

# Package: EvCombR (via r-universe)

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**Type** Package

**Title** Evidence Combination in R

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**Description** Combine pieces of evidence in the form of uncertainty representations.

**License** GPL (>= 3)

**Imports** methods, utils

**NeedsCompilation** no

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EvCombR-package

*EvCombR - Evidence Combination in R***Description**

Package for combining pieces of evidence.

**Details**

Implements Dempster's, Yager's, modified Dempster's, Bayesian, and credal combination (based on intervals).

**Author(s)**

Alexander Karlsson

Maintainer: Alexander Karlsson <alexander.karlsson@his.se>

## References

- Dempster, A. P. (1969), A generalization of Bayesian inference, *Journal of the Royal Statistical Society*, **30**, 205-247
- Shafer, G. (1976), *A Mathematical Theory of Evidence* Princeton University Press
- Yager, R. (1987), On the Dempster-Shafer Framework and New Combination Rules, *Information Sciences 41*: 93-137.
- Fixsen, D., Mahler, R. P. S. (1997), The modified Dempster-Shafer approach to classification, *IEEE Transactions on Systems, Man and Cybernetics, Part A: Systems and Humans*, **27**, 96-104
- Arnborg, S. (2006), Robust Bayesianism: Relation to Evidence Theory, *Journal of Advances in Information Fusion*, **1**, 63-74
- Karlsson, A., Johansson, R., and Andler, S. F. (2011), Characterization and Empirical Evaluation of Bayesian and Credal Combination Operators, *Journal of Advances in Information Fusion*, **6**, 150-166

## Examples

```
# construct a state space
stateSpace <- c("a", "b", "c")

# construct credal sets with the given state space
c1 <- credal(c(0.1, 0.1, 0.1), c(0.8, 0.8, 0.8), stateSpace)
c2 <- credal(c(0.2, 0.2, 0.2), c(0.9, 0.9, 0.9), stateSpace)

# combine the credal sets
cComb(c1, c2)

# construct mass functions
m1 <- mass(list("a"=0.1, "b"=0.1, "c"=0.4, "a/b/c"=0.4), stateSpace)
m2 <- mass(list("a"=0.2, "b"=0.2, "c"=0.2, "a/b/c"=0.4), stateSpace)

# combine the mass functin by using Dempster's combination
dComb(m1, m2)

# Yager's combination operator
yComb(m1, m2)

# modified Dempster's combination using uniform prior
mComb(m1, m2)
```

---

cComb

*Credal Combination Operator (restricted to intervals)*


---

## Description

Combine evidence in the form of credal sets (based on intervals) using the credal combination operator (also known as the robust Bayesian combination operator). The resulting credal set is approximated by using probability intervals.

**Usage**

```
cComb(x, y)
```

**Arguments**

x	credal set or a list of credal sets
y	credal set if x is a credal set, otherwise missing

**Value**

credal set

**Author(s)**

Alexander Karlsson

**References**

- Levi, I. (1983), *The enterprise of knowledge*, The MIT press
- Arnborg, S. (2006), Robust Bayesianism: Relation to Evidence Theory, *Journal of Advances in Information Fusion*, **1**, 63-74
- Karlsson, A., Johansson, R., and Andler, S. F. (2011), Characterization and Empirical Evaluation of Bayesian and Credal Combination Operators, *Journal of Advances in Information Fusion*, **6**, 150-166

**See Also**

[dComb](#), [yComb](#), [mComb](#)

**Examples**

```
# construct a state space
stateSpace <- c("a", "b", "c")

# construct credal sets with the given state space
c1 <- credal(c(0.1, 0.1, 0.1), c(0.8, 0.8, 0.8), stateSpace)
c2 <- credal(c(0.2, 0.2, 0.2), c(0.9, 0.9, 0.9), stateSpace)

# combine the credal sets
cComb(c1, c2)
# or by
cComb(list(c1, c2))
```

---

`cComb-methods`*Methods for Function cComb*

---

**Description**

Combine credal sets (based on intervals) using the credal combination operator (also known as the robust Bayesian combination operator). For more detail see [cComb](#).

**Methods**

`signature(x = "credal", y = "credal")` Combine two credal sets using the credal combination operator

`signature(x = "list", y = "missing")` Combine a list of credal sets using the credal combination operator

---

`credal`*Constructor Function for Credal Sets (based on intervals)*

---

**Description**

Construct a credal set based on probability intervals or a single probability function. The algorithm used for finding the extreme points corresponding to lower and upper bounds is described in De Campos et al. (1994).

**Usage**

```
credal(x, y, z)
```

**Arguments**

`x` lower bounds of probability intervals (in the form of a numeric vector)  
`y` upper bounds for probability intervals or missing (i.e., upper bound of 1)  
`z` character vector representing the state space

**Value**

A credal set represented by a set of extreme points.

**Author(s)**

Alexander Karlsson

## References

- Levi, I. (1983), *The enterprise of knowledge*, The MIT press
- Arnborg, S. (2006), Robust Bayesianism: Relation to Evidence Theory, *Journal of Advances in Information Fusion*, **1**, 63-74
- Karlsson, A., Johansson, R., Andler, S. F. (2011), Characterization and Empirical Evaluation of Bayesian and Credal Combination Operators, *Journal of Advances in Information Fusion*, **6**, 150-166
- De Campos L. M., Huete, J. F., Moral S., Probability Intervals: a Tool for Uncertain Reasoning, *International Journal of Uncertainty, Fuzziness, and Knowledge-Based Systems*, **2**, 167-196

## See Also

[cComb](#)

## Examples

```
# state space
stateSpace <- c("a", "b", "c")

# lower and upper bounds for probability intervals
c1 <- credal(c(0.1, 0.1, 0.1), c(0.8, 0.8, 0.8), stateSpace)

# single probability function (lower and upper bounds of probability intervals are equal)
c2 <- credal(c(0.1, 0.2, 0.7), c(0.1, 0.2, 0.7), stateSpace)
```

---

credal-class	Class "credal"
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---

## Description

Represents a credal set by a set of extreme points. For more detail see [credal](#).

## Objects from the Class

Objects can be created by [credal](#).

## Slots

**extPoints:** Object of class "matrix". Each row is an extreme point of the credal set.

**Methods**

- [ signature(x="credal", i="ANY", j="ANY"): extract an extreme point
- [<- signature(x="credal", i="ANY", j="ANY", value="ANY"): replace and extreme point
- cComb** signature(x = "credal", y = "credal"): combine two credal sets
- lower** signature(x = "credal", set = "character"): calculate the lower bound for a specific set of states
- lower** signature(x = "credal", set = "missing"): calculate the lower bounds for all singleton states
- upper** signature(x = "credal", set = "character"): calculate the upper bound for a specific set of states
- upper** signature(x = "credal", set = "missing"): calculate the upper bounds for all singleton states
- extPoints** signature(x = "credal"): access method for the slot points
- space** signature(x = "credal"): access method for names of singleton states
- space<-** signature(x = "credal"): replace method for names of singleton states

**Author(s)**

Alexander Karlsson

---

credal-methods

*Methods for Function credal*

---

**Description**

Methods for constructing a credal set. For more detail see [credal](#).

**Methods**

- signature(x = "numeric", y = "missing", z = "character") Construct a credal set based on the lower bounds of probability intervals for states (1 will be the upper bound for all probability intervals)
- signature(x = "numeric", y = "numeric", z = "character") Construct a credal based on probability intervals for states

**Author(s)**

Alexander Karlsson

---

`dComb`*Dempster's Combination Operator*

---

**Description**

Combine evidence in the form of mass functions using Dempster's combination operator.

**Usage**

```
dComb(x, y)
```

**Arguments**

<code>x</code>	single mass function or a list of mass functions
<code>y</code>	single mass function if <code>x</code> is a single mass function, otherwise missing

**Value**

mass function

**Author(s)**

Alexander Karlsson

**References**

Dempster, A. P. (1969), A generalization of Bayesian inference, *Journal of the Royal Statistical Society*, **30**, 205-247

Shafer, G. (1976), *A Mathematical Theory of Evidence* Princeton University Press

**See Also**

[yComb](#), [mComb](#), [cComb](#)

**Examples**

```
# state space
stateSpace <- c("a", "b", "c")

# mass functions
m1 <- mass(list("a"=0.1, "a/b/c"=0.9), stateSpace)
m2 <- mass(list("a"=0.2, "a/b/c"=0.8), stateSpace)

# Dempster's combination
dComb(m1, m2)
# or
dComb(list(m1, m2))
```



---

dComb-methods	<i>Methods for Function dComb</i>
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---

**Description**

Combine mass functions using Dempster's combination operator. For more detail see [dComb](#).

**Methods**

signature(x = "mass", y = "mass") Combine two mass functions using Dempster's combination operator

signature(x = "list", y = "missing") Combine a list of mass functions using Dempster's combination operator

**Author(s)**

Alexander Karlsson

---

disc	<i>Discounting Operator</i>
------	-----------------------------

---

**Description**

Discounts a mass function.

**Usage**

```
disc(x,y)
```

**Arguments**

x	a mass function
y	degree of reliability

**Value**

mass function

**Author(s)**

Alexander Karlsson

**References**

Smets, P. (2000), Data Fusion in the Transferable Belief Model, Proceedings of the Third International Conference on Information Fusion

**Examples**

```
# state space
stateSpace <- c("a", "b", "c")

# mass function
m <- mass(list("a"=0.1, "a/b/c"=0.9), stateSpace)

# source is only 80% reliable
mDisc <- disc(m, 0.8)
```

---

disc-methods

*Methods for Function disc*

---

**Description**

Discount an evidence structure. For more detail see [disc](#)

**Methods**

signature(x = "mass", y = "numeric") Discount a mass function.

---

EvCombRLicense

*License information for EvCombR*

---

**Description**

Displays some license information about EvCombR.

**Usage**

```
EvCombRLicense()
```

**Author(s)**

Alexander Karlsson

**Examples**

```
EvCombRLicense()
```

---

extPoints	<i>Extreme Points of a Credal Set</i>
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---

**Description**

Returns the extreme points of a credal set

**Usage**

```
extPoints(x)
```

**Arguments**

x                    a credal set

**Value**

a matrix where the extreme points are stored by row

**Author(s)**

Alexander Karlsson

**See Also**

[lower](#), [upper](#)

**Examples**

```
# state space
stateSpace <- c("a", "b", "c")

# construct credal set
c <- credal(c(0.1, 0.1, 0.1), c(0.8, 0.8, 0.8), stateSpace)

# obtain extrem points
eMat <- extPoints(c)
```

---

extPoints-methods      *Methods for Function* extPoints

---

**Description**

Returns the set of extreme points of a credal set. For more detail see [extPoints](#).

**Methods**

signature(x = "credal") Returns the set of extreme points

**Author(s)**

Alexander Karlsson

---

focal      *Focal Elements of a Mass Function*

---

**Description**

Returns the set of focal elements of a mass function.

**Usage**

focal(x)

**Arguments**

x      a mass function

**Value**

focal elements of x

**Author(s)**

Alexander Karlsson

**References**

Dempster, A. P. (1969), A generalization of Bayesian inference, *Journal of the Royal Statistical Society*, **30**, 205-247

Shafer, G., (1976), A Mathematical Theory of Evidence Princeton University Press, 1976

**See Also**

[points](#)

**Examples**

```
# state space
stateSpace <- c("a", "b", "c")

# mass functions
m <- mass(list("a"=0.1, "b"=0.1 , "c"=0.4, "a/b/c"=0.4), stateSpace)

# obtain focal elements
focal(m)
```

---

focal-methods	<i>Methods for Function focal</i>
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---

**Description**

Methods for function focal

**Methods**

signature(x = "mass") Access function for slot focal

**Note**

See further [focal](#)

---

focal<-	<i>Replacement Function for Focal Elements</i>
---------	--

---

**Description**

Replaces focal elements of a mass function.

**Usage**

```
focal(x) <- value
```

**Arguments**

x	a mass function
value	new focal elements for the mass function

**Value**

mass function with focal elements replaced.

**Author(s)**

Alexander Karlsson

**References**

Dempster, A. P. (1969), A generalization of Bayesian inference, *Journal of the Royal Statistical Society*, **30**, 205-247

Shafer, G., (1976), *A Mathematical Theory of Evidence* Princeton University Press

**Examples**

```
# state space
stateSpace <- c("a", "b", "c")

# mass functions
m <- mass(list("a"=0.1, "b"=0.1, "c"=0.4, "a/b/c"=0.4), stateSpace)

# replace focal elements
focal(m) <- list("a/b"=1)
```

---

focal<-methods            *Methods for Function focal<-*

---

**Description**

Replacement function for focal elements. For more detail see [focal<-](#)

**Methods**

signature(x = "mass") Replace focal elements

---

lower                    *Lower Bounds Based on Evidence Structure*

---

**Description**

Calculate the lower bounds for a vector of sets

**Usage**

```
lower(x, sets)
```

**Arguments**

x                    credal set or mass function  
sets                vector of sets where each set is represented by state names separated by "/". If sets are missing, lower bounds on singletons are calculated.

**Value**

lower bound of mass or probability for each set in the vector sets or if sets is missing lower bounds on singletons

**Note**

This is equivalent to belief in Dempster-Shafer theory

**Author(s)**

Alexander Karlsson

**References**

Shafer, G., (1976), A Mathematical Theory of Evidence Princeton University Press

Walley, P. (2000), Towards a unified theory of imprecise probability, *International Journal of Approximate Reasoning*, **24**, 125-148

**See Also**

[upper](#)

**Examples**

```
# state space
stateSpace <- c("a", "b", "c")

# mass function
m <- mass(list("a"=0.1, "b"=0.1 ,
              "c"=0.4, "a/b/c"=0.4), stateSpace)

# credal set
c <- credal(c(0.1, 0.1, 0.1),
           c(0.8, 0.8, 0.8), stateSpace)

# calculate lower bounds
lower(m, c("a", "a/b"))
lower(c, c("a", "a/b"))

# lower bounds on singletons
lower(m)
```

---

lower-methods                      *Methods for Function lower*

---

### Description

Calculate lower bounds for a vector of sets with respect to the evidence structure. For more detail see [lower](#)

### Methods

signature(x = "credal", sets = "character") obtain lower bounds for a vector of sets  
signature(x = "credal", sets = "missing") obtain lower bounds for all singleton states  
signature(x = "mass", sets = "character") obtain the belief, or lower bounds, for a vector of sets  
signature(x = "mass", sets = "missing") obtain the belief, or lower bounds, for all singleton states

---

mass                                      *Constructor Function for Mass Functions*

---

### Description

Construct a mass function based on a named list of focal elements or a [massQ-class](#) object. For more information, see the details section.

### Usage

```
mass(x, y)
```

### Arguments

x                                      a named list of focal elements or a [massQ-class](#) object  
y                                      a character vector representing the state space or missing if x is an [massQ](#) object.

### Details

Focal elements are represented by the notation "<sl>/...<sn>" where <sl>...<sn> are any states within the state space (see the examples below). Note that the word "ES" and the symbol "/" are reserved.

### Value

mass function



**Author(s)**

Alexander Karlsson

**References**

Dempster, A. P. (1969), A generalization of Bayesian inference, *Journal of the Royal Statistical Society*, **30**, 205-247

Shafer, G. (1976), A Mathematical Theory of Evidence Princeton University Press

**See Also**

[dComb](#), [mComb](#), [yComb](#)

**Examples**

```
# state space
stateSpace <- c("a", "b", "c")

# construct mass functions
m1 <- mass(list("a"=0.1, "b"=0.1, "c"=0.4, "a/b/c"=0.4), stateSpace)
m2 <- mass(list("a"=0.1, "b"=0.1, "c"=0.1, "a/b"=0.1, "a/c"=0.1,
              "b/c"=0.1, "a/b/c"=0.4), stateSpace)

# apply Yager's combination operator, m12 will be a massQ-object
m12Q <- yComb(m1,m2)

# construct a mass function from an massQ-object
m12 <- mass(m12Q)
```

---

mass-class

Class "mass"

---

**Description**

Represents a mass function by a list of focal elements and corresponding mass. For more detail see [mass](#).

**Objects from the Class**

Objects can be created by [credal](#).

**Slots**

**focal**: a list of focal elements represented by statenames seperated by "/"

**space**: the state space represented by a character vector

## Methods

[ signature(x = "mass", i = "character", j = "missing"): extract focal elements  
 [[ signature(x = "mass", i = "character", j = "missing"): extract a single focal element  
 [<- signature(x="mass", i="character", j="missing", value="ANY"): replace focal elements  
 [[<- signature(x="mass", i="character", j="missing", value="ANY"): replace a single focal element  
**dComb** signature(x = "mass", y = "mass"): combine two mass functions by Dempster's combination  
**focal** signature(x = "mass"): access focal elements  
**focal<-** signature(x = "mass"): replace focal elements  
**lower** signature(x = "mass", set = "character"): calculate the lower bounds for some focal element  
**lower** signature(x = "mass", set = "missing"): calculate the lower bounds for singletons  
**mComb** signature(x = "mass", y = "mass", z = "function"): combine two mass functions by modified Dempster's combination using a prior distribution z  
**mComb** signature(x = "mass", y = "mass", z = "missing"): combine two mass functions by modified Dempster's combination using a uniform prior distribution z  
**pign** signature(x = "mass"): calculate the pignistic transformation for single states  
**relPl** signature(x = "mass"): calculate the relative plausibility for single states  
**space** signature(x = "mass"): access the state space (frame of discernment)  
**space<-** signature(x = "mass"): replace the state space (frame of discernment)  
**upper** signature(x = "mass", set = "character"): calculate the upper bound for some focal element  
**upper** signature(x = "mass", set = "character"): calculate the upper bounds for singletons  
**yComb** signature(x = "mass", y = "mass"): combine two mass functions using Yager's rule  
**disc** signature(x = "mass", y = "numeric"): discount mass function

## Author(s)

Alexander Karlsson

## References

- Dempster, A. P. (1969), A generalization of Bayesian inference, *Journal of the Royal Statistical Society*, **30**, 205-247
- Shafer, G., (1976), A Mathematical Theory of Evidence Princeton University Press
- Yager, R. (1987), On the Dempster-Shafer Framework and New Combination Rules, *Information Sciences* **41**: 93-137.
- Fixsen, D., Mahler, R. P. S. (1997), The modified Dempster-Shafer approach to classification, *IEEE Transactions on Systems, Man and Cybernetics, Part A: Systems and Humans*, **27**, 96-104

---

mass-methods	<i>Methods for Function mass</i>
--------------	----------------------------------

---

**Description**

Methods for constructing a mass function. For more detail see [mass](#)

**Methods**

`signature(x = "list", y = "character")` Construct a mass functions by a named list of focal elements and a given state space

`signature(x = "massQ", y = "missing")` Construct a mass function from a [massQ-class](#) object

**Author(s)**

Alexander Karlsson

---

massQ-class	<i>Class "massQ"</i>
-------------	----------------------

---

**Description**

Class that maintains information about the mass on the empty set. The class is used for Yager's combination operator

**Objects from the Class**

A massQ-object is obtained as a result of Yager's combination operator [yComb](#).

**Slots**

`qEmpty`: mass on the empty set with respect to the previous combination

`focal`: a list of focal elements represented by statenames seperated by "/"

`space`: the state space represented by a character vector

**Extends**

Class "[mass](#)", directly.

**Methods**

All methods inherited from [mass-class](#) and in addition:

**mass** `signature(x = "massQ", y = "missing")`: convert the massQ-object to a mass-object

**Author(s)**

Alexander Karlsson

**References**

Yager, R. (1987), On the Dempster-Shafer Framework and New Combination Rules, *Information Sciences 41*: 93-137.

---

 mComb

---

*Modified Dempster's Combination Operator*


---

**Description**

Combine evidence in the form of mass functions using modified Dempster's combination operator.

**Usage**
 $mComb(x, y, z)$ 
**Arguments**

x	single mass function or a list of mass functions
y	single mass function if x is a single mass function, a prior distribution or missing if x is a list
z	prior distribution if x and y are mass functions, otherwise missing

**Details**

The prior distribution is provided in the form of a list where the names are equivalent to the state space. See the examples.

**Value**

mass function

**Author(s)**

Alexander Karlsson

**References**

Fixsen, D., Mahler, R. P. S. (1997), The modified Dempster-Shafer approach to classification, *IEEE Transactions on Systems, Man and Cybernetics, Part A: Systems and Humans*, **27**, 96-104

**See Also**

[dComb](#), [yComb](#), [cComb](#)

**Examples**

```

# state space
stateSpace <- c("a", "b", "c")

# mass functions
m1 <- mass(list("a"=0.1, "a/b/c"=0.9), stateSpace)
m2 <- mass(list("a"=0.2, "a/b/c"=0.8), stateSpace)

# modified Dempster's combination using the uniform prior
mComb(m1, m2)
# or
mComb(list(m1, m2))

# modified Dempster's combination using a specific prior
mComb(m1, m2, list("a"=0.1, "b"=0.1, "c"=0.8))
# or
mComb(list(m1, m2), list("a"=0.1, "b"=0.1, "c"=0.8))

```

---

mComb-methods

*Methods for Function mComb*


---

**Description**

Combine mass functions using modified Dempster's combination operator. For more detail see [mComb](#).

**Methods**

signature(x = "mass", y = "mass", z = "list") Combine two mass functions using modified Dempster's combination operator and a prior

signature(x = "mass", y = "mass", z = "missing") Combine two mass functions using modified Dempster's combination operator and the uniform prior

signature(x = "list", y = "list", z = "missing") Combine a list of mass functions using modified Dempster's combination operator and a prior

signature(x = "list", y = "missing", z = "missing") Combine a list of mass functions using modified Dempster's combination operator and the uniform prior

---

pign

*Pignistic Transformation*


---

**Description**

The pignistic transformation transforms a mass function into a probability function.

**Usage**

```
pign(x)
```

**Arguments**

x                    a mass function

**Value**

a singleton credal set

**Author(s)**

Alexander Karlsson

**References**

Smets, P. & Kennes, R. (1994), The transferable belief model, *Artificial Intelligence*, **66**, 191-234

**See Also**

[relPl](#)

**Examples**

```
# state space
stateSpace <- c("a", "b", "c")

# mass function
m <- mass(list("a"=0.1, "a/b/c"=0.9), stateSpace)

# obtain a singleton credal set
c <- pign(m)
```

---

pign-methods

*Methods for Function pign*

---

**Description**

The pignistic transformation transform a mass function to probability function. For more detail see [pign](#)

**Methods**

signature(x = "mass") Apply the pignistic transformation on a mass function

---

relPl	<i>Relative Plausibility Transform</i>
-------	--

---

**Description**

The relative plausibility transform transform a mass function to a probability function

**Usage**

```
relPl(x)
```

**Arguments**

x                    a mass function

**Value**

a singleton credal set

**Author(s)**

Alexander Karlsson

**References**

Cobb, B. & Shenoy, P. (2006), On the plausibility transformation for translating belief function models to probability models, *International Journal of Approximate Reasoning*, **42**, 3, 314 - 330

**See Also**

[pign](#)

**Examples**

```
# state space
stateSpace <- c("a", "b", "c")

# mass function
m <- mass(list("a"=0.1, "a/b/c"=0.9), stateSpace)

# obtain a singleton credal set
c <- relPl(m)
```

---

relPl-methods                      *Methods for Function relPl*

---

### Description

The relative plausability transform transforms a mass function to probability function. For more detail see [relPl](#)

### Methods

signature(x = "mass") Apply the relative plausability transform on a mass function

---

space                                      *State Space of and Evidence Structure*

---

### Description

This functions returns the state space of an evidence structure.

### Usage

```
space(x)
```

### Arguments

x                                      mass function or credal set

### Value

a character vector with the names within the state space

### Author(s)

Alexander Karlsson

### Examples

```
# state space
stateSpace <- c("a", "b", "c")

# construct mass function
m <- mass(list("a"=0.1, "b"=0.1 , "c"=0.4, "a/b/c"=0.4), stateSpace)

# obtain state space
space(m)
```



---

space-methods	<i>Methods for Function space</i>
---------------	-----------------------------------

---

**Description**

Returns the state space for an evidence structure. For more detail see [space](#).

**Methods**

`signature(x = "credal")` Returns the state space for a credal set

`signature(x = "mass")` Returns the state space for a mass function

---

space<-	<i>Replacement Function for State Space</i>
---------	---

---

**Description**

Replace the names of the state space

**Usage**

```
space(x) <- value
```

**Arguments**

`x` mass function or credal set

`value` new state space given as a character vector

**Value**

new mass function or credal set with the state space replaced

**Author(s)**

Alexander Karlsson

**See Also**

[focal<-](#)

**Examples**

```
# state space
stateSpace <- c("a", "b", "c")

# construct mass function
m <- mass(list("a"=0.1, "b"=0.1 , "c"=0.4, "a/b/c"=0.4), stateSpace)

# replace state space
space(m) <- c("d", "e", "f")
```

---

space<-methods                    *Methods for Function space<-*

---

**Description**

Replace the state space of an evidence structure. For more details see [space](#).

**Methods**

signature(x = "credal") Replace state space of a credal set  
signature(x = "mass") Replace the state space of a mass function

---

upper                                *Upper Bounds Based on Evidence Structure*

---

**Description**

Calculate the upper bounds for a vector of sets

**Usage**

```
upper(x, sets)
```

**Arguments**

x                                    credal set or mass function  
sets                                 vector of sets where each set is represented by state names separated by "/". If sets are missing, upper bounds on singletons are calculated.

**Value**

upper bound of mass or probability for each set in the vector sets or if sets is missing upper bounds on singletons

**Note**

This is equivalent to Belief in Dempster-Shafer theory

**Author(s)**

Alexander Karlsson

**References**

Shafer, G., (1976), A mathematical theory of evidence, Princeton University Press

Walley, P. (2000), Towards a unified theory of imprecise probability, *International Journal of Approximate Reasoning*, **24**, 125-148

**See Also**

[upper](#)

**Examples**

```
# state space
stateSpace <- c("a", "b", "c")

# mass function
m <- mass(list("a"=0.1, "b"=0.1 ,
              "c"=0.4, "a/b/c"=0.4), stateSpace)

# credal set
c <- credal(c(0.1, 0.1, 0.1),
           c(0.8, 0.8, 0.8), stateSpace)

# calculate upper bounds
upper(m, c("a", "a/b"))
upper(c, c("a", "a/b"))

# upper bounds on singletons
upper(m)
```

---

upper-methods

*Methods for Function upper*

---

**Description**

Calculate lower bounds for a vector of sets with respect to the evidence structure. For more detail see [upper](#)

**Methods**

signature(x = "credal", sets = "character") obtain upper bounds for a vector of sets  
signature(x = "credal", sets = "missing") obtain upper bounds for all singletons  
signature(x = "mass", sets = "character") obtain the plausability, or upper bounds, for a vector of sets  
signature(x = "mass", sets = "missing") obtain the plausability, or upper bounds, for all singletons

yComb

*Yager's Combination Operator***Description**

Combine evidence in the form of mass functions using Yager's combination operator.

**Usage**

```
yComb(x, y)
```

**Arguments**

x                    single mass function or a list of mass functions  
y                    single mass function if x is a single mass function, otherwise missing

**Value**

mass function ([massQ-class](#))

**Note**

Yager's combination operator is quasi-associative and therefore we need to keep track of the mass on the empty set by using the class `massQ`.

**Author(s)**

Alexander Karlsson

**References**

Yager, R. (1987), On the Dempster-Shafer Framework and New Combination Rules, *Information Sciences* 41: 93-137.

**See Also**

[dComb](#), [mComb](#), [cComb](#)

**Examples**

```
# state space
stateSpace <- c("a", "b", "c")

# mass functions
m1 <- mass(list("a"=0.1, "a/b/c"=0.9), stateSpace)
m2 <- mass(list("b"=0.2, "a/b/c"=0.8), stateSpace)

# Yager's combination
yComb(m1, m2)
# or
yComb(list(m1, m2))
```

---

yComb-methods

*Methods for Function yComb*


---

**Description**

Combine mass functions using Yager's combination operator. For more detail see [yComb](#).

**Methods**

signature(x = "mass", y = "mass") Combine two mass functions using Yager's combination operator

signature(x = "list", y = "missing") Combine a list of mass functions using Yager's combination operator

---

[-methods

*Methods for Function [*


---

**Description**

Extract part of evidence structure [

**Methods**

signature(x = "credal", i = "ANY", j="ANY", value="ANY") Extract probabilities

signature(x = "mass", i = "character", j="missing", value="ANY") Extract focal element(s)

**Author(s)**

Alexander Karlsson

**Examples**

```

# construct a state space
stateSpace <- c("a", "b", "c")

# construct credal sets with the given state space
c <- credal(c(0.1, 0.1, 0.1), c(0.8, 0.8, 0.8), stateSpace)

# extract first and second extreme point
c[1:2,]

# mass functions
m <- mass(list("a"=0.1, "b"=0.1 , "c"=0.4, "a/b/c"=0.4), stateSpace)

# extract focal elements
m[c("a","a/b/c")]

```

[&lt;-methods

*Methods for Function* [<-**Description**

Replace part of an evidence structure

**Methods**

```

signature(x="credal", i="ANY", j="ANY", value="ANY") Replace probabilities
signature(x="mass", i="character", j="missing", value="ANY") Replace focal element(s)

```

**Author(s)**

Alexander Karlsson

**Examples**

```

# construct a state space
stateSpace <- c("a", "b", "c")

# construct credal sets with the given state space
c <- credal(c(0.1, 0.1, 0.1), c(0.8, 0.8, 0.8), stateSpace)

# replace first and second extreme point
c[1:2,] <- rbind(c(0.1, 0.1, 0.8), c(0.2, 0.2, 0.6))

# mass function
m <- mass(list("a"=0.1, "b"=0.1 , "c"=0.4, "a/b/c"=0.4), stateSpace)

# switch mass on focal elements "b" and "a/b/c"
temp <- m["b"]
m["b"] <- m["a/b/c"]

```

```
m["a/b/c"] <- temp
```

---

[[-methods                      *Methods for Function* [[

---

### Description

Methods for function [[

### Methods

signature(x="mass", i="character", j="missing") Extract a single focal element from the list of focal elements

### Author(s)

Alexander Karlsson

### Examples

```
# construct a state space
stateSpace <- c("a", "b", "c")

#mass functions
m <- mass(list("a"=0.1, "b"=0.1, "c"=0.4, "a/b/c"=0.4), stateSpace)

# extract focal element
m[["a"]]
```

---

[[<-methods                      *Methods for Function* [[<-

---

### Description

Replace part of an evidence structure

### Methods

signature(x="mass", i="character", j="missing", value="ANY") Replace focal element(s)

### Author(s)

Alexander Karlsson

**Examples**

```
# construct a state space
stateSpace <- c("a", "b", "c")

# mass function
m <- mass(list("a"=0.1, "b"=0.1 , "c"=0.4, "a/b/c"=0.4), stateSpace)

# obtain value only
m[["a"]]
```



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