

An Introduction to MF.beta4 via Examples

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Latest version 1.1.0 (Nov. 1, 2024)

The Latest Update in Nov. 1, 2024: In earlier versions, multifunctionality decomposition (alpha, beta and gamma) was performed only for pairs of plots/ecosystems. In the updated version, we have added a logical argument “by_pair” in the main function “MF2_multiple” to specify whether multifunctionality decomposition will be performed for all pairs of ecosystems or not. If “by_pair = TRUE”, alpha/beta/gamma multifunctionality will be computed for all pairs of ecosystems/plots in the input data; if “by_pair = FALSE”, alpha/beta/gamma multifunctionality will be computed for K plots (i.e., K can be greater than two) when data for K plots are provided in the input data. Default is “by_pair = TRUE”.

MF.beta4 is an R package for measuring ecosystem multifunctionality and assessing BEF relationships. The measures are illustrated by using ecosystem function and biodiversity data collected in a total of 209 plots in six European countries (the FunDivEUROPE dataset). All data are available from the Dryad repository; see Ratchiffe et al. (2017b) and Scherer-Lorenzen et al. (2023) for details. The software was originally developed for the Beta4 project (Müller et al. 2022) on the effect of enhancing the beta diversity between forest patches on ecosystem multifunctionality and forest resilience across spatial scales.

Based on a framework of Hill-Chao numbers of orders $q = 0, 1$ and 2 , MF.beta4 features the following multifunctionality measures for a single and multiple ecosystems; see Chao et al. (2024) for pertinent methodology and decomposition theory.

- (1) Multifunctionality measures in a single ecosystem:

MF.beta4 computes a class of weighted multifunctionality measures for given function weights. Multifunctionality measures that correct for strong correlations between ecosystem functions to avoid redundancy are also provided. When biodiversity data are available, MF.beta4 also provides graphics for assessing biodiversity-ecosystem functioning (BEF) relationships between within-ecosystem multifunctionality and the species diversity for orders $q = 0, 1$, and 2 .

- (2) Multifunctionality measures in multiple ecosystems:

For given function weights, MF.beta4 computes the gamma multifunctionality of pooled ecosystems, the within-ecosystem component (alpha multifunctionality) and the among-ecosystem component (beta multifunctionality). The correlation between functions can also be corrected for. When biodiversity data are available, MF.beta4 also provides graphics for assessing biodiversity-ecosystem functioning (BEF) relationships between gamma/alpha/beta multifunctionality and the species diversity for orders $q = 0, 1$, and 2 for all pairs of ecosystems/plots or for multiple ecosystems/plots.

HOW TO CITE

If you publish your work based on the results from the MF.beta4 package, you should make references to the following methodology paper and the R package.

Chao, A., Chiu, C. H., Hu, K. H., van der Plas, F., Cadotte, M. W., Mitesser, O., et al. (2024). Hill-Chao numbers in multifunctionality allows decomposing gamma multifunctionality into alpha and beta components. *Ecology Letters*, 27, e14336. Available from: <https://doi.org/10.1111/ele.14336>

Chao, A., Liu, C. Y., and Hu, K. H. (2023). MF.beta4 package: measuring ecosystem multifunctionality and assessing BEF relationships. Available from CRAN.

SOFTWARE NEEDED TO RUN MF.beta4 IN R

- Required: R
- Suggested: RStudio IDE

HOW TO DOWNLOAD MF.beta4:

The MF.beta4 package can be downloaded from CRAN or Github MF.beta4_github using the following commands. For a first-time installation, an additional visualization extension package (`ggplot2`) must be installed and loaded.

```
## install MF.beta4 package from CRAN
install.packages("MF.beta4")

## install the latest version from github
install.packages('devtools')
library(devtools)
install_github("AnneChao/MF.beta4")

## import packages
library(MF.beta4)
```

FOUR MAIN FUNCTIONS:

This package includes four functions, as listed below with default arguments. See package manual for the detailed description of each argument.

- **function_normalization**: transforms ecosystem function data to values between 0 and 1; other variables remain unchanged.

```
function_normalization(data, fun_cols = 1:ncol(data), negative = NULL, by_group = NULL)
```

- **MF1_single**: computes multifunctionality measures of orders $q = 0, 1$ and 2 for given function weights in a single ecosystem for two cases: (i) correlations between functions are not corrected for, and (ii) correlations between functions are corrected for.

```
MF1_single(func_data, species_data = NULL, weight = 1, q = c(0, 1, 2))
```

- **MF2_multiple**: if `by_pair = TRUE`, this function computes alpha, beta and gamma multifunctionality measures of orders $q = 0, 1$ and 2 for given function weights for all pairs of ecosystems in the input data; if `by_pair = FALSE`, multifunctionality decomposition (alpha/beta/gamma) will be performed for K plots (K can be greater than two) when data for K plots are provided in the input data. In both cases, decomposition can be done for two cases: (i) correlations between functions are not corrected for, and (ii) correlations between functions are corrected for.

```
MF2_multiple(func_data, species_data = NULL, weight = 1, q = c(0, 1, 2),
             by_group = NULL, by_pair = TRUE)
```

- **MFggplot**: provides the graphical BEF relationships based on the output obtained from the function `MF1_single` or `MF2_multiple`.

```
MFggplot(output, model = "LMM.both", by_group = NULL, caption = "slope")
```

DATA INPUT FORMAT

Ecosystem function data

The FunDivEurope data are used here to demonstrate the use of the four functions; see Ratcliffe et al. (2017a, b) and Scherer-Lorenzen et al. (2023) for the original datasets. There are three datasets provided with the package: raw ecosystem function dataset (`forest_function_data_raw`), normalized function dataset (`forest_function_data_normalized`), and biodiversity dataset (`forest_biodiversity_data`). The first dataset includes the raw values of 26 ecosystem functions collected from 209 plots in six European countries, representing six major European forest types: boreal forest (Finland, 28 plots); hemi-boreal (Poland, 43 plots); temperate deciduous (Germany, 38 plots); mountainous deciduous (Romania, 28 plots); thermophilous deciduous (Italy, 36 plots); and Mediterranean mixed (Spain, 36 plots). Each plot is designated as an ecosystem in assessing BEF relationships. See Table 1 of Ratcliffe et al. (2017a) for a description of the 26 functions, and Ratcliffe et al. (2017a) and Scherer-Lorenzen et al. (2023) for data details of the original datasets.

In addition to row name (plot/ecosystem id) and column name (plot information and function names), the data in the file `forest_function_data_raw` are input as a data.frame with 209 plots (rows) and 32 columns. The first 5 columns show the relevant plot information, followed by 26 raw ecosystem functions (in consecutive columns from 6 to 31). An additional column “country” for each plot is added (as column 32) as a stratification/group variable because function normalization and relevant decomposition analyses will be performed within each country. For each missing value of functions in the original dataset, the mean of the given function within the country was imputed. Thus, the raw ecosystem function dataset provided with the package is slightly different from the original one.

Run the following code for the data `forest_function_data_raw` to view the first ten rows and the first five columns (columns 1:3, 6 and 7); columns 6 and 7 show respectively the first two raw ecosystem functions (earthworm_biomass and fine_woody_debris) :

```
data("forest_function_data_raw")
head(cbind(forest_function_data_raw[1:3], round(forest_function_data_raw[6:7], 3)), 10)
```

```
#>      plotid target_species_richness composition earthworm_biomass fine_woody_debris
#> FIN01  FIN01                      2    Piab.Pisy                0.000             171
#> FIN02  FIN02                      2     Be.Piab                0.465             110
#> FIN03  FIN03                      2     Be.Piab                0.626              81
#> FIN04  FIN04                      2     Be.Piab                0.000              82
```

```

#> FIN05 FIN05                2      Be.Pisy                0.928                38
#> FIN06 FIN06                1        Piab                0.000                75
#> FIN07 FIN07                1         Be                49.672                44
#> FIN08 FIN08                1         Be                28.013                38
#> FIN09 FIN09                1        Pisy                0.204                65
#> FIN10 FIN10                1        Piab                0.000                136

```

To meaningfully quantify multifunctionality in an ecosystem based on multiple functions, all function values should be first normalized to the range [0, 1]. Proper normalization can be performed by using `function_normalization` provided in the package. In the `FunDivEUROPE` data, the forests in the six countries represent different ecosystems, all functions were thus normalized within a country, by specifying the argument `by_group = "country"`. Because different transformations are applied to positive and negative functionality, it is required to specify negative functionality in the argument `"negative"`. In the raw function dataset, there are 26 ecosystem functions (in consecutive columns from 6 to 31). Among them, two are negative functionality: `"soil_cn_ff_10"` and `"wue"`, and others are positive functionality. Run the following code to view the first ten rows and the first five columns (columns 1:3, 6 and 7); columns 6 and 7 show respectively the normalized values of the first two ecosystem functions (earthworm_biomass and fine_woody_debris):

```

data("forest_function_data_raw")
normalized_forest_function_data <- function_normalization(data = forest_function_data_raw,
  fun_cols = 6:31, negative = c("soil_cn_ff_10", "wue"), by_group = "country")
head(cbind(normalized_forest_function_data[1:3], round(normalized_forest_function_data[6:7], 3)), 10)

```

```

#>      plotid target_species_richness composition earthworm_biomass fine_woody_debris
#> FIN01 FIN01                2      Piab.Pisy                0.000                0.416
#> FIN02 FIN02                2       Be.Piab                0.009                0.238
#> FIN03 FIN03                2       Be.Piab                0.013                0.152
#> FIN04 FIN04                2       Be.Piab                0.000                0.155
#> FIN05 FIN05                2       Be.Pisy                0.019                0.026
#> FIN06 FIN06                1         Piab                0.000                0.135
#> FIN07 FIN07                1          Be                1.000                0.044
#> FIN08 FIN08                1          Be                0.564                0.026
#> FIN09 FIN09                1        Pisy                0.004                0.106
#> FIN10 FIN10                1         Piab                0.000                0.314

```

This normalized dataset is exactly the same as the dataset `forest_function_data_normalized` provided with the package.

Biodiversity data

The `forest_biodiversity_data` consist of four columns: the `"plotID"` column includes the name of ecosystems/plots, the `"species"` column includes species names, the `"abundance"` column includes the corresponding species abundance (basal area as a proxy of species abundance), and the `"country"` column includes the corresponding stratifying variable, in addition to row and column names; see Scherer-Lorenzen et al. (2023) for the original data. Because missing values of `"basal area"` in the original dataset were imputed by the mean of the same species within the country, and basal areas were combined for two species (*Betula pendula* and *Betula pubescens*), the dataset provided with the package is slightly different from the original dataset. Run the following code to view the first ten rows of the biodiversity data:

```
data("forest_biodiversity_data")
head(forest_biodiversity_data,10)
```

```
#> # A tibble: 10 x 4
#> # Groups:   plotID [5]
#>   plotID species      abundance country
#>   <chr> <chr>          <dbl> <chr>
#> 1 FIN01 Picea.abies      1.84 FIN
#> 2 FIN01 Pinus.sylvestris 0.535 FIN
#> 3 FIN02 Betula.pendula   1.18 FIN
#> 4 FIN02 Picea.abies      0.408 FIN
#> 5 FIN03 Betula.pendula   1.09 FIN
#> 6 FIN03 Picea.abies      0.215 FIN
#> 7 FIN04 Betula.pendula   0.662 FIN
#> 8 FIN04 Picea.abies      1.14 FIN
#> 9 FIN05 Betula.pendula   0.423 FIN
#> 10 FIN05 Pinus.sylvestris 1.25 FIN
```

WITHIN-ECOSYSTEM MULTIFUNCTIONALITY AND BEF RELATIONSHIPS

Computing multifunctionality within a single ecosystem

Based on normalized function data, `MF1_single()` computes multifunctionality measures of orders $q = 0, 1$ and 2 for given function weights in a single ecosystem separately for two cases: (i) correlations between functions are not corrected for, and (ii) correlations between functions are corrected for.

When `species_data = NULL` (i.e., biodiversity data are not provided), `MF1_single()` only computes multifunctionality measures of orders $q = 0, 1$ and 2 for each plot. When biodiversity data are specified (`species_data = forest_biodiversity_data`), tree species diversity values for $q = 0, 1$ and 2 are also computed.

Run the following code to view the first ten rows of the output:

```
data("forest_function_data_normalized")
data("forest_biodiversity_data")
output1 <- MF1_single(func_data = forest_function_data_normalized[,6:31], weight = 1,
                      species_data = forest_biodiversity_data)
head(output1, 10)
```

```
#>   plotID      Type Order.q  qMF Species.diversity
#> 1  FIN01 corr_uncorrected  q = 0 10.71          2.00
#> 2  FIN01 corr_uncorrected  q = 1 10.03          1.70
#> 3  FIN01 corr_uncorrected  q = 2  9.58          1.53
#> 4  FIN01  corr_corrected  q = 0 10.35          2.00
#> 5  FIN01  corr_corrected  q = 1  9.70          1.70
#> 6  FIN01  corr_corrected  q = 2  9.28          1.53
#> 7  FIN02 corr_uncorrected  q = 0  9.32          2.00
#> 8  FIN02 corr_uncorrected  q = 1  8.36          1.77
#> 9  FIN02 corr_uncorrected  q = 2  7.64          1.62
#> 10 FIN02  corr_corrected  q = 0  9.02          2.00
```

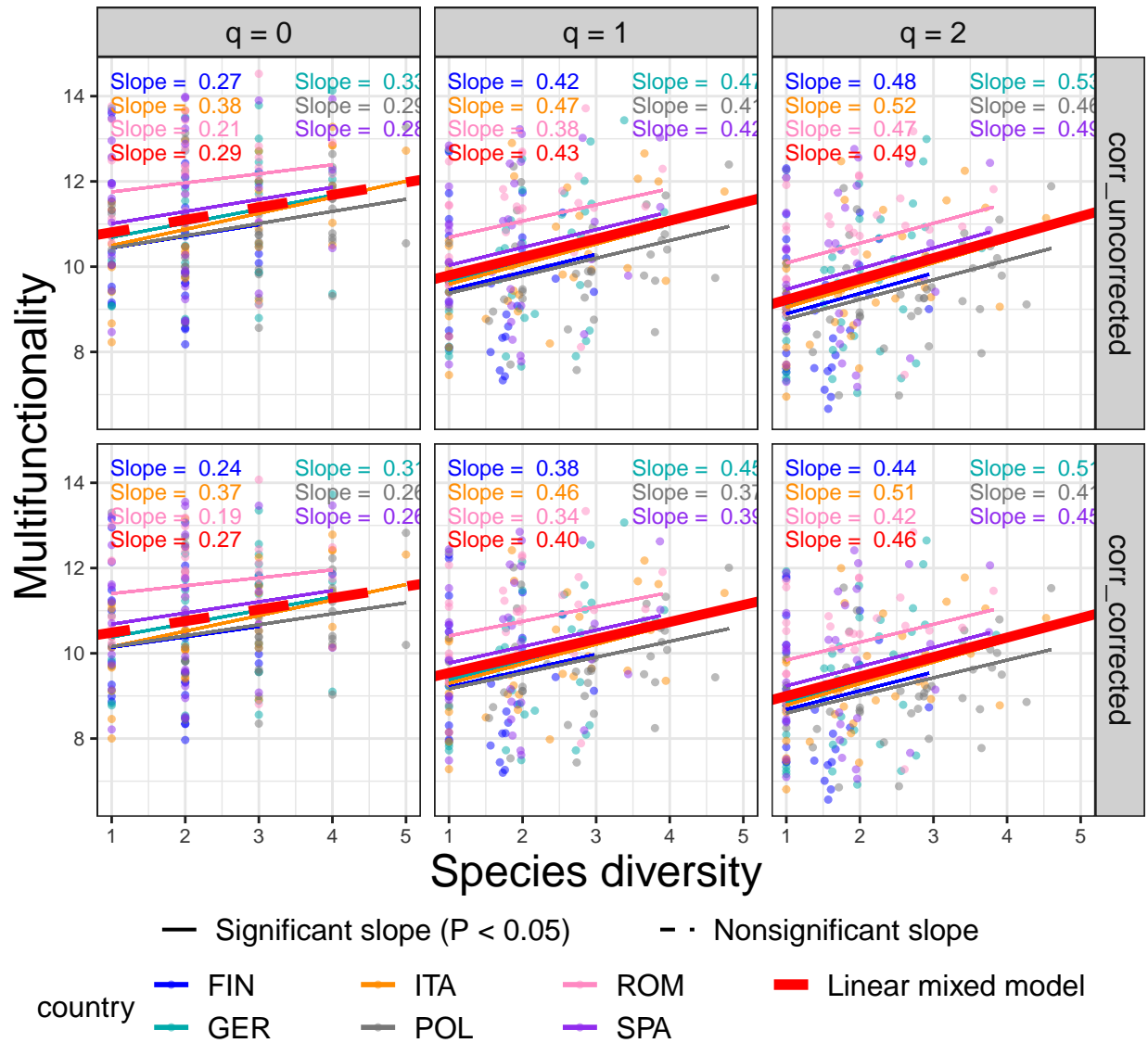
The above output includes the ID of plot (`plotID`), `Type` (`corr_uncorrected` and `corr_corrected`), the diversity order (`Order.q`), the multifunctionality measure of order q (`qMF`) and species diversity (`Species.diversity`).

Assessing within-ecosystem BEF relationships by `MFggplot()`

Function `MFggplot()` provides the graphical BEF relationships based on the output from the function `MF1_single` or `MF2_multiple`. For an `MF1_single` object of given individual function weights, function `MFggplot` plots the BEF relationship between multifunctionality of order q ($= 0, 1$ and 2) and species diversity of the same order q for two cases: (i) correlations between functions are not corrected for. (ii) correlations between functions are corrected for. The fitted lines for the chosen model are also shown in the figure.

Below we demonstrate how to reveal BEF relationships under the most useful linear mixed-effects model (`model = "LMM.both"`). Under the model, for each value of q , the relationship between tree species diversity and multifunctionality is modeled using a linear mixed-effects model with random slopes and random intercepts for each country. To fit a linear mixed-effect model, the stratification/group variable must be specified (e.g., `by_group = "country"` in the following code). If `by_group = NULL`, one can only fit linear model (`model = "lm"`). Run the following code to reveal the overall fixed-effect slopes (bold red lines) and each country's relationships (thin lines) estimated from the same linear mixed model. All the fitted results and the associated test of significance for the overall slopes and R-squared were based on the output using the function "lmer" in the R packages "lme4" and "lmerTest".

```
data("forest_function_data_normalized")
output1 <- data.frame(output1, country=rep(forest_function_data_normalized$country, each = 6))
MFggplot(output1, model = "LMM.both", by_group = "country", caption = "slope")
```



Using partial data to quickly view/obtain output

To quickly view/obtain the output, Users can simply select part of the entire set of 209 plots as input data. Here we only use the first 18 plots from Germany and the last 18 plots from Italy for illustration. Run the following code to view the first ten rows of the within-plot multifunctionality measures in the output:

```
data("forest_function_data_raw")
data("forest_biodiversity_data")
GER_ITA_forest_function_raw <- filter(forest_function_data_raw,
                                     country=="GER"|country=="ITA")[c(1:18,57:74),]
GER_ITA_forest_function_normalized <- function_normalization(data = GER_ITA_forest_function_raw,
                                                            fun_cols = 6:31,
                                                            negative = c("soil_cn_ff_10","wue"),
                                                            by_group = "country")
GER_ITA_forest_biodiversity <- forest_biodiversity_data[c(49:82,181:229),]
output2 <- MF1_single(func_data = GER_ITA_forest_function_normalized[,6:31], weight = 1,
                     species_data = GER_ITA_forest_biodiversity)
```

```
head(output2, 10)
```

```
#>   plotID      Type Order.q  qMF Species.diversity
#> 1  GER01 corr_uncorrected   q = 0 9.99             1
#> 2  GER01 corr_uncorrected   q = 1 8.70             1
#> 3  GER01 corr_uncorrected   q = 2 7.99             1
#> 4  GER01  corr_corrected   q = 0 9.33             1
#> 5  GER01  corr_corrected   q = 1 8.26             1
#> 6  GER01  corr_corrected   q = 2 7.64             1
#> 7  GER02 corr_uncorrected   q = 0 9.20             1
#> 8  GER02 corr_uncorrected   q = 1 8.02             1
#> 9  GER02 corr_uncorrected   q = 2 7.47             1
#> 10 GER02  corr_corrected   q = 0 8.62             1
```

Users then can apply the `MFggplot()` to view the local within-plot BEF relationships. The graphic output is omitted.

MULTIFUNCTIONALITY DECOMPOSITION FOR ALL PAIRS OF PLOTS

Computing alpha, beta and gamma multifunctionality for all pairs of plots within a country

`MF2_multiple()` computes alpha, beta and gamma multifunctionality measures of orders $q = 0, 1$ and 2 for multiple ecosystems separately for two cases: (i) correlations between functions are not corrected for, and (ii) correlations between functions are corrected for. If `by_pair = TRUE` (by default), this function computes alpha, beta and gamma multifunctionality measures of orders $q = 0, 1$ and 2 for given function weights for all pairs of ecosystems in the input data; if `by_pair = FALSE`, multifunctionality decomposition (alpha/beta/gamma) will be performed for K plots (K can be greater than two) when data for K plots are provided in the input data. When biodiversity data are provided (`species_data = forest_biodiversity_data`), species diversity values for $q = 0, 1$ and 2 are also computed.

Due to sparse data in Finland (with richness levels of only one or two species in 90% of plots), data from Finland are excluded from following computation. Run the following code to view the first ten rows of the output:

```
library(dplyr)
data("forest_function_data_normalized")
data("forest_biodiversity_data")
forest_function_data_normalized <- forest_function_data_normalized %>% filter(country != "FIN")
forest_biodiversity_data <- forest_biodiversity_data[-(1:48),]
output3 = MF2_multiple(func_data = forest_function_data_normalized[,6:32],
                       species_data = forest_biodiversity_data,
                       weight = 1,
                       by_group = "country")
head(output3, 10)
```

```
#>   plotID country Order.q      Type Scale  qMF Species.diversity
#> 1  GER01 vs. GER02     GER   q = 0 corr_uncorrected Gamma 9.26             1.000
#> 2  GER01 vs. GER02     GER   q = 0 corr_uncorrected Alpha 9.26             1.000
#> 3  GER01 vs. GER02     GER   q = 0 corr_uncorrected Beta 1.00             1.000
#> 4  GER01 vs. GER02     GER   q = 0  corr_corrected Gamma 8.98             1.000
```



```

#> 5 GER01 vs. GER02 GER q = 0 corr_corrected Alpha 8.98 1.000
#> 6 GER01 vs. GER02 GER q = 0 corr_corrected Beta 1.00 1.000
#> 7 GER01 vs. GER02 GER q = 1 corr_uncorrected Gamma 7.95 1.000
#> 8 GER01 vs. GER02 GER q = 1 corr_uncorrected Alpha 7.84 0.999
#> 9 GER01 vs. GER02 GER q = 1 corr_uncorrected Beta 1.01 1.001
#> 10 GER01 vs. GER02 GER q = 1 corr_corrected Gamma 7.77 1.000

```

The above output includes the names of the paired plots (`plotID`), Country of the two plots, the diversity order (`Order.q`), Type (`corr_uncorrected` or `corr_corrected`), Scale (gamma, alpha or beta), multifunctionality value of order q (`qMF`) and the corresponding gamma/alpha/beta species diversity (`Species.diversity`).

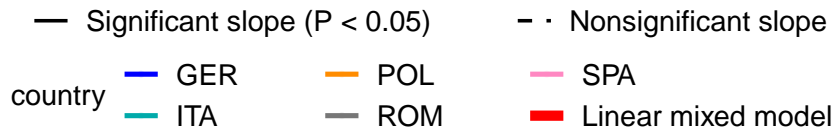
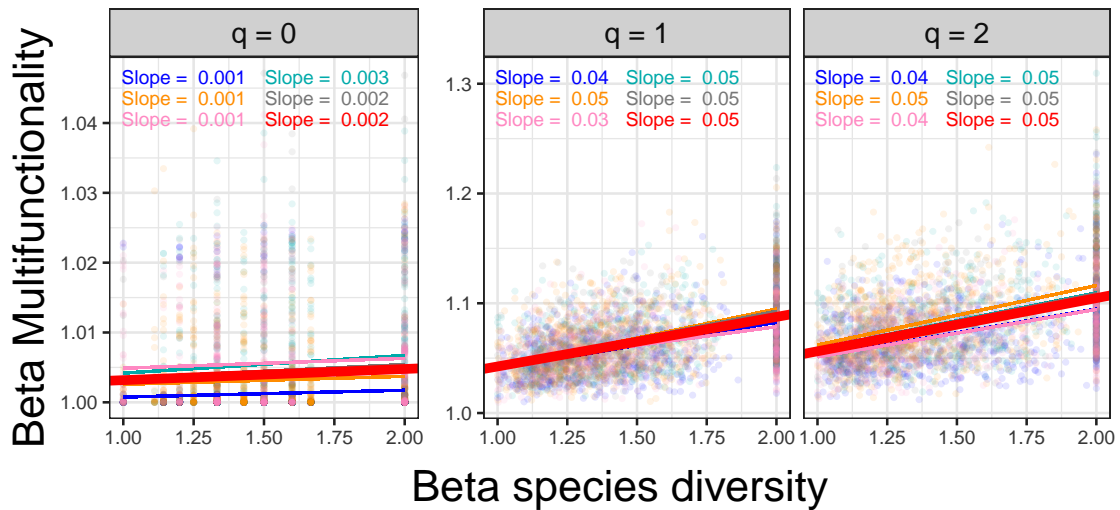
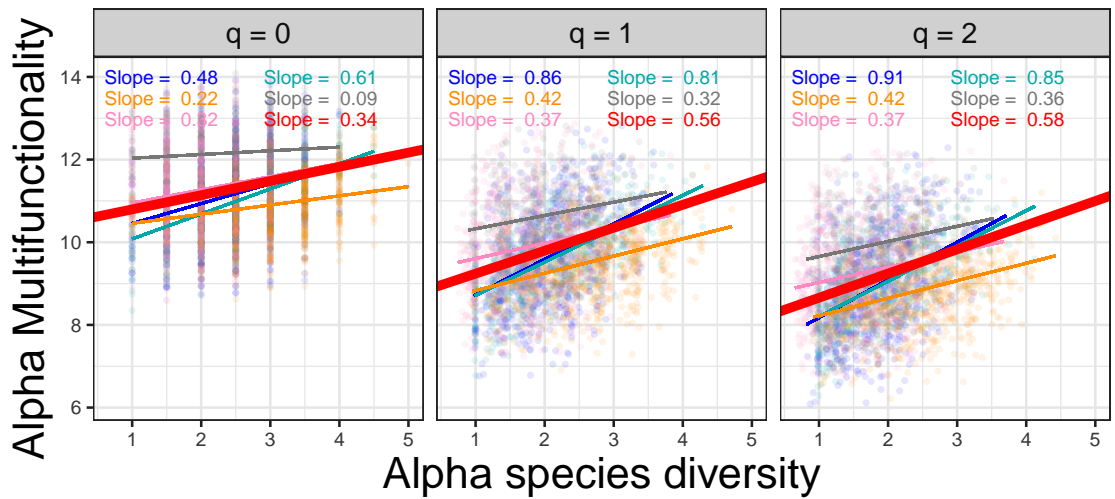
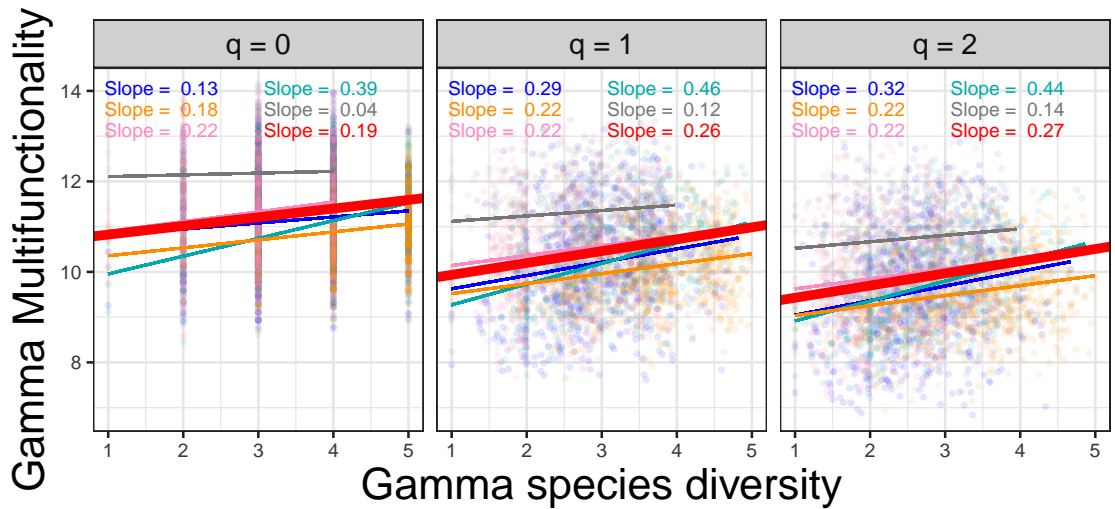
Assessing BEF relationships at gamma, alpha and beta scales

For an `MF2_multiple` object of given individual function weights, function `MFggplot` plots the BEF relationship between alpha/beta/gamma multifunctionality by pairs of plots or all plots of order q ($= 0, 1$ and 2) and the corresponding alpha/beta/gamma species diversity of the same order q for two cases: (i) correlations between functions are not corrected for. (ii) correlations between functions are corrected. The fitted lines for the chosen model are also shown in the figure. By default, the BEF relationship for each scale is modeled using a linear mixed model with random slopes and random intercepts for each country.

Run the following code to obtain the BEF graphical relationships when correlations are not corrected for. (Data from Finland are not considered in the plots, as explained earlier. See later part for a simple example based on only 18 plots from Germany and Italy.)

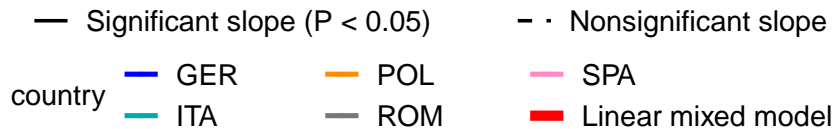
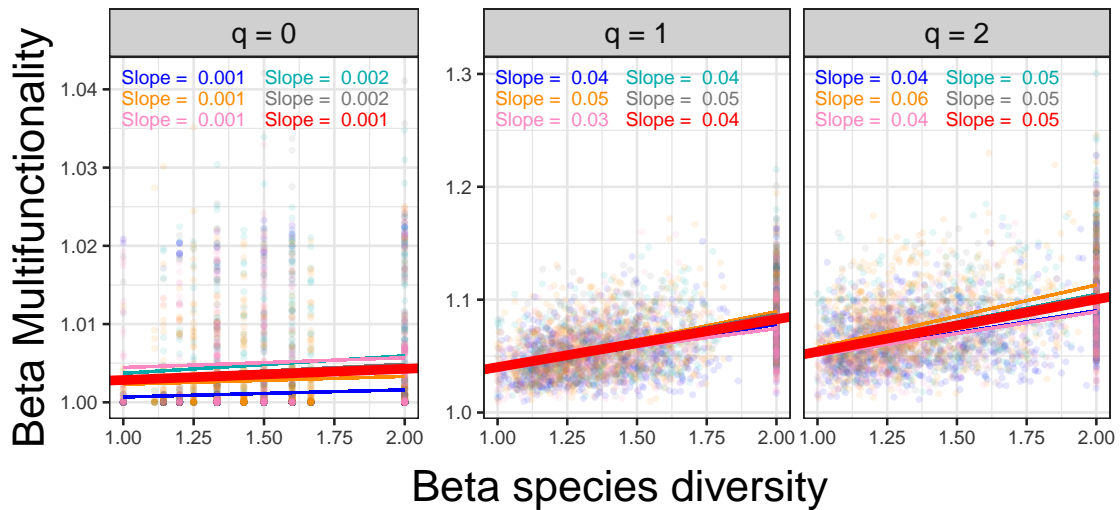
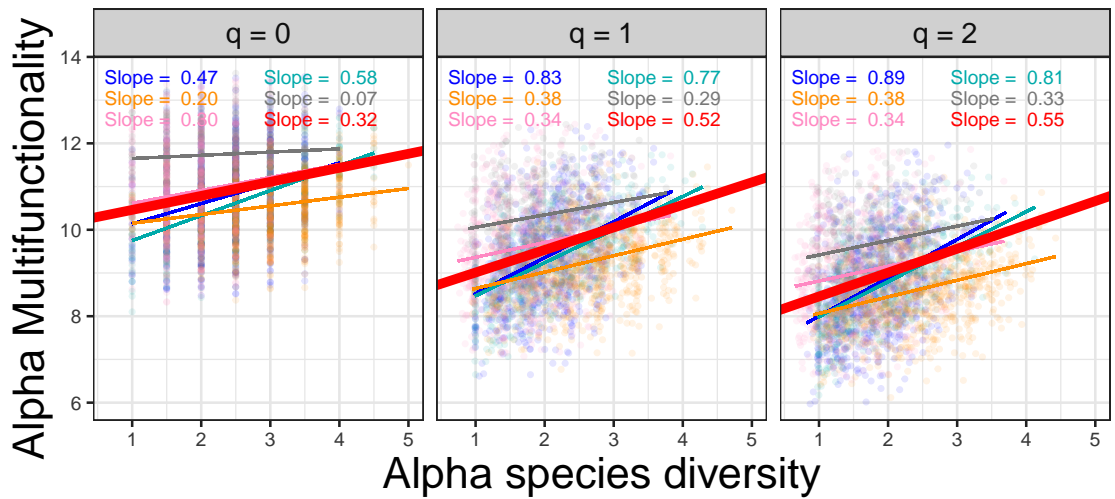
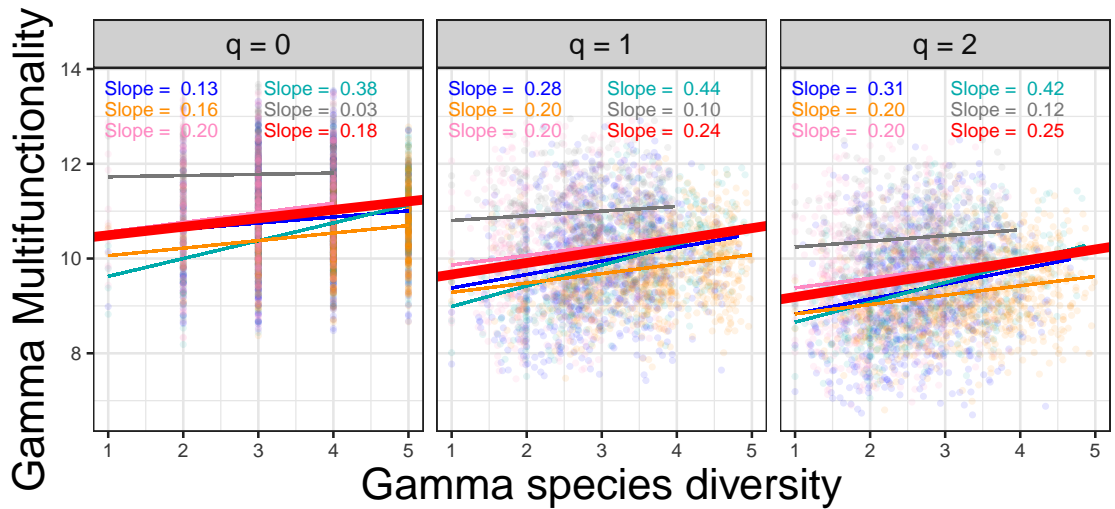
```
figure_LMM <- MFggplot(output3, model = "LMM.both", by_group = "country", caption = "slope")
```

```
figure_LMM$corr_uncorrected$ALL
```



The BEF graphical relationships when correlations are corrected for are shown below.

```
figure_LMM$corr_corrected$ALL
```



NOTE: Because the total number of pair plots is huge, it is very time consuming to obtain the BEF graphical relationships from running the above code for alpha/beta/gamma scales. Users can use partial data to quickly view/obtain the graphical results; see below for an example.

Using partial data to quickly view/obtain output

Here we only use the first 18 plots from Germany and the last 18 plots from Italy for illustration. Run the following code to view the first ten rows of the output:

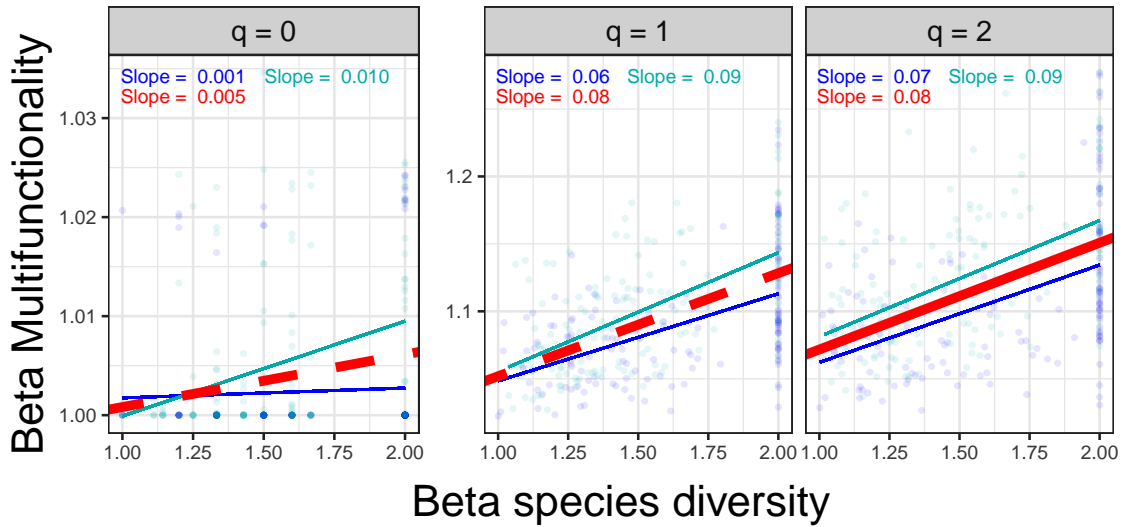
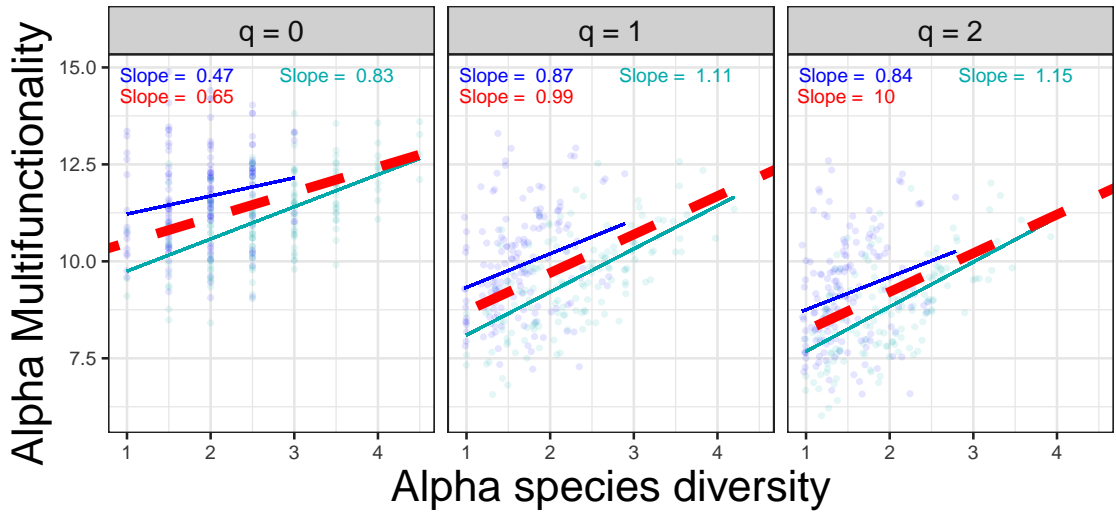
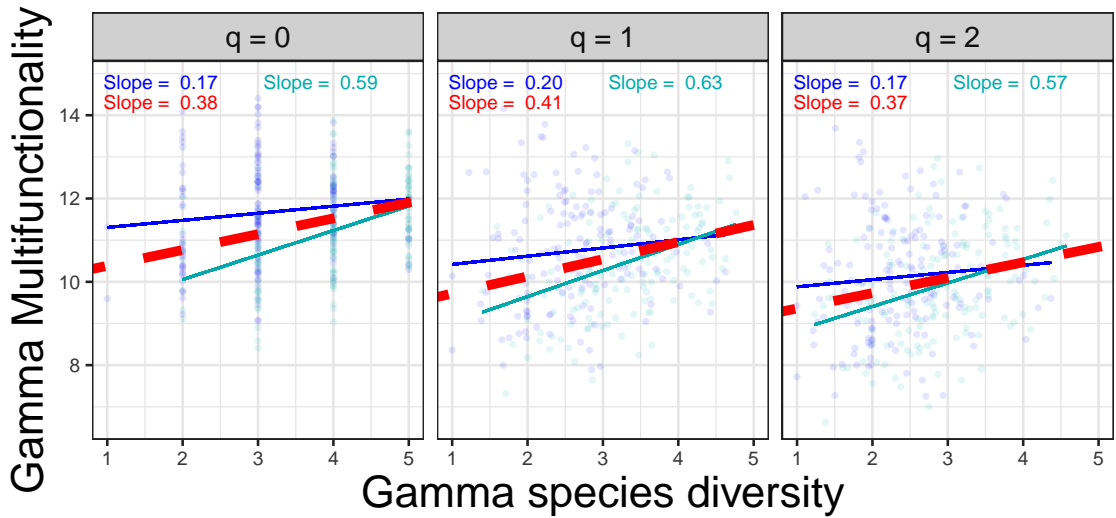
```
data("forest_function_data_raw")
data("forest_biodiversity_data")
GER_ITA_forest_function_raw <- filter(forest_function_data_raw,
                                     country=="GER"|country=="ITA")[c(1:18,57:74),]
GER_ITA_forest_function_normalized <- function_normalization(data = GER_ITA_forest_function_raw,
                                                            fun_cols = 6:31,
                                                            negative = c("soil_cn_ff_10","wue"),
                                                            by_group = "country")
GER_ITA_forest_biodiversity <- forest_biodiversity_data[c(49:82,181:229),]
output4 <- MF2_multiple(func_data = GER_ITA_forest_function_normalized[,6:32],
                       species_data = GER_ITA_forest_biodiversity,
                       weight=1,
                       by_group = "country")
head(output4, 10)
```

```
#>      plotID country Order.q      Type Scale  qMF Species.diversity
#> 1  GER01 vs. GER02     GER   q = 0 corr_uncorrected Gamma 9.59          1.000
#> 2  GER01 vs. GER02     GER   q = 0 corr_uncorrected Alpha 9.59          1.000
#> 3  GER01 vs. GER02     GER   q = 0 corr_uncorrected Beta 1.00           1.000
#> 4  GER01 vs. GER02     GER   q = 0  corr_corrected Gamma 8.96          1.000
#> 5  GER01 vs. GER02     GER   q = 0  corr_corrected Alpha 8.96          1.000
#> 6  GER01 vs. GER02     GER   q = 0  corr_corrected Beta 1.00           1.000
#> 7  GER01 vs. GER02     GER   q = 1 corr_uncorrected Gamma 8.36          1.000
#> 8  GER01 vs. GER02     GER   q = 1 corr_uncorrected Alpha 8.18          0.999
#> 9  GER01 vs. GER02     GER   q = 1 corr_uncorrected Beta 1.02           1.001
#> 10 GER01 vs. GER02     GER   q = 1  corr_corrected Gamma 7.91          1.000
```

Run the following code to obtain the BEF graphical relationships in 18 plots from Germany and Italy when correlations are not corrected for.

```
figure_LMM_GER_ITA <- MFggplot(output4, model = "LMM.both", by_group = "country", caption = "slope")
```

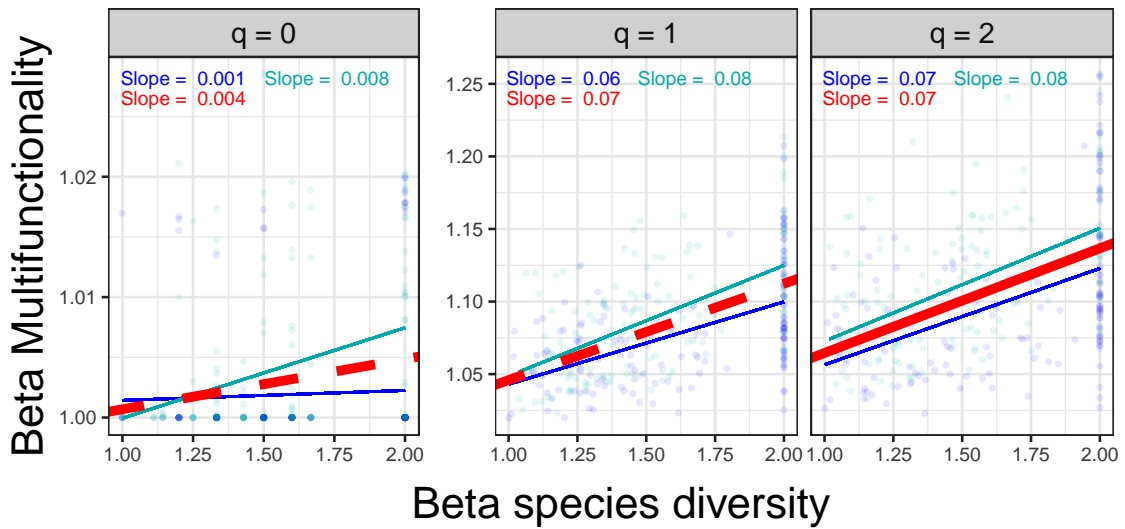
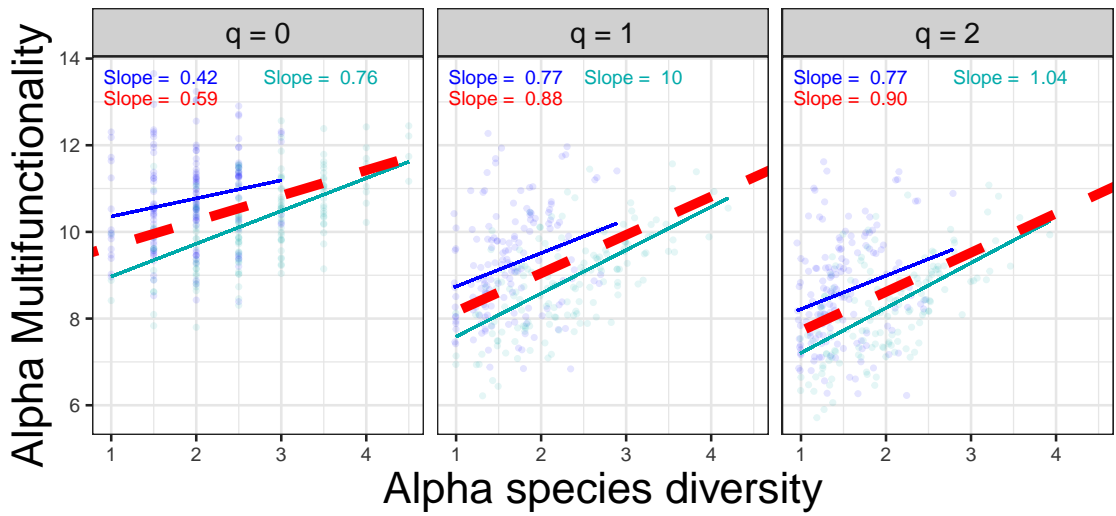
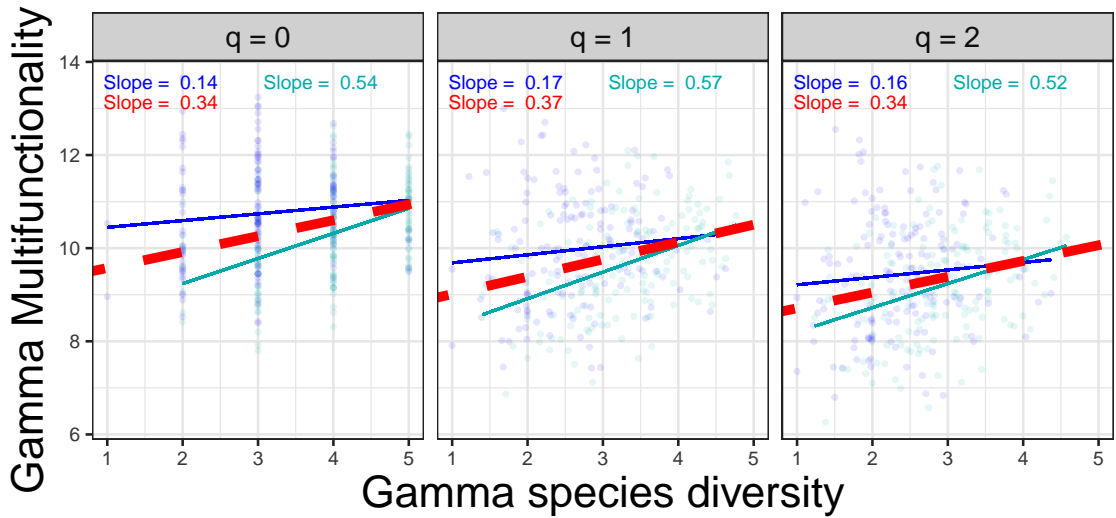
figure_LMM_GER_ITA\$corr_uncorrected\$ALL



— Significant slope ($P < 0.05$) - · Nonsignificant slope
 country — GER — ITA — Linear mixed model

The BEF graphical relationships based on 18 plots from Germany and Italy when correlations are corrected for are shown below.

```
figure_LMM_GER_ITA$corr_corrected$ALL
```

— Significant slope ($P < 0.05$) - · Nonsignificant slope
 country — GER — ITA — Linear mixed model

MULTIFUNCTIONALITY DECOMPOSITION FOR K PLOTS (K>2)

Computing alpha, beta and gamma multifunctionality for 3 plots in each country

Function `MF2_multiple()` can be applied to perform multifunctionality decomposition based on a general number of ecosystems/plots (`by_pair = FALSE`). For illustration, we use the first three plots in each of the six countries as the second demo data to calculate alpha/beta/gamma multifunctionality based on three plots in each country. Run the following code to view the first ten rows of the output.

```
data("forest_function_data_raw")
data("forest_biodiversity_data")
forest_function_data_raw_3plots <- forest_function_data_raw[c(1:3,29:31,67:69,103:105,
                                                             146:148,174:176),]
forest_function_data_normalized_3plots <- function_normalization(data=forest_function_data_raw_3plots,
                                                                fun_cols=6:31,
                                                                negative=c("soil_cn_ff_10","wue"),
                                                                by_group="country")
forest_biodiversity_data_3plots<-forest_biodiversity_data[c(1:6,49:52,141:148,
                                                            230:232,351:355,411:417),]

output5 = MF2_multiple(func_data = forest_function_data_normalized_3plots[,6:32],
                      species_data = forest_biodiversity_data_3plots,
                      weight = 1,
                      by_group = "country", by_pair = FALSE)
head(output5, 10)
```

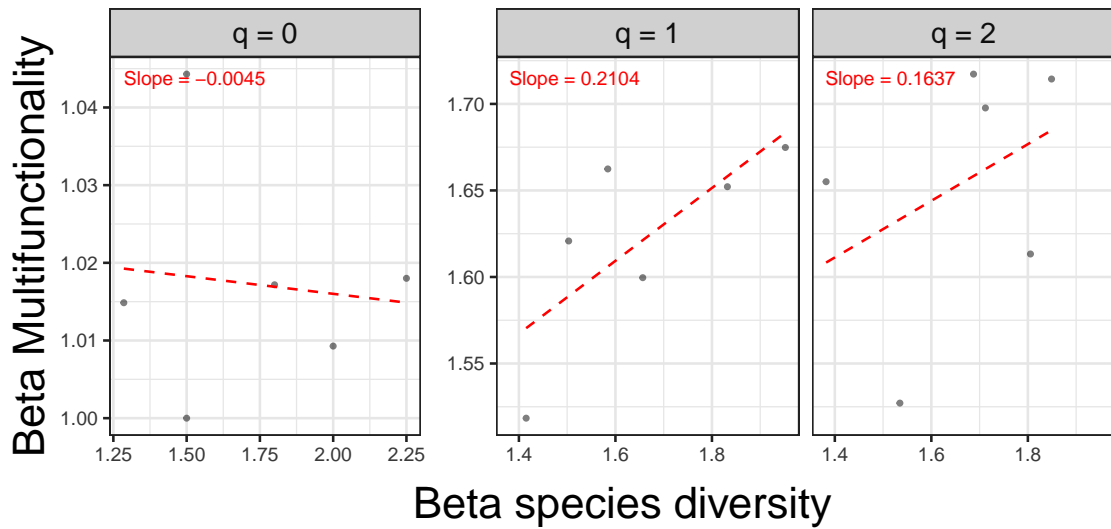
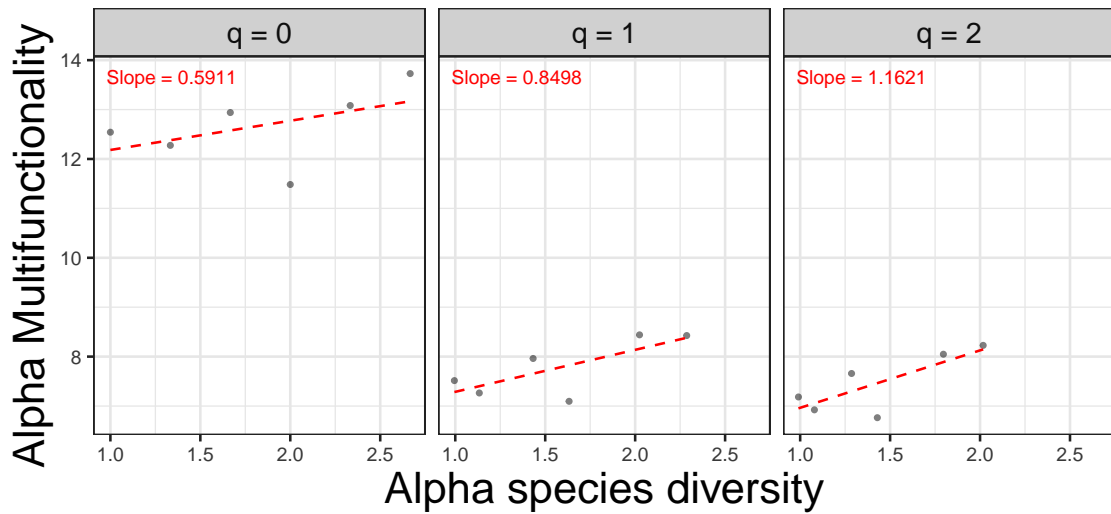
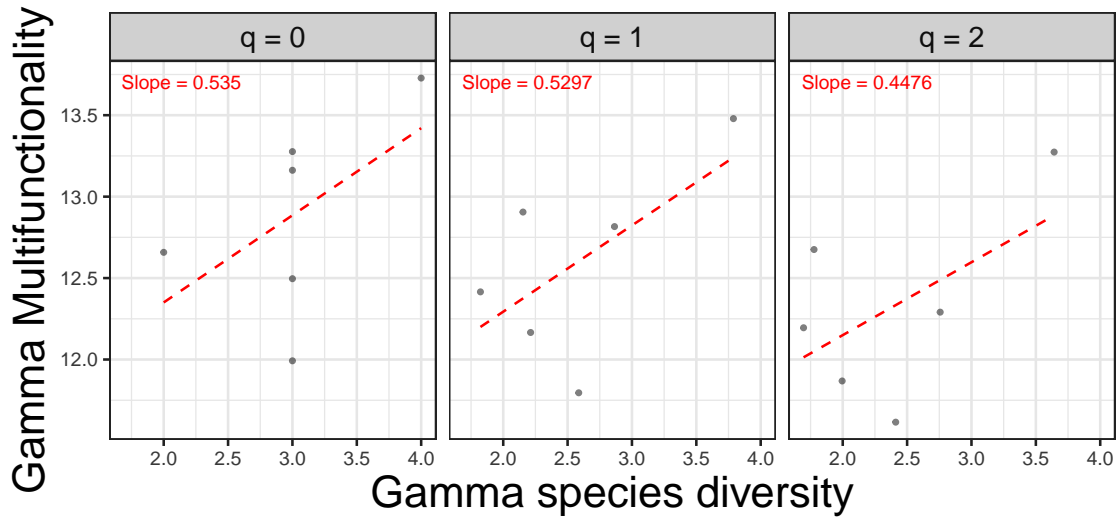
```
#>   country Order.q      Type Scale  qMF Species.diversity
#> 1     FIN   q = 0 corr_uncorrected Gamma 11.99           3.00
#> 2     FIN   q = 0 corr_uncorrected Alpha 11.48           2.00
#> 3     FIN   q = 0 corr_uncorrected Beta  1.04           1.50
#> 4     FIN   q = 0  corr_corrected Gamma  9.81           3.00
#> 5     FIN   q = 0  corr_corrected Alpha  9.56           2.00
#> 6     FIN   q = 0  corr_corrected Beta  1.02           1.50
#> 7     FIN   q = 1 corr_uncorrected Gamma 11.80           2.59
#> 8     FIN   q = 1 corr_uncorrected Alpha  7.10           1.63
#> 9     FIN   q = 1 corr_uncorrected Beta  1.66           1.58
#> 10    FIN   q = 1  corr_corrected Gamma  9.64           2.59
```

Assessing BEF relationships at alpha, beta and gamma scales

When multifunctionality decomposition is performed for K plots (K>2), only linear model can be fitted to the BEF relationships because alpha/beta/gamma data points are not sufficient to fit linear mixed models. Run the following code to obtain the BEF graphical relationships when correlations are not corrected for.

```
figure_all_plots <- MFggplot(output5, model = "lm", caption = "slope")
```

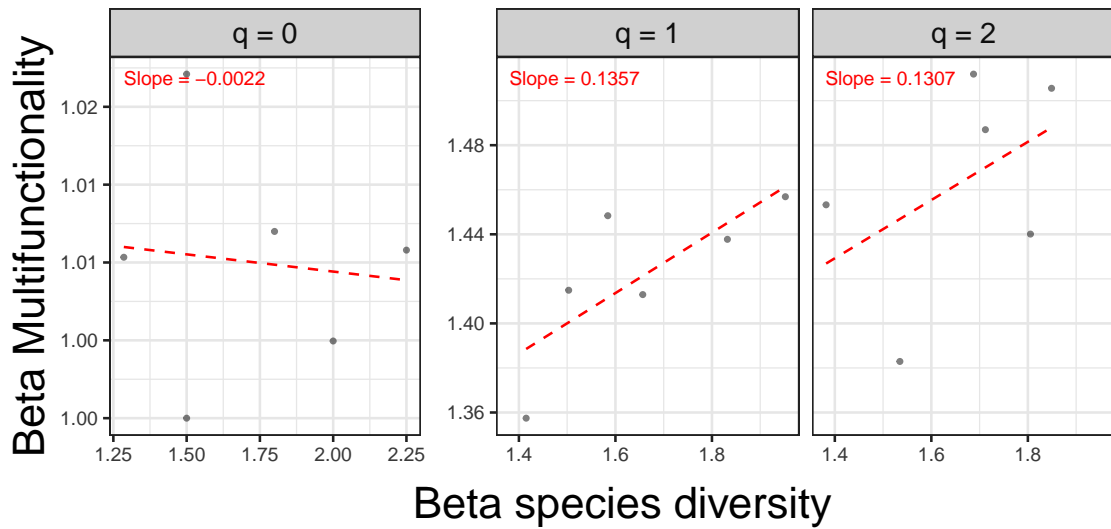
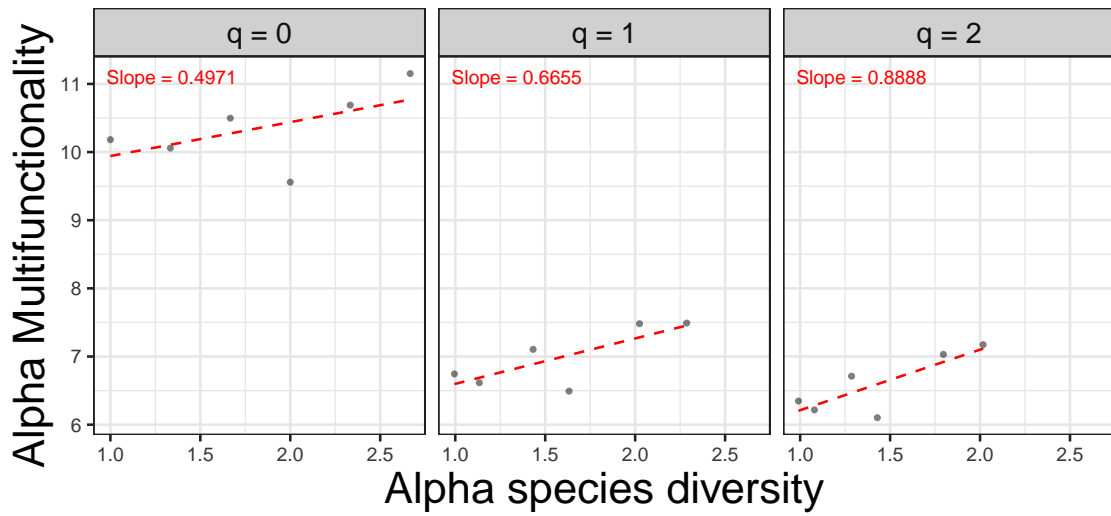
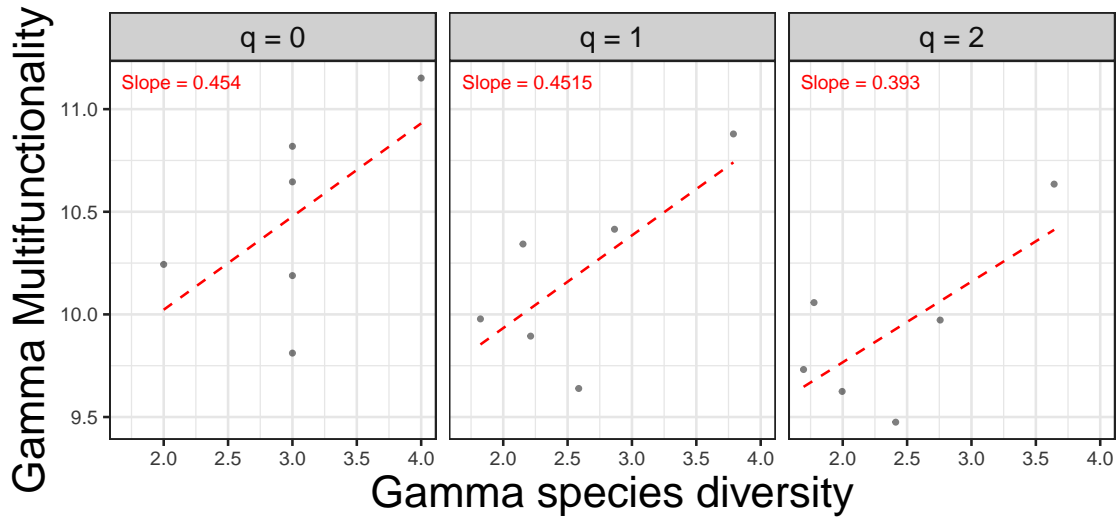
```
figure_all_plots$corr_uncorrected$ALL
```



— Significant slope ($P < 0.05$) - · Nonsignificant slope
 — Linear model

The BEF graphical relationships when correlations are corrected for are shown below.

```
figure_all_plots$corr_corrected$ALL
```



— Significant slope ($P < 0.05$) - · Nonsignificant slope
 — Linear model

REFERENCES

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- Müller, J., Mitesser, O. Cadotte, M. W., van der Plas, F., Mori, A, Ammer, C. . . . , Eisenhauer N. (2022). Enhancing the structural diversity between forest patches – a concept and real-world experiment to study biodiversity and multifunctionality across spatial scales. *Global Change Biology*, 29, 1437–1450.
- Ratcliffe, S., Wirth, C., Jucker, T., van der Plas, F., Scherer-Lorenzen, M., Verheyen, K., et al. (2017a). Biodiversity and ecosystem functioning relations in European forests depend on environmental context. *Ecology Letters*, 20, 1414–1426.
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