Package: MPSEM (via r-universe)

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Type Package **Encoding** UTF-8 Title Modelling Phylogenetic Signals using Eigenvector Maps Version 0.5-1 Date 2024-10-21 Description Computational tools to represent phylogenetic signals using adapted eigenvector maps. **Depends** R (>= 3.0.0), ape, magrittr Suggests knitr, caper, xfun **Imports MASS** License GPL-3 LazyLoad yes NeedsCompilation yes VignetteBuilder knitr **Repository** CRAN RoxygenNote 7.3.1 Author Guillaume Guénard [aut, cre] (<https://orcid.org/0000-0003-0761-3072>), Pierre Legendre [ctb] (<https://orcid.org/0000-0002-3838-3305>) Maintainer Guillaume Guénard <guillaume.guenard@umontreal.ca>

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Contents

PSEM-package	2
tGraph	
aph-class	7
aph-functions	8
-utils	11
M-class	13
M-functions	15
it-simulator	21

Index

MPSEM-package

Modelling Phylogenetic Signals using Eigenvector Maps

Description

Computational tools to represent phylogenetic signals using adapted eigenvector maps.

Details

Phylogenetic eignevector maps (PEM) is a method for using phylogeny to model features of organism, most notably quantitative traits. It consists in calculating sets of explanatory variables (eigenvectors) that are meant to represent different patterns in trait values that are likely to have been inducted by evolution. These patterns are used to model the data, using a linear model for instance.

If one in interested in a 'target' species (i.e. a species for which the trait value is unknown), and provided that we know the phylogenetic relationships between that species and those of the model, the method allows us to obtain the scores of that new species on the phylogenetic eigenfunctions underlying a PEM. These scores are used to make empirical predictions of trait values for the target species on the basis of those observed for the species used in the model.

Functions PEM.build, PEM.updater, PEM.fitSimple, and PEM.forcedSimple allow one to build, update (i.e. recalculate with alternative weighting parameters) as well as to estimate or force arbitrary values for the weighting function parameters.

Functions getGraphLocations and Locations2PEMscores allow one to make predictions using method predict.PEM and a linear model. To obtain this linear model, one can use either function lm or auxiliary functions lmforwardsequentialsidak or lmforwardsequentialAICc, which perform forward-stepwise variable addition on the basis of either familiwise type I error rate or the Akaike Information Criterion (AIC), respectively.

The package provides low-level utility functions for performing operations on graphs (see graph-functions), calculate influence matrix (InflMat), and simulate trait values (see trait-simulator).

A phylogenetic modelling tutorial using MPSEM is available as a package vignette. See example below.

The DESCRIPTION file:

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Type:	Package
Encoding:	UTF-8
Title:	Modelling Phylogenetic Signals using Eigenvector Maps
Version:	0.5-1
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Description:	Computational tools to represent phylogenetic signals using adapted eigenvector maps.
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MPSEM-package

License:	GPL-3
LazyLoad:	yes
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VignetteBuilder:	knitr
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Index of help topics:

MPSEM-package	Modelling Phylogenetic Signals using Eigenvector Maps
PEM-class	Class and Methods for Phylogenetic Eigenvector Maps (PEM)
PEM-functions	Phylogenetic Eigenvector Maps
dstGraph	Distance-Based Directed Graph
graph-class	Class and Method for Directed Graphs
graph-functions	MPSEM graph Manipulation Functions
lm-utils	Linear Modelling Utility Functions
trait-simulator	Simulate the Evolution of a Quantitative Trait

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References

Guénard, G., Legendre, P., and Peres-Neto, P. 2013. Phylogenetic eigenvector maps: a framework to model and predict species traits. Methods in Ecology and Evolution 4: 1120-1131

See Also

Makarenkov, V., Legendre, P. & Desdevise, Y. 2004. Modelling phylogenetic relationships using reticulated networks. Zoologica Scripta 33: 89-96

Blanchet, F. G., Legendre, P. & Borcard, D. 2008. Modelling directional spatial processes in ecological data. Ecological Modelling 215: 325-336

Examples

```
## To view MPSEM tutorial
vignette("MPSEM", package="MPSEM")
```

dstGraph

Description

Calculates a distance-based directed graph from a dissimilarity matrix, a threshold value, and an origin (or root) vertex.

Usage

dstGraph(d, th, origin, stretch)

Arguments

d	A dissimilarity matrix such as the one obtained from dist or dist.dna.
th	Numeric. A threshold value for dissimilarity. Vertices are considered as con- nected whenever their pairwise dissimilarity value is smaller or equal to that value.
origin	Integer. Index of the origin vertex from which the edges are directed.
stretch	Numeric (optional). When a vertex is unreachable, stretch the threshold value for the shortest edge connecting it to the rest of the graph up to that value.

Details

The algorithm

Beginning on a user-defined origin vertex, the algorithm proceeds by connecting all vertices within a given dissimilarity value from the ones that have already been connected, until all the vertices that can be reached has been reached. Optionally, the dissimilarity threshold value can be stretched for the vertices that are unreachable. Vertices that cannot be reached in any way are reported by the function.

Value

A graph-class object.

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Guénard, G., Legendre, P., and Peres-Neto, P. 2013. Phylogenetic eigenvector maps: a framework to model and predict species traits. Methods in Ecology and Evolution 4: 1120-1131

Makarenkov, V., Legendre, L. & Desdevise, Y. 2004. Modelling phylogenetic relationships using reticulated networks. Zoologica Scripta 33: 89-96

dstGraph

Examples

```
## A simple example
## Create a 10-vertex graph with 16 edges:
## The vertices have x and y coordinates to help in plotting the graph.
pop.graph(
 n = 10,
 vertex = list(
   species = rep(TRUE, 10),
   x = c(0,1,1,2,2,2,3,3,4,4),
   y = c(0, 1, -1, 2, 0, -2, 1, -0.5, 0, -2)
 ),
 label = sprintf("V%d",1:10)
) %>%
 add.edge(
   from = c(1,1,2,2,3,3,4,5,5,1,7,7,8,6,9,8),
   to = c(2,3,4,5,5,6,7,7,8,7,6,9,9,9,10,10),
   edge = list(distance=c(1,1,1,1,1,1,1,1,1,4,2,1,1,3,1,1)),
   label = sprintf("E_%d",1:16)
 ) -> x
## Plotting the graph:
plot(x=x$vertex$x, y=x$vertex$y, type="n")
for(i in 1:attr(x,"ev")[1])
 arrows(x0=x$vertex$x[x$edge[[1]][i]], x1=x$vertex$x[x$edge[[2]][i]],
         y0=x$vertex$y[x$edge[[1]][i]], y1=x$vertex$y[x$edge[[2]][i]],
         length=0.2)
points(x=x$vertex$x, y=x$vertex$y, pch=21, bg="white", cex=3)
## This is the influence matrix of that directed graph:
tmp <- InflMat(x)</pre>
## A simple image plot of this influence matrix:
image(t(tmp[nrow(tmp):1,]), col=gray(c(1,0)), asp=1)
## Generate a PEM for that graph:
pem_x <- PEM.build(x)
## Plotting the different eigenvectors one-by-one on the graph plot:
for(i in 1:ncol(pem_x$u)) {
 v <- pem_x$u[,i]</pre>
 plot(x=x$vertex$x, y=x$vertex$y, type="n", main=colnames(pem_x$u)[i])
 for(i in 1:attr(x,"ev")[1])
    arrows(x0=x$vertex$x[x$edge[[1]][i]], x1=x$vertex$x[x$edge[[2]][i]],
           y0=x$vertex$y[x$edge[[1]][i]], y1=x$vertex$y[x$edge[[2]][i]],
           length=0.2)
 points(x=x$vertex$x, y=x$vertex$y, pch=21,
         bg=gray(c(0.9,0.1))[1 + (sign(v) + 1)/2], cex=7*abs(v))
 if(is.null(locator(1))) break
}
## A more elaborate example
```

dstGraph

```
## Here, we set the seed to obtain a consistent example, but feel free to
## experiment with other graphs.
set.seed(7653401)
## Here, the dissimilarity matrix is generated from the Euclidean distance of
## a two-dimensional plot for the sake of simplicity. In practice, the matrix
## will come from DNA data using a dissimilarity method such as those
## implemented by ape packages's function dist.dna().
N <- 100
coords <- cbind(x=runif(N,-1,1), y=runif(N,-1,1))</pre>
rownames(coords) <- sprintf("N%d",1:N)</pre>
dst <- dist(coords)</pre>
## Calculate the distance-based graph:
gr <- dstGraph(d=dst, th=0.25, origin=15)</pre>
## This graph have unconnected vertices.
## Plotting the graph with colors indicating the order of the edges:
plot(coords, type="n", asp=1)
col <- head(rainbow(max(gr$vertex$order) + 1), max(gr$vertex$order))</pre>
for(i in 1L:attr(gr,"ev")[1])
 arrows(x0=coords[gr$edge[[1]][i],1], x1=coords[gr$edge[[2]][i],1],
         y0=coords[gr$edge[[1]][i],2], y1=coords[gr$edge[[2]][i],2],
         length=0.05, col=col[gr$vertex$order[gr$edge[[2]][i]]])
points(coords, pch=21, bg="black", cex=0.25)
## Try again raising the threshold to help in connecting all the vertices:
gr <- dstGraph(d=dst, th=0.28, origin=15)</pre>
## It helped, but does not entirely solve the matter.
plot(coords, type="n", asp=1)
col <- head(rainbow(max(gr$vertex$order) + 1), max(gr$vertex$order))</pre>
for(i in 1L:attr(gr,"ev")[1])
 arrows(x0=coords[gr$edge[[1]][i],1], x1=coords[gr$edge[[2]][i],1],
         y0=coords[gr$edge[[1]][i],2], y1=coords[gr$edge[[2]][i],2],
         length=0.05, col=col[gr$vertex$order[gr$edge[[2]][i]]])
points(coords, pch=21, bg="black", cex=0.25)
## Try again while stretching the threshold for the unconnected vertices:
gr <- dstGraph(d=dst, th=0.28, origin=15, stretch=0.5)</pre>
## All the vertices are now connected.
plot(coords, type="n", asp=1)
col <- head(rainbow(max(gr$vertex$order) + 1), max(gr$vertex$order))</pre>
for(i in 1L:attr(gr,"ev")[1])
 arrows(x0=coords[gr$edge[[1]][i],1], x1=coords[gr$edge[[2]][i],1],
         y0=coords[gr$edge[[1]][i],2], y1=coords[gr$edge[[2]][i],2],
         length=0.05, col=col[gr$vertex$order[gr$edge[[2]][i]]])
```

graph-class

```
points(coords, pch=21, bg="black", cex=0.25)
## This is the influence matrix of that directed graph:
tmp <- InflMat(gr)</pre>
## An image plot of this influence matrix:
image(t(tmp[nrow(tmp):1L,]), col=gray(c(1,0)), asp=1)
## Generate a PEM for that graph:
pem_gr <- PEM.build(gr)</pre>
## Plotting the different eigenvectors one-by-one on the graph plot:
for(i in 1:ncol(pem_gr$u)) {
 v <- pem_gr$u[,i]</pre>
 plot(coords, type="n", asp=1, main=colnames(pem_gr$u)[i])
 col <- head(rainbow(max(gr$vertex$order) + 1), max(gr$vertex$order))</pre>
 for(j in 1L:attr(gr,"ev")[1])
    arrows(x0=coords[gr$edge[[1]][j],1], x1=coords[gr$edge[[2]][j],1],
           y0=coords[gr$edge[[1]][j],2], y1=coords[gr$edge[[2]][j],2],
           length=0.05, col=col[gr$vertex$order[gr$edge[[2]][j]]])
 points(coords, pch=21, bg=gray(c(0.9,0.1))[1 + (sign(v) + 1)/2],
         cex=10*abs(v))
 if(is.null(locator(1L))) break
}
```

graph-class Class and Method for Directed Graphs

Description

Class and methods to handle MPSEM graphs.

Usage

```
## S3 method for class 'graph'
print(x, ...)
```

Arguments

х	An object of graph-class.
	Additional parameters to be passed to the method. Currently ignored.

Format

A graph-class object contains:

edge A list whose first two unnamed members are the indices of the origin and destination vertices. Additional members must be named and are additional edge properties (e.g. length).

vertex A list that optionally contains vertex properties, if any (or an empty list if none).

Details

Prints user-relevant information about the graph: number of edges and vertices, edge and vertex labels, addition edge properties and vertex properties.

Functions

- print(graph): Print Graph
 - A print method for graph-class objects.

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References

Guénard, G., Legendre, P., and Peres-Neto, P. 2013. Phylogenetic eigenvector maps: a framework to model and predict species traits. Methods in Ecology and Evolution 4: 1120-1131

See Also

graph-functions.

graph-functions MPSEM graph Manipulation Functions

Description

A set of primitive functions for creating and munipulating MPSEM graphs.

Usage

```
pop.graph(n, vertex = list(), label = NULL)
add.vertex(x, n, vertex = list(), label = NULL)
add.edge(x, from, to, edge = list(), label = NULL)
rm.edge(x, id)
rm.vertex(x, id)
collapse.vertex(x, id)
Phylo2DirectedGraph(tp)
```

graph-functions

Arguments

n	The number of vertices to populate a new graph (pop.graph) or to add to an existing graph (add.vertex).
vertex	A list of vertex properties.
label	Labels to be given to edges or vertices.
х	A graph-class object.
from	The origins of the edges to be added (vertex labels or indices).
to	The destinations of the edges to be added (vertex labels or indices).
edge	A list of edge properties.
id	Indentity (label or index) of vertex or edge to be removed.
tp	Phylogenetic tree object of class 'phylo', as defined in ape-package.

Details

A new graph can be populated with n vertices using function pop.graph. Additional vertices can be added later with function add.vertex. The graphs so created contain no edges; the latter are added using function add.edge. Vertices and edges are removed using functions rm.vertex and rm.edge, respectively.

Function collapse.vertex allows one to remove a vertex while reestablishing the connections between the vertices located above and below that vertex using a new set of edges.

Function Phylo2DirectedGraph uses the MPSEM graph functions to convert a rooted phylogenetic tree of class 'phylo' (see ape-package) to a graph-class object. It recycles tip labels. It also creates default node labels if they were absent from the 'phylo' object, and uses them as vertex labels. The resulting acyclic graph can then be edited to represent cases that do not have a tree topology.

Value

The function returns a graph-class object. Objects returned by Phylo2DirectedGraph have a numeric edge property called 'distance' featuring branch lengths, and a link{logical} vertex property called 'species' specifying whether a vertex is a tree tip or an internal node.

Functions

- pop.graph(): Create Graph Create a graph and populates it with vertices.
- add.vertex(): Add Vertices Add vertices to an existing graph.
- add.edge(): Add Edges Add edges to a graph.
- rm.edge(): Remove Edges Remove edges from a graph.
- rm.vertex(): Remove Vertices Remove vertices from a graph.

- collapse.vertex(): Collapse Vertices Remove vertices from a graph: remove vertices together with their associated edges.
- Phylo2DirectedGraph(): Phylogenetic Tree Conversion
 Create a new graph-class object from a phylo-class object (phylogenetic tree).

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References

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Makarenkov, V., Legendre, L. & Desdevise, Y. 2004. Modelling phylogenetic relationships using reticulated networks. Zoologica Scripta 33: 89-96

Blanchet, F. G., Legendre, P. & Borcard, D. 2008. Modelling directional spatial processes in ecological data. Ecological Modelling 215: 325-336

See Also

graph-class.

Examples

```
## Populate a graph with 7 vertices labeled A-G having properties x and y:
gr <- pop.graph(n=7,</pre>
                 vertex=list(x=rnorm(7,0,1),y=rnorm(7,0,1)),
                 label=c("A","B","C","D","E","F","G"))
gr
## Adding 3 vertices H, I, and J with property x (y is absent) and a new
## property z (type character), which is unknown for A-G:
gr <- add.vertex(x=gr,</pre>
                  n=3,
                  label=c("H","I","J"),
                  vertex=list(x=rnorm(3,0,1),z=c("A","B","C")))
gr
gr$vertex
## Adding 10 edges, labeled E1-E10 and with properties a and b, to the graph:
gr <- add.edge(x=gr,</pre>
                from=c("A", "B", "B", "C", "C", "D", "D", "E", "E", "F"),
                to=c("A", "C", "D", "E", "F", "F", "G", "H", "I", "J"),
                edge=list(a=rnorm(10,0,1),b=rnorm(10,0,1)),
                label=paste("E",1:10,sep=""))
gr
gr$edge
```

lm-utils

```
## Removing edges 2, 4, and 7 from the graph:
print(rm.edge(gr,id=c(2,4,7)))
## Removing vertices 1, 3, 7, and 10 from the graph:
print(rm.vertex(gr,id=c(1,3,7,10)))
# Notice that the edges that had one of the removed vertex as their
# origin or destination are also removed:
print.default(rm.vertex(gr,id=c(1,3,7,10)))
## Vertex collapsing.
x <- pop.graph(n=9,label=c("A","B","C","D","E","F","G","H","I"))</pre>
x <- add.edge(x,from=c("A","A","B","B","C","C","D","D","E","E"),</pre>
              to=c("B","C","D","E","E","I","F","G","G","H"),
              label=paste("E",1:10,sep=""),
              edge=list(length=c(1,2,3,2,1,3,2,2,1,3)))
print.default(x)
for(i in c("A", "B", "C", "D", "E", "F", "G", "H", "I"))
  print(collapse.vertex(x,id=i))
if(require(ape)) {
  tree1 <- read.tree(</pre>
    text=paste(
      "(((A:0.15,B:0.2)N4:0.15,C:0.35)N2:0.25,((D:0.25,E:0.1)N5:0.3,",
      "(F:0.15,G:0.2)N6:0.3)N3:0.1)N1;",sep=""))
  x <- Phylo2DirectedGraph(tree1)</pre>
  print(x)
}
```

lm-utils

Linear Modelling Utility Functions

Description

Utility functions to build linear models using Phylogenetic Eigenvector Maps among their explanatory variables.

Usage

```
lmforwardsequentialAICc(y, x, object)
```

```
lmforwardsequentialsidak(y, x, object, alpha = 0.05)
```

Arguments

У	A response variable.
x	Descriptors (numeric of factor) to be used as auxiliary traits.
object	A PEM-class object.
alpha	The p-value threshold above which the function will stop adding variables.

Details

Function lmforwardsequentialsidak, performs a forward stepwise selection of the PEM eigenvectors until the familywise test of significance of the new variable to be included exceeds the p-value threshold alpha. The familiwise type I error probability is obtained using the Holm-Sidak correction of the testwise probabilities, thereby correcting for type I error rate inflation due to multiple testing.

Function lmforwardsequentialAICc carries out forward stepwise selection of the eigenvectors as long as the candidate model features a sample-size-corrected Akaike information criterion lower than the previous model. The final model should be regarded as overfitted from the Neyman-Pearson (*i.e.* frequentist) point of view, but this is the model that minimizes information loss from the standpoint of information theory.

Value

An lm-class object.

Functions

• lmforwardsequentialAICc(): Forward Stepwise Regression AICc

Forward stepwise variable addition using the sample-size-corrected Akaike Information Criterion.

• lmforwardsequentialsidak(): Forward Stepwise Regression Sidak

Forward stepwise variable addition using a Sidak multiple testing corrected alpha error threshold as the stopping criterion.

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References

Burnham, K. P. & Anderson, D. R. 2002. Model selection and multimodel inference: a practical information-theoretic approach, 2nd ed. Springer-Verlag. xxvi + 488 pp.

Holm, S. 1979. A simple sequentially rejective multiple test procedure. Scand. J. Statist. 6: 65-70

Sidak, Z. 1967. Rectangular confidence regions for means of multivariate normal distributions. J. Am. Stat. Ass. 62, 626-633

PEM-class

Description

Class and methods to handle Phylogenetic Eigenvector Maps (PEM).

Usage

```
## S3 method for class 'PEM'
print(x, ...)
## S3 method for class 'PEM'
as.data.frame(x, row.names = NULL, optional = FALSE, ...)
## S3 method for class 'PEM'
predict(
    object,
    targets,
    lmobject,
    newdata,
    interval = c("none", "confidence", "prediction"),
    level = 0.95,
    ...
)
```

Arguments

х	A PEM-class object containing a Phylogenetic Eigenvector Map.
	Additional parameters to be passed to the method. Currently ignored.
row.names	Included for method consistency reason; ignored.
optional	Included for method consistency reason; ignored.
object	A PEM-class object.
targets	Output of getGraphLocations.
lmobject	An object of class 'lm' (see 1m for details).
newdata	Auxiliary trait values.
interval	The kind of limits (confidence or prediction) to return with the predictions; interval="none": do not return a confidence interval.
level	Probability associated with the confidence of prediction interval.

Format

A PEM-class object contains:

- x The graph-class object that was used to build the PEM (see PEM.build).
- **sp** A logical vector specifying which of the vertices are tips.
- **B** The influence matrix for those vertices that are tips.
- ne The number of edges.
- **nsp** The number of species (tips).
- Bc The column-centred influence matrix.

means The column means of B.

dist Edge lengths.

- **a** The steepness parameter (see PEM. build for details).
- psi The relative evolution rate along the edges (see PEM. build for details).
- w Edge weights.
- **BcW** The weighted and column-centred influence matrix.
- d The singular values of BcW.
- u The eigenvectors (left singular vectors) of BcW.
- vt The right singular vectors of BcW.

In addition to these standard component, function, PEM.fitSimple and PEM.forcedSimple add the following members, which are necessary to make predictions:

S2 The variances of response data (one value for each response variable).

y A copy of the response data.

opt The list returned by optim.

The estimated weighting parameters are also given as an edge property.

Details

The print.PEM method provides the number of eigenvectors, the number of observations these vectors are spanning, and their associated eigenvalues.

The as.data.frame.PEM method extracts the eigenvectors from the object and allows one to use PEM-class objects as data parameter in function such as lm and glm.

The predict.PEM method is a barebone interface to make predictions. It must be given species locations with respect to the phylogenetic graph (target), which are provided by function getGraphLocations and a linear model in the form of an object from lm. The user must provide auxiliary trait values if lmobject involves such traits.

Functions

• print(PEM): Print PEM-class

A print method for PEM-class objects.

- as.data.frame(PEM): Method as.data.frame for PEM-class Objects A method to extract the phylogenetic eigenvectors from a PEM-class object.
- predict (PEM): Predict Method for PEM-class Objects A predict method to predict species trait values using Phylogenetic Eigenvector Maps.

PEM-functions

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References

Guénard, G., Legendre, P., and Peres-Neto, P. 2013. Phylogenetic eigenvector maps: a framework to model and predict species traits. Methods in Ecology and Evolution 4: 1120-1131

See Also

PEM-functions

PEM-functions

Phylogenetic Eigenvector Maps

Description

Functions to calculate and manipulate Phylogenetic Eigenvector Maps (PEM), which are sets of eigenfunctions describing the structure of a phylogenetic graph. Each computation function is briefly described in section Functions below.

Usage

```
InflMat(x)
PEMweights(d, a = 0, psi = 1)
PEM.build(
  х,
  d = "distance",
  sp = "species",
  a = 0,
 psi = 1,
  tol = .Machine$double.eps^0.5
)
PEM.updater(object, a, psi = 1, tol = .Machine$double.eps^0.5)
PEM.fitSimple(
 у,
  х,
  w.
  d = "distance",
  sp = "species",
  lower = 0,
```

```
upper = 1,
tol = .Machine$double.eps^0.5
)
PEM.forcedSimple(
    y,
    x,
    w,
    d = "distance",
    sp = "species",
    a = 0,
    psi = 1,
    tol = .Machine$double.eps^0.5
)
getGraphLocations(tpall, targets)
getAncGraphLocations(x, tpall)
```

```
Locations2PEMscores(object, gsc)
```

Arguments

x	A graph-class object containing a phylogenetic graph.
d	The name of the member of x\$edge where the phylogenetic distances (edge lengths) can be found.
а	The steepness parameter describing whether changes occur, on average: pro- gressively long edges (a close to 0) or abruptly at vertices (a close to 1).
psi	Relative evolution rate along the edges (default: 1). This parameter is only relevant when multiple values are assigned to different portions of the phylogeny.
sp	Name of the member of x\$vertex where a logical vertex property can be found, specifying which vertices are species (see graph-class).
tol	Eigenvalue threshold indicating that eigenvectors as usable.
object	A PEM-class object containing a Phylogenetic Eigenvector Map.
У	One or many response variable(s) in the form of a single numeric vector or a matrix, respectively.
W	A graph-class object containing a phylogenetic graph.
lower	Lower limit for the L-BFGS-B optimization algorithm implemented in optim.
upper	Upper limit for the L-BFGS-B optimization algorithm implemented in optim.
tpall	First parameter of function getGraphLocations: Phylogenetic tree object with class 'phylo' (package ape) containing all species (model and target) used in the study.
targets	Name of the target species to extract using the tree tpall.
gsc	The output of getGraphLocations.

PEM-functions

Details

Functions InflMat and PEMweights are used internally by PEM.build to create a binary matrix referred to as an 'influence matrix' and weight its columns. That matrix has a row for each vertex (or node) of graph 'x' and a column for each of its edges. The elements of the influence matrix are 1 whenever the vertex associated with a row is located in the tree, either directly or indirectly downward the edge associated with a column. That function is implemented in C language using recursive function calls. Although InflMat allows one to use multiple roots. User must therefore make sure that the graph provided to PEMap is single-rooted.

Function PEM.build is used to produce a phylogenetic eigenvector map, while function PEM.updater allows one to re-calculate a PEM-class object with new weighting function parameters. Function PEM.fitSimple performs a maximum likelihood estimation of parameters a and psi assuming single values for the whole tree, whereas function PEM.forcedSimple allows one to impose values to arguments a and psi of a PEM-class object, while making the function produce the same details as PEM.fitSimple would have produced; these details are necessary to make predictions.

Functions getGraphLocations returns the coordinates of a species in terms of its position with respect to the influence matrix while function Locations2PEMscores transforms these coordinates into sets of scores that can be used to make predictions. Function getAncGraphLocations produces the same output as getGraphLocations, but for the ancestral species (i.e. the nodes of the phylogeny) in order to estimate ancestral trait values.

Value

Function InflMat returns the influence matrix of graph x and function PEMweights returns weights corresponding to the distances. Functions PEM.build, PEM.fitSimple and PEM.forcedSimple return a PEM-class object. Function getGraphLocations returns a list whose first member is an influence coordinate matrix whose rows refer to the target species and columns refer to the edges. The second member contains the lengths of the terminal edges connecting each target species to the rest of the phylogeny.

Function Locations2PEMscores returns a list whose first member is a PEM score matrix whose rows refer to the target species and columns refer to the eigenvectors. The second member contains the variance associated with the terminal edges connecting the target species to the phylogeny.

Functions

• InflMat(): Influence Matrix

Calculates the influence matrix of a phylogenetic graph. The influence matrix is a binary matrix whose rows and columns correspond to the vertices and edges of the phylogenetic graph, respectively, and whose elements describe whether a given edge had been taken by any ancestors of a vertex (representing extinct of extant species) during evolution (value = 1) or not (value = 0).

• PEMweights(): PEM Weighting

A power function to obtain the edge weights used during PEM calculation.

- PEM.build(): PEM Building Calculates a PEM with parameters given by arguments a and psi.
- PEM.updater(): PEM Update Update a PEM with new parameters given by arguments a and psi.

- PEM.fitSimple(): Fitting a PEM to Data while Estimating Global Steepness Fits a PEM to a data set estimating the selection (steepness) parameter using gradient descent. The selection and evolution rate (psi = 1) are assumed to be homogeneous for the whole phylogenetic network.
- PEM. forcedSimple(): Fitting a PEM to Data while Forcing Global Steepness

Fits a PEM to a data set forcing a user-provided selection (steepness) parameter. The selection and evolution rate (psi = 1) are assumed to be homogeneous for the whole phylogenetic network.

• getGraphLocations(): Get Phylogenetic Graph Locations

Takes a phylogenetic tree and a list of species to be removed, and produce a phylogenic graph without these species together with the locations of the removed species on that graph (i.e., the location where the removed species would be found should they be inserted again in the phylogenetic graph).

• getAncGraphLocations(): Get Ancestral Species Location

Get the location on the phylogenetic graph of the immediate ancestors for a list of species. The species of the list remain in the resulting phylogenetic graph. This function is useful for estimating the ancestral state of a trait.

• Locations2PEMscores(): PEM Score Calculation

Calculates the scores of an extant or ancestral species on a phylogenetic eigenvector map (i.e., its value on the eigenvectors of the map) from its location on the phylogenetic graph used to build that map.

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See Also

PEM-class

Examples

Synthetic example

This example describes the phyogeny of 7 species (A to G) in a tree with 6
nodes, presented in Newick format, read by function

```
## read.tree of package ape.
t1 <- read.tree(text=paste(</pre>
            "(((A:0.15,B:0.2)N4:0.15,C:0.35)N2:0.25,((D:0.25,E:0.1)N5:0.3,",
            "(F:0.15,G:0.2)N6:0.3)N3:0.1)N1;",sep=""))
t1
                   # Summary of the structure of the tree
summary(t1)
x <- Phylo2DirectedGraph(t1)</pre>
## Calculate the (binary) influence matrix; E1 to E12 are the tree edges
## Edge E12 comes from the tree origin
InflMat(x)
InflMat(x)[x$vertex$species,]
## Building phylogenetic eigenvector maps
PEM1 <- PEM.build(x)</pre>
PEM2 \leftarrow PEM.build(x, a = 0.2)
PEM3 <- PEM.build(x, a = 1)
PEM4 <- PEM.updater(PEM3,a=0.5)</pre>
## Print summary statistics about PEM1
print(PEM1)
## Extract the eigenvectors (species A--G, 6 eigenvectors)
as.data.frame(PEM4)
## Example of a made up set of trait values for the 7 species
y <- c(A=-1.1436265,B=-0.3186166,C=1.9364105,D=1.7164079,E=1.0013993,
       F=-1.8586351,G=-2.0236371)
## Estimate a single steepness parameter for the whole tree
PEMfs1 <- PEM.fitSimple(y=y, x=NULL, w=x, d="distance", sp="species",</pre>
                         lower=0, upper=1)
PEMfs1$optim
                    # Optimisation results
## Force neutral evolution over the whole tree
PEMfrc1 <- PEM.forcedSimple(y=y,x=NULL,w=x,d="distance",sp="species",a=0)</pre>
PEMfrc1$x$edge$a  # Steepness parameter forced on each individual edge
## Graph locations for target species X, Y, and Z not found in the original
## data set
tpAll <- read.tree(text=paste("((X:0.45,((A:0.15,B:0.2)N4:0.15,",
                               "(C:0.25,Z:0.2)NZ:0.1)N2:0.05)NX:0.2,",
                               "(((D:0.25,E:0.1)N5:0.05,Y:0.25)NY:0.25,",
                               "(F:0.15,G:0.2)N6:0.3)N3:0.1)N1;",sep=""))
tpAll
                   # Summary of the structure of the tree
summary(tpAll)
grloc <- getGraphLocations(tpAll, c("X", "Y", "Z"))</pre>
grloc
PEMfs2 <- PEM.fitSimple(y=y, x=NULL, w=grloc$x, d="distance", sp="species",</pre>
```

```
lower=0, upper=1)
PEMfs2
## Same as for PEMfs1$optim
PEMfs2$optim
## Get the PEM scores from the species graph locations:
PEMsc1 <- Locations2PEMscores(PEMfs2, grloc)</pre>
lm1 <- lm(y ~ V_2 + V_3 + V_5, data=PEMfs2)</pre>
## Making prdictions for the species in locations `grloc`
## using linear model `lm1`:
ypred <- predict(object=PEMfs2, targets=grloc, lmobject=lm1, interval="none")</pre>
## Removing species X, Y, and Z from the tree in `tpAll`:
tpModel <- drop.tip(tpAll, c("X","Y","Z"))</pre>
## Plot the results
layout(t(c(1,1,2)))
par(mar=c(6,2,2,0.5)+0.1)
plot(tpModel, show.tip.label=TRUE, show.node.label=TRUE, root.edge = TRUE,
     srt = 0, adj=0.5, label.offset=0.08, font=1, cex=1.5, xpd=TRUE)
edgelabels(paste("E", 1:nrow(tpModel$edge), sep=""),
           edge=1:nrow(tpModel$edge), bg="white", font=1, cex=1)
points(x=0.20,y=2.25,pch=21,bg="black")
lines(x=c(0.20,0.20,0.65), y=c(2.25,0.55,0.55), xpd=TRUE, lty=2)
text("X", x=0.69, y=0.55, xpd=TRUE, font=1, cex=1.5)
points(x=0.35, y=4.5,pch=21,bg="black")
lines(x=c(0.35,0.35,0.6), y=c(4.5,5.47,5.47), xpd=TRUE, lty=2)
text("Y", x=0.64, y=5.47, xpd=TRUE, font=1, cex=1.5)
points(x=0.35, y=3, pch=21, bg="black")
lines(x=c(0.35,0.35,0.55), y=c(3,3.5,3.5), xpd=TRUE, lty=2)
text("Z", x=0.59, y=3.5, xpd=TRUE, font=1, cex=1.5)
text(c("NX","NY","NZ"), x=c(0.20,0.35,0.35), y=c(2.25,4.5,3)+0.3*c(1,-1,-1),
     font=1, cex=1)
add.scale.bar(length=0.1, cex=1.25)
par(mar=c(3.75,0,2,2)+0.1)
plot(x=y, y=1:7, ylim=c(0.45,7), xlim=c(-4,4), axes=FALSE, type="n", xlab="")
axis(1, label=c("-4","-2","0","2","4"), at=c(-4,-2,0,2,4))
abline(v=0)
## Plot the observed values
points(x=y, y=1:7, xlim=c(-2,2), pch=21, bg="black")
text("B)", x=-3.5, y=7, cex=1.5, xpd=TRUE)
text("Trait value", x=0, y=-0.5, cex=1.25, xpd=TRUE)
## Plot the predicted values
points(x=ypred, y=c(0.5,5.5,3.5), pch=23, bg="white", cex=1.25)
## Estimate the ancestral trait values
ANCloc <- getAncGraphLocations(x)
PEMfsAnc <- PEM.fitSimple(y=y, x=NULL, w=ANCloc$x, d="distance",</pre>
                          sp="species", lower=0, upper=1)
```

trait-simulator

trait-simulator Simulate the Evolution of a Quantitative Trait

Description

Functions to simulate the evolution of a quantitative trait along a phylogenetic tree inputted as an object of class 'phylo' (package ape) or a graph-class object.

Usage

```
EvolveOptimMarkovTree(tp, tw, anc, p = 1, root = tp$edge[1, 1])
TraitOUsimTree(tp, a, sigma, opt, p = 1, root = tp$edge[1, 1])
OUvar(d, a = 0, theta = 1, sigma = 1)
PEMvar(d, a = 0, psi = 1)
TraitVarGraphSim(x, variance, distance = "distance", p = 1, ...)
```

Arguments

tp	A rooted phylogenetic tree of class 'phylo' (see package ape).
tw	Transition matrix giving the probability that the optimum trait value changes from one state (row) to another (column) at vertices. All rows must sum to 1.
anc	Ancestral state of a trait (at the root).
р	Number of variates to generate.
root	Root node of the tree.
а	Selection rate in function (OUvar) or steepness in (PEMvar).
sigma	Neutral evolution rate, i.e. mean trait shift by drift.
opt	An index vector of optima at the nodes.
d	Phylogenetic distances (edge lengths).
theta	Adaptive evolution rate, i.e. mean trait shift by natural selection.
psi	Mean evolution rate.

х	A graph-class object.
variance	Variance function: OUvar, PEMvar, or any other suitable user-defined function.
distance	The name of the member of 'x\$edge' where edge lengths can be found.
	Additional parameters for the specified variance function.

Details

Function EvolveOptimMarkovTree allows one to simulate the changes of optimum trait values as a Markov process. The index whereby the process starts, at the tree root, is set by parameter anc; this is the ancestral character state. From the root onwards to the tips, the optimum is given the opportunity to change following a multinomial random draw with transition probabilities given by the rows of matrix tw. The integers thus obtained can be used as indices of a vector featuring the actual optimum trait values corresponding to the simulated selection regimes.

The resulting optimum trait values at the nodes are used by TraitOUsimTree as its argument opt to simulate trait values at nodes and tips.

Function TraitVarGraphSim uses a graph variance function (either OUvar or PEMvar) to reconstruct a covariance matrix, used to generate covariates drawn from a multi-normal distribution.

Value

Functions EvolveOptimMarkovTree and TraitOUsimTree return a matrix whose rows represent the vertices (nodes and tips) of the phylogenetic tree and whose columns stand for the n different trials the function was asked to perform.

For EvolveQTraitTree, the elements of the matrix are integers, representing the selection regimes prevailing at the nodes and tips, whereas for TraitOUsimTree, the elements are simulated quantitative trait values at the nodes and tips. These functions are implemented in C language and therefore run swiftly even for large (10000+ species) trees.

Function TraitVarGraphSim returns p phylogenetic signals. It is implemented using a rotation of a matrix of standard normal random (mean=0, variance=1) deviates. The rotation matrix is itself obtained by Choleski factorization of the trait covariance matrix expected for a given set of trees, variance function, and variance function parameters.

Functions

- EvolveOptimMarkovTree(): Trait Optima Simulator Simulates the evolution of trait optima along a phylogeny as a Markov process.
- TraitOUsimTree(): Trait Value Simulator Simulates the evolution of trait values along a phylogeny as a Ornstein–Uhlenbeck process.
- OUvar(): Ornstein–Uhlenbeck Variance Calculator

Calculates the expected covariance matrix for a trait evolving following an Ornstein–Uhlenbeck process. This function is meant to be used with function TraitVarGraphSim.

• PEMvar(): Phylogenetic Eigenvector Maps Variance Calculator

Calculates the covariance on the basis of the covariance model (power function) associated used in calculating Phylogenetic Eigenvector Maps. This function is meant to be used with function TraitVarGraphSim.

trait-simulator

TraitVarGraphSim(): Covariance-based Trait Evolution Simulator.
 Simulates trait evolution as covariates drawn from a multi-normal distribution whose covariance is estimated using an external function (functions OUvar, PEMvar provided with the package or any user-provided function).

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Examples

```
opt <- c(-2,0,2) # Three trait optima: -2, 0, and 2
## Transition probabilities:
transit <- matrix(c(0.7,0.2,0.2,0.2,0.7,0.1,0.1,0.1,0.7),</pre>
                  length(opt),length(opt),dimnames=list(from=opt,to=opt))
## In this example, the trait has a probability of 0.7 to stay at a given
## optimum, a probability of 0.2 for the optimum to change from -2 to 0,
## from 0 to -2, and from 2 to -2, and a probability of 0.1 for the
## optimum to change from -2 to 2, from 0 to 2, and from 2 to 0.
nsp <- 25 # A random tree for 25 species.
tree2 <- rtree(nsp,tip.label=paste("Species",1:nsp,sep=""))</pre>
tree2$node.label=paste("N",1:tree2$Nnode,sep="") # Node labels.
## Simulate 10 trials of optimum change.
reg <- EvolveOptimMarkovTree(tp=tree2,tw=transit,p=10,anc=2)</pre>
y1 <- TraitOUsimTree(tp=tree2,a=0,sigma=1,</pre>
                      opt=opt[reg[,1]],p=10)
                                                 ## Neutral
y2 <- TraitOUsimTree(tp=tree2,a=1,sigma=1,</pre>
                     opt=opt[reg[,1]],p=10)
                                                 ## Few selection.
y3 <- TraitOUsimTree(tp=tree2,a=10,sigma=1,</pre>
                     opt=opt[reg[,1]],p=10)
                                                 ## Strong selection.
## Display optimum change with colours.
displayOUprocess <- function(tp,trait,regime,mvalue) {</pre>
  layout(matrix(1:2,1,2))
  n <- length(tp$tip.label)</pre>
  ape::plot.phylo(tp,show.tip.label=TRUE,show.node.label=TRUE,root.edge=FALSE,
```

direction="rightwards",adj=0, edge.color=rainbow(length(trait))[regime[tp\$edge[,2]]])

```
plot(y=1:n,x=mvalue[1:n],type="b",xlim=c(-5,5),ylab="",xlab="Trait value",yaxt="n",
```

```
bg=rainbow(length(trait))[regime[1:n]],pch=21)
```

```
text(trait[regime[1:n]],y=1:n,x=5,col=rainbow(length(trait))[regime[1:n]])
  abline(v=0)
}
displayOUprocess(tree2,opt,reg[,1],y1[,1]) # Trait evolve neutrally,
displayOUprocess(tree2,opt,reg[,1],y2[,1]) # under weak selection,
displayOUprocess(tree2,opt,reg[,1],y3[,1]) # under strong selection.
x <- Phylo2DirectedGraph(tree2)</pre>
y4 <- TraitVarGraphSim(x, variance = OUvar, p=10, a=5)</pre>
DisplayTreeEvol <- function(tp,mvalue) {</pre>
  layout(matrix(1:2,1,2))
  n <- length(tp$tip.label)</pre>
  ape::plot.phylo(tp,show.tip.label = TRUE, show.node.label = TRUE,
                  root.edge = FALSE, direction = "rightwards", adj = 0)
  plot(y=1:n, x=mvalue[1:n], type="b", xlim=c(-5,5), ylab="",
       xlab="Trait value", yaxt="n", pch=21)
  abline(v=0)
}
## Iteratively displays the simulated traits.
## Left-click on the display area to go to the next plot.
## To terminate: right-click (WIndows, X11), esc key (Mac), or hit the
## "finish" button (RStudio).
for(i in 1:10) {
  DisplayTreeEvol(tree2,y4[i,])
  if(is.null(locator(1)))
   break ## Terminate:
}
```

Index

add.edge (graph-functions), 8
add.vertex (graph-functions), 8
ape, 16, 21
as.data.frame.PEM (PEM-class), 13

collapse.vertex(graph-functions), 8

dist,4 dist.dna,4 dstGraph,4

EvolveOptimMarkovTree, 22 EvolveOptimMarkovTree (trait-simulator), 21

factor, 11

getAncGraphLocations, 17
getAncGraphLocations (PEM-functions), 15
getGraphLocations, 2, 13, 14, 17
getGraphLocations (PEM-functions), 15
glm, 14
graph (graph-class), 7
graph-class, 7
graph-functions, 2, 8

InflMat, 2, 17
InflMat (PEM-functions), 15

```
list, 7
lm, 2, 12-14
lm-utils, 11
lmforwardsequentialAICc, 2
lmforwardsequentialAICc (lm-utils), 11
lmforwardsequentialsidak, 2, 12
lmforwardsequentialsidak (lm-utils), 11
Locations2PEMscores, 2, 17
Locations2PEMscores (PEM-functions), 15
logical, 14, 16
```

matrix, 16

MPSEM-package, 2 numeric, 9 optim, 14, 16 OUvar, 21, 22 OUvar (trait-simulator), 21 PEM (PEM-class), 13 PEM-class, 13 PEM-functions, 15 PEM.build, 2, 14, 17 PEM.build (PEM-functions), 15 PEM.fitSimple, 2, 14, 17 PEM.fitSimple (PEM-functions), 15 PEM. forcedSimple, 2, 14, 17 PEM.forcedSimple (PEM-functions), 15 PEM.updater, 2, 17 PEM.updater (PEM-functions), 15 PEMvar, 21, 22 PEMvar (trait-simulator), 21 PEMweights, 17 PEMweights (PEM-functions), 15 Phylo2DirectedGraph, 9 Phylo2DirectedGraph (graph-functions), 8 pop.graph(graph-functions), 8 predict.PEM, 2 predict.PEM(PEM-class), 13 print.graph(graph-class),7 print.PEM(PEM-class), 13 rm.edge (graph-functions), 8 rm.vertex(graph-functions), 8

simulation(trait-simulator), 21

```
trait(trait-simulator), 21
trait-simulator, 2, 21
TraitOUsimTree, 22
TraitOUsimTree(trait-simulator), 21
TraitVarGraphSim, 22
```

TraitVarGraphSim(trait-simulator), 21

utils(lm-utils), 11