Package: HQM (via r-universe)

September 17, 2024

Type Package

Title Superefficient Estimation of Future Conditional Hazards Based on Marker Information

Version 0.1.0

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Description Provides a nonparametric smoothed kernel density estimator for the future conditional hazard when time-dependent covariates are present. It also provides pointwise and uniform confidence bands and a bandwidth selection.

Encoding UTF-8

LazyData true

Depends R (>= 3.5.0)

Imports stats, utils

License GPL (>= 2)

NeedsCompilation no

RoxygenNote 6.1.0

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Repository CRAN

Date/Publication 2022-09-12 07:52:55 UTC

Contents

`b_selection` *Cross validation bandwidth selection*

Description

Implements the bandwidth selection for the future conditional hazard rate $\hat{h}_x(t)$ based on K-fold cross validation.

Usage

```
b_selection(data, marker_name, event_time_name = 'years',
            time_name = 'year', event_name = 'status2', I, b_list)
```

Arguments

`data`	A data frame of time dependent data points. Missing values are allowed.
`marker_name`	The column name of the marker values in the data frame `data`.
`event_time_name`	The column name of the event times in the data frame `data`.
`time_name`	The column name of the times the marker values were observed in the data frame `data`.
`event_name`	The column name of the events in the data frame `data`.
`I`	Number of observations leave out for a K cross validation.
`b_list`	Vector of bandwidths that need to be tested.

Details

The function `b_selection` implements the cross validation bandwidth selection for the future conditional hazard rate $\hat{h}_x(t)$ given by

$$b_{CV} = argmin_b \sum_{i=1}^{N} \int_0^T \int_s^T Z_i(t) Z_i(s) (\hat{h}_{X_i(s)}(t-s) - h_{X_i(s)}(t-s))^2 dt ds,$$

where $\hat{h}_x(t)$ is a smoothed kernel density estimator of $h_x(t)$ and Z_i the exposure process of individual i. Note that $\hat{h}_x(t)$ is dependent on b.

Value

A list with the tested bandwidths and its cross validation scores.

See Also

b_selection_prep_g, Q1, R_K, prep_cv, dataset_split

Examples

```
I = 26
b_list = seq(0.9, 1.3, 0.1)

b_scores_alb = b_selection(pbc2, 'albumin', 'years', 'year', 'status2', I, b_list)
b_scores_alb[[2]][which.min(b_scores_alb[[1]])]
```

---

b_selection_prep_g *Preparations for bandwidth selection*

Description

Calculates an intermediate part for the K-fold cross validation.

Usage

```
b_selection_prep_g(h_mat, int_X, size_X_grid, n, Yi)
```

Arguments

h_mat	A matrix of the estimator for the future conditional hazard rate for all values x and t.
int_X	Vector of the position of the observed marker values in the grid for marker values.
size_X_grid	Numeric value indicating the number of grid points for marker values.
n	Number of individuals.
Yi	A matrix made by make_Yi indicating the exposure.

Details

The function b_selection_prep_g calculates a key component for the bandwidth selection

$$\hat{g}_i^{-I_j}(t) = \int_0^t Z_i(s)\hat{h}^{-I_j}_{X_i(s)}(t-s)ds,$$

where $\hat{h}^{-I_j}$ is estimated without information from all counting processes i with $i \in I_j$ and Z is the exposure.

Value

A matrix with $\hat{g}_i^{-I_j}(t)$ for all individuals `i` and time grid points `t`.

See Also

`b_selection`

Examples

```
pbc2_id = to_id(pbc2)
size_s_grid <- size_X_grid <- 100
n = max(as.numeric(pbc2$id))
s = pbc2$year
X = pbc2$serBilir
XX = pbc2_id$serBilir
ss <- pbc2_id$years
delta <- pbc2_id$status2
br_s = seq(0, max(s), max(s)/( size_s_grid-1))
br_X = seq(min(X), max(X), (max(X)-min(X))/( size_X_grid-1))

X_lin = lin_interpolate(br_s, pbc2_id$id, pbc2$id, X, s)

int_X <- findInterval(X_lin, br_X)
int_s = rep(1:length(br_s), n)

N <- make_N(pbc2, pbc2_id, breaks_X=br_X, breaks_s=br_s, ss, XX, delta)
Y <- make_Y(pbc2, pbc2_id, X_lin, br_X, br_s, size_s_grid, size_X_grid, int_s, int_X, 'years', n)

b = 1.7
alpha<-get_alpha(N, Y, b, br_X, K=Epan )

Yi <- make_Yi(pbc2, pbc2_id, X_lin, br_X, br_s, size_s_grid, size_X_grid, int_s, int_X,'years', n)
Ni  <- make_Ni(breaks_s=br_s, size_s_grid, ss, delta, n)

t = 2

h_xt_mat = t(sapply(br_s[1:99], function(si){
                    h_xt_vec(br_X, br_s, size_s_grid, alpha, t, b, Yi, int_X, n)}))

b_selection_prep_g(h_xt_mat, int_X, size_X_grid, n, Yi)
```

`Conf_bands` *Confidence bands*

Description

Implements the uniform and pointwise confidence bands for the future conditional hazard rate based on the last observed marker measure.

Usage

```
Conf_bands(data, marker_name, event_time_name = 'years',
           time_name = 'year', event_name = 'status2', x, b)
```

Arguments

data	A data frame of time dependent data points. Missing values are allowed.
marker_name	The column name of the marker values in the data frame data.
event_time_name	The column name of the event times in the data frame data.
time_name	The column name of the times the marker values were observed in the data frame data.
event_name	The column name of the events in the data frame data.
x	Numeric value of the last observed marker value.
b	Bandwidth.

Details

The function Conf_bands implements the pointwise and uniform confidence bands for the estimator of the future conditional hazard rate $\hat{h}_x(t)$. The confidence bands are based on a wild bootstrap approach ${h^*}_{x_*,B}(t)$.

Pointwise: For a given $t \in (0,T)$ generate ${h^*}^{(1)}_{x_*,B}(t), ..., {h^*}^{(N)}_{x_*,B}(t)$ for $N = 1000$ and order it ${h^*}^{[1]}_{x_*,B}(t) \leq ... \leq {h^*}^{[N]}_{x_*,B}(t)$. Then

$$\hat{I}^1_{n,N} = \left[\hat{h}_{x_*}(t) - \hat{\sigma}_{G_{x_*}}(t)\frac{{h^*}^{[N(1-\frac{\alpha}{2})]}_{x_*,B}(t)}{\sqrt{n}}, \hat{h}_{x_*}(t) - \hat{\sigma}_{G_x}(t)\frac{{h^*}^{[N\frac{\alpha}{2}]}_{x_*,B}(t)}{\sqrt{n}}\right]$$

is a $1-\alpha$ pointwise confidence band for $h_{x_*}(t)$, where $\hat{\sigma}_{G_{x_*}}(t)$ is a bootrap estimate of the variance. For more details on the wild bootstrap approach, please see prep_boot and g_xt.

Uniform: Generate $\bar{h}^{(1)}_{x_*,B}(t), ..., \bar{h}^{(N)}_{x_*,B}(t)$ for $N = 1000$ for all $t \in [\delta_T, T - \delta_T]$ and define $W^{(i)} = \sup_{t\in[0,T]} \left|\bar{h}^{(i)}_{x_*,B}(t)\right|$ for $i = 1, ..., N$. Order $W^{[1]} \leq ... \leq W^{[N]}$. Then

$$\hat{I}^2_{n,N} = \left[\hat{h}_{x_*}(t) \pm \hat{\sigma}_{G_{x_*}}(t)\frac{W^{[N(1-\alpha)]}}{\sqrt{n}}\right]$$

is a $1-\alpha$ uniform confidence band for $h_{x_*}(t)$.

Value

A list with pointwise, uniform confidence bands and the estimator $\hat{h}_x(t)$ for all possible time points t.

See Also

g_xt, prep_boot

Examples

```
b = 10
x = 3
size_s_grid <- 100
s = pbc2$year
br_s = seq(0, max(s), max(s)/( size_s_grid-1))


c_bands = Conf_bands(pbc2, 'serBilir', event_time_name = 'years',
                     time_name = 'year', event_name = 'status2', x, b)

J = 60
plot(br_s[1:J], c_bands$h_hat[1:J], type = "l", ylim = c(0,1), ylab = 'Hazard', xlab = 'Years')

lines(br_s[1:J], c_bands$I_p_up[1:J], col = "red")
lines(br_s[1:J], c_bands$I_p_do[1:J], col = "red")
lines(br_s[1:J], c_bands$I_nu[1:J], col = "blue")
lines(br_s[1:J], c_bands$I_nd[1:J], col = "blue")
```

`dataset_split` *Split dataset for K-fold cross validation*

Description

Creates multiple splits of a dataset which is then used in the bandwidth selection with K-fold cross validation.

Usage

```
dataset_split(I, data)
```

Arguments

`data`	A data frame of time dependent data points. Missing values are allowed.
`I`	The number of individuals that should be left out. Optimally, $K = n/I$ should be an integer, where n is the number of individuals.

Details

The function `dataset_split` takes a data frame and transforms it into $K = n/I$ data frames with I individuals missing from each data frame. Let I_j be sets of indices with $\cup_{j=1}^{K} I_j = \{1, ..., n\}$, $I_k \cap I_j = \emptyset$ and $|I_j| = |I_k| = I$ for all $j, k \in \{1, ..., K\}$. Then data frames with $\{1, ..., n\}/I_j$ individuals are created.

Value

A list of data frames with `I` individuals missing in the above way.

See Also

b_selection

Examples

```
splitted_dataset = dataset_split(26, pbc2)
```

`get_alpha` *Marker-only hazard rate*

Description

Calculates the marker-only hazard rate for time dependent data.

Usage

```
get_alpha(N, Y, b, br_X, K=Epan )
```

Arguments

N	A matrix made by make_N indicating the occurences of events.
Y	A matrix made by make_Y indicating the exposure.
b	Bandwidth.
br_X	Vector of grid points for the marker values X.
K	Used kernel function.

Details

The function get_alpha implements the marker-only hazard estimator

$$\hat{\alpha}_i(z) = \frac{\sum_{k \neq i} \int_0^T K_{b_1}(z - X_k(s)) \mathrm{d}N_k(s)}{\sum_{k \neq i} \int_0^T K_{b_1}(z - X_k(s)) Z_k(s) \mathrm{d}s},$$

where X is the marker and Z is the exposure. The marker-only hazard is defined as the underlying hazard which is not dependent on time

$$\alpha(X(t), t) = \alpha(X(t))$$

.

Value

A vector of marker-only values for br_X.

See Also

h_xt

Examples

```
pbc2_id = to_id(pbc2)
size_s_grid <- size_X_grid <- 100
n = max(as.numeric(pbc2$id))
s = pbc2$year
X = pbc2$serBilir
XX = pbc2_id$serBilir
ss <- pbc2_id$years
delta <- pbc2_id$status2
br_s = seq(0, max(s), max(s)/( size_s_grid-1))
br_X = seq(min(X), max(X), (max(X)-min(X))/( size_X_grid-1))

X_lin = lin_interpolate(br_s, pbc2_id$id, pbc2$id, X, s)

int_X <- findInterval(X_lin, br_X)
int_s = rep(1:length(br_s), n)

N  <- make_N(pbc2, pbc2_id, breaks_X=br_X, breaks_s=br_s, ss, XX, delta)
Y <- make_Y(pbc2, pbc2_id, X_lin, br_X, br_s, size_s_grid,
            size_X_grid, int_s, int_X, event_time = 'years', n)

b = 1.7
alpha<-get_alpha(N, Y, b, br_X, K=Epan )
```

`get_h_x` *Future conditional hazard rate for all time values*

Description

Calculates the future conditional hazard rate for a marker value `x` and all possible time values.

Usage

```
get_h_x(data, marker_name, event_time_name = 'years',
        time_name = 'year', event_name = 'status2', x, b)
```

Arguments

`data`	A data frame of time dependent data points. Missing values are allowed.
`marker_name`	The column name of the marker values in the data frame `data`.
`event_time_name`	The column name of the event times in the data frame `data`.
`time_name`	The column name of the times the marker values were observed in the data frame `data`.
`event_name`	The column name of the events in the data frame `data`.
`x`	Numeric value of the last observed marker value.
`b`	Bandwidth.

Details

The function h_xt implements the future conditional hazard estimator

$$\hat{h}_x(t) = \frac{\sum_{i=1}^{n} \int_0^T \hat{\alpha}_i(X_i(t+s)) Z_i(t+s) Z_i(s) K_b(x - X_i(s)) \mathrm{d}s}{\sum_{i=1}^{n} \int_0^T Z_i(t+s) Z_i(s) K_b(x - X_i(s)) \mathrm{d}s},$$

where X is the marker, Z is the exposure and $\alpha(z)$ is the marker-only hazard, see get_alpha for more details.

Value

A vector of $\hat{h}_x(t)$ for a grid of possible time values t.

See Also

get_alpha, h_xt

Examples

```
b = 10
x = 3

get_h_x(pbc2, 'serBilir', event_time_name = 'years',
        time_name = 'year', event_name = 'status2', x, b)
```

---

g_xt *Computation of a key component for wild bootstrap*

Description

Implements a key part for the wild bootstrap of the hqm estimator.

Usage

```
g_xt(br_X, br_s, size_s_grid, int_X, x, t, b, Yi, Y, n)
```

Arguments

br_X	Marker value grid points that will be used in the evaluatiuon.
br_s	Time value grid points that will be used in the evaluatiuon.
size_s_grid	Size of the time grid.
int_X	Position of the linear interpolated marker values on the marker grid.
x	Numeric value of the last observed marker value.
t	Numeric value of the time the function should be evaluated.
b	Bandwidth.
Yi	A matrix made by make_Yi indicating the exposure.
Y	A matrix made by make_Y indicating the exposure.
n	Number of individuals.

Details

The function implements

$$\hat{g}_{t,x}(z) = \frac{1}{n}\sum_{j=1}^{n}\int_0^{T-t} \hat{E}(X_j(t+s))^{-1} K_b(z, X_j(t+s)) Z_j(t+s) Z_j(s) K_b(x, X_j(s)) ds,$$

for every value z on the marker grid, where $\hat{E}(x) = \frac{1}{n}\sum_{j=1}^{n}\int_0^T K_b(x, X_j(s)) Z_j(s) ds$, Z the exposure and X the marker.

Value

A vector of $\hat{g}_{t,x}(z)$ for all values z on the marker grid.

Examples

```
pbc2_id = to_id(pbc2)
size_s_grid <- size_X_grid <- 100
n = max(as.numeric(pbc2$id))
X = pbc2$serBilir
s = pbc2$year
br_s = seq(0, max(s), max(s)/( size_s_grid-1))
br_X = seq(min(X), max(X), (max(X)-min(X))/( size_X_grid-1))

X_lin = lin_interpolate(br_s, pbc2_id$id, pbc2$id, X, s)

int_X <- findInterval(X_lin, br_X)
int_s = rep(1:length(br_s), n)

Yi<-make_Yi(pbc2, pbc2_id, X_lin, br_X, br_s, size_s_grid, size_X_grid, int_s, int_X, 'years', n)
Y<-make_Y(pbc2, pbc2_id, X_lin, br_X, br_s,size_s_grid,size_X_grid, int_s,int_X, 'years', n)

t = 2
x = 2
b = 10

g_xt(br_X, br_s, size_s_grid, int_X, x, t, b, Yi, Y, n)
```

---

h_xt *Future conditional hazard rate*

Description

Calculates the future conditional hazard rate for a marker value `x` and a time value `t`.

Usage

```
h_xt(br_X, br_s, int_X, size_s_grid, alpha, x,t, b, Yi,n)
```

Arguments

br_X	Vector of grid points for the marker values X.
br_s	Vector of grid points for the time values s.
int_X	Position of the linear interpolated marker values on the marker grid.
size_s_grid	Size of the time grid.
alpha	Marker-hazard obtained from get_alpha.
x	Numeric value of the last observed marker value.
t	Numeric time value.
b	Bandwidth.
Yi	A matrix made by make_Yi indicating the exposure.
n	Number of individuals.

Details

The function h_xt implements the future conditional hazard estimator

$$\hat{h}_x(t) = \frac{\sum_{i=1}^{n} \int_0^T \hat{\alpha}_i(X_i(t+s)) Z_i(t+s) Z_i(s) K_b(x - X_i(s)) \mathrm{d}s}{\sum_{i=1}^{n} \int_0^T Z_i(t+s) Z_i(s) K_b(x - X_i(s)) \mathrm{d}s},$$

where X is the marker, Z is the exposure and $\alpha(z)$ is the marker-only hazard, see get_alpha for more details. The future conditional hazard is defined as

$$h_{x,T}(t) = P\left(T_i \in (t+T, t+T+dt) | X_i(T) = x, T_i > t+T\right),$$

where T_i is the survival time and X_i the marker of individual i observed in the time frame $[0, T]$.

Value

A single numeric value of $\hat{h}_x(t)$.

See Also

get_alpha

Examples

```
pbc2_id = to_id(pbc2)
size_s_grid <- size_X_grid <- 100
n = max(as.numeric(pbc2$id))
s = pbc2$year
X = pbc2$serBilir
XX = pbc2_id$serBilir
ss <- pbc2_id$years
delta <- pbc2_id$status2
br_s = seq(0, max(s), max(s)/( size_s_grid-1))
br_X = seq(min(X), max(X), (max(X)-min(X))/( size_X_grid-1))
```

```
X_lin = lin_interpolate(br_s, pbc2_id$id, pbc2$id, X, s)

int_X <- findInterval(X_lin, br_X)
int_s = rep(1:length(br_s), n)

N <- make_N(pbc2, pbc2_id, breaks_X=br_X, breaks_s=br_s, ss, XX, delta)
Y <- make_Y(pbc2, pbc2_id, X_lin, br_X, br_s, size_s_grid, size_X_grid, int_s, int_X, 'years', n)

b = 1.7
alpha<-get_alpha(N, Y, b, br_X, K=Epan )

Yi <- make_Yi(pbc2, pbc2_id, X_lin, br_X, br_s, size_s_grid, size_X_grid, int_s, int_X,'years', n)

x = 2
t = 2
h_hat = h_xt(br_X, br_s, int_X, size_s_grid, alpha, x, t, b, Yi, n)
```

`h_xt_vec` *Hqm estimator on the marker grid*

Description

Computes the hqm estimator on the marker grid.

Usage

```
h_xt_vec(br_X, br_s, size_s_grid, alpha, t, b, Yi, int_X, n)
```

Arguments

`br_X`	Marker value grid points that will be used in the evaluatiuon.
`br_s`	Time value grid points that will be used in the evaluatiuon.
`size_s_grid`	Size of the time grid.
`alpha`	Marker-hazard obtained from `get_alpha`.
`t`	Numeric value of the time the function should be evaluated.
`b`	Bandwidth.
`Yi`	A matrix made by `make_Yi` indicating the exposure.
`int_X`	Position of the linear interpolated marker values on the marker grid.
`n`	Number of individuals.

Details

The function implements the future conditional hazard estimator

$$\hat{h}_x(t) = \frac{\sum_{i=1}^{n} \int_0^T \hat{\alpha}_i(X_i(t+s)) Z_i(t+s) Z_i(s) K_b(x - X_i(s)) \mathrm{d}s}{\sum_{i=1}^{n} \int_0^T Z_i(t+s) Z_i(s) K_b(x - X_i(s)) \mathrm{d}s},$$

for every x on the marker grid where X is the marker, Z is the exposure and $\alpha(z)$ is the marker-only hazard, see `get_alpha` for more details.

Value

A vector of $\hat{h}_x(t)$ for all values x on the marker grid.

Examples

```
pbc2_id = to_id(pbc2)
size_s_grid <- size_X_grid <- 100
n = max(as.numeric(pbc2$id))
s = pbc2$year
X = pbc2$serBilir
XX = pbc2_id$serBilir
ss <- pbc2_id$years
delta <- pbc2_id$status2
br_s = seq(0, max(s), max(s)/( size_s_grid-1))
br_X = seq(min(X), max(X), (max(X)-min(X))/( size_X_grid-1))

X_lin = lin_interpolate(br_s, pbc2_id$id, pbc2$id, X, s)

int_X <- findInterval(X_lin, br_X)
int_s = rep(1:length(br_s), n)

N <- make_N(pbc2, pbc2_id, br_X, br_s, ss, XX, delta)
Y <- make_Y(pbc2, pbc2_id, X_lin, br_X, br_s,
            size_s_grid, size_X_grid, int_s, int_X, event_time = 'years', n)

b = 1.7
alpha<-get_alpha(N, Y, b, br_X, K=Epan )

Yi <- make_Yi(pbc2, pbc2_id, X_lin, br_X, br_s,
              size_s_grid, size_X_grid, int_s, int_X, event_time = 'years', n)

t = 2

h_xt_vec(br_X, br_s, size_s_grid, alpha, t, b, Yi, int_X, n)
```

`Kernels` *Epanechnikov kernel and pdf kernel estimate*

Description

Implements the Epanechnikov kernel function and the standard kernel function estimate.

Usage

```
Epan(x)
K_b(b,x,y, K)
K_b_mat(b,x,y, K)
```

Arguments

x	A vector of design points where the kernel will be evaluated.
y	A vector of sample data points.
b	The bandwidth to use (a scalar).
K	The kernel function to use.

Details

Implements the Epanechnikov kernel function

$$K(x) = \frac{3}{4}(1 - x^2) * (|x| < 1)),$$

and the classical kernel density estimate

$$\hat{f}(x) = n^{-1} \sum_{i=1}^{n} K_h(x - X_i).$$

Value

In all three cases the functions return the value calculated at x.

---

lin_interpolate *Linear interpolation*

Description

Implements a linear interpolation between observered marker values.

Usage

```
lin_interpolate(t, i, data_id, data_marker, data_time)
```

Arguments

t	A vector of time values where the function should be evaluated.
i	A vector of ids of individuals for whom the marker values should be interpolated.
data_id	The vector of ids from a data frame of time dependent variables.
data_marker	The vector of marker values from a data frame of time dependent variables.
data_time	The vector of time values from a data frame of time dependent variables.

Details

Given time points $t_1, ..., t_K$ and marker values $m_1, ..., m_J$ at different time points $t_1^m, ..., t_J^m$, the function calculates a linear interpolation f with $f(t_i^m) = m_i$ at the time points $t_1, ..., t_K$ for all indicated individuals. Returned are then $(f(t_1), ..., f(t_K))$. Note that the first value is always observed at time point 0 and the function f is extrapolated constantly after the last observed marker value.

Value

A matrix with columns $(f(t_1), ..., f(t_K))$ as described above for every individual in the vector `i`.

Examples

```
size_s_grid <- 100
X = pbc2$serBilir
s = pbc2$year
br_s = seq(0, max(s), max(s)/( size_s_grid-1))
pbc2_id = to_id(pbc2)

X_lin = lin_interpolate(br_s, pbc2_id$id, pbc2$id, X, s)
```

---

make_N, make_Ni, make_Y, make_Yi

Occurance and Exposure on grids

Description

Auxiliary functions that help automate the process of calculating integrals with occurances or exposure processes.

Usage

```
make_N(data, data.id, breaks_X, breaks_s, ss, XX, delta)
make_Ni(breaks_s, size_s_grid, ss, delta, n)
make_Y(data, data.id, X_lin, breaks_X, breaks_s,
        size_s_grid, size_X_grid, int_s, int_X, event_time = 'years', n)
make_Yi(data, data.id, X_lin, breaks_X, breaks_s,
        size_s_grid, size_X_grid, int_s,int_X, event_time = 'years', n)
```

Arguments

`data`	A data frame of time dependent data points. Missing values are allowed.
`data.id`	An id data frame obtained from `to_id`.
`breaks_X`	Marker value grid points where the function will be evaluated.
`breaks_s`	Time value grid points where the function will be evaluated.
`ss`	Vector with event times.

XX	Vector of last observed marker values.
delta	0-1 vector of whether events happened.
size_s_grid	Size of the time grid.
size_X_grid	Size of the marker grid.
n	Number of individuals.
X_lin	Linear interpolation of observed marker values evaluated on the marker grid.
int_s	Position of the observed time values on the time grid.
int_X	Position of the linear interpolated marker values on the marker grid.
event_time	String of the column name with the event times.

Details

Implements matrices for the computation of integrals with occurences and exposures of the form

$$\int f(s)Z(s)Z(s+t)ds, \int f(s)Z(s)ds, \int f(s)dN(s).$$

where N is a 0-1 counting process, Z the exposure and f an arbitrary function.

Value

The functions make_N and make_Y return a matrix on the time grid and marker grid for occurence and exposure, respectively, while make_Ni and make_Yi return a matrix on the time grid for evey individual again for occurence and exposure, respectively.

See Also

h_xt, g_xt, get_alpha

Examples

```
pbc2_id = to_id(pbc2)
size_s_grid <- size_X_grid <- 100
n = max(as.numeric(pbc2$id))
s = pbc2$year
X = pbc2$serBilir
XX = pbc2_id$serBilir
ss <- pbc2_id$years
delta <- pbc2_id$status2
br_s = seq(0, max(s), max(s)/( size_s_grid-1))
br_X = seq(min(X), max(X), (max(X)-min(X))/( size_X_grid-1))

X_lin = lin_interpolate(br_s, pbc2_id$id, pbc2$id, X, s)

int_X <- findInterval(X_lin, br_X)
int_s = rep(1:length(br_s), n)

N <- make_N(pbc2, pbc2_id, br_X, br_s, ss, XX, delta)
Y <- make_Y(pbc2, pbc2_id, X_lin, br_X, br_s,
```

```
            size_s_grid, size_X_grid, int_s, int_X, event_time = 'years', n)
Yi <- make_Yi(pbc2, pbc2_id, X_lin, br_X, br_s,
              size_s_grid, size_X_grid, int_s, int_X, event_time = 'years', n)
Ni  <- make_Ni(br_s, size_s_grid, ss, delta, n)
```

---

make_sf *Survival function from a hazard*

Description

Creates a survival function from a hazard rate which was calculated on a grid.

Usage

```
make_sf(step_size_s_grid, haz)
```

Arguments

step_size_s_grid	Numeric value indicating the distance between two grid continuous grid points.
haz	Vector of hazard values. Hazard rate must have been calculated on a time grid.

Details

The function make_sf calculates the survival function

$$S(t) = \exp(-\int_0^t h(t)dt),$$

where h is the hazard rate. Here, a discritisation via an equidistant grid $\{t_i\}$ on $[0, t]$ is used to calculate the integral and it is assumed that h has been calculated for exactly these time points t_i.

Value

A vector of values $S(t_i)$.

Examples

```
make_sf(0.1, rep(0.1,10))
```

pbc2 *Mayo Clinic Primary Biliary Cirrhosis Data*

Description

Followup of 312 randomised patients with primary biliary cirrhosis, a rare autoimmune liver disease, at Mayo Clinic.

Usage

```
pbc2
```

Format

A data frame with 1945 observations on the following 20 variables.

`id` patients identifier; in total there are 312 patients.

`years` number of years between registration and the earlier of death, transplantion, or study analysis time.

`status` a factor with levels `alive`, `transplanted` and `dead`.

`drug` a factor with levels `placebo` and `D-penicil`.

`age` at registration in years.

`sex` a factor with levels `male` and `female`.

`year` number of years between enrollment and this visit date, remaining values on the line of data refer to this visit.

`ascites` a factor with levels `No` and `Yes`.

`hepatomegaly` a factor with levels `No` and `Yes`.

`spiders` a factor with levels `No` and `Yes`.

`edema` a factor with levels `No edema` (i.e., no edema and no diuretic therapy for edema), `edema no diuretics` (i.e., edema present without diuretics, or edema resolved by diuretics), and `edema despite diuretics` (i.e., edema despite diuretic therapy).

`serBilir` serum bilirubin in mg/dl.

`serChol` serum cholesterol in mg/dl.

`albumin` albumin in gm/dl.

`alkaline` alkaline phosphatase in U/liter.

`SGOT` SGOT in U/ml.

`platelets` platelets per cubic ml / 1000.

`prothrombin` prothrombin time in seconds.

`histologic` histologic stage of disease.

`status2` a numeric vector with the value 1 denoting if the patient was dead, and 0 if the patient was alive or transplanted.

References

Fleming, T. and Harrington, D. (1991) *Counting Processes and Survival Analysis*. Wiley, New York.

Therneau, T. and Grambsch, P. (2000) *Modeling Survival Data: Extending the Cox Model*. Springer-Verlag, New York.

Examples

```
summary(pbc2)
```

`prep_boot` *Precomputation for wild bootstrap*

Description

Implements key components for the wild bootstrap of the hqm estimator in preparation for obtaining confidence bands.

Usage

```
prep_boot(g_xt, alpha, Ni, Yi, size_s_grid, br_X, br_s, t, b, int_X, x, n)
```

Arguments

`g_xt`	A vector obtained by `g_xt`.
`alpha`	A vector of the marker only hazard on the marker grid obtained by `get_alpha`.
`Ni`	A matrix made by `make_Ni` indicating the occurence.
`Yi`	A matrix made by `make_Yi` indicating the exposure.
`size_s_grid`	Size of the time grid.
`br_X`	Vector of grid points for the marker values.
`br_s`	Time value grid points that will be used in the evaluatiuon.
`t`	Numeric value of the time the function should be evaluated.
`b`	Bandwidth.
`int_X`	Position of the linear interpolated marker values on the marker grid.
`x`	Numeric value of the last observed marker value.
`n`	Number of individuals.

Details

The function implements

$$A_B(t) = \frac{1}{\sqrt{n}} \sum_{i=1}^{n} \int_0^T \hat{g}_{i,t,x_*}(X_i(s)) V_i \{dN_i(s) - \hat{\alpha}_i(X_i(s)) Z_i(s) ds\},$$

and

$$B_B(t) = \frac{1}{\sqrt{n}} \sum_{i=1}^{n} V_i \{\hat{\Gamma}(t, x_*)^{-1} W_i(t, x_*) - \hat{h}_{x_*}(t)\},$$

where $V \sim N(0, 1)$,

$$W_i(t) = \int_0^T \hat{\alpha}_i(X_i(t+s)) Z_i(t+s) Z_i(s) K_b(x_*, X_i(s)) \mathrm{d}s,$$

and

$$\hat{\Gamma}(t, x) = \frac{1}{n} \sum_{i=1}^{n} \int_0^{T-t} Z_i(t+s) Z_i(s) K_b(x, X_i(s)) ds,$$

with Z being the exposure and X the marker.

Value

A list of 5 items. The first two are vectors for calculating A_B and the third one a vector for B_B. The 4th one is the value of the hqm estimator that can also be obtained by `h_xt` and the last one is the value of Γ.

See Also

`Conf_bands`

Examples

```
pbc2_id = to_id(pbc2)
size_s_grid <- size_X_grid <- 100
n = max(as.numeric(pbc2$id))
s = pbc2$year
X = pbc2$serBilir
XX = pbc2_id$serBilir
ss <- pbc2_id$years
delta <- pbc2_id$status2
br_s = seq(0, max(s), max(s)/( size_s_grid-1))
br_X = seq(min(X), max(X), (max(X)-min(X))/( size_X_grid-1))

X_lin = lin_interpolate(br_s, pbc2_id$id, pbc2$id, X, s)

int_X <- findInterval(X_lin, br_X)
int_s = rep(1:length(br_s), n)

N <- make_N(pbc2, pbc2_id, br_X, br_s, ss, XX, delta)
Y <- make_Y(pbc2, pbc2_id, X_lin, br_X, br_s,
```

```
            size_s_grid, size_X_grid, int_s, int_X, event_time = 'years', n)

b = 1.7
alpha<-get_alpha(N, Y, b, br_X, K=Epan )

Yi <- make_Yi(pbc2, pbc2_id, X_lin, br_X, br_s,
              size_s_grid, size_X_grid, int_s, int_X, event_time = 'years', n)
Ni  <- make_Ni(br_s, size_s_grid, ss, delta, n)

t = 2
x = 2

g = g_xt(br_X, br_s, size_s_grid, int_X, x, t, b, Yi, Y, n)

Boot_all = prep_boot(g, alpha, Ni, Yi, size_s_grid, br_X, br_s, t, b, int_X, x, n)
Boot_all
```

---

prep_cv *Prepare for Cross validation bandwidth selection*

Description

Implements the calculation of the hqm estimator on cross validation data sets. This is a preparation for the cross validation bandwidth selection technique for future conditional hazard rate estimation based on marker information data.

Usage

```
prep_cv(data, data.id, marker_name, event_time_name = 'years',
        time_name = 'year',event_name = 'status2', n, I, b)
```

Arguments

data	A data frame of time dependent data points. Missing values are allowed.
data.id	An id data frame obtained from to_id.
marker_name	The column name of the marker values in the data frame data.
event_time_name	The column name of the event times in the data frame data.
time_name	The column name of the times the marker values were observed in the data frame data.
event_name	The column name of the events in the data frame data.
n	Number of individuals.
I	Number of observations leave out for a K cross validation.
b	Bandwidth.

Details

The function splits the data set via `dataset_split` and calculates for every splitted data set the hqm estimator

$$\hat{h}_x(t) = \frac{\sum_{i=1}^{n} \int_0^T \hat{\alpha}_i(X_i(t+s)) Z_i(t+s) Z_i(s) K_b(x - X_i(s)) \mathrm{d}s}{\sum_{i=1}^{n} \int_0^T Z_i(t+s) Z_i(s) K_b(x - X_i(s)) \mathrm{d}s},$$

for all x on the marker grid and t on the time grid, where X is the marker, Z is the exposure and $\alpha(z)$ is the marker-only hazard, see `get_alpha` for more details.

Value

A list of matrices for every cross validation data set with $\hat{h}_x(t)$ for all x on the marker grid and t on the time grid.

See Also

`b_selection`

Examples

```
pbc2_id = to_id(pbc2)
n = max(as.numeric(pbc2$id))
b = 1.5
I = 26
h_xt_mat_list = prep_cv(pbc2, pbc2_id, 'serBilir', 'years', 'year', 'status2', n, I, b)
```

Q1 *Bandwidth selection score Q1*

Description

Calculates a part for the K-fold cross validation score.

Usage

```
Q1(h_xt_mat, int_X, size_X_grid, n, Yi)
```

Arguments

`h_xt_mat`	A matrix of the estimator for the future conditional hazard rate for all values `x` and `t`.
`int_X`	Vector of the position of the observed marker values in the grid for marker values.
`size_X_grid`	Numeric value indicating the number of grid points for marker values.
`n`	Number of individuals.
`Yi`	A matrix made by `make_Yi` indicating the exposure.

Details

The function implements

$$Q_1 = \sum_{i=1}^{N} \int_0^T \int_s^T Z_i(t) Z_i(s) \hat{h}^2_{X_i(s)}(t-s) dt ds,$$

where $\hat{h}$ is the hqm estimator, Z the exposure and X the marker.

Value

A value of the score Q1.

See Also

b_selection

Examples

```
pbc2_id = to_id(pbc2)
size_s_grid <- size_X_grid <- 100
n = max(as.numeric(pbc2$id))
s = pbc2$year
X = pbc2$serBilir
XX = pbc2_id$serBilir
ss <- pbc2_id$years
delta <- pbc2_id$status2
br_s = seq(0, max(s), max(s)/( size_s_grid-1))
br_X = seq(min(X), max(X), (max(X)-min(X))/( size_X_grid-1))

X_lin = lin_interpolate(br_s, pbc2_id$id, pbc2$id, X, s)

int_X <- findInterval(X_lin, br_X)
int_s = rep(1:length(br_s), n)

N <- make_N(pbc2, pbc2_id, br_X, br_s, ss, XX, delta)
Y <- make_Y(pbc2, pbc2_id, X_lin, br_X, br_s,
            size_s_grid, size_X_grid, int_s, int_X, event_time = 'years', n)

b = 1.7
alpha<-get_alpha(N, Y, b, br_X, K=Epan )

Yi <- make_Yi(pbc2, pbc2_id, X_lin, br_X, br_s,
              size_s_grid, size_X_grid, int_s, int_X, event_time = 'years', n)
Ni  <- make_Ni(br_s, size_s_grid, ss, delta, n)

t = 2

h_xt_mat = t(sapply(br_s[1:99],
            function(si){h_xt_vec(br_X, br_s, size_s_grid, alpha, t, b, Yi, int_X, n)}))

Q = Q1(h_xt_mat, int_X, size_X_grid, n, Yi)
```

R_K *Bandwidth selection score R*

Description

Calculates a part for the K-fold cross validation score.

Usage

```
R_K(h_xt_mat_list, int_X, size_X_grid, Yi, Ni, n)
```

Arguments

h_xt_mat_list	A list of matrices for all cross validation data sets. Each matrix contains the estimator with the future conditional hazard rate for all values x and t and the respected data set.
int_X	Vector of the position of the observed marker values in the grid for marker values.
size_X_grid	Numeric value indicating the number of grid points for marker values.
Yi	A matrix made by make_Yi indicating the exposure.
Ni	A matrix made by make_Ni indicating the occurence.
n	Number of individuals.

Details

The function implements the estimator

$$\hat{R}_K = \sum_{j=1}^{K} \sum_{i \in I_j} \int_0^T g_i^{-I_j}(t) dN_i(t),$$

where $\hat{g}_i^{-I_j}(t) = \int_0^t Z_i(s) \hat{h}_{X_i(s)}^{-I_j}(t-s) ds$, and $\hat{h}^{-I_j}$ is estimated without information from all counting processes i with $i \in I_j$. This function estimates

$$R = \sum_{i=1}^{N} \int_0^T \int_s^T Z_i(t) Z_i(s) \hat{h}_{X_i(s)}(t-s) h_{X_i(s)}(t-s) dt ds.$$

where $\hat{h}$ is the hqm estimator, Z the exposure and X the marker.

Value

A matrix with $\hat{g}_i^{-I_j}(t)$ for all individuals i and time grid points t.

See Also

b_selection

Examples

```
pbc2_id = to_id(pbc2)
n = max(as.numeric(pbc2$id))
b = 1.5
I = 104
h_xt_mat_list = prep_cv(pbc2, pbc2_id, 'serBilir', 'years', 'year', 'status2', n, I, b)


size_s_grid <- size_X_grid <- 100
s = pbc2$year
X = pbc2$serBilir
br_s = seq(0, max(s), max(s)/( size_s_grid-1))
br_X = seq(min(X), max(X), (max(X)-min(X))/( size_X_grid-1))

ss <- pbc2_id$years
delta <- pbc2_id$status2

X_lin = lin_interpolate(br_s, pbc2_id$id, pbc2$id, X, s)
int_X <- findInterval(X_lin, br_X)
int_s = rep(1:length(br_s), n)

Yi <- make_Yi(pbc2, pbc2_id, X_lin, br_X, br_s,
              size_s_grid, size_X_grid, int_s, int_X, 'years', n)
Ni  <- make_Ni(br_s, size_s_grid, ss, delta, n)

R = R_K(h_xt_mat_list, int_X, size_X_grid, Yi, Ni, n)
R
```

---

to_id *Event data frame*

Description

Creates a data frame with only one entry per individual from a data frame with time dependent data. The resulting data frame focusses on the event time and the last observed marker value.

Usage

```
to_id(data_set)
```

Arguments

data_set	A data frame of time dependent data points. Missing values are allowed.

Details

The function to_id uses a data frame of time dependent marker data to create a smaller data frame with only one entry per individual, the last observed marker value and the event time. Note that the column indicating the individuals must have the name id. Note also that this data frame is similar

to pbc2.id from the JM package with the difference that the last observed marker value instead of the first one is captured.

Value

A data frame with only one entry per individual.

Examples

```
data_set.id = to_id(pbc2)
```

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