# Package: FlexVarJM (via r-universe)

October 16, 2024

Title Estimate Joint Models with Subject-Specific Variance

Version 0.1.0

**Description** Estimation of mixed models including a subject-specific variance which can be time and covariate dependent. In the joint model framework, the package handles left truncation and allows a flexible dependence structure between the competing events and the longitudinal marker. The estimation is performed under the frequentist framework, using the Marquardt-Levenberg algorithm. (Courcoul, Tzourio, Woodward, Barbieri, Jacqmin-Gadda (2023) <arXiv:2306.16785>).

**License** GPL (>= 3)

**Encoding** UTF-8

RoxygenNote 7.2.3

**Imports** ggplot2, lcmm, marqLevAlg, mvtnorm, randtoolbox, Rcpp, stats, survminer, utils

**Depends** R (>= 3.5.0), splines, survival

URL https://github.com/LeonieCourcoul/FlexVarJM

BugReports https://github.com/LeonieCourcoul/FlexVarJM/issues

LazyData true

Suggests knitr, rmarkdown

VignetteBuilder knitr

LinkingTo Rcpp, RcppArmadillo

**NeedsCompilation** yes

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data.GaussKronrod

Initialisation of Survival Data at Gauss Kronrod time points

# Description

Initialisation of Survival Data at Gauss Kronrod time points

# Usage

```
data.GaussKronrod(data.id, Time, k = 15)
```

# Arguments

data.id A database with covariates of interest and 1 line per subject

Time A vector of time event

k The number of Gauss Kronrod points, by default k = 15

# Value

A list with the following components:

K an integer, the number of points

P a vector, of value Time/2

st a matrix with nrow = number of subjects and ncol = k. The new time to compute the survival function

wk a vector of weights

data.GaussKronrod2 3

```
data.id2 a database with K lines per subjects id.GK the vector of IDs
```

data.GaussKronrod2

Initialisation of Survival Data at Gauss Kronrod time points 2

# Description

Initialisation of Survival Data at Gauss Kronrod time points 2

# Usage

```
data.GaussKronrod2(data.id, a, b, k = 15)
```

# Arguments

data.id	A database with covariates of interest and 1 line per subject
a	First born
b	Second born
k	The number of Gauss Kronrod points, by default $k = 15$

### Value

A list with the following components:

K an integer, the number of points

P a vector, of value Time/2

st a matrix with nrow = number of subjects and ncol = k. The new time to compute the survival function

wk a vector of weights

data.id2 a database with K lines per subjects

id. GK the vector of IDs

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data.manag.long	Management of longitudinal data
-----------------	---------------------------------

### **Description**

Management of longitudinal data

### Usage

```
data.manag.long(formGroup, formFixed, formRandom, data.long1)
```

### Arguments

formGroup A formula which indicates the group variable

formFixed A formula which indicates the fixed effects for the longitudinal submodel formRandom A formula which indicates the random effects for the longitudinal submodel

data.long1 A dataframe with the longitudinal data

#### Value

A list with the following components:

data\_long a clean dataframe for the longitudinal data

y.new.prog the vector of responses variable

X a matrix with the fixed effects

U a matrix with the random effects

id a vector with the identification of individuals

offset a vector with the number of measurements for each individual

I an integer, the number of individuals

data.manag.surv Management of survival data

# Description

Management of survival data

## Usage

```
data.manag.surv(formGroup, formSurv, data.long1, formSurv_CompRisk)
```

data.time 5

### **Arguments**

formGroup A formula which indicates the group variable

formSurv A formula which indicates the variables used in the survival submodel

data.long1 Database

formSurv\_CompRisk

A formula which indicates the variables used in the competing survival sub-

model

#### Value

A list with the following components:

tmp the final database for survival analysis

Time a vector of observed times

event1 a vector of first event indicator

nTime length of Time vector

Z matrix of covariables of first survival submodel

event2 a vector of second event indicator

Z\_CR matrix of covariables of second survival submodel

data.time

Management of data for longitudinal submodel

# Description

Management of data for longitudinal submodel

### Usage

```
data.time(data.id, Time, formFixed, formRandom, timeVar)
```

# **Arguments**

data.id A dataframe

Time A vector of Time of events

formFixed A formula for the fixed effects of the longitudinal submodel formRandom A formula for the random effects of the longitudinal submodel

timeVar The name of the column of time in data.id. This variable must appears in data.id

### Value

A list with the following components

Xtime a matrix of fixed effects at each time of measure

Utime a matrix of random effects at each time of measure

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Data\_toy

Data\_toy

# Description

A simulated dataset for the example of the FlexVarJM package.

### Usage

Data\_toy

### **Format**

A data frame with 2076 rows and 5 variables:

ID the Id of each subject

visit the time of measurement

y the value of the marker

time the time of the first event observed

**event** the first event observed : 0 = censoring, 1 = first event, 2 = second event

gaussKronrod

Gauss-Kronrod nodes and weights

# Description

Gauss-Kronrod nodes and weights

### Usage

```
gaussKronrod(k = 15)
```

### **Arguments**

k

the number of points for Gauss-Kronrod approximation : choice between 7 and 15. 15 by default.

### Value

A list with the following components:

sk A k-vector of nodes

wk A k-vector of weights

goodness\_of\_fit 7

goodness_of_fit	Predictions for the goodness of fit, of the random effects, the current value for each individuals and the cumulative hazard function for both events
-----------------	-------------------------------------------------------------------------------------------------------------------------------------------------------

### **Description**

Predictions for the goodness of fit, of the random effects, the current value for each individuals and the cumulative hazard function for both events

### Usage

```
goodness_of_fit(object, graph = FALSE, break.times = NULL)
```

### **Arguments**

object an object of class lsjm

graph a boolean to indicate to print graphics, False by default break.times a vector of times for the time points of longitudinal graphic

#### Value

A list which contains the following elements:

tables A list with the table of the predicted random effect, the table of the predicted current value, table(s) of predictive cumulative hazard function(s)

graphs A list with 2 or 3 graphs: one for the longitudinal adjustment and one for each risk function

### **Examples**

```
#Fit a joint model with competing risks and subject-specific variability
example <- lsjm(formFixed = y~visit,
formRandom = ~ visit,
formGroup = ~ID,
formSurv = Surv(time, event ==1 ) ~ 1,
timeVar = "visit",
data.long = Data_toy,
variability_hetero = TRUE,
formFixedVar =~visit,
formRandomVar =~visit,
correlated_re = TRUE,
sharedtype = c("current value", "variability"),
hazard_baseline = "Weibull",
formSlopeFixed =~1,
formSlopeRandom = ~1,</pre>
```

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```
indices_beta_slope = c(2),
competing_risk = TRUE,
formSurv_CR = Surv(time, event ==2 ) ~ 1,
hazard_baseline_CR = "Weibull",
sharedtype_CR = c("current value", "variability"),
S1 = 100,
S2 = 1000,
nproc = 1,
maxiter = 100,
Comp.Rcpp = TRUE
)

#Assesment of the goodness of fit:
gof <- goodness_of_fit(example, graph = TRUE)
gof$tables
gof$graphs</pre>
```

initial.long

Initialisation of Longitudinal Submodel

### **Description**

Initialisation of Longitudinal Submodel

# Usage

```
initial.long(formFixed, formRandom, idVar, data.long1, ncX, nproc = nproc)
```

### **Arguments**

formFixed A formula which indicates the fixed effects for the longitudinal submodel formRandom A formula which indicates the random effects for the longitudinal submodel

idVar A character, indicates the name of the group variable

data.long1 A dataframe with the longitudinal data

ncX An integer, the number of columns of matrix X, ie, the number of fixed effects

nproc An integer, the number of cores for parallel computation

#### Value

A list with the following components:

long\_model the result of the hlme function

priorMean.beta the estimated parameters for fixed effects in the linear mixed effects model sigma the estimated sigma of the model

log\_llh

 $log_1lh$ 

Log-likelihood computation

# Description

Log-likelihood computation

# Usage

```
log_llh(
 param,
 nb.e.a,
 nb.priorMean.beta,
 nb.alpha,
  competing_risk,
 nb.alpha.CR,
  variability_hetero,
  S,
  Ζq,
  sharedtype,
  sharedtype_CR,
  hazard_baseline,
 hazard_baseline_CR,
 ord.splines,
 Xtime,
 Utime,
  nb_pointsGK,
 Χs,
 Us,
 Xslope,
 Uslope,
 Xs.slope,
 Us.slope,
  indices_beta_slope,
 Time,
  st_calc,
 В,
 Вs,
 wk,
  Ζ,
 Ρ,
 left_trunc,
 Z_CR,
 X_base,
 offset,
 y.new.prog,
```

log\_llh

```
event1,
      event2,
      Ind,
      Xs.0,
      Us.0,
      Xs.slope.0,
      Us.slope.0,
      P.0,
      st.0,
      Bs.0,
      B.CR,
      Bs.CR,
      Bs.0.CR,
      nb.e.a.sigma = nb.e.a.sigma,
      nb.omega = nb.omega,
      Otime = Otime,
      Wtime = Wtime,
      0s = 0s,
      Ws = Ws,
      0_{base} = 0_{base}
      W_base = W_base,
      correlated_re = correlated_re,
      0s.0 = 0s.0,
      Ws.0 = Ws.0
    )
Arguments
    param
                     a vector: paramaters to be estimated
    nb.e.a
                     integer: number of RE
    nb.priorMean.beta
                     integer: number of fixed effects
    nb.alpha
                     integer: number of covariates in survival model
    competing_risk boolean: allow competing risk or not, FALSE by default
    nb.alpha.CR
                     integer: number of covariates in survival model for competing risks
    variability_hetero
                     boolean: allow the heterogeneous variability or not
    S
                     integer: the number of QMC points
                      vector: sobol points
    Zq
    sharedtype
                     vector: dependence structure for survival model: "RE" (random effects) or
                      "CV" (current value) or "CVS" (current value and slope) or "S" (slope)
                     vector: dependence structure for competing risk survival model: "RE" (ran-
    sharedtype_CR
                      dom effects) or "CV" (current value) or "CVS" (current value and slope) or "S"
                      (slope)
```

char: baseline hazard function: "Exponential" or "Weibull" or "Splines"

hazard\_baseline

log\_llh

hazard\_baseline\_CR

char: baseline hazard function, competing risk: "Exponential" or "Weibull" or

"Splines"

ord.splines integer: the order of splines function for baseline hazard function

Xtime matrix: fixed effects at event time

Utime matrix : RE at event time

nb\_pointsGK integer: number of points for Gauss-Kronrod approximation, 7 or 15 (default)

Xs matrix: fixed effects at Gauss-Kronrod times

Us matrix : RE at Gauss-Kronrod times

Xslope matrix: fixed effects of slope at event times

Uslope matrix : RE of slope at event times

Xs.slope matrix: fixed effects of slope at Gauss-Kronrod times

Us.slope matrix: RE of slope at Gauss-Kronrod times

indices\_beta\_slope

vector: position of beta which will be used in the slope computation

Time vector : observed event times st\_calc matrix : Gauss-Kronrod times

B matrix : splines for baseline hazard function of event 1
Bs matrix : splines for baseline survival function of event 1

wk vector: Gauss-Kronrod weights

Z matrix: covariates for survival function of event 1

P vector: Time/2

left\_trunc boolean : left truncation indicator

Z\_CR matrix : covariates for survival function of event 2X\_base matrix : fixed effects for longitudinal submodel

offset vector : number of lines per subjects
U matrix : RE for longitudinal submodel

y.new.prog vector: y measures for longitudinal submodel

event1 vector: event 1 indicator event2 vector: event 2 indicator Ind integer: number of subjects Xs.0 same for left truncation same for left truncation Us.0 same for left truncation Xs.slope.0 Us.slope.0 same for left truncation same for left truncation P.0 same for left truncation st.0 same for left truncation Bs.0

B. CR same for left truncationBs. CR same for left truncationBs. O. CR same for left truncation

nb.e.a.sigma integer: number of RE for variability

nb.omega integer: number of fixed effects for variability

Otime matrix: fixed effects of variability at event time

Wtime matrix: RE of variability at event time

Os matrix : fixed effects of variability at Gauss-Kronrod times

Ws matrix : random effects of variability at Gauss-Kronrod times

O\_base matrix : fixed effects for variability
W\_base matrix : fixed effects for variability

correlated\_re boolean: indicator to allow all the random effects to be correlated

Os.0 matrix : same for left truncation
Ws.0 matrix : same for left truncation

#### Value

The value of the log-likelihood

log\_llh\_rcpp

Log-likelihood computation in RCPP

### Description

Log-likelihood computation in RCPP

# Usage

```
log_llh_rcpp(
  param,
  nb.e.a,
  nb.priorMean.beta,
  nb.alpha,
  competing_risk,
  nb.alpha.CR,
  variability_hetero,
  S,
  Zq,
  sharedtype,
  sharedtype_CR,
  hazard_baseline,
  hazard_baseline,
  ord.splines,
```

```
Xtime,
 Utime,
 nb_pointsGK,
 Χs,
 Us,
 Xslope,
 Uslope,
 Xs.slope,
 Us.slope,
  indices_beta_slope,
 Time,
  st_calc,
 Β,
 Вs,
 wk,
  Ζ,
 Р,
 left_trunc,
 Z_CR,
 X_base,
 offset,
 U,
 y.new.prog,
 event1,
 event2,
  Ind,
 Xs.0,
 Us.0,
 Xs.slope.0,
 Us.slope.0,
 P.0,
  st.0,
 Bs.0,
 B.CR,
 Bs.CR,
 Bs.0.CR,
 nb.e.a.sigma = nb.e.a.sigma,
 nb.omega = nb.omega,
 Otime = Otime,
 Wtime = Wtime,
 0s = 0s,
 Ws = Ws,
 0_base = 0_base,
 W_base = W_base,
 correlated_re = correlated_re,
 0s.0 = 0s.0,
 Ws.0 = Ws.0
)
```

#### **Arguments**

param a vector : paramaters to be estimated

nb.e.a integer: number of RE

nb.priorMean.beta

integer: number of fixed effects

nb.alpha integer: number of covariates in survival model

competing\_risk boolean: allow competing risk or not, FALSE by default

nb.alpha.CR integer: number of covariates in survival model for competing risks

variability\_hetero

boolean: allow the heterogeneous variability or not

S integer: the number of QMC points

Zq vector: sobol points

sharedtype vector: dependence structure for survival model: "RE" (random effects) or

"CV" (current value) or "CVS" (current value and slope) or "S" (slope)

sharedtype\_CR vector: dependence structure for competing risk survival model: "RE" (ran-

dom effects) or "CV" (current value) or "CVS" (current value and slope) or "S"

(slope)

hazard\_baseline

char: baseline hazard function: "Exponential" or "Weibull" or "Splines"

hazard\_baseline\_CR

char: baseline hazard function, competing risk: "Exponential" or "Weibull" or

"Splines"

ord.splines integer: the order of splines function for baseline hazard function

Xtime matrix: fixed effects at event time

Utime matrix: RE at event time

nb\_pointsGK integer: number of points for Gauss-Kronrod approximation, 7 or 15 (default)

Xs matrix: fixed effects at Gauss-Kronrod times

Us matrix : RE at Gauss-Kronrod times

Xslope matrix: fixed effects of slope at event times

Uslope matrix : RE of slope at event times

Xs.slope matrix: fixed effects of slope at Gauss-Kronrod times

Us. slope matrix: RE of slope at Gauss-Kronrod times

indices\_beta\_slope

vector: position of beta which will be used in the slope computation

Time vector: observed event times st\_calc matrix: Gauss-Kronrod times

B matrix : splines for baseline hazard function of event 1
Bs matrix : splines for baseline survival function of event 1

wk vector: Gauss-Kronrod weights

Ζ matrix: covariates for survival function of event 1

Ρ vector: Time/2

event1

Bs.0.CR

boolean: left truncation indicator left\_trunc

Z\_CR matrix: covariates for survival function of event 2 matrix: fixed effects for longitudinal submodel X\_base

offset vector: number of lines per subjects matrix: RE for longitudinal submodel

vector: y measures for longitudinal submodel y.new.prog

vector: event 1 indicator vector: event 2 indicator event2 Ind integer: number of subjects Xs.0 same for left truncation Us.0 same for left truncation same for left truncation Xs.slope.0 same for left truncation Us.slope.0 P.0 same for left truncation st.0 same for left truncation same for left truncation Bs.0 B.CR same for left truncation same for left truncation Bs.CR

integer: number of RE for variability nb.e.a.sigma

same for left truncation

nb.omega integer: number of fixed effects for variability Otime matrix: fixed effects of variability at event time

matrix: RE of variability at event time Wtime

0s matrix : fixed effects of variability at Gauss-Kronrod times matrix: random effects of variability at Gauss-Kronrod times Ws

matrix: fixed effects for variability 0\_base W\_base matrix: fixed effects for variability

boolean: indicator to allow all the random effects to be correlated correlated\_re

matrix: same for left truncation 0s.0 Ws.0 matrix: same for left truncation

# Value

The value of the log-likelihood

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lsjm

*lsjm*: Estimation of joint model for longitudinal data with a subjectspecific time-dependent variability and time-to-event data.

#### **Description**

This function fits complex joint models with shared random effects. The longitudinal submodel estimates longitudinal data with a mixed-effects model in which we suppose that the variance of the residual error is time-dependent and subject-specific. The survival submodel handles right-censored and left-truncated time-to-event data and competing risks. The dependence structure between the longitudinal and the survival data can be the random effects from the mixed model or the current value of the marker and/or the slope of the marker. We can also adjust on the current variance of the marker. (See below) Parameters are estimated simultaneously through a maximum likelihood method, using a Marquardt-Levenberg algorithm.

## Usage

```
lsjm(
  formFixed,
  formRandom,
  formGroup,
  formSurv,
  timeVar,
  data.long,
  variability_hetero = TRUE,
  formFixedVar,
  formRandomVar,
  correlated_re = FALSE,
  sharedtype = c("current value", "variability"),
  hazard_baseline = "Exponential",
  formSlopeFixed = NULL,
  formSlopeRandom = NULL,
  indices_beta_slope = NULL,
  nb_pointsGK = 15,
  ord.splines = 3,
  competing_risk = FALSE,
  formSurv_CR = NULL,
  hazard_baseline_CR = "Exponential",
  sharedtype_CR = c("current value", "variability"),
  left_trunc = FALSE,
  Time.0 = NULL,
  S1 = 1000,
  S2 = 5000,
  nproc = 1,
  clustertype = "SOCK",
  maxiter = 100,
  print.info = FALSE,
```

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```
file = NULL,
epsa = 0.001,
epsb = 0.001,
epsd = 0.001,
binit = NULL,
Comp.Rcpp = TRUE
```

### **Arguments**

formFixed A formula for the fixed effects of the longitudinal submodel formRandom A formula for the random effects of the longitudinal submodel

formGroup A formula which indicates the group variable

formSurv A formula which indicates the variables used in the survival submodel

timeVar The name of the column of time in data.long. This variable must appears in

data.long

data.long A dataframe with the longitudinal data

variability\_hetero

A logical to indicate if we suppose a subject\_specific variability

formFixedVar A formula for the fixed effects of the variance predictor formRandomVar A formula for the random effects of the variance predictor

correlated\_re A logical to indicate if the random effects of the marker and the variance pre-

dictors are correlated (By default there are supposed to be independent)

sharedtype char: dependence structure for survival model: "RE" (random effects) or "CV"

(current value) or "CVS" (current value and slope) or "S" (slope)

hazard\_baseline

char: baseline hazard function: "Exponential" or "Weibull" or "Splines"

formSlopeFixed A formula for the fixed effects of the slope of the longitudinal submodel : the

derivative of the formFixed

formSlopeRandom

A formula for the random effects of the slope of the longitudinal submodel : the derivative of the formRandom

indices\_beta\_slope

A vector of index indicating which beta of the formFixed formula is used in the

formSlopeFixed formula

nb\_pointsGK the number of points for Gauss-Kronrod approximation: choice between 7 and

15. 15 by default.

ord. splines A numeric, the order of splines for the baseline risk function (3 by default)

competing\_risk A logical indicating if the model handles with competing risks

formSurv\_CR In case of competing risk A formula which indicates the variables used in the

survival submodel for the second event

hazard\_baseline\_CR

In case of competing risk: a character for the baseline hazard function of the second event

sharedtype\_CR In case of competing risk; a character for the dependence structure left\_trunc A logical indicating if the model handles with left truncated data

Time.0 In case of left truncation: a vector of entry times

An integer: the number of QMC draws for the first step S1 An integer: the number of QMC draws for the second step S2 An integer: the number of processors for parallel computing nproc

clustertype one of the supported types from makeCluster function

maxiter optional maximum number of iterations for the marqLevAlg iterative algorithm.

logical indicating if the outputs of each iteration should be written print.info

file optional character giving the name of the file where the outputs of each iteration

should be written (if print.info=TRUE)

optional threshold for the convergence criterion based on the parameter stability. epsa optional threshold for the convergence criterion based on the objective function epsb

stability.

epsd optional threshold for the relative distance to maximum. This criterion has the

> nice interpretation of estimating the ratio of the approximation error over the statistical error, thus it can be used for stopping the iterative process whatever

the problem.

binit optional initials parameters.

boolean to indicate if the computation is performed with RCPP program or R Comp.Rcpp

program. True by default.

#### **Details**

### A. LONGITUDINAL SUBMODEL

The longitudinal submodel is defined by a linear mixed effects model with the residual variance

which could be supposed to be time-dependent and subject-specific:

$$\begin{cases} Y_{ij} = Y_i(t_{ij}) = \widetilde{Y}_i(t_{ij}) + \epsilon_{ij} = X_{ij}^{\top} \beta + Z_{ij}^{\top} b_i + \epsilon_{ij} \\ \epsilon_{ij}(t_{ij}) \sim \mathcal{N}(0, \sigma_i^2(t_{ij})) & \text{with} \quad \log(\sigma_i(t_{ij})) = C \end{cases}$$

with  $X_{ij}$ ,  $O_{ij}$ ,  $Z_{ij}$  and  $M_{ij}$  four vectors of explanatory variables for subject i at visit j, re-

spectively associated with the fixed-effect vectors 
$$\beta$$
 and  $\mu$ , and the subject-specific random-effect vector  $b_i$  and  $\tau_i$ , such as  $\begin{pmatrix} b_i \\ \tau_i \end{pmatrix} \sim N\left(\begin{pmatrix} 0 \\ 0 \end{pmatrix}, \begin{pmatrix} \Sigma_b & \Sigma_{\tau b} \\ \Sigma'_{\tau b} & \Sigma_{\tau} \end{pmatrix}\right)$ :

$$Y_i(t_{ij}) = \tilde{Y}_i(t_{ij}) + \epsilon_{ij} = X_{ij}^{\top} \beta + Z_{ij}^{\top} b_i + \epsilon_{ij}$$

with  $X_{ij}$  and  $Z_{ij}$  two covariate vectors for subject i at visit j, respectively associated with the vector of fixed effects  $\beta$  and the vector of subject-specific individual random effects  $b_i$ . The vector  $b_i$  is assumed to be normally distributed and a specific-subject random effect on the variance of the measure error can be added:  $\epsilon_{ij} \sim \mathcal{N}(0, \sigma_i^2)$  and

$$\left(\begin{array}{c}b_i\\\log\sigma_i\end{array}\right)\sim\mathcal{N}\left(\left(\begin{array}{c}0\\\mu_\sigma\end{array}\right),\left(\begin{array}{cc}\Sigma_b&0\\0&\tau_\sigma^2\end{array}\right)\right)$$

B. SURVIVAL SUBMODEI

The risk function for the event  $k = \{1,2\}$  is defined by:  $\lambda_{ik}(t) = \lambda_{0k}(t) \exp\left(W_i^{\top} \gamma_k + \alpha_{1k} \tilde{y}_i(t) + \alpha_{2k} \tilde{y}_i'(t) + \alpha_{\sigma k} \sigma_i(t)\right)$ with  $\lambda_{0k}(t)$  the baseline risk function,  $W_i$  a vector of baseline covariates associated with the regression coefficient  $\gamma_k$ , and  $\alpha_{1k}$ ,  $\alpha_{2k}$  and  $\alpha_{\sigma k}$  the regression coefficients associated with the

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current value  $\tilde{y}_i(t)$ , the current slope  $\tilde{y}_i'(t)$  and the current variability  $\sigma_i(t)$  of the marker, respectively. Different parametric forms for the baseline risk function can be considered, such as exponential, Weibull, or, for more flexibility, a B-splines base.

### Value

```
A FlexVarJoint object which contains the following elements:

result A marqLevAlg object with the results of the estimation.

table.res The table of results: Estimation and SE

time.compute Computation time

control A list of control elements
```

### **Examples**

```
#fit a joint model with competing risks and subject-specific variability
example <- lsjm(formFixed = y~visit,
formRandom = ~ visit,
formGroup = ~ID,
formSurv = Surv(time, event ==1 ) ~ 1,
timeVar = "visit",
data.long = Data_toy,
variability_hetero = TRUE,
formFixedVar =~visit,
formRandomVar =~visit,
correlated_re = TRUE,
sharedtype = c("current value", "variability"),
hazard_baseline = "Weibull",
formSlopeFixed =~1,
formSlopeRandom = ~1,
indices_beta_slope = c(2),
competing_risk = TRUE,
formSurv_CR = Surv(time, event ==2 ) ~ 1,
hazard_baseline_CR = "Weibull",
sharedtype_CR = c("current value", "variability"),
S1 = 100,
S2 = 1000,
nproc = 1,
maxiter = 100,
Comp.Rcpp = TRUE
)
summary(example)
```

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1smm

lsmm: Estimation of location scale mixed model

### **Description**

This function fits complex mixed effects model with a time and covariate dependent variance. We suppose that the variance of the residual error is time-dependent and subject-specific. Parameters are estimated simultaneously through a maximum likelihood method, using a Marquardt-Levenberg algorithm.

### Usage

```
1smm(
  formFixed,
  formRandom,
  formGroup,
  timeVar,
  data.long,
  variability_hetero = TRUE,
  formFixedVar,
  formRandomVar,
  correlated_re = FALSE,
  S1 = 1000,
  S2 = 5000,
 nproc = 1,
  clustertype = "SOCK",
 maxiter = 100,
 print.info = FALSE,
  file = NULL,
  epsa = 0.001,
  epsb = 0.001,
 epsd = 0.001,
 binit = NULL
)
```

### **Arguments**

formFixed	A formula for the fixed effects of the longitudinal submodel			
formRandom	A formula for the random effects of the longitudinal submodel			
formGroup	A formula which indicates the group variable			
timeVar	The name of the column of time in data.long. This variable must appears in data.long			
data.long	A dataframe with the longitudinal data			
variability_hetero				

A logical to indicate if we suppose a subject\_specific variability

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formFixedVar A formula for the fixed effects of the variance predictor formRandomVar A formula for the random effects of the variance predictor

A logical to indicate if the random effects of the marker and the variance precorrelated re

dictors are correlated (By default there are supposed to be independent)

An integer: the number of OMC draws for the first step S1 S2 An integer: the number of QMC draws for the second step An integer: the number of processors for parallel computing nproc one of the supported types from makeCluster function clustertype

optional maximum number of iterations for the marqLevAlg iterative algorithm. maxiter

print.info logical indicating if the outputs of each iteration should be written

file optional character giving the name of the file where the outputs of each iteration

should be written (if print.info=TRUE)

optional threshold for the convergence criterion based on the parameter stability. epsa optional threshold for the convergence criterion based on the objective function epsb

stability.

epsd optional threshold for the relative distance to maximum. This criterion has the

nice interpretation of estimating the ratio of the approximation error over the statistical error, thus it can be used for stopping the iterative process whatever

the problem.

binit optional initials parameters.

#### **Details**

The model is defined by : #' 
$$\left\{ \begin{array}{l} Y_{ij} = Y_i(t_{ij}) = \widetilde{Y}_i(t_{ij}) + \epsilon_{ij} = X_{ij}^\top \beta + Z_{ij}^\top b_i + \epsilon_{ij}, \\ \epsilon_{ij}(t_{ij}) \sim \mathcal{N}(0, \sigma_i^2(t_{ij})) \quad \text{with} \quad \log(\sigma_i(t_{ij})) = O_{ij}^\top \mu + M_{ij}^\top \tau_i \end{array} \right.$$

with  $X_{ij}$ ,  $O_{ij}$ ,  $Z_{ij}$  and  $M_{ij}$  four vectors of explanatory variables for subject i at visit j, re-

spectively associated with the fixed-effect vectors 
$$\beta$$
 and  $\mu$ , and the subject-specific random-effect vector  $b_i$  and  $\tau_i$ , such as  $\begin{pmatrix} b_i \\ \tau_i \end{pmatrix} \sim N \begin{pmatrix} \begin{pmatrix} 0 \\ 0 \end{pmatrix}, \begin{pmatrix} \sum_b & \sum_{\tau b} \\ \Sigma'_{\tau b} & \Sigma_{\tau} \end{pmatrix}$ :

$$Y_i(t_{ij}) = \tilde{Y}_i(t_{ij}) + \epsilon_{ij} = X_{ij}^{\top} \beta + Z_{ij}^{\top} b_i + \epsilon_{ij}$$

with  $X_{ij}$  and  $Z_{ij}$  two covariate vectors for subject i at visit j, respectively associated with the vector of fixed effects  $\beta$  and the vector of subject-specific individual random effects  $b_i$ . The vector  $b_i$  is assumed to be normally distributed and a specific-subject random effect on the variance of the measure error can be added:  $\epsilon_{ij} \sim \mathcal{N}(0, \sigma_i^2)$  and

$$\left(\begin{array}{c}b_i\\\log\sigma_i\end{array}\right) \sim \mathcal{N}\left(\left(\begin{array}{c}0\\\mu_\sigma\end{array}\right),\left(\begin{array}{cc}\Sigma_b&0\\0&\tau_\sigma^2\end{array}\right)\right)$$

#### Value

A FlexVarJoint object which contains the following elements:

result A marqLevAlg object with the results of the estimation.

table.res The table of results: Estimation and SE

time.compute Computation time control A list of control elements 22 predyn

# **Examples**

```
#fit a joint model with competing risks and subject-specific variability
example <- lsmm(formFixed = y~visit,
formRandom = ~ visit,
formGroup = ~ID,
timeVar = "visit",
data.long = Data_toy,
variability_hetero = TRUE,
formFixedVar =~visit,
formRandomVar =~visit,
correlated_re = TRUE,
S1 = 100,
S2 = 1000,
nproc = 1,
maxiter = 100
)
summary(example)</pre>
```

predyn

Dynamic prediction for new individuals

### **Description**

Dynamic prediction for new individuals

# Usage

```
predyn(
  newdata,
  object,
  s,
  times,
  event = 1,
  IC = 95,
  nb.draws = 500,
  graph = FALSE
)
```

# Arguments

newdata data frame: collected data for a new individual

object lsjm object: estimation of the model

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S	numeric: the time to begin prediction
times	numeric vector: future times to calculate predictions
event	integer (0, 1 or 2): the event of interest for the prediction
IC	integer : percentage of confidence for the interval confidence (between 0 and 100), 95 by default, NULL if no IC $$
nb.draws	integer: the number of simulations to compute the interval confidence (by bootstrap), 500 by default
graph	boolean: indicator to plot the graphs or not

### Value

A table of dynamic predictions

### **Examples**

```
#fit a joint model with competing risks and subject-specific variability
example <- lsjm(formFixed = y~visit,
formRandom = ~ visit,
formGroup = ~ID,
formSurv = Surv(time, event ==1 ) ~ 1,
timeVar = "visit",
data.long = Data_toy,
variability_hetero = TRUE,
formFixedVar =~visit,
formRandomVar =~visit,
correlated_re = TRUE,
sharedtype = c("current value", "variability"),
hazard_baseline = "Weibull",
formSlopeFixed =~1,
formSlopeRandom = ~1,
indices\_beta\_slope = c(2),
competing_risk = TRUE,
formSurv_CR = Surv(time, event ==2) ~ 1,
hazard_baseline_CR = "Weibull",
sharedtype_CR = c("current value", "variability"),
S1 = 100,
S2 = 1000,
nproc = 1,
maxiter = 100,
Comp.Rcpp = TRUE
#Prediction for individuals 1 and 3 to experiment the event 1
#at time 1.5, 2, and 3, given their measurements until time 1:
newdata <- Data_toy[which(Data_toy$ID %in% c(1,3)),]</pre>
pred.new <- predyn(newdata, example, 1, c(1.5, 2, 2.8, 3), event = 1, IC = 95,
nb.draws = 100, graph = TRUE)
```

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```
pred_s.t.bootstrap.tps
```

Predictions computation

### **Description**

Predictions computation

# Usage

```
pred_s.t.bootstrap.tps(newdata, object, s, window, event = 1, nb.draws)
```

# Arguments

newdata data frame: collected data for a new individual

object lsjm object : estimation of the model s numeric : the time to begin prediction

window numeric: the side of the prediction window

event integer (0, 1 or 2): the event of interest for the prediction

nb.draws integer: the number of draws to compute the IC

pred\_s.t.ponctuel.tps Predictions computation

# Description

Predictions computation

### Usage

```
pred_s.t.ponctuel.tps(newdata, object, s, window, event = 1)
```

### **Arguments**

newdata data frame: collected data for a new individual

object lsjm object : estimation of the model
s numeric : the time to begin prediction
window numeric : the side of the prediction window

event integer (0, 1 or 2): the event of interest for the prediction

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