Package: SLOPE (via r-universe)

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Title Sorted L1 Penalized Estimation

Version 2.1.1

Description Efficient implementations for Sorted L-One Penalized Estimation (SLOPE): generalized linear models regularized with the sorted L1-norm (Bogdan et al. 2015). Supported models include ordinary least-squares regression, binomial regression, multinomial regression, and Poisson regression. Both dense and sparse predictor matrices are supported. In addition, the package features predictor screening rules that enable fast and efficient solutions to high-dimensional problems.

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BugReports https://github.com/jolars/SLOPE/issues

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`abalone` *Abalone*

Description

This data set contains observations of abalones. The goal is to predict the age of an individual abalone given physical measurements such as sex, weight, and height.

Usage

```
abalone
```

Format

A list with two items representing 211 observations from 9 variables

sex sex of abalone, 1 for female

infant indicates that the person is an infant

length longest shell measurement in mm

diameter perpendicular to length in mm

height height in mm including meat in shell

weight_whole weight of entire abalone

weight_shucked weight of meat

weight_viscera weight of viscera

weight_shell weight of shell

rings rings. +1.5 gives the age in years

Details

Only a stratified sample of 211 rows of the original data set are used here.

Source

Pace, R. Kelley and Ronald Barry, Sparse Spatial Autoregressions, Statistics and Probability Letters, 33 (1997) 291-297.

See Also

Other datasets: `bodyfat`, `heart`, `student`, `wine`

`bodyfat` *Bodyfat*

Description

The response (`y`) corresponds to estimates of percentage of body fat from application of Siri's 1956 equation to measurements of underwater weighing, as well as age, weight, height, and a variety of body circumference measurements.

Usage

```
bodyfat
```

Format

A list with two items representing 252 observations from 14 variables

age age (years)

weight weight (lbs)

height height (inches)

neck neck circumference (cm)

chest chest circumference (cm)

abdomen abdomen circumference (cm)

hip hip circumference (cm)

thigh thigh circumference (cm)

knee knee circumference (cm)

ankle ankle circumference (cm)

biceps biceps circumference (cm)

forearm forearm circumference (cm)

wrist wrist circumference (cm)

Source

http://lib.stat.cmu.edu/datasets/bodyfat

See Also

Other datasets: `abalone`, `heart`, `student`, `wine`

coef.SLOPE *Obtain Coefficients*

Description

This function returns coefficients from a model fit by SLOPE().

Usage

```
## S3 method for class 'SLOPE'
coef(
  object,
  alpha = NULL,
  exact = FALSE,
  simplify = TRUE,
  intercept = TRUE,
  scale = c("original", "normalized"),
  sigma,
  ...
)
```

Arguments

object	an object of class 'SLOPE'.
alpha	penalty parameter for SLOPE models; if NULL, the values used in the original fit will be used
exact	if TRUE and the given parameter values differ from those in the original fit, the model will be refit by calling stats::update() on the object with the new parameters. If FALSE, the predicted values will be based on interpolated coefficients from the original penalty path.
simplify	if TRUE, base::drop() will be called before returning the coefficients to drop extraneous dimensions
intercept	whether to include the intercept in the output. The intercept is included as the first row of the returned array.
scale	whether to return the coefficients in the original scale or in the normalized scale.
sigma	deprecated. Please use alpha instead.
...	arguments that are passed on to stats::update() (and therefore also to SLOPE()) if exact = TRUE and the given penalty is not in object

Details

If exact = FALSE and alpha is not in object, then the returned coefficients will be approximated by linear interpolation. If coefficients from another type of penalty sequence (with a different lambda) are required, however, please use SLOPE() to refit the model.

Value

Coefficients from the model.

See Also

predict.SLOPE(), SLOPE()

Other SLOPE-methods: deviance.SLOPE(), plot.SLOPE(), predict.SLOPE(), print.SLOPE(), score(), summary.SLOPE()

Examples

```
fit <- SLOPE(mtcars$mpg, mtcars$vs, path_length = 10)
coef(fit)
coef(fit, scale = "normalized")
```

---

cvSLOPE *Tune SLOPE with Cross-Validation*

Description

This function trains a model fit by SLOPE() by tuning its parameters through cross-validation.

Usage

```
cvSLOPE(
  x,
  y,
  q = 0.2,
  gamma = 0,
  n_folds = 10,
  n_repeats = 1,
  measure = c("mse", "mae", "deviance", "misclass", "auc"),
  refit = TRUE,
  ...
)
```

Arguments

x	the design matrix, which can be either a dense matrix of the standard *matrix* class, or a sparse matrix inheriting from Matrix::sparseMatrix. Data frames will be converted to matrices internally.
y	the response, which for family = "gaussian" must be numeric; for family = "binomial" or family = "multinomial", it can be a factor.
q	a vector of quantiles for the q parameter in SLOPE
gamma	relaxation parameter for SLOPE. Default is 0.0, which implies to relaxation of the penalty.

n_folds	number of folds (cross-validation)
n_repeats	number of folds (cross-validation)
measure	DEPRECATED
refit	logical; if TRUE, refits the model on the full dataset using the optimal parameters. Default is TRUE.
...	other arguments to pass on to SLOPE()

Value

An object of class "TrainedSLOPE", with the following slots:

summary	a summary of the results with means, standard errors, and 0.95 confidence levels
data	the raw data from the model training
optima	a data.frame of the best (mean) values for the different metrics and their corresponding parameter values
measure	a data.frame listing the used metric and its label
model	the model fit to the entire dataset using optimal parameters (only present if refit = TRUE)
training_data	the training data used for tuning (x and y)
call	the call

See Also

Other model-tuning: plot.TrainedSLOPE(), refit(), summary.TrainedSLOPE(), trainSLOPE()

Examples

```
# 8-fold cross-validation
tune <- cvSLOPE(
  subset(mtcars, select = c("mpg", "drat", "wt")),
  mtcars$hp,
  q = c(0.1, 0.2),
  n_folds = 8,
  n_repeats = 2,
  measure = "mse"
)

# Access the refitted model
tune$model

# Or use refit() to refit with different measure
fit <- refit(
  tune,
  subset(mtcars, select = c("mpg", "drat", "wt")),
  mtcars$hp
)
coef(fit)
```

deviance.SLOPE *Model Deviance*

Description

Model Deviance

Usage

```
## S3 method for class 'SLOPE'
deviance(object, ...)
```

Arguments

object	an object of class 'SLOPE'.
...	ignored

Value

For Gaussian models this is twice the residual sums of squares. For all other models, two times the negative loglikelihood is returned.

See Also

SLOPE()

Other SLOPE-methods: coef.SLOPE(), plot.SLOPE(), predict.SLOPE(), print.SLOPE(), score(), summary.SLOPE()

Examples

```
fit <- SLOPE(heart$x, heart$y, family = "binomial")
deviance(fit)
```

glioma *Glioma Metabolomics*

Description

Metabolomics dataset from 165 different plasma measurements from 94 patients (cases) with glioma (brain tumours) and 71 healthy controls. The goal is to predict whether a sample is from a patient or a control based on the metabolite measurements.

Usage

```
glioma
```

Format

165 observations from 138 variables represented as a list consisting of a binary response (factor) vector `y` with levels 'control' and 'case' indicating whether the sample is from a healthy control or a patient with glioma, as well as `x`: a matrix of 138 metabolite measurements.

Preprocessing

We have removed the patients with meningioma from the original dataset (which contained 235 samples) to create a binary classification problem. Also, the authors originally had 188 features but removed some of these due to missing data.

Source

Godlewski, A., Czajkowski, M., Mojsak, P., Pienkowski, T., Gosk, W., Lyson, T., Mariak, Z., Reszec, J., Kondraciuk, M., Kaminski, K., Kretowski, M., Moniuszko, M., Kretowski, A., & Ciborowski, M. (2023). A comparison of different machine-learning techniques for the selection of a panel of metabolites allowing early detection of brain tumors. Scientific Reports, 13(1), 11044. doi:10.1038/s41598023382431

`heart` *Heart Disease*

Description

Diagnostic attributes of patients classified as having heart disease or not.

Usage

```
heart
```

Format

270 observations from 17 variables represented as a list consisting of a binary factor response vector `y`, with levels 'absence' and 'presence' indicating the absence or presence of heart disease and `x`: a sparse feature matrix of class 'dgCMatrix' with the following variables:

age age

bp diastolic blood pressure

chol serum cholesterol in mg/dl

hr maximum heart rate achieved

old_peak ST depression induced by exercise relative to rest

vessels the number of major blood vessels (0 to 3) that were colored by fluoroscopy

sex sex of the participant: 0 for male, 1 for female

angina a dummy variable indicating whether the person suffered angina-pectoris during exercise

glucose_high indicates a fasting blood sugar over 120 mg/dl

cp_typical typical angina

cp_atypical atypical angina

cp_nonanginal non-anginal pain

ecg_abnormal indicates a ST-T wave abnormality (T wave inversions and/or ST elevation or depression of > 0.05 mV)

ecg_estes probable or definite left ventricular hypertrophy by Estes' criteria

slope_flat a flat ST curve during peak exercise

slope_downsloping a downwards-sloping ST curve during peak exercise

thal_reversible reversible defect

thal_fixed fixed defect

Preprocessing

The original dataset contained 13 variables. The nominal of these were dummycoded, removing the first category. No precise information regarding variables `chest_pain`, `thal` and `ecg` could be found, which explains their obscure definitions here.

Source

Dua, D. and Karra Taniskidou, E. (2017). UCI Machine Learning Repository http://archive.ics.uci.edu/ml/. Irvine, CA: University of California, School of Information and Computer Science.

See Also

Other datasets: abalone, bodyfat, student, wine

---

plot.SLOPE *Plot Coefficients*

Description

Plot the fitted model's regression coefficients along the regularization path. When the path contains a single solution (only one alpha value), a dot chart is displayed showing the coefficient values. When the path contains multiple solutions, a line plot is displayed showing how coefficients evolve along the regularization path.

Usage

```
## S3 method for class 'SLOPE'
plot(
  x,
  intercept = FALSE,
  x_variable = c("alpha", "deviance_ratio", "step"),
  magnitudes = FALSE,
```

```
  add_labels = FALSE,
  mark_zero = TRUE,
  ...
)
```

Arguments

x	an object of class "SLOPE"
intercept	whether to plot the intercept
x_variable	what to plot on the x axis. "alpha" plots the scaling parameter for the sequence, "deviance_ratio" plots the fraction of deviance explained, and "step" plots step number.
magnitudes	whether to plot the magnitudes of the coefficients
add_labels	whether to add labels (numbers) on the right side of the plot for each coefficient (only used when the path contains multiple solutions)
mark_zero	whether to add a vertical line at zero in the dot chart (only used when the path contains a single solution)
...	for multiple solutions: arguments passed to graphics::matplot(). For a single solution: arguments passed to graphics::dotchart().

Value

Invisibly returns NULL. The function is called for its side effect of producing a plot.

See Also

SLOPE(), plotDiagnostics()

Other SLOPE-methods: coef.SLOPE(), deviance.SLOPE(), predict.SLOPE(), print.SLOPE(), score(), summary.SLOPE()

Examples

```
# Multiple solutions along regularization path
fit <- SLOPE(heart$x, heart$y)
plot(fit)

# Single solution with dot chart
fit_single <- SLOPE(heart$x, heart$y, alpha = 0.1)
plot(fit_single)

# Single solution for multinomial regression
fit_multi <- SLOPE(wine$x, wine$y, family = "multinomial", alpha = 0.05)
plot(fit_multi)
```

`plot.TrainedSLOPE` *Plot Results from Cross-Validation*

Description

Plot Results from Cross-Validation

Usage

```
## S3 method for class 'TrainedSLOPE'
plot(
  x,
  plot_min = TRUE,
  ci_alpha = 0.2,
  ci_border = NA,
  ci_col = "salmon",
  plot_args = list(),
  polygon_args = list(),
  lines_args = list(),
  abline_args = list(),
  index = NULL,
  measure,
  ...
)
```

Arguments

`x`	an object of class `'TrainedSLOPE'`, typically from a call to `cvSLOPE()`
`plot_min`	whether to mark the location of the penalty corresponding to the best prediction score
`ci_alpha`	alpha (opacity) for fill in confidence limits
`ci_border`	color (or flag to turn off and on) the border of the confidence limits
`ci_col`	color for border of confidence limits
`plot_args`	list of additional arguments to pass to `plot()`, which sets up the plot frame
`polygon_args`	list of additional arguments to pass to `graphics::polygon()`, which fills the confidence limits
`lines_args`	list of additional arguments to pass to `graphics::lines()`, which plots the mean
`abline_args`	list of additional arguments to pass to `graphics::abline()`, which plots the minimum
`index`	an optional index, to plot only one (the index-th) set of the parameter combinations.
`measure`	any of the measures used in the call to `trainSLOPE()`. If `measure = "auto"` then deviance will be used for binomial and multinomial models, whilst mean-squared error will be used for Gaussian and Poisson models.
`...`	ignored

Value

A plot for every value of q is produced on the current device.

See Also

Other model-tuning: `cvSLOPE()`, `refit()`, `summary.TrainedSLOPE()`, `trainSLOPE()`

Examples

```
# Cross-validation for a SLOPE binomial model
set.seed(123)
tune <- cvSLOPE(
  subset(mtcars, select = c("mpg", "drat", "wt")),
  mtcars$hp,
  q = c(0.1, 0.2),
  n_folds = 10
)
plot(tune, ci_col = "salmon", index = 1)
```

---

plotClusters *Plot Cluster Structure*

Description

Note that this function requires the `patterns` argument to be set to `TRUE` in the call to `SLOPE()`. Calling this function on a `SLOPE` object without patterns will result in an error.

Usage

```
plotClusters(
  x,
  plot_signs = FALSE,
  color_clusters = TRUE,
  include_zeroes = TRUE,
  show_alpha = FALSE,
  alpha_steps = NULL,
  palette = "viridis",
  ...
)
```

Arguments

`x`	an object of class `'SLOPE'`
`plot_signs`	logical, indicating whether to plot signs of estimated coefficients on the plot
`color_clusters`	logical, indicating whether the clusters should have different colors
`include_zeroes`	logical, indicating whether zero variables should be plotted. Default to TRUE

show_alpha	logical, indicating whether labels with alpha values or steps in the path should be plotted.
alpha_steps	a vector of integer alpha steps to plot. If NULL, all the steps are plotted.
palette	a character string specifying the color palette to use for the clusters. This is passed to grDevices::hcl.colors().
...	additional arguments passed to graphics::image().

Value

Invisibly returns NULL. The function is called for its side effect of producing a plot.

See Also

SLOPE(), graphics::image(), graphics::text().

Examples

```
set.seed(10)
X <- matrix(rnorm(10000), ncol = 10)
colnames(X) <- paste0("X", 1:10)
beta <- c(rep(10, 3), rep(-20, 2), rep(20, 2), rep(0, 3))
Y <- X %*% beta + rnorm(1000)
fit <- SLOPE(X, Y, patterns = TRUE)

plotClusters(fit)
plotClusters(fit, alpha_steps = 1:10)
```

---

plotDiagnostics *Plot Results from Diagnostics Collected During Model Fitting*

Description

This function plots various diagnostics collected during the model fitting resulting from a call to SLOPE() *provided that* diagnostics = TRUE.

Usage

```
plotDiagnostics(
  object,
  ind = max(object$diagnostics$penalty),
  xvar = c("time", "iteration")
)
```

Arguments

object	an object of class "SLOPE".
ind	either "last"
xvar	what to place on the x axis. iteration plots each iteration, time plots the wall-clock time.

Value

Invisibly returns NULL. The function is called for its side effect of producing a plot.

See Also

SLOPE()

Examples

```
x <- SLOPE(abalone$x, abalone$y, diagnostics = TRUE)
plotDiagnostics(x)
```

---

predict.SLOPE *Generate Predictions from SLOPE Models*

Description

Return predictions from models fit by SLOPE().

Usage

```
## S3 method for class 'SLOPE'
predict(
  object,
  x,
  alpha = NULL,
  type = "link",
  simplify = TRUE,
  exact = FALSE,
  sigma,
  ...
)

## S3 method for class 'GaussianSLOPE'
predict(
  object,
  x,
  sigma = NULL,
  type = c("link", "response"),
  simplify = TRUE,
  ...
)

## S3 method for class 'BinomialSLOPE'
predict(
  object,
  x,
```

```
  sigma = NULL,
  type = c("link", "response", "class"),
  simplify = TRUE,
  ...
)

## S3 method for class 'PoissonSLOPE'
predict(
  object,
  x,
  sigma = NULL,
  type = c("link", "response"),
  exact = FALSE,
  simplify = TRUE,
  ...
)

## S3 method for class 'MultinomialSLOPE'
predict(
  object,
  x,
  sigma = NULL,
  type = c("link", "response", "class"),
  exact = FALSE,
  simplify = TRUE,
  ...
)
```

Arguments

object	an object of class "SLOPE", typically the result of a call to SLOPE()
x	new data
alpha	penalty parameter for SLOPE models; if NULL, the values used in the original fit will be used
type	type of prediction; "link" returns the linear predictors, "response" returns the result of applying the link function, and "class" returns class predictions.
simplify	if TRUE, base::drop() will be called before returning the coefficients to drop extraneous dimensions
exact	if TRUE and the given parameter values differ from those in the original fit, the model will be refit by calling stats::update() on the object with the new parameters. If FALSE, the predicted values will be based on interpolated coefficients from the original penalty path.
sigma	deprecated. Please use alpha instead.
...	ignored and only here for method consistency

Value

Predictions from the model with scale determined by type.

See Also

stats::predict(), stats::predict.glm()

Other SLOPE-methods: coef.SLOPE(), deviance.SLOPE(), plot.SLOPE(), print.SLOPE(), score(), summary.SLOPE()

Examples

```
fit <- with(mtcars, SLOPE(cbind(mpg, hp), vs, family = "binomial"))
predict(fit, with(mtcars, cbind(mpg, hp)), type = "class")
```

---

print.SLOPE *Print Results from SLOPE Fit*

Description

Print Results from SLOPE Fit

Usage

```
## S3 method for class 'SLOPE'
print(x, ...)

## S3 method for class 'TrainedSLOPE'
print(x, ...)
```

Arguments

x	an object of class 'SLOPE' or 'TrainedSLOPE'
...	other arguments passed to print()

Value

Prints output on the screen

See Also

SLOPE(), print.SLOPE()

Other SLOPE-methods: coef.SLOPE(), deviance.SLOPE(), plot.SLOPE(), predict.SLOPE(), score(), summary.SLOPE()

Examples

```
fit <- SLOPE(wine$x, wine$y, family = "multinomial")
print(fit, digits = 1)
```

print.summary_SLOPE *Print Summary of SLOPE Model*

Description

Print Summary of SLOPE Model

Usage

```
## S3 method for class 'summary_SLOPE'
print(x, digits = 3, ...)
```

Arguments

x	an object of class 'summary_SLOPE'
digits	number of significant digits to print
...	other arguments passed to print()

Value

Invisibly returns the input object

See Also

summary.SLOPE()

print.summary_TrainedSLOPE *Print Summary of TrainedSLOPE Model*

Description

Print Summary of TrainedSLOPE Model

Usage

```
## S3 method for class 'summary_TrainedSLOPE'
print(x, digits = 3, ...)
```

Arguments

x	an object of class 'summary_TrainedSLOPE'
digits	number of significant digits to print
...	other arguments passed to print()

Value

Invisibly returns the input object

See Also

summary.TrainedSLOPE()

---

refit *Refit SLOPE Model with Optimal Parameters*

Description

Refits a SLOPE model using the optimal parameters found through cross-validation. This is a convenience function to avoid having to manually extract optimal parameters and refit.

Usage

```
refit(object, x = NULL, y = NULL, measure = NULL, ...)
```

Arguments

object	an object of class 'TrainedSLOPE', typically from a call to cvSLOPE() or trainSLOPE()
x	the design matrix. If NULL (default), uses the training data stored in object.
y	the response vector. If NULL (default), uses the training data stored in object.
measure	which performance measure to use for selecting optimal parameters. If NULL (default), uses the first measure in the TrainedSLOPE object.
...	additional arguments passed to SLOPE()

Value

An object of class 'SLOPE' fit with the optimal parameters

See Also

SLOPE()

Other model-tuning: cvSLOPE(), plot.TrainedSLOPE(), summary.TrainedSLOPE(), trainSLOPE()

Examples

```
# Cross-validation
tune <- trainSLOPE(
  bodyfat$x,
  bodyfat$y,
  q = c(0.1, 0.2),
  measure = "mse"
)
```

```
# Refit with optimal parameters
fit <- refit(tune)

# Use the fitted model
coef(fit)
predict(fit, bodyfat$x)
```

`regularizationWeights` *Generate Regularization (Penalty) Weights for SLOPE*

Description

This function generates sequences of regularizations weights for use in `SLOPE()` (or elsewhere).

Usage

```
regularizationWeights(
  n_lambda = 100,
  type = c("bh", "gaussian", "oscar", "lasso"),
  q = 0.2,
  theta1 = 1,
  theta2 = 0.5,
  n = NULL
)
```

Arguments

`n_lambda`	The number of lambdas to generate. This should typically be equal to the number of predictors in your data set.
`type`	The type of lambda sequence to use. See documentation for in `SLOPE()`, including that related to the `lambda` parameter in that function.
`q`	parameter controlling the shape of the lambda sequence, with usage varying depending on the type of path used and has no effect is a custom `lambda` sequence is used. Must be greater than `1e-6` and smaller than 1.
`theta1`	parameter controlling the shape of the lambda sequence when `lambda == "OSCAR"`. This parameter basically sets the intercept for the lambda sequence and is equivalent to λ_1 in the original OSCAR formulation.
`theta2`	parameter controlling the shape of the lambda sequence when `lambda == "OSCAR"`. This parameter basically sets the slope for the lambda sequence and is equivalent to λ_2 in the original OSCAR formulation.
`n`	The number of rows (observations) in the design matrix.

Details

Please see SLOPE() for detailed information regarding the parameters in this function, in particular the section *Regularization Sequences*.

Note that these sequences are automatically scaled (unless a value for the alpha parameter is manually supplied) when using SLOPE(). In this function, no such scaling is attempted.

Value

A vector of length n_lambda with regularization weights.

See Also

SLOPE()

Examples

```
# compute different penalization sequences
bh <- regularizationWeights(100, q = 0.2, type = "bh")

gaussian <- regularizationWeights(
  100,
  q = 0.2,
  n = 300,
  type = "gaussian"
)

oscar <- regularizationWeights(
  100,
  theta1 = 1.284,
  theta2 = 0.0182,
  type = "oscar"
)

lasso <- regularizationWeights(100, type = "lasso") * mean(oscar)

# Plot a comparison between these sequences
plot(bh, type = "l", ylab = expression(lambda))
lines(gaussian, col = "dark orange")
lines(oscar, col = "navy")
lines(lasso, col = "red3")

legend(
  "topright",
  legend = c("BH", "Gaussian", "OSCAR", "lasso"),
  col = c("black", "dark orange", "navy", "red3"),
  lty = 1
)
```

score *Compute One of Several Loss Metrics on a New Data Set*

Description

This function is a unified interface to return various types of loss for a model fit with `SLOPE()`.

Usage

```
score(object, x, y, measure)

## S3 method for class 'GaussianSLOPE'
score(object, x, y, measure = c("mse", "mae"))

## S3 method for class 'BinomialSLOPE'
score(object, x, y, measure = c("mse", "mae", "deviance", "misclass", "auc"))

## S3 method for class 'MultinomialSLOPE'
score(object, x, y, measure = c("mse", "mae", "deviance", "misclass"))

## S3 method for class 'PoissonSLOPE'
score(object, x, y, measure = c("mse", "mae"))
```

Arguments

`object`	an object of class `"SLOPE"`
`x`	feature matrix
`y`	response
`measure`	type of target measure. `"mse"` returns mean squared error. `"mae"` returns mean absolute error, `"misclass"` returns misclassification rate, and `"auc"` returns area under the ROC curve.

Value

The measure along the regularization path depending on the value in `measure`.#'

See Also

`SLOPE()`, `predict.SLOPE()`

Other SLOPE-methods: `coef.SLOPE()`, `deviance.SLOPE()`, `plot.SLOPE()`, `predict.SLOPE()`, `print.SLOPE()`, `summary.SLOPE()`

Examples

```
x <- subset(infert, select = c("induced", "age", "pooled.stratum"))
y <- infert$case

fit <- SLOPE(x, y, family = "binomial")
score(fit, x, y, measure = "auc")
```

SLOPE *Sorted L-One Penalized Estimation*

Description

Fit a generalized linear model regularized with the sorted L1 norm, which applies a non-increasing regularization sequence to the coefficient vector (β) after having sorted it in decreasing order according to its absolute values.

Usage

```
SLOPE(
  x,
  y,
  family = c("gaussian", "binomial", "multinomial", "poisson"),
  intercept = TRUE,
  center = c("mean", "min", "none"),
  scale = c("sd", "l1", "l2", "max_abs", "none"),
  alpha = c("path", "estimate"),
  lambda = c("bh", "gaussian", "oscar", "lasso"),
  alpha_min_ratio = if (NROW(x) < NCOL(x)) 0.01 else 1e-04,
  path_length = 100,
  q = 0.1,
  theta1 = 1,
  theta2 = 0.5,
  tol_dev_change = 1e-05,
  tol_dev_ratio = 0.999,
  max_variables = NROW(x) + 1,
  solver = c("auto", "hybrid", "pgd", "fista", "admm"),
  max_passes = 1e+06,
  tol = 1e-04,
  threads = 1,
  diagnostics = FALSE,
  patterns = FALSE,
  gamma = 1,
  cd_type = c("permuted", "cyclical"),
  tol_abs,
  tol_rel,
  tol_rel_gap,
  tol_infeas,
```

```
  tol_rel_coef_change,
  prox_method,
  screen,
  verbosity,
  screen_alg
)
```

Arguments

x	the design matrix, which can be either a dense matrix of the standard *matrix* class, or a sparse matrix inheriting from Matrix::sparseMatrix. Data frames will be converted to matrices internally.
y	the response, which for `family = "gaussian"` must be numeric; for `family = "binomial"` or `family = "multinomial"`, it can be a factor.
family	model family (objective); see **Families** for details.
intercept	whether to fit an intercept
center	whether to center predictors or not by their mean. Defaults to `TRUE` if `x` is dense and `FALSE` otherwise.
scale	type of scaling to apply to predictors. • `"l1"` scales predictors to have L1 norms of one. • `"l2"` scales predictors to have L2 norms of one.#' • `"sd"` scales predictors to have a population standard deviation one. • `"none"` applies no scaling.
alpha	scale for regularization path: either a decreasing numeric vector (possibly of length 1) or a character vector; in the latter case, the choices are: • `"path"`, which computes a regularization sequence where the first value corresponds to the intercept-only (null) model and the last to the almost-saturated model, and • `"estimate"`, which estimates a *single* `alpha` using Algorithm 5 in Bogdan et al. (2015). When a value is manually entered for `alpha`, it will be scaled based on the type of standardization that is applied to `x`. For `scale = "l2"`, `alpha` will be scaled by $\sqrt{n}$. For `scale = "sd"` or `"none"`, alpha will be scaled by n, and for `scale = "l1"` no scaling is applied. Note, however, that the `alpha` that is returned in the resulting value is the **unstandardized** alpha.
lambda	either a character vector indicating the method used to construct the lambda path or a numeric non-decreasing vector with length equal to the number of coefficients in the model; see section **Regularization sequences** for details.
alpha_min_ratio	smallest value for `lambda` as a fraction of `lambda_max`; used in the selection of `alpha` when `alpha = "path"`.
path_length	length of regularization path; note that the path returned may still be shorter due to the early termination criteria given by `tol_dev_change`, `tol_dev_ratio`, and `max_variables`.

q	parameter controlling the shape of the lambda sequence, with usage varying depending on the type of path used and has no effect is a custom `lambda` sequence is used. Must be greater than `1e-6` and smaller than 1.
theta1	parameter controlling the shape of the lambda sequence when `lambda == "OSCAR"`. This parameter basically sets the intercept for the lambda sequence and is equivalent to λ_1 in the original OSCAR formulation.
theta2	parameter controlling the shape of the lambda sequence when `lambda == "OSCAR"`. This parameter basically sets the slope for the lambda sequence and is equivalent to λ_2 in the original OSCAR formulation.
tol_dev_change	the regularization path is stopped if the fractional change in deviance falls below this value; note that this is automatically set to 0 if a alpha is manually entered
tol_dev_ratio	the regularization path is stopped if the deviance ratio $1-\text{deviance}/(\text{null}-\text{deviance})$ is above this threshold
max_variables	criterion for stopping the path in terms of the maximum number of unique, nonzero coefficients in absolute value in model. For the multinomial family, this value will be multiplied internally with the number of levels of the response minus one.
solver	type of solver use, either `"auto"`, `"hybrid"`, `"pgd"`, or `"fista"`; `"auto"` means that the solver is automatically selected, which currently means that `"hybrid"` is used for all objectives except multinomial ones, in which case FISTA (`"fista"`) is used.
max_passes	maximum number of passes (outer iterations) for solver
tol	stopping criterion for the solvers in terms of the relative duality gap
threads	number of threads to use in the solver; if `NULL`, half of the available (logical) threads will be used
diagnostics	whether to save diagnostics from the solver (timings and other values depending on type of solver)
patterns	whether to return the SLOPE pattern (cluster, ordering, and sign information) as a list of sparse matrices, one for each step on the path.
gamma	relaxation mixing parameter, between 0 and 1. Has no effect if set to 0. If larger than 0, the solver will mix the coefficients from the ordinary SLOPE solutions with the coefficients from the relaxed solutions (fitting OLS on the SLOPE pattern).
cd_type	Type of coordinate descent to use, either `"cyclical"` or `"permuted"`. The former means that the cluster are cycled through in descending order of their coefficients' magnitudes, while the latter means that the clusters are permuted randomly for each pass.
tol_abs	DEPRECATED
tol_rel	relative DEPRECATED
tol_rel_gap	DEPRECATED
tol_infeas	DEPRECATED
tol_rel_coef_change	DEPRECATED

prox_method	DEPRECATED
screen	DEPRECATED
verbosity	DEPRECATED
screen_alg	DEPRECATED

Details

SLOPE() solves the convex minimization problem

$$f(\beta) + \alpha \sum_{i=j}^{p} \lambda_j |\beta|_{(j)},$$

where $f(\beta)$ is a smooth and convex function and the second part is the sorted L1-norm. In ordinary least-squares regression, $f(\beta)$ is simply the squared norm of the least-squares residuals. See section **Families** for specifics regarding the various types of $f(\beta)$ (model families) that are allowed in SLOPE().

By default, SLOPE() fits a path of models, each corresponding to a separate regularization sequence, starting from the null (intercept-only) model to an almost completely unregularized model. These regularization sequences are parameterized using λ and α, with only α varying along the path. The length of the path can be manually, but will terminate prematurely depending on arguments tol_dev_change, tol_dev_ratio, and max_variables. This means that unless these arguments are modified, the path is not guaranteed to be of length path_length.

Value

An object of class "SLOPE" with the following slots:

coefficients	a list of the coefficients from the model fit, not including the intercept. The coefficients are stored as sparse matrices.
nonzeros	a three-dimensional logical array indicating whether a coefficient was zero or not
lambda	the lambda vector that when multiplied by a value in alpha gives the penalty vector at that point along the regularization path
alpha	vector giving the (unstandardized) scaling of the lambda sequence
class_names	a character vector giving the names of the classes for binomial and multinomial families
passes	the number of passes the solver took at each step on the path
deviance_ratio	the deviance ratio (as a fraction of 1)
null_deviance	the deviance of the null (intercept-only) model
family	the name of the family used in the model fit
diagnostics	a data.frame of objective values for the primal and dual problems, as well as a measure of the infeasibility, time, and iteration; only available if diagnostics = TRUE in the call to SLOPE().
n_observations	the number of observations in the training data
n_predictors	the number of predictors in the training data
call	the call used for fitting the model

Families

Gaussian

The Gaussian model (Ordinary Least Squares) minimizes the following objective:

$$\frac{1}{2}\|y - X\beta\|_2^2$$

Binomial

The binomial model (logistic regression) has the following objective:

$$\sum_{i=1}^{n} \log\left(1 + \exp\left(-y_i\left(x_i^T\beta + \beta_0\right)\right)\right)$$

with $y \in \{-1, 1\}$.

Poisson

In poisson regression, we use the following objective:

$$-\sum_{i=1}^{n}\left(y_i\left(x_i^T\beta + \beta_0\right) - \exp\left(x_i^T\beta + \beta_0\right)\right)$$

Multinomial

In multinomial regression, we minimize the full-rank objective

$$-\sum_{i=1}^{n}\left(\sum_{k=1}^{m-1} y_{ik}(x_i^T\beta_k + \beta_{0,k}) - \log\sum_{k=1}^{m-1}\exp\left(x_i^T\beta_k + \beta_{0,k}\right)\right)$$

with y_{ik} being the element in a n by $(m-1)$ matrix, where m is the number of classes in the response.

Regularization Sequences

There are multiple ways of specifying the `lambda` sequence in `SLOPE()`. It is, first of all, possible to select the sequence manually by using a non-increasing numeric vector, possibly of length one, as argument instead of a character. The greater the differences are between consecutive values along the sequence, the more clustering behavior will the model exhibit. Note, also, that the scale of the λ vector makes no difference if `alpha = NULL`, since `alpha` will be selected automatically to ensure that the model is completely sparse at the beginning and almost unregularized at the end. If, however, both `alpha` and `lambda` are manually specified, then the scales of both do matter, so make sure to choose them wisely.

Instead of choosing the sequence manually, one of the following automatically generated sequences may be chosen.

BH (Benjamini–Hochberg)

If `lambda = "bh"`, the sequence used is that referred to as $\lambda^{(\mathrm{BH})}$ by Bogdan et al, which sets λ according to

$$\lambda_i = \Phi^{-1}(1 - iq/(2p)),$$

for $i = 1, \dots, p$, where Φ^{-1} is the quantile function for the standard normal distribution and q is a parameter that can be set by the user in the call to `SLOPE()`.

Gaussian

This penalty sequence is related to BH, such that

$$\lambda_i = \lambda_i^{(\mathrm{BH})} \sqrt{1 + w(i-1) \cdot \mathrm{cumsum}(\lambda^2)_i},$$

for $i = 1, \dots, p$, where $w(k) = 1/(n-k-1)$. We let $\lambda_1 = \lambda_1^{(\mathrm{BH})}$ and adjust the sequence to make sure that it's non-increasing. Note that if p is large relative to n, this option will result in a constant sequence, which is usually not what you would want.

OSCAR

This sequence comes from Bondell and Reich and is a linear non-increasing sequence, such that

$$\lambda_i = \theta_1 + (p-i)\theta_2.$$

for $i = 1, \dots, p$. We use the parametrization from Zhong and Kwok (2021) but use θ_1 and θ_2 instead of λ_1 and λ_2 to avoid confusion and abuse of notation.

lasso

SLOPE is exactly equivalent to the lasso when the sequence of regularization weights is constant, i.e.

$$\lambda_i = 1$$

for $i = 1, \dots, p$. Here, again, we stress that the fact that all λ are equal to one does not matter as long as `alpha == NULL` since we scale the vector automatically. Note that this option is only here for academic interest and to highlight the fact that SLOPE is a generalization of the lasso. There are more efficient packages, such as **glmnet** and **biglasso**, for fitting the lasso.

Solvers

There are currently three solvers available for SLOPE: Hybrid (Beck and Teboulle 2009), proximal gradient descent (PGD), and FISTA (Beck and Teboulle, 2009). The hybrid method is the preferred and generally fastest method and is therefore the default for the Gaussian and binomial families, but not currently available for multinomial and disabled for Poisson due to convergence issues.

References

Bogdan, M., van den Berg, E., Sabatti, C., Su, W., & Candès, E. J. (2015). SLOPE – adaptive variable selection via convex optimization. The Annals of Applied Statistics, 9(3), 1103–1140.

Larsson, J., Klopfenstein, Q., Massias, M., & Wallin, J. (2023). Coordinate descent for SLOPE. In F. Ruiz, J. Dy, & J.-W. van de Meent (Eds.), Proceedings of the 26th international conference on artificial intelligence and statistics (Vol. 206, pp. 4802–4821). PMLR. https://proceedings.mlr.press/v206/larsson23a.html

Bondell, H. D., & Reich, B. J. (2008). Simultaneous Regression Shrinkage, Variable Selection, and Supervised Clustering of Predictors with OSCAR. Biometrics, 64(1), 115–123. JSTOR.

Boyd, S., Parikh, N., Chu, E., Peleato, B., & Eckstein, J. (2010). Distributed Optimization and Statistical Learning via the Alternating Direction Method of Multipliers. Foundations and Trends® in Machine Learning, 3(1), 1–122.

Beck, A., & Teboulle, M. (2009). A Fast Iterative Shrinkage-Thresholding Algorithm for Linear Inverse Problems. SIAM Journal on Imaging Sciences, 2(1), 183–202.

See Also

plot.SLOPE(), plotDiagnostics(), score(), predict.SLOPE(), trainSLOPE(), coef.SLOPE(), print.SLOPE(), print.SLOPE(), deviance.SLOPE(), sortedL1Prox()

Examples

```
# Gaussian response, default lambda sequence
fit <- SLOPE(bodyfat$x, bodyfat$y)

# Multinomial response, custom alpha and lambda
m <- length(unique(wine$y)) - 1
p <- ncol(wine$x)

alpha <- 0.005
lambda <- exp(seq(log(2), log(1.8), length.out = p * m))

fit <- SLOPE(
  wine$x,
  wine$y,
  family = "multinomial",
  lambda = lambda,
  alpha = alpha
)
```

---

sortedL1Prox *Sorted L1 Proximal Operator*

Description

The proximal operator for the Sorted L1 Norm, which is the penalty function in SLOPE. It solves the problem

$$\arg\min_x \left(J(x, \lambda) + \frac{1}{2}||x - v||_2^2 \right)$$

where $J(x, \lambda)$ is the Sorted L1 Norm.

Usage

```
sortedL1Prox(x, lambda, method)
```

Arguments

x	A vector. In SLOPE, this is the vector of coefficients.
lambda	A non-negative and decreasing sequence of weights for the Sorted L1 Norm. Needs to be the same length as x.
method	DEPRECATED

Value

An evaluation of the proximal operator at `x` and `lambda`.

Source

M. Bogdan, E. van den Berg, Chiara Sabatti, Weijie Su, and Emmanuel J. Candès, "SLOPE – adaptive variable selection via convex optimization," Ann Appl Stat, vol. 9, no. 3, pp. 1103–1140, 2015.

`student` *Student Performance*

Description

A data set of the attributes of 382 students in secondary education collected from two schools. The goal is to predict the grade in math and Portugese at the end of the third period. See the cited sources for additional information.

Usage

```
student
```

Format

382 observations from 13 variables represented as a list consisting of a binary factor response matrix `y` with two responses: `portugese` and `math` for the final scores in period three for the respective subjects. The list also contains `x`: a sparse feature matrix of class 'dgCMatrix' with the following variables:

school_ms student's primary school, 1 for Mousinho da Silveira and 0 for Gabriel Pereira

sex sex of student, 1 for male

age age of student

urban urban (1) or rural (0) home address

large_family whether the family size is larger than 3

cohabitation whether parents live together

Medu mother's level of education (ordered)

Fedu fathers's level of education (ordered)

Mjob_health whether the mother was employed in health care

Mjob_other whether the mother was employed as something other than the specified job roles

Mjob_services whether the mother was employed in the service sector

Mjob_teacher whether the mother was employed as a teacher

Fjob_health whether the father was employed in health care

Fjob_other whether the father was employed as something other than the specified job roles

Fjob_services whether the father was employed in the service sector

Fjob_teacher whether the father was employed as a teacher

reason_home school chosen for being close to home

reason_other school chosen for another reason

reason_rep school chosen for its reputation

nursery whether the student attended nursery school

internet Pwhether the student has internet access at home

Preprocessing

All of the grade-specific predictors were dropped from the data set. (Note that it is not clear from the source why some of these predictors are specific to each grade, such as which parent is the student's guardian.) The categorical variables were dummy-coded. Only the final grades (G3) were kept as dependent variables, whilst the first and second period grades were dropped.

Source

P. Cortez and A. Silva. Using Data Mining to Predict Secondary School Student Performance. In A. Brito and J. Teixeira Eds., Proceedings of 5th FUture BUsiness TEChnology Conference (FUBUTEC 2008) pp. 5-12, Porto, Portugal, April, 2008, EUROSIS, ISBN 978-9077381-39-7.

Dua, D. and Karra Taniskidou, E. (2017). UCI Machine Learning Repository http://archive.ics.uci.edu/ml/. Irvine, CA: University of California, School of Information and Computer Science.

See Also

Other datasets: abalone, bodyfat, heart, wine

---

summary.SLOPE *Summarize SLOPE Model*

Description

Produces a summary of a fitted SLOPE model, including information about the regularization path, model family, and fitted values.

Usage

```
## S3 method for class 'SLOPE'
summary(object, ...)
```

Arguments

object	an object of class "SLOPE", typically from a call to SLOPE()
...	other arguments (currently ignored)

Value

An object of class "summary_SLOPE" with the following components:

call	the call that produced the model
family	the model family
n_obs	number of observations
n_predictors	number of predictors
has_intercept	whether an intercept was fit
path_length	number of steps in the regularization path
alpha_range	range of alpha values in the path
deviance_ratio_range	range of deviance ratios in the path
null_deviance	null deviance
path_summary	data frame summarizing the regularization path

See Also

SLOPE(), print.summary_SLOPE()

Other SLOPE-methods: coef.SLOPE(), deviance.SLOPE(), plot.SLOPE(), predict.SLOPE(), print.SLOPE(), score()

Examples

```
fit <- SLOPE(heart$x, heart$y)
summary(fit)

# Multinomial example
fit_multi <- SLOPE(wine$x, wine$y, family = "multinomial")
summary(fit_multi)
```

---

summary.TrainedSLOPE *Summarize TrainedSLOPE Model*

Description

Produces a summary of a trained SLOPE model from cross-validation, including information about the optimal parameters and performance metrics.

Usage

```
## S3 method for class 'TrainedSLOPE'
summary(object, ...)
```

Arguments

object	an object of class 'TrainedSLOPE', typically from a call to cvSLOPE() or trainSLOPE()
...	other arguments (currently ignored)

Value

An object of class 'summary_TrainedSLOPE' with the following components:

call	the call that produced the model
measure	the performance measure(s) used
optima	optimal parameter values and corresponding performance
n_folds	number of cross-validation folds
n_repeats	number of cross-validation repeats
n_models	total number of models evaluated

See Also

cvSLOPE(), trainSLOPE(), print.summary_TrainedSLOPE()

Other model-tuning: cvSLOPE(), plot.TrainedSLOPE(), refit(), trainSLOPE()

Examples

```
tune <- cvSLOPE(
  subset(mtcars, select = c("mpg", "drat", "wt")),
  mtcars$hp,
  q = c(0.1, 0.2),
  n_folds = 5
)
summary(tune)
```

---

trainSLOPE *Train a SLOPE Model*

Description

This function trains a model fit by SLOPE() by tuning its parameters through cross-validation.

Usage

```
trainSLOPE(
  x,
  y,
  q = 0.2,
  number = 10,
  repeats = 1,
  measure = c("mse", "mae", "deviance", "misclass", "auc"),
  ...
)
```

Arguments

x	the design matrix, which can be either a dense matrix of the standard *matrix* class, or a sparse matrix inheriting from Matrix::sparseMatrix. Data frames will be converted to matrices internally.
y	the response, which for `family = "gaussian"` must be numeric; for `family = "binomial"` or `family = "multinomial"`, it can be a factor.
q	parameter controlling the shape of the lambda sequence, with usage varying depending on the type of path used and has no effect is a custom `lambda` sequence is used. Must be greater than `1e-6` and smaller than 1.
number	number of folds (cross-validation)
repeats	number of repeats for each fold (for repeated *k*-fold cross validation)
measure	measure to try to optimize; note that you may supply *multiple* values here and that, by default, all the possible measures for the given model will be used.
...	other arguments to pass on to `SLOPE()`

Details

Note that by default this method matches all of the available metrics for the given model family against those provided in the argument `measure`. Collecting these measures is not particularly demanding computationally so it is almost always best to leave this argument as it is and then choose which argument to focus on in the call to `plot.TrainedSLOPE()`.

Value

An object of class `"TrainedSLOPE"`, with the following slots:

summary	a summary of the results with means, standard errors, and 0.95 confidence levels
data	the raw data from the model training
optima	a `data.frame` of the best (mean) values for the different metrics and their corresponding parameter values
measure	a `data.frame` listing the used metrics and their labels
model	the model fit to the entire data set
training_data	the training data used for tuning (`x` and `y`)
call	the call

See Also

Other model-tuning: `cvSLOPE()`, `plot.TrainedSLOPE()`, `refit()`, `summary.TrainedSLOPE()`

Examples

```
# 8-fold cross-validation repeated 5 times
tune <- trainSLOPE(subset(mtcars, select = c("mpg", "drat", "wt")),
  mtcars$hp,
  q = c(0.1, 0.2),
  number = 8,
```

```
  repeats = 5,
  measure = "mse"
)
```

`wine` *Wine Cultivars*

Description

A data set of results from chemical analysis of wines grown in Italy from three different cultivars.

Usage

```
wine
```

Format

178 observations from 13 variables represented as a list consisting of a categorical response vector y with three levels: *A*, *B*, and *C* representing different cultivars of wine as well as `x`: a sparse feature matrix of class 'dgCMatrix' with the following variables:

alcohol alcoholic content

malic malic acid

ash ash

alcalinity alcalinity of ash

magnesium magnemium

phenols total phenols

flavanoids flavanoids

nonflavanoids nonflavanoid phenols

proanthocyanins proanthocyanins

color color intensity

hue hue

dilution OD280/OD315 of diluted wines

proline proline

Source

Dua, D. and Karra Taniskidou, E. (2017). UCI Machine Learning Repository http://archive.ics.uci.edu/ml/. Irvine, CA: University of California, School of Information and Computer Science.

https://raw.githubusercontent.com/hadley/rminds/master/1-data/wine.csv

See Also

Other datasets: `abalone`, `bodyfat`, `heart`, `student`

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