike `alaam_mple` (a pseudo-likelihood), the fitted model reproduces the observed moments. Pure R over the native engine (no Python).

## Usage

```
alaam_mcmc(y, net, cov = NULL, contagion = "out", coef0 = NULL,
           nsim = 500L, sweeps = NULL, maxit = 30L, tol = 0.12,
           damp = 0.5, seed = 1234L, verbose = FALSE)
```

## Arguments

|                        |                                                                                                     |
|------------------------|-----------------------------------------------------------------------------------------------------|
| <code>y</code>         | Binary actor attribute (0/1), length <code>n</code> .                                               |
| <code>net</code>       | Integer/logical <code>n*n</code> adjacency of the fixed network.                                    |
| <code>cov</code>       | Optional actor covariate(s) (length- <code>n</code> vector or <code>n*p</code> matrix).             |
| <code>contagion</code> | "out" (undirected neighbour count, default) or "total" (adds in-neighbours for a directed network). |
| <code>coef0</code>     | Optional starting parameters (default: the MPLE).                                                   |

|                  |                                                                                                        |
|------------------|--------------------------------------------------------------------------------------------------------|
| nsim             | Chains simulated per iteration (must exceed the parameter count).                                      |
| sweeps           | Gibbs sweeps per chain (default scales with n).                                                        |
| maxit, tol, damp | Outer iterations, convergence tolerance on the standardized deviations, and Hummel-style step damping. |
| seed             | Integer RNG seed.                                                                                      |
| verbose          | Print the per-iteration trajectory.                                                                    |

### Value

An `alaam_mcmle` object with `coef`, `se` (from the inverse Fisher information), `tstat`, `iterations`, `converged`, `sim_mean` and `obs`.

### Examples

```
set.seed(1)
net <- matrix(as.integer(runif(30 * 30) < 0.1), 30, 30)
net <- ((net + t(net)) > 0) * 1L
diag(net) <- 0L
y <- as.integer(runif(30) < 0.4)
fit <- alaam_mcmle(y, net, nsim = 300L, maxit = 20L)
fit
```

---

|            |                                                                                |
|------------|--------------------------------------------------------------------------------|
| alaam_mple | <i>Autologistic actor attribute model by maximum pseudo-likelihood (ALAAM)</i> |
|------------|--------------------------------------------------------------------------------|

---

### Description

Fits an ALAAM (Robins, Pattison & Elliott 2001) – a model for a binary actor attribute at a fixed, exogenous network – by maximum pseudo-likelihood, i.e. a logistic regression of the attribute on the native contagion change statistic (the number of network neighbours that also carry the attribute, a masked popcount) plus any actor covariates. The dependent variable is the attribute, not a tie; the network enters through the same bit-kernel primitive applied to (network-row AND attribute-vector). Best suited to an undirected network, where the contagion is the neighbour count with  $y = 1$ . Host C++ (no Python; works in the CPU-only build).

### Usage

```
alaam_mple(y, net, cov = NULL, contagion = "out", directed = FALSE)
```

### Arguments

|     |                                                                                                                                             |
|-----|---------------------------------------------------------------------------------------------------------------------------------------------|
| y   | Binary actor attribute (0/1), length n – the dependent variable.                                                                            |
| net | Integer/logical $n \times n$ adjacency of the fixed (exogenous) network.                                                                    |
| cov | Optional actor covariate(s): a length-n vector or an $n \times p$ matrix, entered as change statistics (the covariate value at each actor). |

|           |                                                                                                                                                                          |
|-----------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| contagion | Which contagion change statistic to include: "out" (out-neighbours with $y = 1$ , the default and the neighbour count when undirected), "in", "both", or FALSE for none. |
| directed  | Logical: is net directed? (documentation only; the contagion columns are selected by contagion).                                                                         |

### Value

An `alaam_mple` object with `coef`, `se`, `z`, `pval` (from the logistic regression), `glm` (the fitted model) and `n`.

### Examples

```
set.seed(1)
net <- matrix(as.integer(runif(30 * 30) < 0.1), 30, 30)
net <- ((net + t(net)) > 0) * 1L      # undirected
diag(net) <- 0L
y <- as.integer(runif(30) < 0.4)
fit <- alaam_mple(y, net)
fit
```

---

alaam\_simulate

---

*Simulate the actor attribute from an ALAAM (Gibbs sampler)*


---

### Description

Draws `nsim` binary attribute vectors from an ALAAM at a fixed network with the native Gibbs sampler: each full conditional is a logistic regression of  $y_i$  on the contagion (the number of neighbours with  $y = 1$ , the masked popcount used by `alaam_mple`, so estimator and simulator share one statistic) plus the actor covariates. Python-free (host engine, CPU-only).

### Usage

```
alaam_simulate(net, coef, cov = NULL, y0 = NULL, contagion = "out",
               nsim = 100L, sweeps = 200L, seed = 1234L)
```

### Arguments

|                        |                                                                                                                                    |
|------------------------|------------------------------------------------------------------------------------------------------------------------------------|
| <code>net</code>       | Integer/logical $n \times n$ adjacency of the fixed network.                                                                       |
| <code>coef</code>      | Parameters in the order density (intercept), contagion, then one per covariate column of <code>cov</code> .                        |
| <code>cov</code>       | Optional actor covariate(s) (length- $n$ vector or $n \times p$ matrix) matching the covariate coefficients in <code>coef</code> . |
| <code>y0</code>        | Optional start attribute (length $n$ ); default all zero.                                                                          |
| <code>contagion</code> | "out" (default) uses out-neighbours; "total" adds in-neighbours (the joint-consistent contagion for a directed network).           |

|        |                                                             |
|--------|-------------------------------------------------------------|
| nsim   | Number of independent chains.                               |
| sweeps | Gibbs sweeps per chain (burn-in over the attribute vector). |
| seed   | Integer RNG seed.                                           |

### Value

A list with `y` (a `nsim` x `n` matrix of simulated attributes) and `stats` (a `nsim` x 2 matrix of density and contagion).

### Examples

```
set.seed(1)
net <- matrix(as.integer(runif(30 * 30) < 0.1), 30, 30)
net <- ((net + t(net)) > 0) * 1L      # undirected
diag(net) <- 0L
sim <- alaam_simulate(net, coef = c(density = -1, contagion = 0.3), nsim = 20L)
colMeans(sim$stats)
```

---

|                                |                                                               |
|--------------------------------|---------------------------------------------------------------|
| <code>cusna_abi_version</code> | <i>Native cusna engine: ABI version and CUDA availability</i> |
|--------------------------------|---------------------------------------------------------------|

---

### Description

`cusna_abi_version()` returns the C ABI version compiled into the package. `cusna_has_cuda()` returns TRUE when the package was built with the GPU path (a CUDA toolkit was detected at configure time) and a usable device is present; the CRAN CPU-only build always returns FALSE.

### Usage

```
cusna_abi_version()

cusna_has_cuda()
```

### Value

An integer (`cusna_abi_version`) or logical (`cusna_has_cuda`).

---

cusna\_behavior\_stats     *Host behavior evaluation statistics*


---

**Description**

Wrapper over the native cusna\_behavior\_stats, a port of behavior\_stats (RSiena convention 9: totSim subtracts nb\*simMean, avSim divides by nb, avAlt uses the full out-degree).

**Usage**

```
cusna_behavior_stats(z, bty, xnet, bkdist, zbar, brange, bsimmean)
```

**Arguments**

|                        |                                                                                                 |
|------------------------|-------------------------------------------------------------------------------------------------|
| z                      | Integer M*n matrix of end behavior values (rows = chains).                                      |
| bty                    | Integer vector (kb) of behavior effect type ids (0 linear, 1 quad, 2 avAlt, 3 avSim, 4 totSim). |
| xnet                   | Integer/logical n*n predictor network (start-of-period, less missing ties).                     |
| bkdist                 | Integer vector (n): 1 if the actor counts (kmask_dist).                                         |
| zbar, brange, bsimmean | Numeric: overall mean, range and simMean.                                                       |

**Value**

Numeric M\*kb matrix (rows = chains).

---

cusna\_effect     *Specify SAOM model effects*


---

**Description**

Constructors for the terms of a stochastic actor-oriented model. They return lightweight R objects; [mom\\_estimate](#) translates them into the native engine's effect descriptors at fit time.

**Usage**

```
cusna_effect(name, covariate = NULL, parameter = NULL, dyn = FALSE,
             type = c("eval", "creation", "endow"), net_ref = NULL)

cusna_beh_effect(name)

cusna_rate_effect(name, covariate = NULL)

cusna_interaction(components)
```

**Arguments**

|            |                                                                                                                                                                                                                                                                                                                                                                                                      |
|------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| name       | effect name. For <code>cusna_effect</code> , a structural effect (e.g. "density", "recip", "transTrip", the gwesp/gwdsp families), a covariate effect ("egoX", "altX", "simX", "sameX", ...), or a dyadic-covariate effect ("X"). For <code>cusna_beh_effect</code> , one of "linear", "quad", "avAlt", "avSim", "totSim". For <code>cusna_rate_effect</code> , one of "RateX", "outRate", "inRate". |
| covariate  | covariate values. Actor covariate: a numeric vector of length <i>n</i> (constant) or an <i>n</i> by (waves) matrix (changing). Dyadic covariate: an <i>n</i> by <i>n</i> matrix, or <i>n</i> by <i>n</i> by (periods) for a changing one. Centered by the engine.                                                                                                                                    |
| parameter  | optional internal effect parameter (RSiena's parameter); NULL uses the effect's default. The engine truncates this to an integer for gwesp/gwdsp/threshold effects, matching RSiena.                                                                                                                                                                                                                 |
| dyn        | logical; if TRUE the covariate is the co-evolving dependent behavior (choice dynamics use the current values, statistics use the start-of-period values).                                                                                                                                                                                                                                            |
| type       | effect type: "eval" (default), "creation", or "endow" (endowment).                                                                                                                                                                                                                                                                                                                                   |
| net_ref    | for cross-network effects in multi-network models (see <a href="#">mom_estimate_multinet</a> ), the 1-based index of the source network; NULL otherwise.                                                                                                                                                                                                                                             |
| components | for <code>cusna_interaction</code> , a length-2 or length-3 vector of 1-based positions of the component effects in the effects list. The components must appear earlier in that list.                                                                                                                                                                                                               |

**Value**

A lightweight specification object of class `cusna_effect`, `cusna_beh_effect`, `cusna_rate_effect`, or `cusna_interaction`, to be passed to [mom\\_estimate](#).

**See Also**

[mom\\_estimate](#), [saom\\_data](#).

**Examples**

```
effects <- list(
  cusna_effect("density"),
  cusna_effect("recip"),
  cusna_effect("transTrip")
)

# A covariate effect and a user interaction of effects 1 and 2.
alcohol <- runif(50)
list(
  cusna_effect("egoX", covariate = alcohol),
  cusna_effect("altX", covariate = alcohol),
  cusna_interaction(c(1, 2))
)

# Behavior and rate effects.
cusna_beh_effect("linear")
cusna_rate_effect("outRate")
```



cusna\_fit

*Fitted SAOM model***Description**

The object returned by `mom_estimate` and `mom_estimate_multinet`, with the usual R accessors.

**Usage**

```
## S3 method for class 'cusna_fit'
print(x, ...)

## S3 method for class 'cusna_fit'
summary(object, ...)

## S3 method for class 'cusna_fit'
coef(object, ...)

## S3 method for class 'cusna_fit'
vcov(object, ...)

## S3 method for class 'cusna_fit'
as.data.frame(x, ...)
```

**Arguments**

`x, object` a `cusna_fit` object.  
`...` ignored.

**Value**

`coef` returns the named parameter estimates; `vcov` the delta-method covariance matrix (whose diagonal squares to the reported standard errors); `as.data.frame` a data frame with columns `effect`, `estimate`, `se`, and `t_conv`. `print` and `summary` report the fit and return the object invisibly.

A `cusna_fit` is a list with elements `coefficients`, `se`, `tconv`, `estimates` (data frame), `rates` (conditional rate estimates, or `NULL`), `tconv_max`, `n_sims`, `wall_time`, `backend`, `conditional`, `targets`, `sim_means`, `D` (derivative matrix), and `msf` (moment covariance).

**See Also**

`mom_estimate`.

**Examples**

```
## Not run:
fit <- mom_estimate(dat, effects)
print(fit)
```

```
summary(fit)
coef(fit)
vcov(fit)
as.data.frame(fit)

## End(Not run)
```

cusna\_fran

*Native simulation backend for RSiena's siena07()*

## Description

Returns a FRAN closure that plugs the native SAOM simulator into the unmodified `RSiena::siena07()` estimator. `RSiena` keeps its full Robbins–Monro machinery (and hence its convergence behavior); only the network simulation runs on the compiled engine. The full bridge (mapping an arbitrary `siena07` effects object onto the native descriptors) is under development; this closure covers the structural and single-covariate effects named in `effect_names`.

## Usage

```
cusna_fran(waves, effect_names, covariate = NULL, conditional = TRUE)
```

## Arguments

|                           |                                                                                                                                          |
|---------------------------|------------------------------------------------------------------------------------------------------------------------------------------|
| <code>waves</code>        | a list of adjacency matrices (0/1), one per wave, matching the <code>RSiena</code> data object.                                          |
| <code>effect_names</code> | character vector of the included effect names, in the same order as the <code>RSiena</code> effects object rows (after the basic rates). |
| <code>covariate</code>    | optional actor-covariate values (numeric vector) used by the covariate effects ( <code>egoX/altX/simX/sameX/...</code> ).                |
| <code>conditional</code>  | logical; must match the <code>cond</code> setting of the <code>RSiena</code> algorithm.                                                  |

## Value

A function suitable for assignment to `alg$FRAN`.

## See Also

[mom\\_estimate](#) for the standalone native estimator.

## Examples

```
## Not run:
alg <- RSiena::sienaAlgorithmCreate(projname = NULL, cond = FALSE)
alg$FRAN <- cusna_fran(waves = list(w1, w2, w3),
                      effect_names = c("density", "recip", "transTrip"),
                      conditional = FALSE)
ans <- RSiena::siena07(alg, data = dat, effects = eff, useCluster = FALSE)
```

```
## End(Not run)
```

---

```
cusna_gof_distribution
```

*sienaGOF auxiliary distributions*

---

## Description

Wrapper over the native `cusna_gof_distribution` (port of `gof.py`): cumulative indegree/outdegree actor counts, or geodesic-distance ordered-pair counts for a batch of simulated end networks.

## Usage

```
cusna_gof_distribution(a, kind, levls)
```

## Arguments

|                    |                                                                           |
|--------------------|---------------------------------------------------------------------------|
| <code>a</code>     | Integer $M \times n \times n$ array of end networks (first dim = chains). |
| <code>kind</code>  | Integer: 0 indegree, 1 outdegree, 2 geodesic.                             |
| <code>levls</code> | Integer vector of cut levels.                                             |

## Value

Numeric matrix with  $M$  rows and  $\text{length}(\text{levls})$  columns (kind 0/1) or  $\text{length}(\text{levls}) + 1$  columns (kind 2, the extra column is the unreachable pair count).

---

```
cusna_network_stats
```

*Host network evaluation statistics (RSiena conventions)*

---

## Description

Thin R wrapper over the native `cusna_network_stats`, a bit-exact port of the reference `network_stats_ex`. On public datasets these statistics reproduce the RSiena targets to machine precision.

## Usage

```
cusna_network_stats(a, type_ids, p1, p2, vmat, vmiss, dyn_flags, vb,
                    od0, id0, wtab, symflag = 0L)
```

**Arguments**

|                        |                                                                                                                      |
|------------------------|----------------------------------------------------------------------------------------------------------------------|
| <code>a</code>         | Integer/logical $n \times n$ adjacency matrix (the masked statistic network (A & keep)   force), 0/1, zero diagonal. |
| <code>type_ids</code>  | Integer vector (k) of effect type ids.                                                                               |
| <code>p1, p2</code>    | Numeric vectors (k) of effect parameters 1 and 2.                                                                    |
| <code>vmat</code>      | Numeric $k \times n$ matrix of per-effect covariate values (rows = effects).                                         |
| <code>vmiss</code>     | Integer/logical $k \times n$ matrix of covariate missing flags.                                                      |
| <code>dyn_flags</code> | Integer vector (k): 1 if the effect covariate is behavior.                                                           |
| <code>vb</code>        | Numeric vector (n): centered start behavior (for dyn effects).                                                       |
| <code>od0, id0</code>  | Integer vectors (n): start out/in degrees.                                                                           |
| <code>wtab</code>      | Numeric $k \times (n+1)$ matrix of gwesp/gwdsp weight tables (rows = effects).                                       |
| <code>symflag</code>   | Integer: 1 for symmetric-network conventions (density halved).                                                       |

**Value**

Numeric vector of length k.

---

|                                |                                                               |
|--------------------------------|---------------------------------------------------------------|
| <code>cusna_set_threads</code> | <i>Set the OpenMP thread count for the native CPU backend</i> |
|--------------------------------|---------------------------------------------------------------|

---

**Description**

Explicitly caps the number of threads the CPU backend uses for its OpenMP-parallel batch loops (SAOM simulation, ERGM sampling and MPLE). Unlike `Sys.setenv(OMP_NUM_THREADS = ...)`, this takes effect immediately via the OpenMP runtime API and does not depend on when the environment variable would otherwise be read. Has no effect on a build without OpenMP (e.g. the default macOS toolchain without `libomp`).

**Usage**

```
cusna_set_threads(n)
```

**Arguments**

|                |                                                             |
|----------------|-------------------------------------------------------------|
| <code>n</code> | Requested thread count (coerced to an integer, at least 1). |
|----------------|-------------------------------------------------------------|

**Value**

Invisibly, the previous maximum thread count (0L if OpenMP is not compiled in).

**Examples**

```
old <- cusna_set_threads(1L)
cusna_set_threads(old)
```

ergm\_mcmle

*Maximum likelihood estimate of an ERGM (MCMC-MLE)***Description**

Fits an ERGM by MCMC maximum likelihood: an external moment-matching loop over the native TNT sampler. For the canonical exponential family the Fisher information is the covariance of the sufficient statistics, so each iteration simulates from the current parameters, forms the mean and covariance of the sufficient statistics, and takes a damped Newton step until the observed statistics are matched. The loop is pure R over the native engine (no Python). This closes the sampler + MPLE -> maximum likelihood gap; full MCMC-MLE for arbitrary specifications remains the domain of the ergm package.

**Usage**

```
ergm_mcmle(x, terms, attr = NULL, directed = FALSE, coef0 = NULL,
           nsim = 500L, burnin = NULL, interval = 1024L, maxit = 25L,
           tol = 0.1, damp = 0.5, seed = 1234L, verbose = FALSE)
```

**Arguments**

|                               |                                                                                                                                                                 |
|-------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <code>x</code>                | Integer/logical $n \times n$ observed adjacency (0/1, zero diagonal).                                                                                           |
| <code>terms</code>            | A non-empty list of <a href="#">ergm_term</a> objects.                                                                                                          |
| <code>attr</code>             | Optional numeric node covariate of length $n$ ; NULL for none.                                                                                                  |
| <code>directed</code>         | Logical: is the network directed?                                                                                                                               |
| <code>coef0</code>            | Optional starting parameters (default: edges from density, rest 0).                                                                                             |
| <code>nsim</code>             | Networks simulated per iteration (must exceed the number of terms).                                                                                             |
| <code>burnin, interval</code> | MCMC schedule per iteration; chains start from the observed network, so a modest burn-in decorrelates near the MLE. Default burn-in scales with the dyad count. |
| <code>maxit</code>            | Maximum outer iterations.                                                                                                                                       |
| <code>tol</code>              | Convergence: stop when every standardized deviation $ t $ is below it.                                                                                          |
| <code>damp</code>             | Step-length damping (Hummel-style partial stepping when far off).                                                                                               |
| <code>seed</code>             | Integer RNG seed.                                                                                                                                               |
| <code>verbose</code>          | Print the per-iteration trajectory.                                                                                                                             |

**Value**

An `ergm_mcmle` object with `coef`, `se` (from the inverse Fisher information), `tstat`, `iterations`, `converged`, `sim_mean` and `obs`.

**Examples**

```

set.seed(1)
a <- matrix(as.integer(runif(18 * 18) < 0.3), 18, 18)
diag(a) <- 0L
fit <- ergm_mcmle(a, list(ergm_term("edges"), ergm_term("mutual")),
                  directed = TRUE, nsim = 200L, seed = 1L)
fit

```

---

|           |                                                                                |
|-----------|--------------------------------------------------------------------------------|
| ergm_mple | <i>Maximum pseudo-likelihood estimate (directed edges/mutual/ttriple demo)</i> |
|-----------|--------------------------------------------------------------------------------|

---

**Description**

A logistic regression of tie presence on the dyadic change statistics the native engine computes (Strauss & Ikeda 1990). This is the MPLE demo for the three directed terms edges / mutual / transitive-triple; full MCMC-MLE stays with the ergm package (framing M-3).

**Usage**

```
ergm_mple(x)
```

**Arguments**

x                      Integer/logical n\*n directed adjacency matrix (0/1, zero diagonal).

**Value**

A named numeric vector of pseudo-MLE coefficients (edges, mutual, transitive).

**Examples**

```

set.seed(1)
a <- matrix(as.integer(runif(20 * 20) < 0.2), 20, 20)
diag(a) <- 0L
ergm_mple(a)

```

---

|               |                                                     |
|---------------|-----------------------------------------------------|
| ergm_simulate | <i>Simulate networks from an ERGM (TNT sampler)</i> |
|---------------|-----------------------------------------------------|

---

## Description

Draws `nsim` independent networks with the native TNT Metropolis sampler (the CPU mirror, validated distributionally against `ergm::simulate`) and returns their sufficient statistics. Full MCMC-MLE for ERGMs remains the domain of the `ergm` package; `cusna` provides the simulator and MPLE.

## Usage

```
ergm_simulate(x, coef, terms, nsim = 100, attr = NULL, directed = FALSE,
              burnin = 16384L, interval = 1024L, seed = 1234L,
              return_nets = FALSE)
```

## Arguments

|                               |                                                                                                                                               |
|-------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------|
| <code>x</code>                | Integer/logical $n \times n$ start adjacency matrix (0/1, zero diagonal).                                                                     |
| <code>coef</code>             | Numeric vector of natural parameters, one per term.                                                                                           |
| <code>terms</code>            | A non-empty list of <a href="#">ergm_term</a> objects.                                                                                        |
| <code>nsim</code>             | Number of independent chains / simulated networks.                                                                                            |
| <code>attr</code>             | Optional numeric node covariate of length $n$ ; NULL for none.                                                                                |
| <code>directed</code>         | Logical: is the network directed?                                                                                                             |
| <code>burnin, interval</code> | Metropolis burn-in and interval; raise the burn-in to $\sim 10 \times$ the dyad count for large networks so chains forget the observed start. |
| <code>seed</code>             | Integer RNG seed.                                                                                                                             |
| <code>return_nets</code>      | Logical: if TRUE, also return the simulated networks.                                                                                         |

## Value

If `return_nets = FALSE` (default) a `nsim` x `length(terms)` matrix of sampled statistics (named columns). If `return_nets = TRUE`, a list with `stats` (that matrix) and `nets` (a list of `nsim`  $n \times n$  integer adjacency matrices, one per simulated network).

## Examples

```
a <- matrix(0L, 6, 6)
a[1, 2] <- a[2, 1] <- a[2, 3] <- a[3, 2] <- 1L
sf <- ergm_simulate(a, coef = -1, terms = list(ergm_term("edges")),
                   nsim = 8, burnin = 2000L, seed = 1L)
colMeans(sf)
```

---

|            |                                              |
|------------|----------------------------------------------|
| ergm_stats | <i>Observed ERGM statistics of a network</i> |
|------------|----------------------------------------------|

---

### Description

Native host statistics for the ERGM term list, a bit-exact port of the reference `network_stats_ergm` (validated to machine zero in `native/test`).

### Usage

```
ergm_stats(x, terms, attr = NULL, directed = FALSE)
```

### Arguments

|                       |                                                                                                             |
|-----------------------|-------------------------------------------------------------------------------------------------------------|
| <code>x</code>        | Integer/logical $n \times n$ adjacency matrix (0/1, zero diagonal).                                         |
| <code>terms</code>    | A non-empty list of <a href="#">ergm_term</a> objects.                                                      |
| <code>attr</code>     | Optional numeric node covariate of length $n$ (for <code>nodecov/nodematch/absdiff</code> ); NULL for none. |
| <code>directed</code> | Logical: is the network directed (enables mutual)?                                                          |

### Value

A named numeric vector of length `length(terms)`.

### Examples

```
a <- matrix(0L, 4, 4)
a[1, 2] <- a[2, 1] <- a[2, 3] <- a[3, 2] <- 1L
ergm_stats(a, list(ergm_term("edges")))
```

---

|           |                               |
|-----------|-------------------------------|
| ergm_term | <i>Construct an ERGM term</i> |
|-----------|-------------------------------|

---

### Description

Construct an ERGM term for use with [ergm\\_stats](#) and [ergm\\_simulate](#).

### Usage

```
ergm_term(name, parameter = 0)
```



**Arguments**

|           |                                                                                                                                                                                     |
|-----------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| name      | A single ERGM term name: one of edges, mutual, nodecov, nodematch, absdiff, gwesp, gwdsp, or the temporal (tergm-only) terms memory (lagged tie) and delrecip (lagged reciprocity). |
| parameter | Numeric term parameter (e.g. the gwesp/gwdsp decay); ignored by terms that take none.                                                                                               |

**Value**

An `ergm_term` object.

**Examples**

```
ergm_term("edges")
ergm_term("gwesp", 0.25)
```

---

mom\_estimate

*Method-of-Moments estimation of a SAOM*


---

**Description**

Fits a stochastic actor-oriented model by the RSiena-style method of moments (Robbins–Monro), driving the compiled native simulator – no Python. The moment targets and per-period masks reproduce the reference implementation bit-for-bit; the estimates agree with the reference estimator within simulation standard errors.

**Usage**

```
mom_estimate(data, effects, beh_effects = NULL, rate_effects = NULL,
             conditional = FALSE, backend = c("cpu", "gpu"), maxdegree = 0,
             control = mom_control(), verbose = FALSE)

mom_control(firstg = 0.4, nsub = 4, n2 = c(40, 40, 60, 80),
            batch2 = 256, n1 = 1000, n3 = 4000, nD = 1000,
            diagonalize = 0.2, seed = 1234)
```

**Arguments**

|              |                                                                                                                                                                                                    |
|--------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| data         | a <code>cusna_data</code> object from <a href="#">saom_data</a> .                                                                                                                                  |
| effects      | a non-empty list of <a href="#">cusna_effect</a> objects (network evaluation/creation/endowment effects) and, optionally, <a href="#">cusna_interaction</a> objects placed after their components. |
| beh_effects  | optional list of <a href="#">cusna_beh_effect</a> objects for network–behavior co-evolution (requires behavior in the data; forces unconditional estimation).                                      |
| rate_effects | optional list of <a href="#">cusna_rate_effect</a> objects (outRate/inRate/RateX); unconditional only.                                                                                             |

|             |                                                                                                                                                                                                                                            |
|-------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| conditional | logical; FALSE (default) estimates the basic rate parameters jointly with the evaluation effects. TRUE conditions each period on the observed distance (RSiena's default for a single dependent network) and reports the rates separately. |
| backend     | "cpu" (default; the from-source CRAN build) or "gpu" (needs a CUDA build).                                                                                                                                                                 |
| maxdegree   | optional maximum out-degree constraint (0 = none).                                                                                                                                                                                         |
| control     | a list of tuning parameters from mom_control.                                                                                                                                                                                              |
| verbose     | logical; if TRUE, print per-phase progress.                                                                                                                                                                                                |
| firstg      | initial Robbins–Monro gain.                                                                                                                                                                                                                |
| nsub        | number of phase-2 subphases.                                                                                                                                                                                                               |
| n2          | integer vector (length >= nsub) of phase-2 iteration counts per subphase.                                                                                                                                                                  |
| batch2      | simulation batch size within phase-2 iterations.                                                                                                                                                                                           |
| n1          | number of phase-1 simulations (derivative estimation).                                                                                                                                                                                     |
| n3          | number of phase-3 simulations (standard errors and convergence).                                                                                                                                                                           |
| nD          | simulations used to re-estimate the derivative each subphase.                                                                                                                                                                              |
| diagonalize | shrinkage of the derivative matrix towards its diagonal, in [0, 1]; higher is more robust on ill-conditioned models.                                                                                                                       |
| seed        | random seed for the simulation stream.                                                                                                                                                                                                     |

## Details

For nearly collinear specifications the Robbins–Monro estimator may not converge from a cold start; increase diagonalize or the phase counts. The estimator currently drives the CPU simulator; the CUDA path of the engine is exposed through the lower-level statistics entry points.

## Value

mom\_estimate returns a [cusna\\_fit](#) object. mom\_control returns a list of tuning parameters (class cusna\_control).

## See Also

[cusna\\_fit](#), [cusna\\_effect](#), [saom\\_data](#), [mom\\_estimate\\_multinet](#), [cusna\\_fran](#).

## Examples

```
# A small two-wave panel; tiny simulation counts keep the example fast.
set.seed(7)
w1 <- matrix(as.integer(runif(400) < 0.12), 20, 20); diag(w1) <- 0L
w2 <- w1; flip <- sample(400, 40); w2[flip] <- 1L - w2[flip]; diag(w2) <- 0L
dat <- saom_data(list(w1, w2))

fit <- mom_estimate(
  dat,
  effects = list(cusna_effect("density"), cusna_effect("recip")),
  control = mom_control(n1 = 100, nsub = 1, n2 = 10, batch2 = 50, n3 = 200))
summary(fit)
coef(fit)
```

saom\_data

*Create a SAOM data panel***Description**

Builds a longitudinal network panel for estimation, applying RSiena's imputation and per-period masks (first-wave missings to 0, later waves carried forward; structural values fixed; composition-change gating) in native R code – no Python. The construction is validated bit-for-bit against the reference implementation on public datasets.

**Usage**

```
saom_data(waves, behavior = NULL, composition = NULL, cc_option = 1)
```

**Arguments**

|             |                                                                                                                                                                                                                                                               |
|-------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| waves       | a list of at least two square adjacency matrices, one per observation wave, all on the same actor set. Missing ties are NA (or the code 9); structural zeros and ones are the codes 10 and 11.                                                                |
| behavior    | optional co-evolving dependent behavior: a numeric matrix with one row per actor and one column per wave (NA for missing).                                                                                                                                    |
| composition | optional composition change (joiners/leavers): a list with one entry per actor, each a numeric vector <code>c(start, end)</code> (or several stacked pairs) of 1-based wave numbers the actor is present for. Estimation is then unconditional, as in RSiena. |
| cc_option   | the <code>sienaCompositionChange</code> option (1–3) controlling how absent actors' entries are treated.                                                                                                                                                      |

**Value**

An object of class `cusna_data` with fields `n` (actors), `n_waves`, and `n_periods`, carrying the prepared engine data in `$internal`.

**See Also**

[mom\\_estimate](#), [cusna\\_effect](#), [saom\\_multinet\\_data](#).

**Examples**

```
set.seed(1)
w1 <- matrix(as.integer(runif(400) < 0.1), 20, 20); diag(w1) <- 0L
w2 <- w1; flip <- sample(400, 30); w2[flip] <- 1L - w2[flip]; diag(w2) <- 0L
dat <- saom_data(list(w1, w2))
dat
```

---

|                    |                                   |
|--------------------|-----------------------------------|
| saom_multinet_data | <i>Multi-network co-evolution</i> |
|--------------------|-----------------------------------|

---

## Description

Several dependent networks that co-evolve over one actor set, with cross-network effects. `saom_multinet_data` builds the panel and `mom_estimate_multinet` fits it by the method of moments on the native multi-network simulator (unconditional only, as in RSiena for more than one dependent variable).

## Usage

```
saom_multinet_data(waves_list, composition = NULL, cc_option = 1)

mom_estimate_multinet(data, effects_by_net, backend = c("cpu", "gpu"),
                      control = mom_control(), verbose = FALSE)
```

## Arguments

|                             |                                                                                                                                                                                                                                                                                     |
|-----------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <code>waves_list</code>     | a list with one entry per dependent network; each entry is itself a list of wave matrices (as in <a href="#">saom_data</a> ). All networks share the actor set and the number of waves.                                                                                             |
| <code>composition</code>    | optional composition change applied to the shared actor set (see <a href="#">saom_data</a> ).                                                                                                                                                                                       |
| <code>cc_option</code>      | the composition-change option (1–3).                                                                                                                                                                                                                                                |
| <code>data</code>           | a <code>cusna_multinet_data</code> object.                                                                                                                                                                                                                                          |
| <code>effects_by_net</code> | a list with one effects list per network. Within-network effects are ordinary <a href="#">cusna_effect</a> objects; cross-network effects ("crprod", "crprodRecip", "crprodMutual", "from", "to") additionally take <code>net_ref</code> , the 1-based index of the source network. |
| <code>backend</code>        | "cpu" (default) or "gpu".                                                                                                                                                                                                                                                           |
| <code>control</code>        | tuning parameters from <a href="#">mom_control</a> .                                                                                                                                                                                                                                |
| <code>verbose</code>        | logical; print per-phase progress.                                                                                                                                                                                                                                                  |

## Details

Cross-network statistics read the other network at its period-start state; the dynamics read the current co-evolving state. Multi-network models do not support behavior co-evolution, interactions, or degree bounds.

## Value

`saom_multinet_data` returns a `cusna_multinet_data` object. `mom_estimate_multinet` returns a [cusna\\_fit](#); its parameters are laid out per network (rates then effects), following RSiena's convention.

**See Also**

[mom\\_estimate](#), [cusna\\_effect](#).

**Examples**

```
# Building the container is plain R.
set.seed(11)
mk <- function() { m <- matrix(as.integer(runif(400) < 0.1), 20, 20); diag(m) <- 0L; m }
x1 <- mk(); x2 <- mk(); w1 <- mk(); w2 <- mk()
dat <- saom_multinet_data(list(list(x1, x2), list(w1, w2)))
dat

## Not run:
# Fitting drives the native multi-network simulator.
fit <- mom_estimate_multinet(dat, effects_by_net = list(
  list(cusna_effect("density"), cusna_effect("recip")),
  list(cusna_effect("density"), cusna_effect("recip"))
))
summary(fit)

## End(Not run)
```

---

stergm\_cmle

---

*Separable temporal ERGM by conditional MLE (STERGM CMLE)*


---

**Description**

Fits a STERGM (Krivitsky & Handcock 2014) to a network sequence by conditional maximum likelihood. Each transition separates into two conditionally independent ERGMs on discord-constrained networks: a formation model on the union (only dyads absent at t-1 are free to toggle) and a dissolution model on the intersection (only dyads present at t-1 are free), the latter in the persistence parameterisation (positive coefficients favour tie persistence, matching `tergm`'s `Persist()`). The CMLE is two ERGM MCMC-MLE fits (a reuse of [ergm\\_mcmle](#)) with the native TNT sampler restricted to the free dyads; statistics are pooled across transitions. Python-free (CPU engine).

**Usage**

```
stergm_cmle(nets, formation, dissolution = formation, attr = NULL,
            directed = TRUE, nsim = 500L, burnin = NULL, interval = 1024L,
            maxit = 30L, tol = 0.1, damp = 0.5, seed = 1234L, verbose = FALSE)
```

**Arguments**

|                          |                                                                                                                        |
|--------------------------|------------------------------------------------------------------------------------------------------------------------|
| <code>nets</code>        | A list of $\geq 2$ $n \times n$ adjacency matrices (0/1, zero diagonal), in time order.                                |
| <code>formation</code>   | A non-empty list of <code>[ergm_term()]</code> objects for the formation model.                                        |
| <code>dissolution</code> | A list of <code>[ergm_term()]</code> objects for the dissolution (persistence) model; defaults to the formation terms. |

|                  |                                                                                             |
|------------------|---------------------------------------------------------------------------------------------|
| attr             | Optional numeric node covariate of length n (for nodecov/nodematch/absdiff); NULL for none. |
| directed         | Logical: are the networks directed?                                                         |
| nsim             | Networks simulated per iteration per transition.                                            |
| burnin, interval | MCMC schedule (default burn-in scales with the dyad count).                                 |
| maxit, tol, damp | Outer iterations, convergence tolerance and step damping.                                   |
| seed             | Integer RNG seed.                                                                           |
| verbose          | Print the per-iteration trajectory.                                                         |

### Value

A `stergm_cmle` object with formation and dissolution sub-fits (each a list with `coef`, `se`, `tstat`, `iterations`, `converged`, `sim_mean`, `obs`) and transitions.

### Examples

```
set.seed(1)
base <- matrix(as.integer(runif(20 * 20) < 0.2), 20, 20)
diag(base) <- 0L
nets <- list(base)
for (t in 2:3) {
  nx <- base
  flip <- matrix(runif(20 * 20) < 0.1, 20, 20)
  nx[flip] <- 1L - nx[flip]
  diag(nx) <- 0L
  nets[[t]] <- nx
  base <- nx
}
fit <- stergm_cmle(nets, formation = list(ergm_term("edges"), ergm_term("mutual")),
                  nsim = 200L, maxit = 20L)
fit
```

---

tergm\_mple

*Temporal ERGM by bootstrap pseudo-likelihood (btergm style)*


---

### Description

Fits a temporal ERGM to a sequence of directed networks by pooled maximum pseudo-likelihood – the `btergm` estimator (Desmarais & Cranmer 2012). For every transition the native engine builds the 0->1 change statistics of every dyad of the current network (edges / mutual / transitive triple) and the temporal terms are read off the lagged network (memory = lagged tie, `delrecip` = lagged reciprocity); the rows are pooled across transitions and fit by weighted logistic regression, with bootstrap confidence intervals. The design matrix is host C++ (no Python; works in the CPU-only build).

**Usage**

```
tergm_mple(nets, mutual = TRUE, ttriple = TRUE, memory = TRUE,
           delrecip = TRUE, R = 200L, level = 0.95, seed = 1234L)
```

**Arguments**

**nets** A list of  $\geq 2$  directed  $n \times n$  adjacency matrices (0/1, zero diagonal), in time order.

**mutual, ttriple** Include the cross-sectional mutual / transitive-triple terms (from the native change-statistic matrix).

**memory, delrecip** Include the temporal terms (lagged tie / lagged reciprocity).

**R** Bootstrap replications for the confidence intervals.

**level** Confidence level for the bootstrap intervals.

**seed** Integer RNG seed for the bootstrap.

**Value**

A `tergm_mple` object with `coef`, `ci` (bootstrap interval), `boot` (replicate coefficients), `nobs` (pooled dyads) and transitions.

**Examples**

```
set.seed(1)
nets <- lapply(1:3, function(t) {
  m <- matrix(as.integer(runif(20 * 20) < 0.2), 20, 20)
  diag(m) <- 0L
  m
})
fit <- tergm_mple(nets, R = 50L)
fit
```

---

|                             |                                                                          |
|-----------------------------|--------------------------------------------------------------------------|
| <code>tergm_simulate</code> | <i>Simulate from a temporal ERGM (TNT sampler with a lagged network)</i> |
|-----------------------------|--------------------------------------------------------------------------|

---

**Description**

Draws `nsim` directed networks from the conditional ERGM of the current wave given the previous one, with the native CPU TNT sampler. The term list may mix the cross-sectional ERGM terms (edges, mutual, nodecov, nodematch, absdiff) with the temporal terms `memory` (lagged tie) and `delrecip` (lagged reciprocity). Python-free (CPU engine). The pooled estimator is [tergm\\_mple](#).

**Usage**

```
tergm_simulate(x_start, lag, coef, terms = NULL, attr = NULL,
              mutual = TRUE, memory = TRUE, delrecip = TRUE,
              nsim = 100, burnin = NULL, seed = 1234L,
              return_nets = FALSE)
```

**Arguments**

|                                       |                                                                                                                                                                                                            |
|---------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <code>x_start</code>                  | Integer/logical $n \times n$ start adjacency (0/1, zero diagonal), the chain's starting state.                                                                                                             |
| <code>lag</code>                      | Integer/logical $n \times n$ lagged network (the previous wave).                                                                                                                                           |
| <code>coef</code>                     | Numeric parameters, one per active term (matching terms, or the legacy order edges, [mutual], [memory], [delrecip] when terms is NULL).                                                                    |
| <code>terms</code>                    | A list of <a href="#">ergm_term</a> objects (may include the temporal terms memory / delrecip). If NULL (default) the term list is assembled from the deprecated logical flags for backward compatibility. |
| <code>attr</code>                     | Optional numeric node covariate of length $n$ (for the nodecov / nodematch / absdiff cross-sectional terms); NULL for none.                                                                                |
| <code>mutual, memory, delrecip</code> | Deprecated: include the corresponding term. Used only when terms is NULL; the assembled order is edges, mutual, memory, delrecip.                                                                          |
| <code>nsim</code>                     | Number of independent chains / simulated networks.                                                                                                                                                         |
| <code>burnin</code>                   | MCMC burn-in per chain (default scales with the dyad count).                                                                                                                                               |
| <code>seed</code>                     | Integer RNG seed.                                                                                                                                                                                          |
| <code>return_nets</code>              | Logical: if TRUE, also return the simulated networks.                                                                                                                                                      |

**Value**

If `return_nets = FALSE` (default) a `nsim x k` matrix of sampled statistics (named columns). If `return_nets = TRUE`, a list with `stats` (that matrix) and `nets` (a list of `nsim`  $n \times n$  integer adjacency matrices).

**Examples**

```
set.seed(1)
lag <- matrix(as.integer(runif(20 * 20) < 0.2), 20, 20); diag(lag) <- 0L
sf <- tergm_simulate(lag, lag, coef = c(-2, 1, 1.5, 0.5), nsim = 20,
                    burnin = 3000L, seed = 1L)
colMeans(sf)
```



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