Package: HSAR (via r-universe)

October 22, 2026

Title Hierarchical Spatial Autoregressive Model

Version 0.6.0

Description A Hierarchical Spatial Autoregressive Model (HSAR), based on a Bayesian Markov Chain Monte Carlo (MCMC) algorithm (Dong and Harris (2014) <doi:10.1111/gean.12049>). The creation of this package was supported by the Economic and Social Research Council (ESRC) through the Applied Quantitative Methods Network: Phase II, grant number ES/K006460/1.

License GPL (>= 2)

Encoding UTF-8

RoxygenNote 7.3.2

URL https://spatlyu.github.io/HSAR/, https://github.com/spatlyu/HSAR

BugReports https://github.com/spatlyu/HSAR/issues

Depends R (>= 3.5)

Imports spdep, spatialreg, stats

Suggests knitr, Matrix, RColorBrewer, Rcpp, RcppArmadillo, rmarkdown, sdsfun, sf, tidyverse

LinkingTo Rcpp, RcppArmadillo

VignetteBuilder knitr

LazyData true

NeedsCompilation yes

Author Guanpeng Dong [aut, cph] (<https://orcid.org/0000-0003-3420-9622>), Wenbo Lv [aut, cre] (<https://orcid.org/0009-0002-6003-3800>), Richard Harris [aut], Angelos Mimis [aut]

Maintainer Wenbo Lv <lyu.geosocial@gmail.com>

Repository https://cran.r-universe.dev

Date/Publication 2024-12-23 10:30:02 UTC

RemoteUrl https://github.com/cran/HSAR

RemoteRef HEAD

RemoteSha 194ea11e012b84b0e83c43c588c09f08b379a669

Contents

Beijingdistricts 2
depmunic 2
hsar 3
land 7
landprice 7
properties 8
sar 9

Index **12**

`Beijingdistricts` *Boundaries of districts in Beijing*

Description

Boundaries of districts in Beijing

Usage

```
Beijingdistricts
```

Format

An object of class `sf` (inherits from `data.frame`) with 111 rows and 2 columns.

`depmunic` *Municipality departments of Athens*

Description

Municipality departments of Athens

Usage

```
depmunic
```

Format

An object of class `sf` (inherits from `data.frame`) with 7 rows and 8 columns.

Details

An sf object of 7 polygons with the following 7 variables:

num_dep An unique identifier for each municipality department.

airbnb The number of airbnb properties in 2017

museums The number of museums

population The population recorded in census at 2011.

pop_rest The number of citizens that the origin is a non european country.

greensp The area of green spaces (unit: square meters).

area The area of the polygon (unit: square kilometers).

`hsar` *Hierarchical SAR model estimation*

Description

The specification of a HSAR model is as follows:

$$y_{i,j} = \rho * \mathbf{W}_i * \mathbf{y} + \mathbf{x}'_{i,j} * \beta + \mathbf{z}'_j * \gamma + \theta_j + \epsilon_{i,j}$$

$$\theta_j = \lambda * \mathbf{M}_j * \theta + \mu_j$$

$$\epsilon_{i,j} \sim N(0, \sigma_e^2), \qquad \mu_j \sim N(0, \sigma_u^2)$$

where $i = 1, 2, ..., n_j$ and $j = 1, 2, ..., J$ are indicators of lower- and higher-level spatial units. n_j is the number of lower-level units in the $j-th$ higher level unit and $\sum_{j=1}^{J} = \mathbf{N}$. $\mathbf{x}'_{i,j}$ and $\mathbf{z}'_j$ represent vectors of lower- and higher-level independent variables. β and γ are regression coefficients to estimate. θ, a $N \times J$ vector of higher-level random effects, also follows a simultaneous autoregressive process. $\mathbf{W}$ and $\mathbf{M}$ are two spatial weights matrices (or neighbourhood connection matrices) at the lower and higher levels, defining how spatial units at each level are connected. ρ and λ are two spatial autoregressive parameters measuring the strength of the dependencies/correlations at the two spatial scales. A succinct matrix formulation of the model is,

$$\mathbf{y} = \rho * \mathbf{W} * \mathbf{y} + \mathbf{X} * \beta + \mathbf{Z} * \gamma + \Delta * \theta + \epsilon$$

$$\theta = \lambda * \mathbf{M} * \theta + \mu$$

It is also useful to note that the HSAR model nests a standard (random intercept) multilevel model model when ρ and λ are both equal to zero and a standard spaital econometric model when λ and σ_u^2 are both equal to zero.

Usage

```
hsar(
  formula,
  data = NULL,
  W = NULL,
  M = NULL,
  Delta,
  burnin = 5000,
  Nsim = 10000,
  thinning = 1,
  parameters.start = NULL
)
```

Arguments

formula	A symbolic description of the model to fit. A formula for the covariate part of the model using the syntax of the lm() function fitting standard linear regression models. Neither the response variable nor the explanatory variables are allowed to contain NA values.
data	A `data.frame` containing variables used in the formula object.
W	The N by N lower-level spatial weights matrix or neighbourhood matrix where N is the total number of lower-level spatial units. The formulation of W could be based on geographical distances separating units or based on geographical contiguity. To ensure the maximum value of the spatial autoregressive parameter ρ less than 1, W should be row-normalised before running the HSAR model. As in most cases, spatial weights matrix is very sparse, therefore W here should be converted to a sparse matrix before imported into the `hsar()` function to save computational burden and reduce computing time. More specifically, W should be a column-oriented numeric sparse matrices of a `dgCMatrix` class defined in the `Matrix` package. The converion between a dense numeric matrix and a sparse numeric matrix is made quite convenient through the `Matrix`library.
M	The J by J higher-level spatial weights matrix or neighbourhood matrix where J is the total number of higher-level spatial units. Similar with W, the formulation of M could be based on geographical distances separating units or based on geographical contiguity. To ensure the maximum value of the spatial autoregressive parameter λ less than 1, M is also row-normalised before running the HSAR model. As with W, M should also be a column-oriented numeric sparse matrices.
Delta	The N by J random effect design matrix that links the J by 1 higher-level random effect vector back to the N by 1 response variable under investigation. It is simply how lower-level units are grouped into each high-level units with columns of the matrix being each higher-level units. As with W and M, δ should also be a column-oriented numeric sparse matrices.
burnin	The number of MCMC samples to discard as the burnin period.
Nsim	The total number of MCMC samples to generate.
thinning	MCMC thinning factor.

`parameters.start`
: A list with names "rho", "lambda", "sigma2e", "sigma2u" and "beta" corresponding to initial values for the model parameters $\rho, \lambda, \sigma_e^2, \sigma_u^2$ and the regression coefficients respectively.

Value

A `list`.

cbetas A matrix with the MCMC samples of the draws for the coefficients.

Mbetas A vector of estimated mean values of regression coefficients.

SDbetas The standard deviations of estimated regression coefficients.

Mrho The estimated mean of the lower-level spatial autoregressive parameter ρ.

SDrho The standard deviation of the estimated lower-level spatial autoregressive parameter.

Mlamda The estimated mean of the higher-level spatial autoregressive parameter λ.

SDlambda The standard deviation of the estimated higher-level spatial autoregressive parameter.

Msigma2e The estimated mean of the lower-level variance parameter σ_e^2.

SDsigma2e The standard deviation of the estimated lower-level variance parameter σ_e^2.

Msigma2u The estimated mean of the higher-level variance parameter σ_u^2.

SDsigma2u The standard deviation of the estimated higher-level variance parameter σ_u^2.

Mus Mean values of θ

SDus Standard deviation of θ

DIC The deviance information criterion (DIC) of the fitted model.

pd The effective number of parameters of the fitted model.

Log_Likelihood The log-likelihood of the fitted model.

R_Squared A pseudo R square model fit indicator.

impact_direct Summaries of the direct impact of a covariate effect on the outcome variable.

impact_idirect Summaries of the indirect impact of a covariate effect on the outcome variable.

impact_total Summaries of the total impact of a covariate effect on the outcome variable.

Note

In order to use the hsar() function, users need to specify the two spatial weights matrices W and M and the random effect design matrix δ. However, it is very easy to extract such spatial weights matrices from spatial data using the package **spdep**. Geographic distance-based or contiguity-based spatial weights matrix for both spatial points data and spatial polygons data are available in the **spdep** package. Before the extraction of W and M, it is better to first sort the data using the higher-level unit identifier. Then, the random effect design matrix can be extracted simply (see the following example) and so are the two spatial weights matrices. Make sure the order of higher-level units in the weights matrix M is in line with that in the δ matrix. Two simpler versions of the HSAR model can also be fitted using the hsar() function. The first is a HSAR model with λ equal to zero, indicating an assumption of independence in the higher-level random effect θ. The second is a HSAR with ρ equal to zero, indicating an independence assumption in the outcome variable conditioning on the hgiher-level random effect. This model is useful in situations where we are interested in the neighbourhood/contextual effect on individual's outcomes and have good reasons to suspect the effect from geographical contexts upon individuals to be dependent. Meanwhile we have no information on how lower-level units are connnected.

References

Dong, G. and Harris, R. 2015. Spatial Autoregressive Models for Geographically Hierarchical Data Structures. *Geographical Analysis*, 47:173-191.

LeSage, J. P., and R. K. Pace. (2009). *Introduction to Spatial Econometrics*. Boca Raton, FL: CRC Press/Taylor & Francis.

Examples

```
library(spdep)

# Running the hsar() function using the Beijing land price data
data(landprice)

# load shapefiles of Beijing districts and land parcels
data(Beijingdistricts)
data(land)

plot(Beijingdistricts,border="green")
plot(land,add=TRUE,col="red",pch=16,cex=0.8)

# Define the random effect matrix
model.data <- landprice[order(landprice$district.id),]
head(model.data,50)

# the number of individuals within each neighbourhood
MM <- as.data.frame(table(model.data$district.id))
# the total number of neighbourhood, 100
Utotal <- dim(MM)[1]
Unum <- MM[,2]
Uid <- rep(c(1:Utotal),Unum)

n <- nrow(model.data)
Delta <- matrix(0,nrow=n,ncol=Utotal)
for(i in 1:Utotal) {
  Delta[Uid==i,i] <- 1
}
rm(i)
# Delta[1:50,1:10]
Delta <- as(Delta,"dgCMatrix")

# extract the district level spatial weights matrix using the queen's rule
nb.list <- spdep::poly2nb(Beijingdistricts)
mat.list <- spdep::nb2mat(nb.list,style="W")
M <- as(mat.list,"dgCMatrix")

# extract the land parcel level spatial weights matrix
nb.25 <- spdep::dnearneigh(land,0,2500)
# to a weights matrix
dist.25 <- spdep::nbdists(nb.25,land)
dist.25 <- lapply(dist.25,function(x) exp(-0.5 * (x / 2500)^2))
mat.25 <- spdep::nb2mat(nb.25,glist=dist.25,style="W")
```

```
W <- as(mat.25,"dgCMatrix")


## run the hsar() function
res.formula <- lnprice ~ lnarea + lndcbd + dsubway + dpark + dele +
  popden + crimerate + as.factor(year)

betas= coef(lm(formula=res.formula,data=landprice))
pars=list( rho = 0.5,lambda = 0.5, sigma2e = 2.0, sigma2u = 2.0, betas = betas )


  res <- hsar(res.formula, data=landprice, W=W, M=M, Delta=Delta,
              burnin=500, Nsim=1000, thinning = 1, parameters.start=pars)
  summary(res)

  # visualise the district level random effect
  groups <- sdsfun::discretize_vector(res$Mus,n = 4,method = "natural")
  palette <- RColorBrewer::brewer.pal(4, "Blues")
  plot(Beijingdistricts,col=palette[groups],border="grey")
```

`land` *The spatial locations of the Beijing land price data*

Description

The spatial locations of the Beijing land price data

Usage

```
land
```

Format

An object of class `sf` (inherits from `data.frame`) with 1117 rows and 3 columns.

`landprice` *Leased residential land parcels, from 2003 to 2009 in Beijing, China*

Description

Leased residential land parcels, from 2003 to 2009 in Beijing, China

Usage

```
landprice
```

Format

An object of class `data.frame` with 1117 rows and 11 columns.

Details

A `data.frame` with 1117 observations on the following 11 variables.

obs An unique identifier for each land parcel.

lnprice The log of the leasing price per square metre of each residential land parcel (unit: RMB, Chinese yuan)

dsubway The log of the distance of each land parcel to the nearest railway station (unit:meters)

dele The log of the distance of each land parcel to the nearest elementary school (unit:meters)

dpark The log of the distance of each land parcel to the nearest green park (unit:meters)

lnarea The log of the size of each land parcel (unit: square meters).

lndcbd The log of the distance of each land parcel to the CBD (centre business district) in Beijing (unit:meters)

year The year when each land parcel was leased with values of 0,1,2,3,4,5,6 representing year 2003,2004,2005,2006,2007,2008,2009

popden The population density of each district (unit: 1000 persons per square kilometers)

crimerate The number of reported serious crimes committed in each district per 1000 persons.

district.id The identifier of the district where each land parcel is located.

`properties` *Dataset of properties in the municipality of Athens*

Description

A dataset of apartments in the municipality of Athens for 2017. Point location of the properties is given together with their main characteristics and the distance to the closest metro/train station.

Usage

```
properties
```

Format

An object of class `sf` (inherits from `data.frame`) with 1000 rows and 7 columns.

Details

An sf object of 1000 points with the following 6 variables.

id An unique identifier for each property.

size The size of the property (unit: square meters)

price The asking price (unit: euros)

prpsqm The asking price per squre meter (unit: euroes/square meter).

age Age of property in 2017 (unit: years).

dist_metro The distance to closest train/metro station (unit: meters).

`sar` *SAR model estimation*

Description

The `sar()` function implements a standard spatial econometrics model (SAR) or a spatially lagged dependent variable model using the Markov chain Monte Carlo (McMC) simulation approach.

Usage

```
sar(
  formula,
  data = NULL,
  W,
  burnin = 5000,
  Nsim = 10000,
  thinning = 1,
  parameters.start = NULL
)
```

Arguments

`formula`	A symbolic description of the model to fit. A formula for the covariate part of the model using the syntax of the `stats::lm()` function fitting standard linear regression models. Neither the response variable nor the explanatory variables are allowed to contain NA values.
`data`	A `data.frame` containing variables used in the formula object.
`W`	The N by N spatial weights matrix or neighbourhood matrix where N is the number of spatial units. The formulation of W could be based on geographical distances separating units or based on geographical contiguity. To ensure the maximum value of the spatial autoregressive parameter ρ less than 1, W is usually row-normalised before implementing the SAR model. As in most cases, spatial weights matrix is very sparse, therefore W here should be converted to a sparse matrix before imported into the `sar()` function to save computational

burden and reduce computing time. More specifically, W should be a column-oriented numeric sparse matrices of a `dgCMatrix` class defined in the `Matrix` package. The converion between a dense numeric matrix and a sparse numeric matrix is made quite convenient through the `Matrix` library.

`burnin` The number of McMC samples to discard as the burnin period.

`Nsim` The total number of McMC samples to generate.

`thinning` MCMC thinning factor.

`parameters.start`
A list with names "rho", "sigma2e", and "beta" corresponding to initial values for the model parameters ρ, σ_e^2 and the regression coefficients respectively.

Value

A `list`.

cbetas A matrix with the MCMC samples of the draws for the coefficients.

Mbetas A vector of estimated mean values of regression coefficients.

SDbetas The standard deviations of estimated regression coefficients.

Mrho The estimated mean of the lower-level spatial autoregressive parameter ρ.

SDrho The standard deviation of the estimated lower-level spatial autoregressive parameter.

Msigma2e The estimated mean of the lower-level variance parameter σ_e^2.

SDsigma2e The standard deviation of the estimated lower-level variance parameter σ_e^2.

DIC The deviance information criterion (DIC) of the fitted model.

pd The effective number of parameters of the fitted model.

Log_Likelihood The log-likelihood of the fitted model.

R_Squared A pseudo R square model fit indicator.

impact_direct Summaries of the direct impact of a covariate effect on the outcome variable.

impact_idirect Summaries of the indirect impact of a covariate effect on the outcome variable.

impact_total Summaries of the total impact of a covariate effect on the outcome variable.

References

Anselin, L. (1988). *Spatial Econometrics: Methods and Models*. Dordrecht: Kluwer Academic Publishers.

LeSage, J. P., and R. K. Pace. (2009). *Introduction to Spatial Econometrics*. Boca Raton, FL: CRC Press/Taylor & Francis

Examples

```
data(landprice)
head(landprice)
data(land)

# extract the land parcel level spatial weights matrix
library(spdep)
```

```
library(Matrix)
nb.25 <- spdep::dnearneigh(land,0,2500)
# to a weights matrix
dist.25 <- spdep::nbdists(nb.25,land)
dist.25 <- lapply(dist.25,function(x) exp(-0.5 * (x / 2500)^2))
mat.25 <- spdep::nb2mat(nb.25,glist=dist.25,style="W")
W <- as(mat.25,"dgCMatrix")

## run the sar() function
res.formula <- lnprice ~ lnarea + lndcbd + dsubway + dpark + dele +
                popden + crimerate + as.factor(year)
betas= coef(lm(formula=res.formula,data=landprice))
pars=list(rho = 0.5, sigma2e = 2.0, betas = betas)

res <- sar(res.formula,data=landprice,W=W,
           burnin=500, Nsim=1000, thinning=1,
           parameters.start=pars)
summary(res)
```

Index

∗ **datasets**
Beijingdistricts, 2
depmunic, 2
land, 7
landprice, 7
properties, 8

Beijingdistricts, 2

depmunic, 2

hsar, 3

land, 7
landprice, 7

properties, 8

sar, 9