

Package: NAM (via r-universe)

May 24, 2026

Type Package

Title Nested Association Mapping

Version 1.8.0

Date 2026-01-23

Maintainer Alencar Xavier <alenvav@gmail.com>

Description Designed for association studies in nested association mapping (NAM) panels, experimental and random panels. The method is described by Xavier et al. (2015) <[doi:10.1093/bioinformatics/btv448](https://doi.org/10.1093/bioinformatics/btv448)>. It includes tools for genome-wide associations of multiple populations, marker quality control, population genetics analysis, genome-wide prediction, solving mixed models and finding variance components through likelihood and Bayesian methods.

License GPL-3

Imports Rcpp

LinkingTo Rcpp

Depends R (>= 3.2.0)

NeedsCompilation yes

Suggests knitr, rmarkdown, bWGR

VignetteBuilder knitr

Author Alencar Xavier [aut, cre], William Muir [aut], Katy Rainey [aut], Shizhong Xu [aut]

Repository <https://cran.r-universe.dev>

Date/Publication 2026-01-24 06:49:49 UTC

RemoteUrl <https://github.com/cran/NAM>

RemoteRef HEAD

RemoteSha e2980d8fc7be457e0a5e65abead7b96a1ce01111

Contents

NAM-package	2
Dataset 1	3
Dataset 2	3
FST	4
GWAS	5
GWP	8
Manhattan	10
MLM Gibbs	11
MLM MV-PEGS	14
MLM REML	16
MLM Trials	17
Optimizations	19
SNP H2	22
SNP QC	23
Index	25

NAM-package	<i>Nested Association Mapping</i>
-------------	-----------------------------------

Description

Designed for association studies in nested association mapping (NAM) panels, also handling experimental and random panels. The method is described by Xavier et al. (2015) <doi:10.1093/bioinformatics/btv448>. It includes tools for genome-wide associations of multiple populations, marker quality control, population genetics analysis, genome-wide prediction, solving mixed models and finding variance components through likelihood and Bayesian methods.

Details

Package: NAM
 Type: Package
 Version: 1.8.0
 Date: 2026-01-23
 License: GPL-3

Author(s)

Alencar Xavier, William Muir, Katy Rainey, Shizhong Xu.
 Maintainer: Alencar Xavier <alencav@gmail.com>

See Also

Package include functions to perform association analysis (`gwas`, `gwas2`, `gwas3`), meta-gwas (`gwasGE`, `meta3`), solve mixed models (`gibbs`, `reml`, `pegs`), genomic prediction (`wgr`, `gmm`, `press`), populations genetic analysis (`Fst`, `Gdist`, `LD`), data quality control (`snpQC`, `snpH2`, `markov`), spatial analysis (`covar`, `SPC`, `SPM`), build kinships (`GRM`, `GAU`, `PedMat`) and more.

Dataset 1

Tetra-seed Pods

Description

Two soybean bi-parental crosses phenotyped for the percentage of pods containing four seeds

Usage

```
data(tpod)
```

Details

Soybean nested association panel with 2 families (*fam*) containing 196 individuals. Genotypic matrix (*gen*) have 376 SNP across 20 chromosome (*chr*). Phenotypic information (*y*) regards the proportion of four seed pods. Data provided by Rainey Lab for Soybean Breeding and Genetics, Purdue University.

Author(s)

Alencar Xavier and Katy Rainey

Dataset 2

Multi-environmental trial

Description

Data collected from the SoyNAM population in Indiana 2013-2015.

Usage

```
data(met)
```

Details

Data provided by Rainey Lab for Soybean Breeding and Genetics, Purdue University. Genotypic matrix (*Gen*) have 4240 SNPs. The data frame *Obs* contains the soybean id (*ID*), environment (*Year*), field location (*Block*, *Row*, *Col*) and three phenotypes: grain yield (*YLD*), days to maturity (*DTM*) and average canopy closure (*ACC*).

Author(s)

Alencar Xavier, Ben Hall and Katy Rainey

References

Xavier, A., Hall, B., Hearst, A.A., Cherkauer, K.A. and Rainey, K.M., 2017. Genetic Architecture of Phenomic-Enabled Canopy Coverage in *Glycine max*. *Genetics*, 206(2), pp.1081-1089.

FST

Fixation Index

Description

Genetic variation associated with markers distributed among subpopulations. The function generates a plot for structure diagnosis.

Usage

`Fst(gen, fam)`

Arguments

gen	Numeric matrix containing the genotypic data. A matrix with n rows of observations and (m) columns of molecular markers. SNPs must be coded as 0, 1, 2, for founder homozygous, heterozygous and reference homozygous. NA is allowed.
fam	Numeric vector of length (n) indicating which subpopulations (<i>i.e.</i> family) each observation comes from. NA is not allowed.

Details

F-statistics (Wright 1965) represent the differentiation among populations for a given locus. Weir and Cockerham (1984) provided an unbiased version for molecular analysis.

FIT is the correlation between gametes that unite to produce the individuals, relative to the gametes of the total population. FIS is the average over all subdivisions of the correlation between uniting gametes relative to those of their own subdivision. FST is the correlation between random gametes within subdivisions, relative to gametes of the total population. Neutral markers have an expected FST 0.05.

Value

List with values of FST, FIS and FIT. Unbiased F-statistics from weighted AOV (Weir and Cockerham 1984).

Author(s)

Alencar Xavier and William Muir

References

- Weir, B. S., and Cockerham, C. C. (1984). Estimating F-statistics for the analysis of population structure. *Evolution*, 38(6), 1358-1370.
- Wright, S. (1965). The interpretation of population structure by F-statistics with special regard to systems of mating. *Evolution*, 19(3), 395-420.

Examples

```
## Not run:
data(tpod)
Fstat = Fst(gen=gen, fam=fam)
plot(Fstat, chr=chr)

## End(Not run)
```

GWAS

Empirical Bayes Genome Wide Association Mapping

Description

The `gwas` function calculates the likelihood ratio for each marker under the empirical Bayesian framework. The method allows analysis with multiple populations. `gwas2` is computationally optimized. `gwas3` was design for multiple random populations.

Usage

```
gwas(y, gen, fam=NULL, chr=NULL, window=NULL, fixed=FALSE)
gwas2(y, gen, fam=NULL, chr=NULL, fixed=FALSE, EIG=NULL, cov=NULL)
gwas3(y, gen, fam=NULL, chr=NULL, EIG=NULL, cov=NULL)
gwasGE(Phe, gen, fam, chr=NULL, cov=NULL, ge=FALSE, ammi=1)
meta3(ByEnv, ammi=1)
```

Arguments

- | | |
|------------------|---|
| <code>y</code> | Numeric vector of observations (n) describing the trait to be analyzed. NA is allowed. |
| <code>gen</code> | Numeric matrix containing the genotypic data. A matrix with n rows of observations and (m) columns of molecular markers. SNPs must be coded as 0, 1, 2, for founder homozygous, heterozygous and reference homozygous. NA is allowed. |
| <code>fam</code> | Numeric vector of length n indicating a stratification factor or which subpopulation (<i>e.g.</i> family) that each observation comes from. Default assumes that all observations are from the same populations. |
| <code>chr</code> | Numeric vector indicating the number of markers in each chromosome. The sum of <code>chr</code> must be equal to the number of columns in <code>gen</code> . Default assumes that all markers are from the same chromosome. |

window	Numeric. If specified, genetic distance between markers is used for moving window strategy. Window must be specified in Morgans (<i>e.g.</i> 0.05 would represent 5cM). Genetic distance is calculated assuming that individuals are RILs.
fixed	Logical. If TRUE, markers are treated as fixed effect and hence, evaluated through Wald statistics. If markers are specified as fixed, the argument 'window' is not applicable.
EIG	Output of the R function 'eigen'. It is used for user-defined kinship matrix.
cov	Numeric vector of length n to be used as covariate in the association analysis.
Phe	Numeric matrix of observations ($n * e$) where rows represent genotypes and columns represent environments. NA is allowed.
ge	Logical. If TRUE, meta-analysis (function <code>gwasGE</code>) will be done for the $G \times E$ interactions term only. If FALSE, variance components will be computed for three terms: genotype, environment and interaction.
ammi	Integer. It indicates the number of principal components used to represent $G \times E$ interactions through additive main-effects and multiplicative interaction (AMMI).
ByEnv	List of objected output from <code>gwas3</code> to perform meta-analysis.

Details

Empirical Bayes model (Wang 2016) with a special incidence matrix is recreated to optimize the information provided by the subpopulations. Each locus is recoded as a vector with length f equal to number of subpopulations, or NAM families, as the interaction locus by family. For example, a locus heterozygous from an individual from subpopulation 2 is coded as [1, 0, 1, ..., f], a locus homozygous for the reference allele from any subpopulation is coded as [2, 0, 0, ..., f] and a locus homozygous for the founder allele from an individual from subpopulation 1 is coded as [0, 2, 0, ..., f]. The base model for genome scanning is described by:

$$y = Xb + Zu + g + e$$

That includes the fixed effect (Xb), the marker (Zu), the polygene (g) and the residuals (e). If the *window* term is specified, the model for genome scanning is expanded as follows:

$$y = Xb + Zu[k - 1] + Zu + Zu[k + 1] + g - g[k] + e$$

This model includes three extra terms: the left side genome ($Zu[k - 1]$) and the right side genome ($Zu[k + 1]$), also subtracting the window polygene ($-g[k]$). Windows are based on genetic distance, which is computed using Kosambi map function. The recombination rate is estimated under the assumption markers are ordered and that genotypes are recombinant inbred lines.

The polygenic term is calculated only once (Zhang et al 2010) using eigendecomposition with a GEMMA-like algorithm (Zhou and Stephens 2012). Efficient inversion of capacitance matrix is obtained through the Woodbury matrix identities. Models and algorithms are described with more detail by Xavier et al (2015) and Wei and Xu (2016).

In order to analyze large dataset, one can avoid memory issues by using the function `gwas2`, but that the argument 'window' is not implemented for `gwas2`. This function also allows user-defined kinship through the argument EIG, and the use of a numeric covariate vector through the argument cov.

When multi-environmental trials are the target of mapping, one may use the function *gwasGE* to perform analysis by environment, followed by "meta-analysis" used to combine the results. This strategy provides an idea of the variation on QTL effect due to environment, genetic background (provided by the stratification factor) and the interaction between environment and genetics.

An alternative to this method is the mega-analysis, where one can provide the stratification factor as a combination of subpopulation and environment. Meta-analysis can be performed in a single step with function *gwasGE*, or users can perform multiple association analyses using *gwas3* and perform meta-analysis with *meta3*. In *gwasGE*, the same genotype will often appear more than once in the phenotypic and genotypic data, so that phenotypes are provided as a matrix. The statistical detail about the meta-analysis are available in the vignette *BackgroundforMeta – analysis*.

The function *gwas3* is an alternative for association analysis and meta-analysis, also solved in the Empirical-Bayes framework for multiple populations. Unlike *gwas*, *gwas2* and *gwasGE*, this function does not set a reference allele and analysis each marker as the interaction of allele by stratification factor (ie. family or subpopulation). Therefore, *gwas3* is compatible with any allele coding.

For further statistical background:

- 1) `system(paste('open', system.file("doc", "gwa_description.pdf", package="NAM")))`
- 2) `system(paste('open', system.file("doc", "gwa_ge_interactions.pdf", package="NAM")))`

Value

The function *gwas* returns a list containing the method deployed (*Method*), a summary of predicted parameters and statistical tests (*PolyTest*), estimated genetic map for NAM panels (*MAP*) and the marker names (*SNPs*).

Author(s)

Alencar Xavier, Tiago Pimenta, Qishan Wang and Shizhong Xu

References

- Wang, Q., Wei, J., Pan, Y., & Xu, S. (2016). An efficient empirical Bayes method for genomewide association studies. *Journal of Animal Breeding and Genetics*, 133(4), 253-263.
- Wei, J., & Xu, S. (2016). A Random Model Approach to QTL Mapping in Multi-parent Advanced Generation Inter-cross (MAGIC) Populations. *Genetics*, 202(2), 471-486.
- Xavier, A., Xu, S., Muir, W. M., & Rainey, K. M. (2015). NAM: Association Studies in Multiple Populations. *Bioinformatics*, 31(23), 3862-3864.
- Zhang et al. 2010. Mixed linear model approach adapted for genome-wide association studies. *Nat. Genet.* 42:355-360.
- Zhou, X., & Stephens, M. (2012). Genome-wide efficient mixed-model analysis for association studies. *Nature genetics*, 44(7), 821-824.

Examples

```
## Not run:
data(tpod)
gen=reference(gen)
gwa=gwas2(y=y, gen=gen, fam=fam, chr=chr, fixed=TRUE)
```

```
plot(gwa,pch=20,lwd=4)

## End(Not run)
```

GWP

Genome-wide prediction

Description

Univariate model to find breeding values through regression with optional resampling techniques (SBMC) and polygenic term (Kernel).

Usage

```
wgr(y,X,it=1500,bi=500,th=1,bag=1,rp=FALSE,iv=FALSE,de=FALSE,
    pi=0,df=5,R2=0.5,eigK=NULL,VarK=0.95,verb=FALSE)
```

Arguments

y	Numeric vector of observations (n) describing the trait to be analyzed. NA is allowed.
X	Numeric matrix containing the genotypic data. A matrix with n rows of observations and (m) columns of molecular markers.
it	Integer. Number of iterations or samples to be generated.
bi	Integer. Burn-in, the number of iterations or samples to be discarded.
th	Integer. Thinning parameter, used to save memory by storing only one every 'th' samples.
bag	If different than one, it indicates the proportion of data to be subsampled in each Markov chain. For datasets with moderate number of observations, values of bag from 0.30 to 0.60 may speed up computation without losses in prediction properties. This argument enable users to enhance MCMC through Subsampling bootstrap Markov chain (SBMC).
rp	Logical. Use replacement for bootstrap samples when bag is different than one.
iv	Logical. Assign markers independent variance, a T prior from a mixture of normals. If true, turns the default model BLUP into BayesA.
de	Logical. Assign markers independent variance through double-exponential prior. If true, turns the default model BLUP into Bayesian LASSO. This argument overrides iv.
pi	Value between 0 and 1. If greater than zero it activates variable selection, where markers have expected probability pi of having null effect.
df	Prior degrees of freedom of variance components.
R2	Expected R2, used to calculate the prior shape.
eigK	Output of function 'eigen'. Spectral decomposition of the kernel used to compute the polygenic term.

VarK	Numeric between 0 and 1. For reduction of dimensionality. Indicates the proportion of variance explained by Eigenpairs used to fit the polygenic term.
verb	Logical. If verbose is TRUE, function displays MCMC progress bar.

Details

The model for the whole-genome regression is as follows:

$$y = \mu + Xb + u + e$$

where y is the response variable, μ is the intercept, X is the genotypic matrix, b is the regression coefficient or effect of an allele substitution, with d probability of being included into the model, u is the polygenic term if a kernel is used, and e is the residual term.

Users can obtain four WGR methods out of this function: BRR ($\pi=0, iv=F$), BayesA ($\pi=0, iv=T$), BayesB ($\pi=0.95, iv=T$), BayesC ($\pi=0.95, iv=F$) and Bayesian LASSO or BayesL ($\pi=0, de=T$). Theoretical basis of each model is described by de los Campos et al. (2013).

Gibbs sampler that updates regression coefficients is adapted from GSRU algorithm (Legarra and Misztal 2008). The variable selection works through the unconditional prior algorithm proposed by Kuo and Mallick (1998). Prior shape estimates are computed as $S_b = R^2 * df * var(y) / MS_x$ and $S_e = (1 - R^2) * df * var(y)$. The polygenic term is solved by Bayesian algorithm of reproducing kernel Hilbert Spaces proposed by de los Campos et al. (2010).

Value

The function `wgr` returns a list with expected value from the marker effect (b), probability of marker being in the model (d), regression coefficient (g), variance of each marker (Vb), the intercept (μ), the polygene (u) and polygenic variance (Vk), residual variance (Ve) and the fitted value (hat).

Author(s)

Alencar Xavier

References

- de los Campos, G., Hickey, J. M., Pong-Wong, R., Daetwyler, H. D., and Calus, M. P. (2013). Whole-genome regression and prediction methods applied to plant and animal breeding. *Genetics*, 193(2), 327-345.
- de los Campos, G., Gianola, D., Rosa, G. J., Weigel, K. A., & Crossa, J. (2010). Semi-parametric genomic-enabled prediction of genetic values using reproducing kernel Hilbert spaces methods. *Genetics Research*, 92(04), 295-308.
- Kuo, L., & Mallick, B. (1998). Variable selection for regression models. *Sankhya: The Indian Journal of Statistics, Series B*, 65-81.
- Legarra, A., & Misztal, I. (2008). Technical note: Computing strategies in genome-wide selection. *Journal of dairy science*, 91(1), 360-366.

Examples

```

## Not run:
# Load data
data(tpod)

# BLUP
BRR = wgr(y,gen,iv=FALSE,pi=0)
cor(y,BRR$hat)

# BayesA
BayesA = wgr(y,gen,iv=TRUE,pi=0)
cor(y,BayesA$hat)

# BayesB
BayesB = wgr(y,gen,iv=TRUE,pi=.95)
cor(y,BayesB$hat)

# BayesC
BayesC = wgr(y,gen,iv=FALSE,pi=.95)
cor(y,BayesC$hat)

# BayesCpi
BayesCpi = BCpi(y,gen)
cor(y,BayesCpi$hat)

# BayesL
BayesL = wgr(y,gen,de=TRUE)
cor(y,BayesL$hat)

## End(Not run)

```

Manhattan

Manhattan plot for Association Studies

Description

Generates a graphical visualization for the output of the function `gwas/gwas2/gwasGE`.

Usage

```

## S3 method for class 'NAM'
plot(x, ..., alpha=0.05, colA=2, colB=4, find=NULL, FDR=NULL, gtz=FALSE, phys=NULL)

```

Arguments

<code>x</code>	Output of the <code>gwas/gwas2/gwas3</code> function.
<code>...</code>	Further arguments passed to or from other methods.
<code>alpha</code>	Numeric. Significance threshold to display in the Manhattan plot.

colA	Color of odd chromosomes in the Manhattan plot.
colB	Color of even chromosomes in the Manhattan plot.
find	Integer. If provided, you can click on the specified number of hits in the Manhattan plot to obtain the name of the markers.
FDR	Null or numeric between zero and one. If provided, it will display the Manhattan plot with Bonferroni threshold by chromosome, adjusted for the specified false discovery rate (FDR). Thus, zero provides the Bonferroni correction.
gtz	Logical. If TRUE, the argument FDR will just take into account markers with p-value Greater Than Zero (GTZ).
phys	Numeric vector with length equal to the number of markers. If provided, the Manhattan plot is generated using the physical distance in the x axis.

Author(s)

Alencar Xavier and William Beavis

Examples

```
## Not run:
data(tpod)
test=gwas2(y=y,gen=gen[,1:240],fam=fam,chr=chr[1:12])
par(mfrow=c(2,1))

# Example Manhattan 1
SIGNIF = 1+(2*test$PolyTest$lrt>4.9)
plot(x=test,pch=SIGNIF+3,lwd=SIGNIF,main="Example 2")

# Example Manhattan 2
plot(x=test,main="Example 3",pch=20,lwd=2)
Kern = ksmooth(1:240,test$PolyTest$lrt,bandwidth=1)
lines(Kern,type="l",lwd=2)

## End(Not run)
```

MLM Gibbs

Bayesian Mixed Model

Description

Mixed model solver through Bayesian Gibbs Sampling or iterative solution.

Usage

```
gibbs(y,Z=NULL,X=NULL,iK=NULL,iR=NULL,Iter=1500,Burn=500,
      Thin=2,DF=5,S=NULL,nor=TRUE,GSRU=FALSE)
m1(y,Z=NULL,X=NULL,iK=NULL,iR=NULL,DF=5,S=0.5,nor=TRUE)
gibbs2(Y,Z=NULL,X=NULL,iK=NULL,Iter=150,Burn=50,Thin=1,DF=5,S=0.5,nor=TRUE)
```

Arguments

y	Numeric vector of observations (n) describing the trait to be analyzed. NA is allowed.
Z	Right-hand side formula or list of numeric matrices (n by p) with incidence matrices for random effect. NA is not allowed.
X	Right-hand side formula or incidence matrices (n by p) for fixed effect. NA is not allowed.
iK	Numeric matrix or list of numeric matrices (p by p) corresponding to the the inverse kinship matrix of each random effect with p parameters.
iR	Numeric matrix (n by n) corresponding to the inverse residual correlation matrix.
Iter	Integer. Number of iterations or samples to be generated.
Burn	Integer. Number of iterations or samples to be discarded.
Thin	Integer. Thinning parameter, used to save memory by storing only one every 'Thin' samples.
DF	Integer. Hyperprior degrees of freedom of variance components.
S	Integer or NULL. Hyperprior shape of variance components. If NULL, the hyperprior solution for the scale parameter is calculated as proposed by de los Campos et al. (2013).
nor	Logical. If TRUE, it normilizes the response variable(s).
GSRU	Logical. If TRUE, it updates the regression coefficient using Gauss-Seidel Residual Update (Legarra and Misztal 2008). Useful for $p \gg n$, but does not work when iK or iR are provided.
Y	Numeric matrix of observations for multivariate mixed models. Each column represents a trait. NA is allowed.

Details

The general model is $y = Xb + Zu + e$, where $u = N(0, A\sigma^2a)$ and $e = N(0, R\sigma^2e)$. The function solves Gaussian mixed models in the Bayesian framework as described by Garcia-Cortes and Sorensen (1996) and Sorensen and Gianola (2002) with conjugated priors. The alternative function, "ml", finds the solution iteratively using the full-conditional expectation. The function "gibbs2" can be used for the multivariate case, check Xavier et al. (2017) for an example of multivariate mixed model using Gibbs sampling.

Value

The function gibbs returns a list with variance components distribution a posteriori (Posterior.VC) and mode estimated (VC.estimate), a list with the posterior distribution of regression coefficients (Posterior.Coef) and the posterior mean (Coef.estimate), and the fitted values using the mean (Fit.mean) of posterior coefficients.

Author(s)

Alencar Xavier

References

- de los Campos, G., Hickey, J. M., Pong-Wong, R., Daetwyler, H. D., and Calus, M. P. (2013). Whole-genome regression and prediction methods applied to plant and animal breeding. *Genetics*, 193(2), 327-345.
- Legarra, A., & Misztal, I. (2008). Technical note: Computing strategies in genome-wide selection. *Journal of dairy science*, 91(1), 360-366.
- Garcia-Cortes, L. A., and Sorensen, D. (1996). On a multivariate implementation of the Gibbs sampler. *Genetics Selection Evolution*, 28(1), 121-126.
- Sorensen, D., & Gianola, D. (2002). *Likelihood, Bayesian, and MCMC methods in quantitative genetics*. Springer Science & Business Media.
- Xavier, A., Hall, B., Casteel, S., Muir, W. and Rainey, K.M. (2017). Using unsupervised learning techniques to assess interactions among complex traits in soybeans. *Euphytica*, 213(8), p.200.

Examples

```
## Not run:

data(tpod)

# Fitting GBLUP
K = GRM(gen)
iK = chol2inv(K)

# FIT
test1 = gibbs(y,iK=iK,S=1)

# PLOT
par(mfrow=c(1,3))
plot(test1$Fit.mean,y,pch=20,lwd=2,col=3,main='GBLUP')
plot(test1,col=4,lwd=2)

# Heritability
print(paste('h2 = ',round(test1$VC.estimate[1]/sum(test1$VC.estimate),3)))

# Fitting RKHS
G = GAU(gen)
EIG = eigen(G,symmetric = TRUE)
ev = 20
U = EIG$vectors[,1:ev]
iV = diag(1/EIG$values[1:ev])

# FIT
test2 = gibbs(y,Z=U,iK=iV,S=1)

# PLOT
par(mfrow=c(1,3))
plot(test2$Fit.mean,y,pch=20,lwd=2,col=2,main='RKHS')
plot(test2,col=3,lwd=2)

# Heritability
```

```
print(paste('h2 =', round(test2$VC.estimate[1]/sum(test2$VC.estimate), 3)))

## End(Not run)
```

MLM MV-PEGS

Pseudo-Expectation Gauss-Seidel for Multivariate Models

Description

This function implements the Pseudo-Expectation Gauss-Seidel (PEGS) algorithm for multi-trait genomic prediction models. It supports fitting one or more random effects and can apply factor-analytic approximations to the genetic covariance structure.

Usage

```
pegs(Y, X, maxit = 100, logtol = -4, NNC = FALSE,
     covbend = 1.1, covMinEv = 10e-4, XFA = -1)
```

Arguments

Y	A numeric matrix (n x k) of dependent variables, where n is the number of observations and k is the number of response variables. Missing values should be NA.
X	A numeric matrix (n x p) of predictors (i.e., markers) for a single random effect, or a named list of such matrices for multiple random effects.
maxit	An integer specifying the maximum number of iterations.
logtol	A numeric value for the convergence tolerance on a log10 scale. The algorithm stops when the log10 of the sum of squared changes in coefficients is less than this value.
NNC	A logical value. If TRUE, imposes a constraint of non-negative correlations on the genetic covariance matrix.
covbend	A numeric bending factor used to inflate the diagonal of the covariance matrix if it is not positive semi-definite. The bending amount is calculated as $\text{abs}(\text{min_eigenvalue}) * \text{covbend}$.
covMinEv	The minimum allowable eigenvalue for the genetic covariance matrix. If the smallest eigenvalue falls below this threshold, the matrix is "bent" (diagonally inflated) to make it positive semi-definite.
XFA	An integer specifying the number of factors (principal components) to use in the factor-analytic approximation of the genetic covariance matrix. <ul style="list-style-type: none"> • XFA = -1 (Default): Fits a full-rank model (no approximation). • XFA = 0: Fits a diagonal model, assuming independent genetic effects among traits. • XFA > 0: Fits a reduced-rank model using the specified number of factors.

Value

A list containing the following components:

mu Vector of intercepts for each response variable.

b A matrix of regression coefficients ($p \times k$) if a single X matrix is provided, or a named list of such matrices if a list is provided for X .

hat Matrix of predicted values ($n \times k$).

h2 Vector of heritability estimates for each trait.

GC The genetic correlation matrix ($k \times k$) if a single X matrix is provided, or a named list of such matrices for each random effect.

band The inflation factor added to the diagonal of the genetic variance matrix. This will be a single value if one random effect is fit, or a named vector if multiple effects are fit.

numit The number of iterations until convergence.

cnv The final convergence value.

References

Xavier, A., Runcie, D., & Habier, D. (2025). Megavariate methods capture complex genotype-by-environment interactions. *Genetics*, 229(4), iyae179.

Xavier, A., & Habier, D. (2022). A new approach fits multivariate genomic prediction models efficiently. *Genetics Selection Evolution*, 54(1), 45.

Examples

```
# Load simulated data with one random effect
data(test)

# Fit a standard multi-trait model
fit <- pegs(Y, X)

# Heritability
print(fit$h2)

# Genetic correlations
print(fit$GC)

# Accuracy
print(mean(diag(cor(fit$hat, simu$tbv))))
```

MLM REML

*Restricted Maximum Likelihood***Description**

Univariate REML estimators and variance components for a single random variable fitted by an EMMA-like algorithm.

Usage

```
reml(y, X=NULL, Z=NULL, K=NULL)
MCreml(y, K, X=NULL, MC=300, samp=300)
```

Arguments

y	Numeric vector of observations (n) describing the trait to be analyzed. NA is allowed.
X	Formula or incidence matrix (n by p) for fixed effect. NA is not allowed.
Z	Formula or numeric matrix (n by p) that corresponds to the incidence matrix of random effect. NA is not allowed.
K	Numeric matrix (p by p). Kinship matrix for random effect with p parameters. NA is not allowed.
MC	Number of sampling procedures to estimate variance components using MCreml.
samp	Sample size of the sampling procedure to estimate variance components using MCreml.

Details

Solve mixed models with a single random effects minimizing the log restricted maximum likelihood (REML) using the EMMA algorithm (Kang et al 2008). Prediction of random coefficients for ridge-type model are performed according to VanRaden (2008), and kernel-type model via RKHS according to de los Campos et al. (2010).

If y is a matrix with multiple traits, the function solves the mixed model via an ECM algorithm adapted from the EMMREML package (Akdemir and Godfrey 2014).

MCreml is based on subsampling with `samp` observations at a time, repeating the procedure `MC` times. Subsampling is a common Monte Carlo strategy to reduce the computational burden to estimate variance components in large datasets.

Value

The function `reml` returns a list with variance components and heritability (VC), fixed effect coefficients and standard variations (Fixed) and estimated breeding values (EBV).

Author(s)

Alencar Xavier, Tiago Pimenta and Shizhong Xu

References

- Akdemir, D., and O. U. Godfrey (2014) EMMREML: Fitting Mixed Models with Known Covariance Structures. R Package Version 2.0. Available at: <http://CRAN.R-project.org/package=EMMREML>.
- de los Campos, G., Gianola, D., Rosa, G. J., Weigel, K. A., & Crossa, J. (2010). Semi-parametric genomic-enabled prediction of genetic values using reproducing kernel Hilbert spaces methods. *Genetics Research*, 92(04), 295-308.
- Kang, H. M., Zaitlen, N. A., Wade, C. M., Kirby, A., Heckerman, D., Daly, M. J., & Eskin, E. (2008). Efficient control of population structure in model organism association mapping. *Genetics*, 178(3), 1709-1723.
- VanRaden, P. M. (2008). Efficient methods to compute genomic predictions. *Journal of dairy science*, 91(11), 4414-4423.

Examples

```
## Not run:
# Fitting a random model
data(tpod)
FIT = reml(y=y,Z=~as.factor(fam))

# Fitting GBLUP
G = GRM(gen)
GBLUP = reml(y=y,K=G)

# GBLUP vs RRBLUP
g = tcrossprod(gen)
gblup = reml(y=y,K=g)
rrblup = reml(y=y,Z=gen)
rbind(gblup$VC,rrblup$VC)
gebv_gblup = gblup$EBV
gebv_rrblup = c(tcrossprod(t(rrblup$EBV),gen))
plot(gebv_gblup,gebv_rrblup)

## End(Not run)
```

Description

This function was developed to solve a mixel model for multi-environmental trials and/or replicated trials when genomic is available. The model includes a semi-parametric term to account for spatial variation when the field layout of the experiment is know. Covariates (fixed effects), genetics (random effect) and spatial term are fitted all in a single step.

Usage

```
gmm(y,gen,dta=NULL,it=75,bi=25,th=1,model="BRR",...)
```

Arguments

<code>y</code>	Numeric vector of phenotypes of length <i>obs</i> (missing values are allowed). NA is allowed.
<code>gen</code>	Numeric matrix, with dimension $n \times p$. Attention: Rows must be named with genotype IDs. Missing values are replaced by the SNP expectation.
<code>dta</code>	Data frame with <i>obs</i> number of rows containing the genotype ID, spatial information and any other set covariates. Make sure to add a column called "ID" (with capital letters) informing the genotype ID with some match in the object <code>gen</code> . For the spatial adjustment, it is necessary to add three numeric columns (not factors) to <code>dta</code> : "Block", "Row" and "Col" (case sensitive), where Block may refer to a field block or an environment without blocks. Therefore, make sure that blocks from different environments are named differently. Row and Col provide the coordinates for the identification of neighbor plots.
<code>it</code>	Integer. Total numeric of MCMC iterations used to fit the model.
<code>bi</code>	Integer. Burn-in of MCMC iterations, i.e., number of iteration to be discarded prior to model convergence.
<code>th</code>	Integer. Thinning parameter: saves only 1 iteration every <code>th</code> . Thinning is used to reduce the auto-correlation between Markov chains.
<code>model</code>	Prediction model: The options are: BRR, BayesA, GBLUP and RKHS.
<code>...</code>	Pass arguments to the function that builds the spatial splines <code>NNsrc</code> : <code>rho</code> and <code>dist</code> . By default, <code>rho=1</code> and <code>dist=3</code> . To check how it looks like in the field, type <code>NNsrc(rho=1,dist=3)</code> .

Details

The general model is $y = Xb + Zu + f(x) + e$, where y is the response variable, Xb refers to the fixed effects, Zu regards the genetic effect, $f(x)$ represents the field variation, and e is the vector of residuals. In this model u is a link function that represents the genetic component, which depends on the model specified.

For whole-genome regression models (BRR or BayesA), $u = Ma$, where M is the matrix of genotypes. For kernel models (RKHS and GBLUP), $u = N(0, K\sigma^2a)$, where K is either a Gaussian kernel (RKHS) or a linear kernel (GBLUP). To avoid over-representation of genotypes, u is not weighted according to the number of observations of each genotype.

Unobserved genotypes not provided in `dta` but provided in `gen` are predicted in the output of the function. Genotypes without genotypic information are transferred to the fixed effect (eg. checks). Missing loci are imputed with the expectation. If `dta` is not provided, the function will work as a regular genomic prediction model, so the length of `y` must match the number of rows of `gen`.

In whole-genome regression models, the regularization of the genetic term is either based on chosen prior (`t`, Gaussian), Gaussian (from ridge regression) and `t` (from BayesA). Kernel models (GBLUP and RKHS) are regularized as Gaussian process, which is similar to a ridge regression of Eigenvectors where the regularization of Eigenpairs also relies on the Eigenvalues.

If there is a large number of trials and users acknowledge the necessity of sparse matrices, we recommend installing the Matrix package and run the following code that enables sparsity:

```
source(system.file("add", "sparseGMM.R", package="NAM"))
```

Value

The function `gmm` returns a list containing the fitted values (`hat`), observed values (`obs`), intercept (`mu`), incidence matrix of genotypes (`Z`) and the vector of breeding values (`EBV`). If fixed effects are provided, it also returns the design matrices and coefficients of fixed effects (`X,b`). If the model was kernel or regression, output will include the random effect coefficients (`g`), variance components of markers (`Vg`) and residuals (`Ve`). Kernel models regress the Eigenvectors of the kernel, weighted by the Eigenvalue. The coefficient (`cxx`) used in the BRR model to convert marker variance Vb into genetic variance Va . If spatial information is provided, the output includes the fitted spatial term (`sp`).

Author(s)

Alencar Xavier

Examples

```
## Not run:

# Checking heritability
data(tpod)
fit = gmm(y,gen,model = 'BRR')
fit$Vg*fit$cxx / (fit$Vg*fit$cxx+fit$Ve)

# For a demo with multi-environmental trial type:
# demo(fittingMET)

## End(Not run)
```

Optimizations

Internal functions

Description

Internal function under optimization, complimentary statistics, and loops written in C++ to speed up *gwas*, *gibbs* and *wgr*.

Details

Some of the functions available for users include:

01) `Import_data(file,type=c('GBS','HapMap','VCF'))`: This function can be used to import genotypic data in the NAM format, providing a list with a genotypic matrix `gen` coded as 012 and a vector `chr` with count of markers per chromosome. Currently, it helps users to import three types of files: GBS text, HapMap and VCF.

02) `markov(gen,chr)`: Imputation method based forwards Markov model for SNP data coded as 012. We recommend users to remove non-segregating markers before using this function.

- 03) LD(gen): Computes the linkage disequilibrium in terms of r^2 for SNP data coded as 012. Missing data is not allowed.
- 04) PedMat(ped): Builds a kinship from a pedigree. Input format is provided with PedMat().
- 05) PedMat2(ped, gen=NULL, IgnoreInbr=FALSE, PureLines=FALSE): Builds a kinship from a genomic data and pedigree. Useful when not all individuals are genotyped. Row names of gen must indicate the genotype id.
- 06) Gdist(gen, method = 1): Computes genetic distance among individuals. Five methods are available: 1) Nei distance; 2) Edwards distance; 3) Reynolds distance; 4) Rogers distance; 5) Provesti's distance. 6) Modified Rogers distance
- 07) covar(sp=NULL, rho=3.5, type=1, dist=2.5): Builds a spatial kernel from field plot information. Input format is provided with covar(). Parameter rho determines the decay of relationship among neighbor plots. type defines if the kernel is exponential (1), Gaussian (2) or some intermediate. dist informs the distance ratio between range neighbors and row neighbors.
- 08) eigX(gen, fam): Computes the input of the argument EIG of the function gwas2.
- 09) G2A_Kernels(gen): Computes a list of orthogonal kernels containing additive, dominant and first-order epistatic effects, in accordance to the G2A model from ZB Zeng et al. 2005. These kernels can be used for description of genetic architecture through variance components, for that we recommend packages varComp and BGLR.
- 10) NNSrc(sp=NULL, rho=1, dist=3): Using the same field data input required by the function covar, this function provides a list of nearest neighbor plots for each entry.
- 11) NNCov(NN, y): This function utilizes the output of NNSrc to generate a numeric vector, averaging the observed values of y. This function is useful to generate field covariates to control micro-environmental variance without kriging.
- 11) emXX(y, gen, . . .): Fits whole-genome regressions using the expectation-maximization algorithm as opposed to MCMC. Currently available methods include BayesA (emBA), BayesB (emBB), BayesC (emBC), BayesD (emBD), BLASSO (emBL), FLM (emDE), Elastic-Net (emEN), maximum likelihood (emML) and ridge regression (emRR). A cross-validation option is also available (emCV).
- 12) CNT(X): Centralizes parameters from matrix X.
- 13) IMP(X): Imputes missing points from matrix X with the average value of the column.
- 14) GAU(X): Creates a Gaussian kernel from matrix X.
- 15) GRM(X, Code012=FALSE): Creates genomic relationship matrix as linear kernel from matrix X. If genotypes are coded as 012 and Code012=TRUE, the kinship is the same as proposed by VanRaden (2008), otherwise the outcome is an additive G2A kernel.
- 16) MSX(X): Computes the cross-product of each column of X and the sum of variances of each column of X.
- 17) NOR(y, X, cxx, xx, maxit=50, tol=10e-6): Solves a ridge regression using GSRU, where y corresponds to the response variable, X is the set of parameters, cxx and xx are the output from the MSX function, maxit and tol are the convergence criteria.
- 18) SPC(y, blk, row, col, rN=3, cN=1): Computes a spatial covariate, similar to what could be obtained using NNSrc and NNCov but in a single step. It often is faster than NNSrc/NNcov.
- 19) SPM(blk, row, col, rN=3, cN=1): Computes a spatial matrix that capture nearest neighbors, to be used as design matrix of random effects. The least-square solution gives the same as SPC.

20) `BRR2(y, X1, X2, it=1500, bi=500, df=5, R2=0.5)`: A simple C++ implementation of a Bayesian Ridge Regression that accomodates two random effects.

21) `emML2(y, X1, X2, D1=NULL, D2=NULL)`: A simple C++ implementation of emML that accomodates two random effects.

22) `press(y, K, MaxIt=10)`: Solves a PRESS-regularized GBLUP. You can provide `K` as a matrix or as the output of the function `eigen`. `MaxIt` the maximum number of iterations to for updating missing values (if any) if H^*y does not converge.

23) `emGWA(y, gen)`: A vanilla algorithm written in C++ for GWAS (very simple, but very efficient). It fits a snpBLUP via EM-REML based GSRU, then run an additional round checking the likelihood of treating each marker as fixed effect instead of random, thus avoiding double-fitting. It returns the marker p-values, snpBLUP marker effects for genomic prediction, LS marker effects from the GWAS, variance components, heritability, and GEBVs (fitted values).

24) `BCpi(y, X, it=3000, bi=500, df=5, R2=0.5)`: A vanilla implementation in C++ of BayesCpi for GWAS or GWP. It returns the marker p-values (as the minus log probability of marker excluded), marker effects for genomic prediction, probability of marker included, variance components, heritability, and GEBVs (fitted values).

25) `mrr(Y, X)/mkr(Y, K)/mrrV2(Y, X)/mrr2X(Y, X1, X2)/mkr2X(Y, K1, K2)`: A C++ implementation for multivariate regression.

Author(s)

Alencar Xavier

Examples

```
## Not run:

# Forward gen imputation
data(tpod)
fast.impute = markov(gen, chr)

# Wright's A matrix
PedMat()

# Pairwise LD
ld = LD(gen[,1:10])
heatmap(ld)

# Spatial correlation (kernel-based)
covar()

# Spatial correlation (NN-based)
NNSrc()

# Genetic distance
round(Gdist(gen[1:10,], method=1), 2)

# PCs of a NAM kinship
```

```

eG = eigX(gen,fam)
plot(eG[[2]],col=fam)

# Polygenic kinship matrices
Ks = G2A_Kernels(gen)
ls(Ks)

# Genomic regression fitted via EM
h = emBA(y,gen)
plot(h$b,pch=20)

# GBLUP and RRBLUP
g = GRM(gen)
eg = eigen(g)
gblup = emML(y=y, gen=eg$eigenvectors,D=eg$values)
rrblup = emML(y=y, gen=gen)
plot(gblup$hat,rrblup$hat,xlab = 'gblup',ylab='rrblup')

# Vanilla GWAS
gwa = emGWA(y,gen)
plot(gwa$PVAL,pch=20)

## End(Not run)

```

SNP H2

SNP heritability

Description

Calculates the ability of markers to carry a gene (Foneris et al. 2015). The index is also an indicator of Mendelian segregation.

Usage

```
snpH2(gen,K=NULL)
```

Arguments

gen	Numeric matrix containing the genotypic data. A matrix with n rows of observations and (m) columns of molecular markers.
K	Optional. Numeric matrix containing the genetic relationship matrix. A square and symmetric matrix ($n \times n$) with the same observations as the matrix gen, also in the same order. If not provided, the kinship matrix is estimated from the genotypic matrix.

Value

Numeric vector containing the heritability of each markers. Foneris et al. (2015) recommends to avoid using markers with index lower than 0.98.

Author(s)

Alencar Xavier

References

Forneris, N. S., Legarra, A., Vitezica, Z. G., Tsuruta, S., Aguilar, I., Misztal, I., & Cantet, R. J. (2015). Quality Control of Genotypes Using Heritability Estimates of Gene Content at the Marker. *Genetics* 199(3):675-681.

Examples

```
## Not run:
data(tpod)
Heritability=snpH2(gen)
plot(Heritability,chr=chr)

## End(Not run)
```

 SNP QC

SNP Quality Control

Description

Functions for quality control. 'snpQC' may be used to count/remove neighbor repeated SNPs, markers with MAF lower than a given threshold, and imputations. 'cleanREP' identifies and merge duplicate genotypes. The 'reference' function changes the reference genotype. For NAM populations, this function must be used when genotypes are coded according to the reference genome instead of the standard parent.

Usage

```
snpQC(gen,psy=1,MAF=0.05,misThr=0.8,remove=TRUE,impute=FALSE)
cleanREP(y,gen,fam=NULL,thr=0.95)
reference(gen,ref=NULL)
```

Arguments

gen	Numeric matrix containing the genotypic data. A matrix with n rows of observations and (m) columns of molecular markers. SNPs must be coded as 0, 1, 2, for founder homozygous, heterozygous and reference homozygous. NA is allowed.
psy	Tolerance parameter for markers in Perfect SYmmetry (psy). This QC remove identical markers (aka. full LD) that carry the same information. Default is 1, which removes only SNPs 100% equal to its following neighbor.
MAF	Minor Allele Frequency. Default is 0.05. Useful to inform or remove markers below the MAF threshold. Markers with standard deviation below the MAF threshold will be also removed.

<code>misThr</code>	Missing value threshold. Default is 0.8, removing markers with more than 80 percent missing values.
<code>remove</code>	Logical. Remove SNPs due to PSY or MAF.
<code>impute</code>	If TRUE, impute missing values using the expected value.
<code>y</code>	Numeric vector (n) or numeric matrix ($n \times t$) of observations describing the trait to be analyzed. NA is allowed.
<code>fam</code>	Numeric vector of length (n) indicating which subpopulations (<i>i.e.</i> family) each observation comes from. Default assumes that all observations are from the same populations.
<code>thr</code>	Threshold above which genotypes are considered identical. Default is 0.95, merging genotypes >95 percent identical.
<code>ref</code>	Numeric vector of length n with elements coded as 0, 1, 2, it represents the genotypic information of a new reference genotype. Default assumes that more frequent allele represents the reference genome.

Value

`snpQC` - Returns the genomic matrix without missing values, redundancy or low MAF markers.

`cleanREP` - List containing the inputs without replicates. Groups of replicates are replaced by a single observation with the phenotypic expected value. The algorithm keeps the genotypic information of the first individual (genotypic matrix order).

`reference` - Returns a recoded *gen* matrix

Author(s)

Alencar Xavier, Katy Rainey and William Muir

Examples

```
## Not run:
data(tpod)
gen=reference(gen)
gen=snpQC(gen=gen,psy=1,MAF=0.05,remove=TRUE,impute=FALSE)
test=cleanREP(y,gen)

## End(Not run)
```

Index

- * **BGS**
 - MLM Gibbs, [11](#)
 - MLM Trials, [17](#)
 - NAM-package, [2](#)
- * **BLUP**
 - GWAS, [5](#)
 - MLM Gibbs, [11](#)
 - MLM REML, [16](#)
 - MLM Trials, [17](#)
 - NAM-package, [2](#)
 - Optimizations, [19](#)
- * **Fst**
 - FST, [4](#)
- * **GRM**
 - MLM Trials, [17](#)
 - Optimizations, [19](#)
- * **GWAS**
 - GWAS, [5](#)
 - Manhattan, [10](#)
 - NAM-package, [2](#)
 - Optimizations, [19](#)
- * **LD**
 - Optimizations, [19](#)
- * **NAM**
 - GWAS, [5](#)
 - Manhattan, [10](#)
 - NAM-package, [2](#)
 - Optimizations, [19](#)
- * **PEDIGREE**
 - Optimizations, [19](#)
- * **REML**
 - MLM REML, [16](#)
 - NAM-package, [2](#)
- * **SPATIAL**
 - MLM Trials, [17](#)
 - Optimizations, [19](#)
- BCpi (Optimizations), [19](#)
- ben (GWP), [8](#)
- BRR2 (Optimizations), [19](#)
- calcSize (Optimizations), [19](#)
- chr (Dataset 1), [3](#)
- cleanREP (SNP QC), [23](#)
- CNT (Optimizations), [19](#)
- covar (Optimizations), [19](#)
- Dataset 1, [3](#)
- Dataset 2, [3](#)
- eigX (Optimizations), [19](#)
- emBA (Optimizations), [19](#)
- emBB (Optimizations), [19](#)
- emBC (Optimizations), [19](#)
- emBD (Optimizations), [19](#)
- emBL (Optimizations), [19](#)
- emCV (Optimizations), [19](#)
- emDE (Optimizations), [19](#)
- emEN (Optimizations), [19](#)
- emGWA (Optimizations), [19](#)
- emML (Optimizations), [19](#)
- emML2 (Optimizations), [19](#)
- emMX (Optimizations), [19](#)
- emRR (Optimizations), [19](#)
- fam (Dataset 1), [3](#)
- FST, [4](#)
- Fst (FST), [4](#)
- funI (Optimizations), [19](#)
- funX (Optimizations), [19](#)
- G2A_Kernels (Optimizations), [19](#)
- GAU (Optimizations), [19](#)
- Gdist (Optimizations), [19](#)
- Gen (Dataset 2), [3](#)
- gen (Dataset 1), [3](#)
- gibbs (MLM Gibbs), [11](#)
- gibbs2 (MLM Gibbs), [11](#)
- gmm (MLM Trials), [17](#)
- GRM (Optimizations), [19](#)
- gs (Optimizations), [19](#)

- GWAS, [5](#)
- gwas (GWAS), [5](#)
- gwas2 (GWAS), [5](#)
- gwas3 (GWAS), [5](#)
- gwasGE (GWAS), [5](#)
- GWP, [8](#)

- IMP (Optimizations), [19](#)
- Import_data (Optimizations), [19](#)
- inputRow (Optimizations), [19](#)

- KMUP (Optimizations), [19](#)
- KMUP2 (Optimizations), [19](#)

- LD (Optimizations), [19](#)

- Manhattan, [10](#)
- markov (Optimizations), [19](#)
- MCrem1 (MLM REML), [16](#)
- met (Dataset 2), [3](#)
- meta3 (GWAS), [5](#)
- mkr (Optimizations), [19](#)
- mkr2X (Optimizations), [19](#)
- m1 (MLM Gibbs), [11](#)
- MLM Gibbs, [11](#)
- MLM MV-PEGS, [14](#)
- MLM REML, [16](#)
- MLM Trials, [17](#)
- mrr (Optimizations), [19](#)
- mrr2X (Optimizations), [19](#)
- mrrFast (Optimizations), [19](#)
- mrrV2 (Optimizations), [19](#)
- MSX (Optimizations), [19](#)

- NAM (NAM-package), [2](#)
- NAM-package, [2](#)
- NNcov (Optimizations), [19](#)
- NNsrc (Optimizations), [19](#)
- NOR (Optimizations), [19](#)

- Obs (Dataset 2), [3](#)
- Optimizations, [19](#)

- PedMat (Optimizations), [19](#)
- PedMat2 (Optimizations), [19](#)
- pegs (MLM MV-PEGS), [14](#)
- PEGS_lapack (MLM MV-PEGS), [14](#)
- plot.fst (FST), [4](#)
- plot.gibbs (MLM Gibbs), [11](#)
- plot.H2 (SNP H2), [22](#)

- plot.NAM (Manhattan), [10](#)
- press (Optimizations), [19](#)

- RcppExports (Optimizations), [19](#)
- reference (SNP QC), [23](#)
- reml (MLM REML), [16](#)

- SAMP (Optimizations), [19](#)
- SAMP2 (Optimizations), [19](#)
- simu (MLM MV-PEGS), [14](#)
- SNP H2, [22](#)
- SNP QC, [23](#)
- snpH2 (SNP H2), [22](#)
- snpQC (SNP QC), [23](#)
- SPC (Optimizations), [19](#)
- SPM (Optimizations), [19](#)

- timesMatrix (Optimizations), [19](#)
- timesVec (Optimizations), [19](#)
- tpod (Dataset 1), [3](#)

- wgr (GWP), [8](#)

- X (MLM MV-PEGS), [14](#)

- Y (MLM MV-PEGS), [14](#)
- y (Dataset 1), [3](#)