

Package: binaryGP (via r-universe)

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Type Package

Title Fit and Predict a Gaussian Process Model with (Time-Series)
Binary Response

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Description Allows the estimation and prediction for binary Gaussian process model. The mean function can be assumed to have time-series structure. The estimation methods for the unknown parameters are based on penalized quasi-likelihood/penalized quasi-partial likelihood and restricted maximum likelihood. The predicted probability and its confidence interval are computed by Metropolis-Hastings algorithm. More details can be seen in Sung et al (2017) <[arXiv:1705.02511](#)>.

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LazyData TRUE

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Contents

| | |
|----------------------------|---|
| binaryGP_fit | 2 |
| predict.binaryGP | 5 |
| print.binaryGP | 7 |
| summary.binaryGP | 9 |

| | |
|--------------|---|
| binaryGP_fit | <i>Binary Gaussian Process (with/without time-series)</i> |
|--------------|---|

Description

The function fits Gaussian process models with binary response. The models can also include time-series term if a time-series binary response is observed. The estimation methods are based on PQL/PQPL and REML (for mean function and correlation parameter, respectively).

Usage

```
binaryGP_fit(X, Y, R = 0, L = 0, corr = list(type = "exponential", power =
  2), nugget = 1e-10, constantMean = FALSE, orthogonalGP = FALSE,
  converge.tol = 1e-10, maxit = 15, maxit.PQPL = 20, maxit.REML = 100,
  xtol_rel = 1e-10, standardize = FALSE, verbose = TRUE)
```

Arguments

| | |
|--------------|--|
| X | a design matrix with dimension n by d. |
| Y | a response matrix with dimension n by T. The values in the matrix are 0 or 1. If no time-series, T = 1. If time-series is included, i.e., T > 1, the first column is the response vector of time 1, and second column is the response vector of time 2, and so on. |
| R | a positive integer specifying the order of autoregression only if time-series is included. The default is 1. |
| L | a positive integer specifying the order of interaction between X and previous Y only if time-series is included. The value couldn't nbe larger than R. The default is 1. |
| corr | a list of parameters for the specifying the correlation to be used. Either exponential correlation function or Matern correlation function can be used. See corr_matrix for details. |
| nugget | a positive value to use for the nugget. If NULL, a nugget will be estimated. The default is 1e-10. |
| constantMean | logical. TRUE indicates that the Gaussian process will have a constant mean, plus time-series structure if R or T is greater than one; otherwise the mean function will be a linear regression in X, plus an intercept term and time-series structure. |
| orthogonalGP | logical. TRUE indicates that the orthogonal Gaussian process will be used. Only available when corr is list(type = "exponential", power = 2). |
| converge.tol | convergence tolerance. It converges when relative difference with respect to η_t is smaller than the tolerance. The default is 1e-10. |
| maxit | a positive integer specifying the maximum number of iterations for estimation to be performed before the estimates are convergent. The default is 15. |

| | |
|-------------|--|
| maxit.PQPL | a positive integer specifying the maximum number of iterations for PQL/PQPL estimation to be performed before the estimates are convergent. The default is 20. |
| maxit.REML | a positive integer specifying the maximum number of iterations in lbfgs for REML estimation to be performed before the estimates are convergent. The default is 100. |
| xtol_rel | a positive value specifying the convergence tolerance for lbfgs. The default is 1e-10. |
| standardize | logical. If TRUE, each column of X will be standardized into $[0, 1]$. The default is FALSE. |
| verbose | logical. If TRUE, additional diagnostics are printed. The default is TRUE. |

Details

Consider the model

$$\text{logit}(p_t(x)) = \eta_t(x) = \sum_{r=1}^R \varphi_r y_{t-r}(\mathbf{x}) + \alpha_0 + \mathbf{x}'\boldsymbol{\alpha} + \sum_{l=1}^L \gamma_l \mathbf{x} y_{t-l}(\mathbf{x}) + Z_t(\mathbf{x}),$$

where $p_t(x) = Pr(y_t(x) = 1)$ and $Z_t(\cdot)$ is a Gaussian process with zero mean, variance σ^2 , and correlation function $R_{\boldsymbol{\theta}}(\cdot, \cdot)$ with unknown correlation parameters $\boldsymbol{\theta}$. The power exponential correlation function is used and defined by

$$R_{\boldsymbol{\theta}}(\mathbf{x}_i, \mathbf{x}_j) = \exp\left\{-\sum_{l=1}^d \frac{(x_{il} - x_{jl})^p}{\theta_l}\right\},$$

where p is given by power. The parameters in the mean functions including $\varphi_r, \alpha_0, \boldsymbol{\alpha}, \gamma_l$ are estimated by PQL/PQPL, depending on whether the mean function has the time-series structure. The parameters in the Gaussian process including $\boldsymbol{\theta}$ and σ^2 are estimated by REML. If orthogonalGP is TRUE, then orthogonal covariance function (Plumlee and Joseph, 2016) is employed. More details can be seen in Sung et al. (unpublished).

Value

| | |
|--------------|--|
| alpha_hat | a vector of coefficient estimates for the linear relationship with X. |
| varphi_hat | a vector of autoregression coefficient estimates. |
| gamma_hat | a vector of the interaction effect estimates. |
| theta_hat | a vector of correlation parameters. |
| sigma_hat | a value of sigma estimate (standard deviation). |
| nugget_hat | if nugget is NULL, then return a nugget estimate, otherwise return nugget. |
| orthogonalGP | orthogonalGP. |
| X | data X. |
| Y | data Y. |
| R | order of autoregression. |
| L | order of interaction between X and previous Y. |

| | |
|-------------|--|
| corr | a list of parameters for the specifying the correlation to be used. |
| Model.mat | model matrix. |
| eta_hat | eta_hat. |
| standardize | standardize. |
| mean.x | mean of each column of X. Only available when standardize=TRUE, otherwise mean.x=NULL. |
| scale.x | max(x)-min(x) of each column of X. Only available when standardize=TRUE, otherwise scale.x=NULL. |

Author(s)

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See Also

[predict.binaryGP](#) for prediction of the binary Gaussian process, [print.binaryGP](#) for the list of estimation results, and [summary.binaryGP](#) for summary of significance results.

Examples

```
library(binaryGP)

#####      Testing function: cos(x1 + x2) * exp(x1*x2) with TT sequences      #####
#####      Thanks to Sonja Surjanovic and Derek Bingham, Simon Fraser University #####
test_function <- function(X, TT)
{
  x1 <- X[,1]
  x2 <- X[,2]

  eta_1 <- cos(x1 + x2) * exp(x1*x2)

  p_1 <- exp(eta_1)/(1+exp(eta_1))
  y_1 <- rep(NA, length(p_1))
  for(i in 1:length(p_1)) y_1[i] <- rbinom(1,1,p_1[i])
  Y <- y_1
  P <- p_1
  if(TT > 1){
    for(tt in 2:TT){
      eta_2 <- 0.3 * y_1 + eta_1
      p_2 <- exp(eta_2)/(1+exp(eta_2))
      y_2 <- rep(NA, length(p_2))
      for(i in 1:length(p_2)) y_2[i] <- rbinom(1,1,p_2[i])
      Y <- cbind(Y, y_2)
      P <- cbind(P, p_2)
      y_1 <- y_2
    }
  }

  return(list(Y = Y, P = P))
}
```

```

set.seed(1)
n <- 30
n.test <- 10
d <- 2
X <- matrix(runif(d * n), ncol = d)

##### without time-series #####
Y <- test_function(X, 1)$Y ## Y is a vector

binaryGP.model <- binaryGP_fit(X = X, Y = Y)
print(binaryGP.model) # print estimation results
summary(binaryGP.model) # significance results

##### with time-series, lag 1 #####
Y <- test_function(X, 10)$Y ## Y is a matrix with 10 columns

binaryGP.model <- binaryGP_fit(X = X, Y = Y, R = 1)
print(binaryGP.model) # print estimation results
summary(binaryGP.model) # significance results

```

predict.binaryGP

Predictions of Binary Gaussian Process

Description

The function computes the predicted response and its variance as well as its confidence interval.

Usage

```

## S3 method for class 'binaryGP'
predict(object, xnew, conf.level = 0.95,
        sim.number = 101, ...)

```

Arguments

| | |
|------------|--|
| object | a class binaryGP object estimated by binaryGP_fit. |
| xnew | a testing matrix with dimension n_new by d in which each row corresponds to a predictive location. |
| conf.level | a value from 0 to 1 specifying the level of confidence interval. The default is 0.95. |
| sim.number | a positive integer specifying the simulation number for Monte-Carlo method. The default is 101. |
| ... | for compatibility with generic method predict. |

Value

| | |
|--------------|---|
| mean | a matrix with dimension <code>n_new</code> by <code>T</code> displaying predicted responses at locations <code>xnew</code> . |
| var | a matrix with dimension <code>n_new</code> by <code>T</code> displaying predictive variances at locations <code>xnew</code> . |
| upper .bound | a matrix with dimension <code>n_new</code> by <code>T</code> displaying upper bounds with <code>conf.level</code> confidence level. |
| lower .bound | a matrix with dimension <code>n_new</code> by <code>T</code> displaying lower bounds with <code>conf.level</code> confidence level. |
| y_pred | a matrix with dimension <code>n_new</code> by <code>T</code> displaying predicted binary responses at locations <code>xnew</code> . |

Author(s)

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See Also

[binaryGP_fit](#) for estimation of the binary Gaussian process.

Examples

```
library(binaryGP)

#####      Testing function: cos(x1 + x2) * exp(x1*x2) with TT sequences      #####
#####      Thanks to Sonja Surjanovic and Derek Bingham, Simon Fraser University #####
test_function <- function(X, TT)
{
  x1 <- X[,1]
  x2 <- X[,2]

  eta_1 <- cos(x1 + x2) * exp(x1*x2)

  p_1 <- exp(eta_1)/(1+exp(eta_1))
  y_1 <- rep(NA, length(p_1))
  for(i in 1:length(p_1)) y_1[i] <- rbinom(1,1,p_1[i])
  Y <- y_1
  P <- p_1
  if(TT > 1){
    for(tt in 2:TT){
      eta_2 <- 0.3 * y_1 + eta_1
      p_2 <- exp(eta_2)/(1+exp(eta_2))
      y_2 <- rep(NA, length(p_2))
      for(i in 1:length(p_2)) y_2[i] <- rbinom(1,1,p_2[i])
      Y <- cbind(Y, y_2)
      P <- cbind(P, p_2)
      y_1 <- y_2
    }
  }
}
```

```

    return(list(Y = Y, P = P))
  }

  set.seed(1)
  n <- 30
  n.test <- 10
  d <- 2
  X <- matrix(runif(d * n), ncol = d)
  X.test <- matrix(runif(d * n.test), ncol = d)

  ##### without time-series #####
  Y <- test_function(X, 1)$Y ## Y is a vector
  test.out <- test_function(X.test, 1)
  Y.test <- test.out$Y
  P.true <- test.out$P

  # fitting
  binaryGP.model <- binaryGP_fit(X = X, Y = Y)

  # prediction
  binaryGP.prediction <- predict(binaryGP.model, xnew = X.test)
  print(binaryGP.prediction$mean)
  print(binaryGP.prediction$var)
  print(binaryGP.prediction$upper.bound)
  print(binaryGP.prediction$lower.bound)

  ##### with time-series #####
  Y <- test_function(X, 10)$Y ## Y is a matrix with 10 columns
  test.out <- test_function(X.test, 10)
  Y.test <- test.out$Y
  P.true <- test.out$P

  # fitting
  binaryGP.model <- binaryGP_fit(X = X, Y = Y, R = 1)

  # prediction
  binaryGP.prediction <- predict(binaryGP.model, xnew = X.test)
  print(binaryGP.prediction$mean)
  print(binaryGP.prediction$var)
  print(binaryGP.prediction$upper.bound)
  print(binaryGP.prediction$lower.bound)

```

print.binaryGP

Print Fitted results of Binary Gaussian Process

Description

The function shows the estimation results by `binaryGP_fit`.

Usage

```
## S3 method for class 'binaryGP'
print(x, ...)
```

Arguments

`x` a class binaryGP object estimated by binaryGP_fit.
`...` for compatibility with generic method print.

Value

a list of estimates by binaryGP_fit.

Author(s)

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See Also

[binaryGP_fit](#) for estimation of the binary Gaussian process.

Examples

```
library(binaryGP)

#####      Testing function: cos(x1 + x2) * exp(x1*x2) with TT sequences      #####
#####      Thanks to Sonja Surjanovic and Derek Bingham, Simon Fraser University #####
test_function <- function(X, TT)
{
  x1 <- X[,1]
  x2 <- X[,2]

  eta_1 <- cos(x1 + x2) * exp(x1*x2)

  p_1 <- exp(eta_1)/(1+exp(eta_1))
  y_1 <- rep(NA, length(p_1))
  for(i in 1:length(p_1)) y_1[i] <- rbinom(1,1,p_1[i])
  Y <- y_1
  P <- p_1
  if(TT > 1){
    for(tt in 2:TT){
      eta_2 <- 0.3 * y_1 + eta_1
      p_2 <- exp(eta_2)/(1+exp(eta_2))
      y_2 <- rep(NA, length(p_2))
      for(i in 1:length(p_2)) y_2[i] <- rbinom(1,1,p_2[i])
      Y <- cbind(Y, y_2)
      P <- cbind(P, p_2)
      y_1 <- y_2
    }
  }
}
```



```

    return(list(Y = Y, P = P))
  }

  set.seed(1)
  n <- 30
  n.test <- 10
  d <- 2
  X <- matrix(runif(d * n), ncol = d)

  ##### without time-series #####
  Y <- test_function(X, 1)$Y ## Y is a vector

  binaryGP.model <- binaryGP_fit(X = X, Y = Y)
  print(binaryGP.model) # print estimation results
  summary(binaryGP.model) # significance results

  ##### with time-series, lag 1 #####
  Y <- test_function(X, 10)$Y ## Y is a matrix with 10 columns

  binaryGP.model <- binaryGP_fit(X = X, Y = Y, R = 1)
  print(binaryGP.model) # print estimation results
  summary(binaryGP.model) # significance results

```

summary.binaryGP

Summary of Fitting a Binary Gaussian Process

Description

The function summarizes estimation and significance results by `binaryGP_fit`.

Usage

```
## S3 method for class 'binaryGP'
summary(object, ...)
```

Arguments

| | |
|---------------------|---|
| <code>object</code> | a class <code>binaryGP</code> object estimated by <code>binaryGP_fit</code> . |
| <code>...</code> | for compatibility with generic method <code>summary</code> . |

Value

A table including the estimates by `binaryGP_fit`, and the corresponding standard deviations, Z-values and p-values.

Author(s)

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See Also

[binaryGP_fit](#) for estimation of the binary Gaussian process.

Examples

```
library(binaryGP)

##### Testing function: cos(x1 + x2) * exp(x1*x2) with TT sequences #####
##### Thanks to Sonja Surjanovic and Derek Bingham, Simon Fraser University #####
test_function <- function(X, TT)
{
  x1 <- X[,1]
  x2 <- X[,2]

  eta_1 <- cos(x1 + x2) * exp(x1*x2)

  p_1 <- exp(eta_1)/(1+exp(eta_1))
  y_1 <- rep(NA, length(p_1))
  for(i in 1:length(p_1)) y_1[i] <- rbinom(1,1,p_1[i])
  Y <- y_1
  P <- p_1
  if(TT > 1){
    for(tt in 2:TT){
      eta_2 <- 0.3 * y_1 + eta_1
      p_2 <- exp(eta_2)/(1+exp(eta_2))
      y_2 <- rep(NA, length(p_2))
      for(i in 1:length(p_2)) y_2[i] <- rbinom(1,1,p_2[i])
      Y <- cbind(Y, y_2)
      P <- cbind(P, p_2)
      y_1 <- y_2
    }
  }

  return(list(Y = Y, P = P))
}

set.seed(1)
n <- 30
n.test <- 10
d <- 2
X <- matrix(runif(d * n), ncol = d)

##### without time-series #####
Y <- test_function(X, 1)$Y ## Y is a vector

binaryGP.model <- binaryGP_fit(X = X, Y = Y)
print(binaryGP.model) # print estimation results
summary(binaryGP.model) # significance results

##### with time-series, lag 1 #####
Y <- test_function(X, 10)$Y ## Y is a matrix with 10 columns
```

```
binaryGP.model <- binaryGP_fit(X = X, Y = Y, R = 1)
print(binaryGP.model) # print estimation results
summary(binaryGP.model) # significance results
```

Index

`binaryGP_fit`, [2](#), [6](#), [8](#), [10](#)

`corr_matrix`, [2](#)

`predict.binaryGP`, [4](#), [5](#)

`print.binaryGP`, [4](#), [7](#)

`summary.binaryGP`, [4](#), [9](#)