Package: Compositional (via r-universe)

October 10, 2024

Type Package

Title Compositional Data Analysis

Version 7.1

Date 2024-10-09

Author Michail Tsagris [aut, cre], Giorgos Athineou [aut], Abdulaziz Alenazi [ctb], Christos Adam [ctb]

Maintainer Michail Tsagris <mtsagris@uoc.gr>

Depends R (>= 4.0)

Imports bigstatsr, cluster, doParallel, emplik, energy, foreach, glmnet, graphics, grDevices, quantreg, MASS, Matrix, mda, minpack.lm, mixture, mvhtests, nnet, quadprog, regda, Rfast, Rfast2, Rnanoflann, sn, stats

Suggests bigparallelr, codalm, FlexDir,

Description Regression, classification, contour plots, hypothesis testing and fitting of distributions for compositional data are some of the functions included. We further include functions for percentages (or proportions). The standard textbook for such data is John Aitchison's (1986) `The statistical analysis of compositional data". Relevant papers include: a) Tsagris M.T., Preston S. and Wood A.T.A. (2011). ` A data-based power transformation for compositional data". Fourth International International Workshop on Compositional Data Analysis. doi:10.48550/arXiv.1106.1451> b) Tsagris M. (2014). `The k-NN algorithm for compositional data: a revised approach with and without zero values present". Journal of Data Science, 12(3): 519--534. <doi:10.6339/JDS.201407_12(3).0008>. c) Tsagris M. (2015). ` A novel, divergence based, regression for compositional data". Proceedings of the 28th Panhellenic Statistics Conference, 15-18 April 2015, Athens, Greece, 430--444. <doi:10.48550/arXiv.1511.07600>. d) Tsagris M. (2015). `Regression analysis with compositional data containing zero values". Chilean Journal of Statistics, 6(2): 47--57. <https://soche.cl/chjs/volumes/06/02/Tsagris(2015).pdf>.e) 2 Contents

Tsagris M., Preston S. and Wood A.T.A. (2016). `Improved	
supervised classification for compositional data using the	
alpha-transformation". Journal of Classification, 33(2):	
243261. <doi:10.1007 s00357-016-9207-5="">. f) Tsagris M.,</doi:10.1007>	
Preston S. and Wood A.T.A. (2017). ``Nonparametric hypothesis	
testing for equality of means on the simplex". Journal of	
Statistical Computation and Simulation, 87(2): 406422.	
<doi:10.1080 00949655.2016.1216554="">. g) Tsagris M. and Stewart</doi:10.1080>	
C. (2018). ``A Dirichlet regression model for compositional data	
with zeros". Lobachevskii Journal of Mathematics, 39(3):	
398412. <doi:10.1134 s1995080218030198="">. h) Alenazi A.</doi:10.1134>	
(2019). ``Regression for compositional data with compositional	
data as predictor variables with or without zero values".	
Journal of Data Science, 17(1): 219238.	
doi:10.6339/JDS.201901_17(1).0010 , i) Tsagris M. and Stewart	
C. (2020). ``A folded model for compositional data analysis".	
Australian and New Zealand Journal of Statistics, 62(2):	
249277. <doi:10.1111 anzs.12289="">. j) Alenazi A. (2021).</doi:10.1111>	
Alenazi, A. (2023). ``A review of compositional data analysis	
and recent advances". Communications in StatisticsTheory and	
Methods, 52(16): 55355567.	
doi:10.1080/03610926.2021.2014890 >. k) Alenazi A.A. (2022).	
``f-divergence regression models for compositional data".	
Pakistan Journal of Statistics and Operation Research, 18(4):	
867882. <doi:10.18187 pjsor.v18i4.3969="">. 1) Tsagris M. and</doi:10.18187>	
Stewart C. (2022). ``A Review of Flexible Transformations for Modeling Compositional Data". In Advances and Innovations in	
Statistics and Data Science, pp. 225234.	
Statistics and Data Science, pp. 223234. <doi:10.1007 978-3-031-08329-7_10="">. m) Tsagris M., Alenazi A.</doi:10.1007>	
and Stewart C. (2023). ``Flexible non-parametric regression	
models for compositional response data with zeros". Statistics	
and Computing, 33(106). <doi:10.1007 s11222-023-10277-5="">. n)</doi:10.1007>	
Tsagris. M. (2024). `Constrained least squares	
simplicial-simplicial regression".	
<doi:10.48550 arxiv.2403.19835="">.</doi:10.48550>	
License GPL (>= 2)	
NeedsCompilation no	
Repository CRAN	
Date/Publication 2024-10-09 09:50:02 UTC	
Contents	
Compositional-package	. 7
Aitchison's test for two mean vectors and/or covariance matrices	
All pairwise additive log-ratio transformations	
Alpha-generalised correlations between two compositional datasets	
ANOVA for the log-contrast GLM versus the uncostrained GLM	

Contents 3

ANOVA for the log-contrast regression versus the uncostrained linear regression	13
Beta regression	14
Column-wise MLE of some univariate distributions	15
Contour plot of mixtures of Dirichlet distributions in S^2	16
Contour plot of the alpha multivariate normal in S^2	17
Contour plot of the alpha-folded model in S^2	18
Contour plot of the Dirichlet distribution in S^2	20
Contour plot of the Flexible Dirichlet distribution in S^2	21
Contour plot of the Gaussian mixture model in S^2	22
Contour plot of the generalised Dirichlet distribution in S^2	23
Contour plot of the kernel density estimate in S^2	24
Contour plot of the normal distribution in S^2	26
Contour plot of the skew skew-normal distribution in S^2	27
Contour plot of the t distribution in S^2	28
Cross validation for some compositional regression models	29
Cross validation for the alpha-k-NN regression with compositional predictor variables	30
Cross validation for the alpha-k-NN regression with compositional response data	32
Cross validation for the alpha-kernel regression with compositional response data	33
Cross validation for the kernel regression with Euclidean response data	35
Cross validation for the regularised and flexible discriminant analysis with composi-	
tional data using the alpha-transformation	36
Cross validation for the ridge regression	38
Cross validation for the ridge regression with compositional data as predictor using the	
alpha-transformation	40
Cross validation for the TFLR model	42
Cross-validation for LASSO with compositional predictors using the alpha-transformation	43
Cross-validation for the alpha-SCLS model	45
Cross-validation for the alpha-TFLR model	46
Cross-validation for the Dirichlet discriminant analysis	47
Cross-validation for the LASSO Kullback-Leibler divergence based regression	48
Cross-validation for the LASSO log-ratio regression with compositional response	50
Cross-validation for the naive Bayes classifiers for compositional data	51
Cross-validation for the naive Bayes classifiers for compositional data using the alpha-	
transformation	52
Cross-validation for the SCLS model	54
Cross-validation for the SCRQ model	55
Density of compositional data from Gaussian mixture models	56
Density of the Flexible Dirichlet distribution	58
Density of the folded normal distribution	59
Density values of a Dirichlet distribution	60
Density values of a generalised Dirichlet distribution	61
Density values of a mixture of Dirichlet distributions	62
Dirichlet discriminant analysis	63
Dirichlet random values simulation	64
Dirichlet regression	65
Distance based regression models for proportions	67
Divergence based regression for compositional data	69

Contents Contents

Divergence based regression for compositional data with compositional data in the co-	
variates side using the alpha-transformation	71
Divergence matrix of compositional data	73
Energy test of equality of distributions using the alpha-transformation	74
Estimating location and scatter parameters for compositional data	75
Estimation of the probability left outside the simplex when using the alpha-transformation	77
Estimation of the value of alpha in the folded model	
Estimation of the value of alpha via the profile log-likelihood	79
Fast estimation of the value of alpha	80
Gaussian mixture models for compositional data	
Gaussian mixture models for compositional data using the alpha-transformation	
Generalised Dirichlet random values simulation	
Generate random folds for cross-validation	
Greenacre's power transformation	
Helper Frechet mean for compositional data	
Helper functions for the Kullback-Leibler regression	
Hypothesis testing for two or more compositional mean vectors	
ICE plot for projection pursuit regression with compositional predictor variables	94
ICE plot for the alpha-k-NN regression	95
ICE plot for the alpha-kernel regression	
ICE plot for univariate kernel regression	
Inverse of the alpha-transformation	
Kernel regression with a numerical response vector or matrix	
Kullback-Leibler divergence and Bhattacharyya distance between two Dirichlet distri-	
butions	101
LASSO Kullback-Leibler divergence based regression	102
LASSO log-ratio regression with compositional response	104
LASSO with compositional predictors using the alpha-transformation	105
Log-contrast GLMs with compositional predictor variables	107
Log-contrast logistic or Poisson regression with with multiple compositional predictors .	108
Log-contrast quantile regression with compositional predictor variables	
Log-contrast quantile regression with with multiple compositional predictors	
Log-contrast regression with compositional predictor variables	113
Log-contrast regression with multiple compositional predictors	114
Log-likelihood ratio test for a Dirichlet mean vector	116
Log-likelihood ratio test for a symmetric Dirichlet distribution	117
Minimized Kullback-Leibler divergence between Dirichlet and logistic normal	118
Mixture model selection via BIC	119
Mixture model selection with the alpha-transformation using BIC	120
MLE for the multivariate t distribution	122
MLE of distributions defined in the $(0, 1)$ interval	123
MLE of the Dirichlet distribution	125
MLE of the Dirichlet distribution via Newton-Rapshon	126
MLE of the folded model for a given value of alpha	127
MLE of the zero adjusted Dirichlet distribution	
Multivariate kernel density estimation	130
Multivariate kernel density estimation for compositional data	
Multivariate linear regression	132

Contents 5

Multivariate normal random values simulation on the simplex
Multivariate or univariate regression with compositional data in the covariates side using
the alpha-transformation
Multivariate regression with compositional data
Multivariate skew normal random values simulation on the simplex
Multivariate t random values simulation on the simplex
Naive Bayes classifiers for compositional data
Naive Bayes classifiers for compositional data using the alpha-transformation 142
Non linear least squares regression for compositional data
Non-parametric zero replacement strategies
Permutation linear independence test in the SCLS model
Permutation linear independence test in the TFLR model
Permutation test for the matrix of coefficients in the SCLS model
Permutation test for the matrix of coefficients in the TFLR model
Perturbation operation
Plot of the LASSO coefficients
Power operation
Principal component analysis
Principal component analysis using the alpha-transformation
Principal component generalised linear models
Principal coordinate analysis using the alpha-distance
Principal coordinate analysis using the Jensen-Shannon divergence
Projection pursuit regression for compositional data
Projection pursuit regression with compositional predictor variables
Projection pursuit regression with compositional predictor variables using the alpha-
transformation
Projections based test for distributional equality of two groups
Proportionality correlation coefficient matrix
Quasi binomial regression for proportions
Random values generation from some univariate distributions defined on the (0,1) interval 167
Read a file as a Filebacked Big Matrix
Regression with compositional data using the alpha-transformation
Regularised and flexible discriminant analysis for compositional data using the alpha-
transformation
Ridge regression
Ridge regression plot
$Ridge\ regression\ with\ compositional\ data\ in\ the\ covariates\ side\ using\ the\ alpha-transformation\ 175$
Ridge regression with the alpha-transformation plot
Simplicial constrained median regression for compositional responses and predictors model
Simulation of compositional data from Gaussian mixture models
Simulation of compositional data from mixtures of Dirichlet distributions
Simulation of compositional data from the Flexible Dirichlet distribution
Simulation of compositional data from the folded normal distribution
Spatial median regression
Ternary diagram
Ternary diagram of regression models

6 Contents

Ternary diagram with confidence region for the mean Ternary diagram with the coefficients of the simplicial-simplicial regression models 190 The additive log-ratio transformation and its inverse 191 The alpha-distance 192 The alpha-IT transformation 193 The alpha-H-distance 195 The alpha-K-NN regression for compositional response data 196 The alpha-K-NN regression with compositional predictor variables 197 The alpha-K-NN regression with compositional predictor variables 197 The alpha-SCLS model 198 The alpha-SCLS model 199 The alpha-TFLR model 200 The alpha-TFLR model 201 The alpha-TFLR model 202 The Box-Cox transformation 202 The Box-Cox transformation applied to ratios of components 204 The FeSOV-distance 205 The Folded power transformation applied to ratios of components 206 The Frechet mean for compositional data 207 The k-narest neighbours using the alpha-distance 208 The k-NN algorithm for compositional data 211 The multiplicative log-ratio transformation and its inverse 213 The pivot coordinate transformation and its inverse 214 The SCLS model 215 The SCLS model with multiple compositional predictors 216 The TFLR model with multiple compositional predictors 217 The transformation-free linear regression (TFLR) for compositional responses and predictors 218 Total variability 229 Tuning of the alpha-generalised correlations between two compositional datasets 221 Tuning of the bandwidth h of the kernel using the maximum likelihood cross validation 222 Tuning of the brojection pursuit regression for compositional predictor variables 223 Tuning of the projection pursuit regression with compositional predictor variables using the alpha-transformation 224 Tuning of the projection pursuit regression with compositional predictor variables using the alpha-transformation 225 Tuning of the projection pursuit regression with compositional data using the alpha-transformation 226 Tuning the principal components with GLMs 237 Tuning the principal components with GLMs 238 Tuning the val	Ternary diagram with confidence region for the matrix of coefficients of the SCLS or	
Ternary diagram with the coefficients of the simplicial-simplicial regression models 190 The additive log-ratio transformation and its inverse 191 The alpha-distance 192 The alpha-IT transformation 193 The alpha-IT transformation 193 The alpha-IT distance 195 The alpha-IT distance 195 The alpha-K-NN regression for compositional response data 196 The alpha-k-NN regression with compositional response data 199 The alpha-kernel regression with compositional response data 199 The alpha-Kernel regression with compositional response data 199 The alpha-SCLS model 200 The alpha-TFLR model 200 The alpha-TFLR model 200 The Box-Cox transformation 200 The Box-Cox transformation 200 The Box-Cox transformation 200 The Ferchet mean for compositional data 200 The Helmert sub-matrix 200 The Helmert sub-matrix 200 The k-nearest neighbours using the alpha-distance 200 The k-NN algorithm for compositional data 211 The multiplicative log-ratio transformation and its inverse 213 The pivot coordinate transformation and its inverse 214 The SCLS model 215 The SCLS model 215 The TFLR model with multiple compositional predictors 216 The TFLR model with multiple compositional predictors 216 Total variability 217 Total variability 217 Total variability 220 Tuning of the alpha-generalised correlations between two compositional datasets 220 Tuning of the bandwidth h of the kernel using the maximum likelihood cross validation 222 Tuning of the brojection pursuit regression for compositional data with compositional data in the covariates side using the alpha-transformation 224 Tuning of the projection pursuit regression with compositional predictor variables using the alpha-transformation 224 Tuning of the projection pursuit regression with compositional predictor variables using the alpha-transformation 224 Tuning of the projection pursuit regression with compositional predictor variables using the alpha-transformation 224 Tuning of the projection pursuit regression with compositional predictor variables using the alpha-transformation 230 Tuni	the TFLR model	
The additive log-ratio transformation and its inverse	Ternary diagram with confidence region for the mean	189
The additive log-ratio transformation and its inverse	Ternary diagram with the coefficients of the simplicial-simplicial regression models	190
The alpha-distance		
The alpha-IT transformation		
The alpha-IT-distance		
The alpha-k-NN regression for compositional response data		
The alpha-k-NN regression with compositional predictor variables 197 The alpha-kernel regression with compositional response data 199 The alpha-SCLS model 200 The alpha-SCLS model 201 The alpha-TFLR model 201 The alpha-transformation 201 The Box-Cox transformation applied to ratios of components 204 The ESOV-distance 205 The folded power transformation 206 The Frechet mean for compositional data 207 The Helmert sub-matrix 208 The k-nearest neighbours using the alpha-distance 209 The k-NN algorithm for compositional data 211 The multiplicative log-ratio transformation and its inverse 213 The pivot coordinate transformation and its inverse 214 The SCLS model 215 The SCLS model with multiple compositional predictors 216 The TFLR model with multiple compositional predictors 216 The transformation-free linear regression (TFLR) for compositional atasets 220 Total variability 220 Tuning of the alpha-generalised correlations between two compositional datasets 221 Tuning of the bandwidth h of the kernel using the maximum likelihood cross validation 222 Tuning of the bandwidth for compositional data 225 Tuning of the Projection pursuit regression for compositional data with compositional data 225 Tuning of the projection pursuit regression with compositional predictor variables 229 Tuning of the projection pursuit regression with compositional predictor variables using the alpha-transformation 230 Tuning the projection pursuit regression with compositional predictor variables using the alpha-transformation 230 Tuning the projection pursuit regression with compositional data using the alpha-transformation 230 Tuning the projection pursuit regression with compositional data using the alpha-transformation 235 Tuning the value of alpha in the alpha-regression 235 Tuning the value of alpha in the alpha-regression 235 Tuning the value of alpha in the alpha-regression 235 Tuning the value of alpha in the alpha-regression 235 Tuning the value of alpha in the alpha-regression 235		
The alpha-kernel regression with compositional response data 199 The alpha-SCLS model 200 The alpha-TFLR model 201 The alpha-TFLR model 201 The alpha-TFLR model 201 The Box-Cox transformation 301 The Box-Cox transformation applied to ratios of components 202 The ESOV-distance 205 The folded power transformation 206 The Frechet mean for compositional data 207 The Helmert sub-matrix 208 The k-nearest neighbours using the alpha-distance 208 The k-NN algorithm for compositional data 211 The multiplicative log-ratio transformation and its inverse 213 The pivot coordinate transformation and its inverse 214 The SCLS model 215 The SCLS model 215 The TFLR model with multiple compositional predictors 217 The transformation-free linear regression (TFLR) for compositional responses and predictors 217 The transformation-free linear regression (TFLR) for compositional datasets 219 Tuning of the alpha-generalised correlations between two compositional datasets 221 Tuning of the bandwidth h of the kernel using the maximum likelihood cross validation 222 Tuning of the bandwidth for compositional data 225 Tuning of the Projection pursuit regression for compositional data with compositional data in the covariates side using the alpha-transformation 224 Tuning of the projection pursuit regression with compositional predictor variables 229 Tuning of the projection pursuit regression with compositional predictor variables using the alpha-transformation 230 Tuning the number of PCs in the PCR with compositional data using the alpha-transformation 233 Tuning the value of alpha in the alpha-regression 235 Two-sample test of high-dimensional means for compositional data 33 Unconstrained GLMs with compositional predictor variables 238		
The alpha-SCLS model		
The alpha-transformation		
The alpha-transformation		
The Box-Cox transformation applied to ratios of components	•	
The ESOV-distance		
The folded power transformation		
The Frechet mean for compositional data 207 The Helmert sub-matrix		
The Helmert sub-matrix	•	
The k-nearest neighbours using the alpha-distance		
The k-NN algorithm for compositional data		
The multiplicative log-ratio transformation and its inverse		
The pivot coordinate transformation and its inverse		
The SCLS model	The multiplicative log-ratio transformation and its inverse	213
The SCLS model with multiple compositional predictors	The pivot coordinate transformation and its inverse	214
The TFLR model with multiple compositional predictors	The SCLS model	215
The transformation-free linear regression (TFLR) for compositional responses and predictors		
The transformation-free linear regression (TFLR) for compositional responses and predictors	· · · · · · · · · · · · · · · · · · ·	
dictors		
Total variability		219
Tuning of the alpha-generalised correlations between two compositional datasets		
Tuning of the bandwidth h of the kernel using the maximum likelihood cross validation . 222 Tuning of the divergence based regression for compositional data with compositional data in the covariates side using the alpha-transformation		
Tuning of the divergence based regression for compositional data with compositional data in the covariates side using the alpha-transformation		
data in the covariates side using the alpha-transformation		
Tuning of the k-NN algorithm for compositional data		224
Tuning of the projection pursuit regression for compositional data		
Tuning of the projection pursuit regression with compositional predictor variables		
Tuning of the projection pursuit regression with compositional predictor variables using the alpha-transformation	• • • • •	
the alpha-transformation		229
Tuning the number of PCs in the PCR with compositional data using the alpha-transformation 2. Tuning the principal components with GLMs		220
Tuning the principal components with GLMs	•	
Tuning the value of alpha in the alpha-regression		
Two-sample test of high-dimensional means for compositional data		
Unconstrained GLMs with compositional predictor variables	• • •	
	Unconstrained linear regression with compositional predictor variables	
Unconstrained linear regression with multiple compositional predictors		
Unconstrained logistic or Poisson regression with multiple compositional predictors 242	Unconstrained logistic or Poisson regression with multiple compositional predictors	242
Unconstrained quantile regression with compositional predictor variables	Unconstrained quantile regression with compositional predictor variables	244
Unconstrained quantile regression with multiple compositional predictors	Unconstrained quantile regression with multiple compositional predictors	245

Compositional-packag	re
----------------------	----

	Unit-Weibull regression models for proportions	
Index		250
Compo	ositional-package Compositional Data Analysis	

Description

A Collection of Functions for Compositional Data Analysis.

Details

Package: Compositional Type: Package Version: 7.1 Date: 2024-10-09

License: GPL-2

Maintainers

Michail Tsagris <mtsagris@uoc.gr>

Note

Acknowledgments:

Michail Tsagris would like to express his acknowledgments to Professor Andy Wood and Professor Simon Preston from the university of Nottingham for being his supervisors during his PhD in compositional data analysis.

We would also like to express our acknowledgments to Profesor Kurt Hornik (and also the rest of the R core team) for his help with this package.

Manos Papadakis, undergraduate student in the department of computer science, university of Crete, is also acknowledged for his programming tips.

Ermanno Affuso from the university of South Alabama suggested that I have a default value in the function mkde.

Van Thang Hoang from Hasselt university spotted a bug in the function js.compreg.

Claudia Wehrhahn Cortes spotted a bug in the function diri.reg.

Philipp Kynast from Bruker Daltonik GmbH found a mistake in the function mkde which is now fixed.

Jasmine Heyse from the university of Ghent spotted a bug in the function kl.compreg which is now fixed.

Magne Neby suggested to add names in the covariance matrix of the divergence based regression models.

John Barry from the Centre for Environment, Fisheries, and Aquaculture Science (UK) suggested that I should add more explanation in the function diri.est. I hope it is clearer now.

Charlotte Fabri and Laura Byrne spotted a possible problem in the function zadr.

Levi Bankston found a bug in the bootstrap version of the function kl.compreg.

Sucharitha Dodamgodage suggested to add an extra case in the function dirimean.test.

Loic Mangnier found a bug in the function lc.glm which is now fixed and also became faster.

Ravi Varadhan found a bug in diri.reg and he is acknowledged for that.

Author(s)

Michail Tsagris <mtsagris@uoc.gr>, Giorgos Athineou <gioathineou@gmail.com>, Abdulaziz Alenazi <a.alenazi@nbu.edu.sa> and Christos Adam <pada4m4@gmail.com>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

Aitchison's test for two mean vectors and/or covariance matrices

Aitchison's test for two mean vectors and/or covariance matrices

Description

Aitchison's test for two mean vectors and/or covariance matrices.

Usage

```
ait.test(x1, x2, type = 1, alpha = 0.05)
```

Arguments

x1	A matrix containing the compositional data of the first sample. Zeros are not allowed.
x2	A matrix containing the compositional data of the second sample. Zeros are not allowed.
type	The type of hypothesis test to perform. Type=1 refers to testing the equality of the mean vectors and the covariance matrices. Type=2 refers to testing the equality of the covariance matrices. Type=2 refers to testing the equality of the mean vectors.
alpha	The significance level, set to 0.05 by default.

Details

The test is described in Aitchison (2003). See the references for more information.

Value

A vector with the test statistic, the p-value, the critical value and the degrees of freedom of the chi-square distribution.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

John Aitchison (2003). The Statistical Analysis of Compositional Data, p. 153-157. Blackburn Press.

See Also

```
comp.test
```

Examples

```
x1 <- as.matrix(iris[1:50, 1:4])
x1 <- x1 / rowSums(x1)
x2 <- as.matrix(iris[51:100, 1:4])
x2 <- x2 / rowSums(x2)
ait.test(x1, x2, type = 1)
ait.test(x1, x2, type = 2)
ait.test(x1, x2, type = 3)</pre>
```

```
All pairwise additive log-ratio transformations

All pairwise additive log-ratio transformations
```

Description

All pairwise additive log-ratio transformations.

Usage

```
alr.all(x)
```

Arguments

x A numerical matrix with the compositional data.

Details

The additive log-ratio transformation with the first component being the commn divisor is applied. Then all the other pairwise log-ratios are computed and added next to each column. For example, divide by the first component, then divide by the second component and so on. This means that no zeros are allowed.

Value

A matrix with all pairwise alr transformed data.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
alr, alfa
```

Examples

```
x <- as.matrix(iris[, 2:4])
x <- x / rowSums(x)
y <- alr.all(x)</pre>
```

Alpha-generalised correlations between two compositional datasets α -generalised correlations between two compositional datasets

Description

 α -generalised correlations between two compositional datasets.

Usage

```
acor(y, x, a, type = "dcor")
```

Arguments

у	A matrix with the compositional data.
x	A matrix with the compositional data.
a	The value of the power transformation, it has to be between -1 and 1. If zero values are present it has to be greater than 0. If $\alpha=0$ the isometric log-ratio transformation is applied. If more than one values are supplied the distance or canonical correlation are computed for all values.
type	The type of correlation to compute, the distance correlation ("edist"), the canonical correlation ("cancor") or "both".

Details

The α -transformation is applied to each composition and then the distance correlation or the canonical correlation is computed. If one value of α is supplied the type="cancor" will return all eigenvalues. If more than one values of α are provided then the first eigenvalue only will be returned.

Value

A vector or a matrix depending on the length of the values of α and the type of the correlation to be computed.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

G.J. Szekely, M.L. Rizzo and N. K. Bakirov (2007). Measuring and Testing Independence by Correlation of Distances. Annals of Statistics, 35(6): 2769-2794.

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. https://arxiv.org/pdf/1106.1451.pdf

See Also

```
acor.tune, aeqdist.etest, alfa, alfa.profile
```

```
y <- rdiri(30, runif(3) )
x <- rdiri(30, runif(4) )
acor(y, x, a = 0.4)</pre>
```

ANOVA for the log-contrast GLM versus the uncostrained GLM $ANOVA \ for \ the \ log-contrast \ GLM \ versus \ the \ uncostrained \ GLM$

Description

ANOVA for the log-contrast GLM versus the uncostrained GLM.

Usage

```
lcglm.aov(mod0, mod1)
```

Arguments

mod0 The log-contrast GLM. The object returned by lc.glm.

mod1 The unconstrained GLM. The object returned by ulc.glm.

Details

A chi-square test is performed to test the zero-to-sum constraints of the regression coefficients.

Value

A vector with two values, the chi-square test statistic and its associated p-value.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

See Also

```
lc.glm, ulc.glm
```

```
y <- rbinom(150, 1, 0.5)
x <- as.matrix(iris[, 2:4])
x <- x / rowSums(x)
mod0 <- lc.glm(y, x)
mod1 <- ulc.glm(y, x)
lcglm.aov(mod0, mod1)</pre>
```

 $\ensuremath{\mathsf{ANOVA}}$ for the log-contrast regression versus the uncostrained linear regression

ANOVA for the log-contrast regression versus the uncostrained linear regression

Description

ANOVA for the log-contrast regression versus the uncostrained linear regression.

Usage

```
lcreg.aov(mod0, mod1)
```

Arguments

mod0	The log-contrast regression model. The object returned by lc.reg.
mod1	The unconstrained linear regression model. The object returned by ulc.reg.

Details

An F-test is performed to test the zero-to-sum constraints of the regression coefficients.

Value

A vector with two values, the F test statistic and its associated p-value.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

See Also

```
lc.reg, ulc.reg, alfa.pcr, alfa.knn.reg
```

```
y <- iris[, 1]
x <- as.matrix(iris[, 2:4])
x <- x / rowSums(x)
mod0 <- lc.reg(y, x)
mod1 <- ulc.reg(y, x)
lcreg.aov(mod0, mod1)</pre>
```

14 Beta regression

Beta regression Beta regression

Description

Beta regression.

Usage

```
beta.reg(y, x, xnew = NULL)
```

Arguments

У	The response variable. It must be a numerical vector with proportions excluding $\boldsymbol{0}$ and $\boldsymbol{1}$.
х	The indendent variable(s). It can be a vector, a matrix or a dataframe with continuous only variables, a data frame with mixed or only categorical variables.
xnew	If you have new values for the predictor variables (dataset) whose response values you want to predict insert them here.

Details

Beta regression is fitted.

Value

A list including:

phi The estimated precision parameter.

info A matrix with the estimated regression parameters, their standard errors, Wald

statistics and associated p-values.

loglik The log-likelihood of the regression model. est The estimated values if xnew is not NULL.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Ferrari S.L.P. and Cribari-Neto F. (2004). Beta Regression for Modelling Rates and Proportions. Journal of Applied Statistics, 31(7): 799-815.

See Also

```
beta.est, propreg, diri.reg
```

Examples

```
y <- rbeta(300, 3, 5)
x <- matrix( rnorm(300 * 2), ncol = 2)
beta.reg(y, x)</pre>
```

Column-wise MLE of some univariate distributions ${\it Column-wise \ MLE \ of some \ univariate \ distributions}$

Description

Column-wise MLE of some univariate distributions.

Usage

```
colbeta.est(x, tol = 1e-07, maxiters = 100, parallel = FALSE)
collogitnorm.est(x)
colunitweibull.est(x, tol = 1e-07, maxiters = 100, parallel = FALSE)
colzilogitnorm.est(x)
```

Arguments

х	A numerical matrix with data. Each column refers to a different vector of observations of the same distribution. The values must by percentages, exluding 0 and 1,
tol	The tolerance value to terminate the Newton-Fisher algorithm.
maxiters	The maximum number of iterations to implement.
parallel	Do you want to calculations to take place in parallel? The default value is FALSE

Details

For each column, the same distribution is fitted and its parameters and log-likelihood are computed.

Value

A matrix with two, three or four columns. The first one, two or three columns contain the parameter(s) of the distribution, while the last column contains the relevant log-likelihood.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

- N.L. Johnson, S. Kotz & N. Balakrishnan (1994). Continuous Univariate Distributions, Volume 1 (2nd Edition).
- N.L. Johnson, S. Kotz & N. Balakrishnan (1970). Distributions in statistics: continuous univariate distributions, Volume 2.
- J. Mazucheli, A. F. B. Menezes, L. B. Fernandes, R. P. de Oliveira & M. E. Ghitany (2020). The unit-Weibull distribution as an alternative to the Kumaraswamy distribution for the modeling of quantiles conditional on covariates. Journal of Applied Statistics, DOI:10.1080/02664763.2019.1657813.

See Also

```
beta.est
```

Examples

```
x <- matrix( rbeta(200, 3, 4), ncol = 4 )
a <- colbeta.est(x)</pre>
```

Contour plot of mixtures of Dirichlet distributions in S^2 Contour plot of mixtures of Dirichlet distributions in S^2

Description

Contour plot of mixtures of Dirichlet distributions in S^2 .

Usage

```
mixdiri.contour(a, prob, n = 100, x = NULL, cont.line = FALSE)
```

Arguments

a	A matrix where each row contains the parameters of each Dirichlet disctribution.
prob	A vector with the mixing probabilities.
n	The number of grid points to consider over which the density is calculated.
x	This is either NULL (no data) or contains a 3 column matrix with compositional data.
cont.line	Do you want the contour lines to appear? If yes, set this TRUE.

Details

The user can plot only the contour lines of a Dirichlet with a given vector of parameters, or can also add the relevant data should he/she wish to.

Value

A ternary diagram with the points and the Dirichlet contour lines.

Author(s)

Michail Tsagris and Christos Adam.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Christos Adam <pada4m4@gmail.com>.

References

Ng Kai Wang, Guo-Liang Tian and Man-Lai Tang (2011). Dirichlet and related distributions: Theory, methods and applications. John Wiley & Sons.

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
diri.contour, gendiri.contour, compnorm.contour,comp.kerncontour, mix.compnorm.contour,diri.nr,
```

Examples

```
a <- matrix( c(12, 30, 45, 32, 50, 16), byrow = TRUE,ncol = 3) prob <- c(0.5, 0.5) mixdiri.contour(a, prob)
```

Contour plot of the alpha multivariate normal in S^2 Contour plot of the α multivariate normal in S^2

Description

Contour plot of the α multivariate normal in S^2 .

Usage

```
alfa.contour(m, s, a, n = 100, x = NULL, cont.line = FALSE)
```

Arguments

m	The mean vector of the α multivariate normal model.
S	The covariance matrix of the α multivariate normal model.
а	The value of a for the α -transformation.
n	The number of grid points to consider over which the density is calculated.
X	This is either NULL (no data) or contains a 3 column matrix with compositional data.
cont.line	Do you want the contour lines to appear? If yes, set this TRUE.

Details

The α -transformation is applied to the compositional data and then for a grid of points within the 2-dimensional simplex, the density of the α multivariate normal is calculated and the contours are plotted.

Value

The contour plot of the α multivariate normal appears.

Author(s)

Michail Tsagris and Christos Adam.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Christos Adam <pada4m4@gmail.com>.

References

Tsagris M. and Stewart C. (2022). A Review of Flexible Transformations for Modeling Compositional Data. In Advances and Innovations in Statistics and Data Science, pp. 225–234. https://link.springer.com/chapter/10.103-031-08329-7_10

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. https://arxiv.org/pdf/1106.1451.pdf

See Also

```
folded.contour, compnorm.contour, diri.contour, mix.compnorm.contour, bivt.contour,
skewnorm.contour
```

Examples

```
x <- as.matrix(iris[, 1:3])
x <- x / rowSums(x)
a <- a.est(x)$best
m <- colMeans(alfa(x, a)$aff)
s <- cov(alfa(x, a)$aff)
alfa.contour(m, s, a)</pre>
```

Contour plot of the alpha-folded model in S^2 ${\it Contour\ plot\ of\ the\ } \alpha\mbox{-}folded\ model\ in\ S^2$

Description

Contour plot of the α -folded model in S^2 .

Usage

```
folded.contour(mu, su, p, a, n = 100, x = NULL, cont.line = FALSE)
```

Arguments

mu	The mean vector of the folded model.
su	The covariance matrix of the folded model.
p	The probability inside the simplex of the folded model.
a	The value of a for the α -transformation.
n	The number of grid points to consider over which the density is calculated.
x	This is either NULL (no data) or contains a 3 column matrix with compositional data.
cont.line	Do you want the contour lines to appear? If yes, set this TRUE.

Details

The α -transformation is applied to the compositional data and then for a grid of points within the 2-dimensional simplex the folded model's density is calculated and the contours are plotted.

Value

The contour plot of the folded model appears.

Author(s)

Michail Tsagris and Christos Adam.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Christos Adam <pada4m4@gmail.com>.

References

Tsagris M. and Stewart C. (2022). A Review of Flexible Transformations for Modeling Compositional Data. In Advances and Innovations in Statistics and Data Science, pp. 225–234. https://link.springer.com/chapter/10.103-031-08329-7_10

Tsagris M. and Stewart C. (2020). A folded model for compositional data analysis. Australian and New Zealand Journal of Statistics, 62(2): 249-277. https://arxiv.org/pdf/1802.07330.pdf

See Also

```
alfa.contour, compnorm.contour, diri.contour, mix.compnorm.contour, bivt.contour, skewnorm.contour
```

```
x <- as.matrix(iris[, 1:3])
x <- x / rowSums(x)
a <- a.est(x)$best
mod <- alpha.mle(x, a)
folded.contour(mod$mu, mod$su, mod$p, a)</pre>
```

Contour plot of the Dirichlet distribution in S^2 Contour plot of the Dirichlet distribution in S^2

Description

Contour plot of the Dirichlet distribution in S^2 .

Usage

```
diri.contour(a, n = 100, x = NULL, cont.line = FALSE)
```

Arguments

cont.line	Do you want the contour lines to appear? If yes, set this TRUE.
X	This is either NULL (no data) or contains a 3 column matrix with compositional data.
n	The number of grid points to consider over which the density is calculated.
a	A vector with three elements corresponding to the 3 (estimated) parameters.

Details

The user can plot only the contour lines of a Dirichlet with a given vector of parameters, or can also add the relevant data should he/she wish to.

Value

A ternary diagram with the points and the Dirichlet contour lines.

Author(s)

Michail Tsagris and Christos Adam.

R implementation and documentation: Michail Tsagris mtsagris@uoc.gr and Christos Adam pada4m4@gmail.com.

References

Ng Kai Wang, Guo-Liang Tian and Man-Lai Tang (2011). Dirichlet and related distributions: Theory, methods and applications. John Wiley & Sons.

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

mixdiri.contour, gendiri.contour, compnorm.contour, comp.kerncontour, mix.compnorm.contour

Examples

```
x <- as.matrix( iris[, 1:3] )
x <- x / rowSums(x)
diri.contour( a = c(3, 4, 2) )</pre>
```

Contour plot of the Flexible Dirichlet distribution in S^2 ${\it Contour\ plot\ of\ the\ Flexible\ Dirichlet\ distribution\ in\ S^2}$

Description

Contour plot of the Flexible Dirichlet distribution in S^2 .

Usage

```
fd.contour(alpha, prob, tau, n = 100, x = NULL, cont.line = FALSE)
```

Arguments

alpha	A vector of the non-negative α parameters.
prob	A vector of the clusters' probabilities. It must sum to one.
tau	The non-negative scalar tau parameter.
n	The number of grid points to consider over which the density is calculated.
X	This is either NULL (no data) or contains a 3 column matrix with compositional data.
cont.line	Do you want the contour lines to appear? If yes, set this TRUE.

Details

The user can plot only the contour lines of a Dirichlet with a given vector of parameters, or can also add the relevant data should they wish to.

Value

A ternary diagram with the points and the Flexible Dirichlet contour lines.

Author(s)

Michail Tsagris and Christos Adam.

R implementation and documentation: Michail Tsagris $\mbox{\em sagris@uoc.gr>}$ and Christos Adam $\mbox{\em pada4m4@gmail.com>}$.

References

Ongaro A. and Migliorati S. (2013). A generalization of the Dirichlet distribution. Journal of Multivariate Analysis, 114, 412–426.

Migliorati S., Ongaro A. and Monti G. S. (2017). A structured Dirichlet mixture model for compositional data: inferential and applicative issues. Statistics and Computing, 27, 963–983.

See Also

```
compnorm.contour, folded.contour, bivt.contour,comp.kerncontour, mix.compnorm.contour
```

Examples

```
fd.contour(alpha = c(10, 11, 12), prob = c(0.25, 0.25, 0.5), tau = 4)
```

Contour plot of the Gaussian mixture model in S^2 ${\it Contour\ plot\ of\ the\ Gaussian\ mixture\ model\ in\ S^2}$

Description

Contour plot of the Gaussian mixture model in S^2 .

Usage

```
mix.compnorm.contour(mod, type = "alr", n = 100, x = NULL, cont.line = FALSE)
```

Arguments

mod	An object containing the output of a mix.compnorm model.
type	The type of trasformation used, either the additive log-ratio ("alr"), the isometric log-ratio ("ilr") or the pivot coordinate ("pivot") transformation.
n	The number of grid points to consider over which the density is calculated.
Х	A matrix with the compositional data.
cont.line	Do you want the contour lines to appear? If yes, set this TRUE.

Details

The contour plot of a Gaussian mixture model is plotted. For this you need the (fitted) model.

Value

A ternary plot with the data and the contour lines of the fitted Gaussian mixture model.

Author(s)

Michail Tsagris and Christos Adam.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Christos Adam <pada4m4@gmail.com>.

References

Ryan P. Browne, Aisha ElSherbiny and Paul D. McNicholas (2015). R package mixture: Mixture Models for Clustering and Classification

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
mix.compnorm, bic.mixcompnorm, diri.contour
```

Examples

```
x <- as.matrix(iris[, 1:3])
x <- x / rowSums(x)
mod <- mix.compnorm(x, 3, model = "EII")
mix.compnorm.contour(mod, "alr")</pre>
```

Contour plot of the generalised Dirichlet distribution in S^2 Contour plot of the generalised Dirichlet distribution in S^2

Description

Contour plot of the generalised Dirichlet distribution in S^2 .

Usage

```
gendiri.contour(a, b, n = 100, x = NULL, cont.line = FALSE)
```

Arguments

a	A vector with three elements corresponding to the 3 (estimated) shape parameter values.
b	A vector with three elements corresponding to the 3 (estimated) scale parameter values.
n	The number of grid points to consider over which the density is calculated.
x	This is either NULL (no data) or contains a 3 column matrix with compositional data.
cont.line	Do you want the contour lines to appear? If yes, set this TRUE.

Details

The user can plot only the contour lines of a Dirichlet with a given vector of parameters, or can also add the relevant data should he/she wish to.

Value

A ternary diagram with the points and the Dirichlet contour lines.

Author(s)

Michail Tsagris and Christos Adam.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Christos Adam <pada4m4@gmail.com>.

References

Ng Kai Wang, Guo-Liang Tian and Man-Lai Tang (2011). Dirichlet and related distributions: Theory, methods and applications. John Wiley & Sons.

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
diri.contour, mixdiri.contour, compnorm.contour, comp.kerncontour, mix.compnorm.contour
```

Examples

```
x <- as.matrix( iris[, 1:3] )
x <- x / rowSums(x)
gendiri.contour( a = c(3, 4, 2), b = c(1, 2, 3) )</pre>
```

```
Contour plot of the kernel density estimate in S^2 
 {\it Contour\ plot\ of\ the\ kernel\ density\ estimate\ in\ S^2}
```

Description

Contour plot of the kernel density estimate in S^2 .

Usage

```
comp.kerncontour(x, type = "alr", n = 50, cont.line = FALSE)
```

Arguments

X	A matrix with the compositional data. It has to be a 3 column matrix.
type	This is either "alr" or "ilr", corresponding to the additive and the isometric log- ratio transformation respectively.
n	The number of grid points to consider, over which the density is calculated.
cont.line	Do you want the contour lines to appear? If yes, set this TRUE.

Details

The alr or the ilr transformation are applied to the compositional data. Then, the optimal bandwidth using maximum likelihood cross-validation is chosen. The multivariate normal kernel density is calculated for a grid of points. Those points are the points on the 2-dimensional simplex. Finally the contours are plotted.

Value

A ternary diagram with the points and the kernel contour lines.

Author(s)

Michail Tsagris and Christos Adam.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Christos Adam <pada4m4@gmail.com>.

References

```
M.P. Wand and M.C. Jones (1995). Kernel smoothing, CrC Press.

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.
```

See Also

```
diri.contour, mix.compnorm.contour, bivt.contour, compnorm.contour
```

```
x <- as.matrix(iris[, 1:3])
x <- x / rowSums(x)
comp.kerncontour(x, type = "alr", n = 20)
comp.kerncontour(x, type = "ilr", n = 20)</pre>
```

Contour plot of the normal distribution in S^2 ${\it Contour\ plot\ of\ the\ normal\ distribution\ in\ S^2}$

Description

Contour plot of the normal distribution in S^2 .

Usage

```
compnorm.contour(m, s, type = "alr", n = 100, x = NULL, cont.line = FALSE)
```

Arguments

m	The mean vector.
S	The covariance matrix.
type	The type of trasformation used, either the additive log-ratio ("alr"), the isometric log-ratio ("ilr") or the pivot coordinate ("pivot") transformation.
n	The number of grid points to consider over which the density is calculated.
x	This is either NULL (no data) or contains a 3 column matrix with compositional data.
cont.line	Do you want the contour lines to appear? If yes, set this TRUE.

Details

The alr or the ilr transformation is applied to the compositional data at first. Then for a grid of points within the 2-dimensional simplex the bivariate normal density is calculated and the contours are plotted along with the points.

Value

A ternary diagram with the points (if appear = TRUE) and the bivariate normal contour lines.

Author(s)

Michail Tsagris and Christos Adam.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Christos Adam <pada4m4@gmail.com>.

See Also

```
diri.contour, mix.compnorm.contour, bivt.contour, skewnorm.contour
```

Examples

```
x <- as.matrix(iris[, 1:3])
x <- x / rowSums(x)
y <- Compositional::alr(x)
m <- colMeans(y)
s <- cov(y)
compnorm.contour(m, s)</pre>
```

Contour plot of the skew skew-normal distribution in S^2 Contour plot of the skew skew-normal distribution in S^2

Description

Contour plot of the skew skew-normal distribution in S^2 .

Usage

```
skewnorm.contour(x, type = "alr", n = 100, appear = TRUE, cont.line = FALSE)
```

Arguments

X	A matrix with the compositional data. It has to be a 3 column matrix.
type	This is either "alr" or "ilr", corresponding to the additive and the isometric log- ratio transformation respectively.
n	The number of grid points to consider over which the density is calculated.
appear	Should the available data appear on the ternary plot (TRUE) or not (FALSE)?
cont.line	Do you want the contour lines to appear? If yes, set this TRUE.

Details

The alr or the ilr transformation is applied to the compositional data at first. Then for a grid of points within the 2-dimensional simplex the bivariate skew skew-normal density is calculated and the contours are plotted along with the points.

Value

A ternary diagram with the points (if appear = TRUE) and the bivariate skew skew-normal contour lines.

Author(s)

Michail Tsagris and Christos Adam.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Christos Adam <pada4m4@gmail.com>.

References

Azzalini A. and Valle A. D. (1996). The multivariate skew-skewnormal distribution. Biometrika 83(4):715-726.

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
diri.contour, mix.compnorm.contour, bivt.contour, compnorm.contour
```

Examples

```
x <- as.matrix(iris[51:100, 1:3])
x <- x / rowSums(x)
skewnorm.contour(x)</pre>
```

```
Contour plot of the t distribution in S^2 {\it Contour\ plot\ of\ the\ t\ distribution\ in\ S^2}
```

Description

Contour plot of the t distribution in S^2 .

Usage

```
bivt.contour(x, type = "alr", n = 100, appear = TRUE, cont.line = FALSE)
```

Arguments

X	A matrix with compositional data. It has to be a 3 column matrix.
type	This is either "alr" or "ilr", corresponding to the additive and the isometric log-ratio transformation respectively.
n	The number of grid points to consider over which the density is calculated.
appear	Should the available data appear on the ternary plot (TRUE) or not (FALSE)?
cont.line	Do you want the contour lines to appear? If yes, set this TRUE.

Details

The alr or the ilr transformation is applied to the compositional data at first and the location, scatter and degrees of freedom of the bivariate t distribution are computed. Then for a grid of points within the 2-dimensional simplex the bivariate t density is calculated and the contours are plotted along with the points.

Value

A ternary diagram with the points (if appear = TRUE) and the bivariate t contour lines.

Author(s)

Michail Tsagris and Christos Adam.

R implementation and documentation: Michail Tsagris $\mbox{\em sagris@uoc.gr>}$ and Christos Adam $\mbox{\em pada4m4@gmail.com>}$.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
diri.contour, mix.compnorm.contour, compnorm.contour, skewnorm.contour
```

Examples

```
x <- as.matrix( iris[, 1:3] )
x <- x / rowSums(x)
bivt.contour(x)
bivt.contour(x, type = "ilr")</pre>
```

Cross validation for some compositional regression models $Cross\ validation\ for\ some\ compositional\ regression\ models$

Description

Cross validation for some compositional regression models.

Usage

```
cv.comp.reg(y, x, type = "comp.reg", nfolds = 10, folds = NULL, seed = NULL)
```

Arguments

У	A matrix with compositional data. Zero values are allowed for some regression models.
x	The predictor variable(s).
type	This can be one of the following: "comp.reg", "robust", "kl.compreg", "js.compreg", "diri.reg" or "zadr".
nfolds	The number of folds to be used. This is taken into consideration only if the folds argument is not supplied.
folds	If you have the list with the folds supply it here. You can also leave it NULL and it will create folds.
seed	If seed is TRUE the results will always be the same.

Details

A k-fold cross validation for a compositional regression model is performed.

Value

A list including:

runtime The runtime of the cross-validation procedure.
kl The Kullback-Leibler divergences for all runs.
js The Jensen-Shannon divergences for all runs.

perf The average Kullback-Leibler divergence and average Jensen-Shannon diver-

gence.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

See Also

```
comp.reg, kl.compreg, compppr.tune, aknnreg.tune
```

Examples

```
y <- as.matrix( iris[, 1:3] )
y <- y / rowSums(y)
x <- iris[, 4]
mod <- cv.comp.reg(y, x)</pre>
```

Cross validation for the alpha-k-NN regression with compositional predictor variables

Cross validation for the α -k-NN regression with compositional predictor variables

Description

Cross validation for the α -k-NN regression with compositional predictor variables.

Usage

```
alfaknnreg.tune(y, x, a = seq(-1, 1, by = 0.1), k = 2:10, nfolds = 10, apostasi = "euclidean", method = "average", folds = NULL, seed = NULL, graph = FALSE)
```

Arguments

The response variable, a numerical vector.
A matrix with the available compositional data. Zeros are allowed.
A vector with a grid of values of the power transformation, it has to be between -1 and 1. If zero values are present it has to be greater than 0. If $\alpha=0$ the isometric log-ratio transformation is applied.
The number of nearest neighbours to consider. It can be a single number or a vector.
The number of folds. Set to 10 by default.
The type of distance to use, either "euclidean" or "manhattan".
If you want to take the average of the reponses of the k closest observations, type "average". For the median, type "median" and for the harmonic mean, type "harmonic".
If you have the list with the folds supply it here. You can also leave it NULL and it will create folds.
If seed is TRUE the results will always be the same.
If graph is TRUE (default value) a filled contour plot will appear.

Details

A k-fold cross validation for the α -k-NN regression for compositional response data is performed.

Value

A list including:

mspe The mean square error of prediction.

performance The minimum mean square error of prediction.

opt_a The optimal value of α . opt_k The optimal value of k.

runtime The runtime of the cross-validation procedure.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Tsagris M., Alenazi A. and Stewart C. (2023). Flexible non-parametric regression models for compositional response data with zeros. Statistics and Computing, 33(106).

https://link.springer.com/article/10.1007/s11222-023-10277-5

See Also

```
alfa.rda, alfa.fda
```

Examples

```
library(MASS)
x <- as.matrix(fgl[, 2:9])
x <- x / rowSums(x)
y <- fgl[, 1]
mod <- alfaknnreg.tune(y, x, a = seq(0.2, 0.4, by = 0.1), k = 2:4, nfolds = 5)</pre>
```

Cross validation for the α -k-NN regression with compositional response data

Description

Cross validation for the α -k-NN regression with compositional response data.

Usage

```
aknnreg.tune(y, x, a = seq(0.1, 1, by = 0.1), k = 2:10, apostasi = "euclidean", nfolds = 10, folds = NULL, seed = NULL, rann = FALSE)
```

Arguments

У	A matrix with the compositional response data. Zeros are allowed.
X	A matrix with the available predictor variables.
a	A vector with a grid of values of the power transformation, it has to be between -1 and 1. If zero values are present it has to be greater than 0. If $\alpha=0$ the isometric log-ratio transformation is applied.
k	The number of nearest neighbours to consider. It can be a single number or a vector.
apostasi	The type of distance to use, either "euclidean" or "manhattan".
nfolds	The number of folds. Set to 10 by default.
folds	If you have the list with the folds supply it here. You can also leave it NULL and it will create folds.
seed	You can specify your own seed number here or leave it NULL.
rann	If you have large scale datasets and want a faster k -NN search, you can use kd -trees implemented in the R package "Rnanoflann". In this case you must set this argument equal to TRUE. Note however, that in this case, the only available distance is by default "euclidean".

Details

A k-fold cross validation for the α -k-NN regression for compositional response data is performed.

Value

	1.		1 1.	
А	list	1nc	luding	τ.
	1100	1110	· carriy	٠.

kl	The Kullback-Leibler divergence for all combinations of α and k .
js	The Jensen-Shannon divergence for all combinations of α and k .
klmin	The minimum Kullback-Leibler divergence.
jsmin	The minimum Jensen-Shannon divergence.
kl.alpha	The optimal $\boldsymbol{\alpha}$ that leads to the minimum Kullback-Leibler divergence.
kl.k	The optimal \boldsymbol{k} that leads to the minimum Kullback-Leibler divergence.
js.alpha	The optimal $\boldsymbol{\alpha}$ that leads to the minimum Jensen-Shannon divergence.
js.k	The optimal \boldsymbol{k} that leads to the minimum Jensen-Shannon divergence.
runtime	The runtime of the cross-validation procedure.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Tsagris M., Alenazi A. and Stewart C. (2023). Flexible non-parametric regression models for compositional response data with zeros. Statistics and Computing, 33(106).

https://link.springer.com/article/10.1007/s11222-023-10277-5

See Also

```
aknn.reg, akernreg.tune, akern.reg, alfa.rda, alfa.fda
```

Examples

```
y <- as.matrix( iris[, 1:3] )
y <- y / rowSums(y)
x <- iris[, 4]
mod <- aknnreg.tune(y, x, a = c(0.4, 0.6), k = 2:4, nfolds = 5)</pre>
```

Cross validation for the alpha-kernel regression with compositional response data

Cross validation for the α -kernel regression with compositional response data

Description

Cross validation for the α -kernel regression with compositional response data.

Usage

```
akernreg.tune(y, x, a = seq(0.1, 1, by = 0.1), h = seq(0.1, 1, length = 10), type = "gauss", nfolds = 10, folds = NULL, seed = NULL)
```

Arguments

У	A matrix with the compositional response data. Zeros are allowed.
x	A matrix with the available predictor variables.
a	A vector with a grid of values of the power transformation, it has to be between -1 and 1. If zero values are present it has to be greater than 0. If $\alpha=0$ the isometric log-ratio transformation is applied.
h	A vector with the bandwidth value(s) to consider.
type	The type of kernel to use, "gauss" or "laplace".
nfolds	The number of folds. Set to 10 by default.
folds	If you have the list with the folds supply it here. You can also leave it NULL and it will create folds.
seed	You can specify your own seed number here or leave it NULL.

Details

A k-fold cross validation for the α -kernel regression for compositional response data is performed.

The Kullback-Leibler divergence for all combinations of α and h.

Value

k1

A list including:

js	The Jensen-Shannon divergence for all combinations of α and h .
klmin	The minimum Kullback-Leibler divergence.
jsmin	The minimum Jensen-Shannon divergence.
kl.alpha	The optimal $\boldsymbol{\alpha}$ that leads to the minimum Kullback-Leibler divergence.
kl.h	The optimal \boldsymbol{h} that leads to the minimum Kullback-Leibler divergence.
js.alpha	The optimal $\boldsymbol{\alpha}$ that leads to the minimum Jensen-Shannon divergence.
js.h	The optimal \boldsymbol{h} that leads to the minimum Jensen-Shannon divergence.
runtime	The runtime of the cross-validation procedure.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Tsagris M., Alenazi A. and Stewart C. (2023). Flexible non-parametric regression models for compositional response data with zeros. Statistics and Computing, 33(106).

https://link.springer.com/article/10.1007/s11222-023-10277-5

See Also

```
akern.reg, aknnreg.tune, aknn.reg, alfa.rda, alfa.fda
```

Examples

```
y <- as.matrix( iris[, 1:3] )
y <- y / rowSums(y)
x <- iris[, 4]
mod <- akernreg.tune(y, x, a = c(0.4, 0.6), h = c(0.1, 0.2), nfolds = 5)</pre>
```

Cross validation for the kernel regression with Euclidean response data

Cross validation for the kernel regression with Euclidean response data

Description

Cross validation for the kernel regression with Euclidean response data.

Usage

```
kernreg.tune(y, x, h = seq(0.1, 1, length = 10), type = "gauss", nfolds = 10, folds = NULL, seed = NULL, graph = FALSE, ncores = 1)
```

Arguments

У	A matrix or a vector with the Euclidean response.
X	A matrix with the available predictor variables.
h	A vector with the bandwidth value(s) h to consider.
type	The type of kernel to use, "gauss" or "laplace".
nfolds	The number of folds. Set to 10 by default.
folds	If you have the list with the folds supply it here. You can also leave it NULL and it will create folds.
seed	You can specify your own seed number here or leave it NULL.
graph	If graph is TRUE (default value) a plot will appear.
ncores	The number of cores to use. Default value is 1.

Details

A k-fold cross validation for the kernel regression with a euclidean response is performed.

36Cross validation for the regularised and flexible discriminant analysis with compositional data using the alpha-transformation

Value

A list including:

mspe The mean squared prediction error (MSPE) for each fold and value of h.

h The optimal h that leads to the minimum MSPE.

performance The minimum MSPE.

runtime The runtime of the cross-validation procedure.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Wand M. P. and Jones M. C. (1994). Kernel smoothing. CRC press.

See Also

```
kern.reg, aknnreg.tune, aknn.reg
```

Examples

```
y <- iris[, 1]
x <- iris[, 2:4]
mod <- kernreg.tune(y, x, h = c(0.1, 0.2, 0.3) )</pre>
```

Cross validation for the regularised and flexible discriminant analysis with compositional data using the alpha-transformation

Cross validation for the regularised and flexible discriminant analysis with compositional data using the α -transformation

Description

Cross validation for the regularised and flexible discriminant analysis with compositional data using the α -transformation.

Usage

```
alfarda.tune(x, ina, a = seq(-1, 1, by = 0.1), nfolds = 10, gam = seq(0, 1, by = 0.1), del = seq(0, 1, by = 0.1), ncores = 1, folds = NULL, stratified = TRUE, seed = NULL) alfafda.tune(x, ina, a = seq(-1, 1, by = 0.1), nfolds = 10, folds = NULL, stratified = TRUE, seed = NULL, graph = FALSE)
```

Cross validation for the regularised and flexible discriminant analysis with compositional data using the alpha-transformation37

Arguments

x A matrix with the available compositional data. Zeros are allowed.

ina A group indicator variable for the avaiable data.

a A vector with a grid of values of the power transformation, it has to be between

-1 and 1. If zero values are present it has to be greater than 0. If $\alpha = 0$ the

isometric log-ratio transformation is applied.

nfolds The number of folds. Set to 10 by default.

gam A vector of values between 0 and 1. It is the weight of the pooled covariance

and the diagonal matrix.

del A vector of values between 0 and 1. It is the weight of the LDA and QDA.

ncores The number of cores to use. If it is more than 1 parallel computing is performed.

It is advisable to use it if you have many observations and or many variables,

otherwise it will slow down th process.

folds If you have the list with the folds supply it here. You can also leave it NULL

and it will create folds.

stratified Do you want the folds to be created in a stratified way? TRUE or FALSE.

seed You can specify your own seed number here or leave it NULL.

graph If graph is TRUE (default value) a plot will appear.

Details

A k-fold cross validation is performed.

Value

For the alfa.rda a list including:

res The estimated optimal rate and the best values of α , γ and δ .

percent For the best value of α the averaged over all folds best rates of correct clas-

sification. It is a matrix, where rows correspond to the γ values and columns

correspond to δ values.

se The estimated standard errors of the "percent" matrix.

runtime The runtime of the cross-validation procedure.

For the alfa.fda a graph (if requested) with the estimated performance for each value of α and a list including:

per The performance of the fda in each fold for each value of α .

performance The average performance for each value of α .

opt_a The optimal value of α .

runtime The runtime of the cross-validation procedure.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Giorgos Athineou <gioathineou@gmail.com>.

References

Friedman Jerome, Trevor Hastie and Robert Tibshirani (2009). The elements of statistical learning, 2nd edition. Springer, Berlin

Tsagris M.T., Preston S. and Wood A.T.A. (2016). Improved classification for compositional data using the α -transformation. Journal of Classification, 33(2):243-261.

Hastie, Tibshirani and Buja (1994). Flexible Disriminant Analysis by Optimal Scoring. Journal of the American Statistical Association, 89(428):1255-1270.

See Also

```
alfa.rda, alfanb.tune, cv.dda, compknn.tune cv.compnb
```

Examples

```
library(MASS)
x <- as.matrix(fgl[, 2:9])
x <- x / rowSums(x)
ina <- fgl[, 10]
moda <- alfarda.tune(x, ina, a = seq(0.7, 1, by = 0.1), nfolds = 10,
gam = seq(0.1, 0.3, by = 0.1), del = seq(0.1, 0.3, by = 0.1) )</pre>
```

Cross validation for the ridge regression

Cross validation for the ridge regression

Description

Cross validation for the ridge regression is performed. There is an option for the GCV criterion which is automatic.

Usage

```
ridge.tune(y, x, nfolds = 10, lambda = seq(0, 2, by = 0.1), folds = NULL, ncores = 1, seed = NULL, graph = FALSE)
```

Arguments

У	A numeric vector containing the values of the target variable. If the values are proportions or percentages, i.e. strictly within 0 and 1 they are mapped into R using the logit transformation.
X	A numeric matrix containing the variables.
nfolds	The number of folds in the cross validation.
lambda	A vector with the a grid of values of λ to be used.
folds	If you have the list with the folds supply it here. You can also leave it NULL and it will create folds.
ncores	The number of cores to use. If it is more than 1 parallel computing is performed.
seed	You can specify your own seed number here or leave it NULL.
graph	If graph is set to TRUE the performances for each fold as a function of the λ values will appear.

Details

A k-fold cross validation is performed. This function is used by alfaridge. tune.

Value

A list including:

msp The performance of the ridge regression for every fold. mspe The values of the mean prediction error for each value of λ . The value of λ which corresponds to the minimum MSPE.

performance The minimum MSPE.

runtime The time required by the cross-validation procedure.

Author(s)

Michail Tsagris.

R implementation and documentation: Giorgos Athineou <gioathineou@gmail.com> and Michail Tsagris <mtsagris@uoc.gr>.

References

Hoerl A.E. and R.W. Kennard (1970). Ridge regression: Biased estimation for nonorthogonal problems. Technometrics, 12(1):55-67.

Brown P. J. (1994). Measurement, Regression and Calibration. Oxford Science Publications.

See Also

```
ridge.reg, alfaridge.tune
```

40Cross validation for the ridge regression with compositional data as predictor using the alpha-transformation

Examples

```
y <- as.vector(iris[, 1])
x <- as.matrix(iris[, 2:4])
ridge.tune( y, x, nfolds = 10, lambda = seq(0, 2, by = 0.1), graph = TRUE )</pre>
```

Cross validation for the ridge regression with compositional data as predictor using the α -transformation

Description

Cross validation for the ridge regression is performed. There is an option for the GCV criterion which is automatic. The predictor variables are compositional data and the α -transformation is applied first.

Usage

```
alfaridge.tune(y, x, nfolds = 10, a = seq(-1, 1, by = 0.1), lambda = seq(0, 2, by = 0.1), folds = NULL, ncores = 1, graph = TRUE, col.nu = 15, seed = NULL)
```

Arguments

Zero values are allowed. The number of folds in the cross validation. A vector with the a grid of values of α to be used. Iambda A vector with the a grid of values of λ to be used. If you have the list with the folds supply it here. You can also leave it NULL and it will create folds. The number of cores to use. If it is more than 1 parallel computing is performed. It is advisable to use it if you have many observations and or many variables, otherwise it will slow down th process. graph If graph is TRUE (default value) a filled contour plot will appear. col.nu A number parameter for the filled contour plot, taken into account only if graph is TRUE.	У	A numeric vector containing the values of the target variable. If the values are proportions or percentages, i.e. strictly within 0 and 1 they are mapped into R using the logit transformation.
a A vector with the a grid of values of α to be used. A vector with the a grid of values of λ to be used. If you have the list with the folds supply it here. You can also leave it NULL and it will create folds. The number of cores to use. If it is more than 1 parallel computing is performed. It is advisable to use it if you have many observations and or many variables, otherwise it will slow down th process. graph If graph is TRUE (default value) a filled contour plot will appear. A number parameter for the filled contour plot, taken into account only if graph is TRUE.	х	A numeric matrix containing the compositional data, i.e. the predictor variables. Zero values are allowed.
 lambda A vector with the a grid of values of λ to be used. folds If you have the list with the folds supply it here. You can also leave it NULL and it will create folds. ncores The number of cores to use. If it is more than 1 parallel computing is performed. It is advisable to use it if you have many observations and or many variables, otherwise it will slow down th process. graph If graph is TRUE (default value) a filled contour plot will appear. col.nu A number parameter for the filled contour plot, taken into account only if graph is TRUE. 	nfolds	The number of folds in the cross validation.
folds If you have the list with the folds supply it here. You can also leave it NULL and it will create folds. ncores The number of cores to use. If it is more than 1 parallel computing is performed. It is advisable to use it if you have many observations and or many variables, otherwise it will slow down th process. graph If graph is TRUE (default value) a filled contour plot will appear. A number parameter for the filled contour plot, taken into account only if graph is TRUE.	a	A vector with the a grid of values of α to be used.
and it will create folds. The number of cores to use. If it is more than 1 parallel computing is performed. It is advisable to use it if you have many observations and or many variables, otherwise it will slow down th process. graph If graph is TRUE (default value) a filled contour plot will appear. A number parameter for the filled contour plot, taken into account only if graph is TRUE.	lambda	A vector with the a grid of values of λ to be used.
It is advisable to use it if you have many observations and or many variables, otherwise it will slow down th process. graph If graph is TRUE (default value) a filled contour plot will appear. A number parameter for the filled contour plot, taken into account only if graph is TRUE.	folds	If you have the list with the folds supply it here. You can also leave it NULL and it will create folds.
col.nu A number parameter for the filled contour plot, taken into account only if graph is TRUE.	ncores	The number of cores to use. If it is more than 1 parallel computing is performed. It is advisable to use it if you have many observations and or many variables, otherwise it will slow down th process.
is TRUE.	graph	If graph is TRUE (default value) a filled contour plot will appear.
Voy on specify your own seed number here or leave it NIII I	col.nu	A number parameter for the filled contour plot, taken into account only if graph is TRUE.
seed from the carrier your own seed number here of leave it NOLL.	seed	You can specify your own seed number here or leave it NULL.

Cross validation for the ridge regression with compositional data as predictor using the alpha-transformation41

Details

A k-fold cross validation is performed.

Value

If graph is TRUE a fileld contour a filled contour will appear. A list including:

mspe The MSPE where rows correspond to the α values and the columns to the num-

ber of principal components.

best.par The best pair of α and λ .

performance The minimum mean squared error of prediction.

runtime The run time of the cross-validation procedure.

Author(s)

Michail Tsagris.

R implementation and documentation: Giorgos Athineou <gioathineou@gmail.com> and Michail Tsagris <mtsagris@uoc.gr>.

References

Hoerl A.E. and R.W. Kennard (1970). Ridge regression: Biased estimation for nonorthogonal problems. Technometrics, 12(1):55-67.

Brown P. J. (1994). Measurement, Regression and Calibration. Oxford Science Publications.

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. https://arxiv.org/pdf/1106.1451.pdf

See Also

```
alfa.ridge, ridge.tune
```

Examples

```
library(MASS)
y <- as.vector(fgl[, 1])
x <- as.matrix(fgl[, 2:9])
x <- x / rowSums(x)
alfaridge.tune( y, x, nfolds = 10, a = seq(0.1, 1, by = 0.1),
lambda = seq(0, 1, by = 0.1) )</pre>
```

Cross validation for the TFLR model $Cross\ validation\ for\ the\ TFLR\ model$

Description

Cross validation for the TFLR model.

Usage

```
cv.tflr(y, x, nfolds = 10, folds = NULL, seed = NULL)
```

Arguments

y A matrix with compositional response data. Zero values are allowed.

x A matrix with compositional predictors. Zero values are allowed.

The number of folds to be used. This is taken into consideration only if the folds argument is not supplied.

folds If you have the list with the folds supply it here. You can also leave it NULL and it will create folds.

seed If seed is TRUE the results will always be the same.

Details

A k-fold cross validation for the transformation-free linear regression for compositional responses and predictors is performed.

Value

A list including:

runtime The runtime of the cross-validation procedure.

kl The Kullback-Leibler divergences for all runs.

js The Jensen-Shannon divergences for all runs.

perf The average Kullback-Leibler divergence and average Jensen-Shannon diver-

gence.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Fiksel J., Zeger S. and Datta A. (2022). A transformation-free linear regression for compositional outcomes and predictors. Biometrics, 78(3): 974–987.

Tsagris. M. (2024). Constrained least squares simplicial-simplicial regression. https://arxiv.org/pdf/2403.19835.pdf

See Also

```
tflr, cv.scls, klalfapcr.tune
```

Examples

```
library(MASS)
y <- rdiri(100, runif(3, 1, 3))
x <- as.matrix(fgl[1:100, 2:9])</pre>
x <- x / rowSums(x)
mod <- cv.tflr(y, x)</pre>
mod
```

Cross-validation for LASSO with compositional predictors using the alpha-transformation

> Cross-validation for LASSO with compositional predictors using the alpha-transformation

Description

Cross-validation for LASSO with compositional predictors using the *alpha*-transformation.

Usage

```
alfalasso.tune(y, x, a = seq(-1, 1, by = 0.1), model = "gaussian", lambda = NULL,
type.measure = "mse", nfolds = 10, folds = NULL, stratified = FALSE)
```

Arguments

lambda

	A				1
١,	Δ τ	nimerical vector	' or a matrix t	or multinomial	logistic regression.
١,	Γ 1	iumencai vectoi	OI a maura i	oi muminomia	iogistic regression.

A numerical matrix containing the predictor variables, compositional data, where Χ zero values are allowed...

A vector with a grid of values of the power transformation, it has to be between а -1 and 1. If zero values are present it has to be greater than 0. If $\alpha = 0$ the isometric log-ratio transformation is applied.

mode1 The type of the regression model, "gaussian", "binomial", "poisson", "multinomial", or "mgaussian".

> This information is copied from the package glmnet. A user supplied lambda sequence. Typical usage is to have the program compute its own lambda sequence based on nlambda and lambda.min.ratio. Supplying a value of lambda overrides this. WARNING: use with care. Avoid supplying a single value for lambda (for predictions after CV use predict() instead). Supply instead a decreasing sequence of lambda values. glmnet relies on its warms starts for speed, and its often faster to fit a whole path than compute a single fit.

This information is taken from the package glmnet. The loss function to use for cross-validation. For gaussian models this can be "mse", "deviance" for logistic and poisson regression, "class" applies to binomial and multinomial logistic regression only, and gives misclassification error. "auc" is for two-class logistic regression only, and gives The area under the ROC curve. "mse" or "mae" (mean absolute error) can be used by all models.

nfolds The number of folds. Set to 10 by default.

folds If you have the list with the folds supply it here. You can also leave it NULL

and it will create folds.

stratified Do you want the folds to be created in a stratified way? TRUE or FALSE.

Details

The function uses the glmnet package to perform LASSO penalised regression. For more details see the function in that package.

Value

A matrix with two columns and number of rows equal to the number of α values used. Each row contains, the optimal value of the λ penalty parameter for the LASSO and the optimal value of the loss function, for each value of α .

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

Friedman, J., Hastie, T. and Tibshirani, R. (2010) Regularization Paths for Generalized Linear Models via Coordinate Descent. Journal of Statistical Software, Vol. 33(1), 1–22.

See Also

```
alfa.lasso, cv.lasso.klcompreg, lasso.compreg, alfa.knn.reg
```

Examples

```
y <- iris[, 1]
x <- rdiri(150, runif(20, 2, 5) )
mod <- alfalasso.tune( y, x, a = c(0.2, 0.5, 1) )</pre>
```

Cross-validation for the alpha-SCLS model ${\it Cross-validation\ for\ the\ alpha-SCLS\ model}$

Description

Cross-validation for the alpha-SCLS model.

Usage

```
cv.ascls(y, x, a = seq(0.1, 1, by = 0.1), nfolds = 10, folds = NULL, seed = NULL)
```

Arguments

У	A numerical matrix with the simplicial response data. Zero values are allowed.
Х	A matrix with the simplicial predictor variables. Zero values are allowed.
a	A vector or a single number of values of the α -parameter. This has to be different from zero, and it can take negative values if there are no zeros in the simplicial response (y).
nfolds	The number of folds for the K-fold cross validation, set to 10 by default.
folds	If you have the list with the folds supply it here. You can also leave it NULL and it will create folds.
seed	You can specify your own seed number here or leave it NULL.

Details

The K-fold cross validation is performed in order to select the optimal value for α of the α -SCLS model.

Value

A list including:

runtime The runtime of the cross-validation procedure. kl The Kullback-Leibler divergence for every value of α . js The Jensen-Shannon divergence for every value of α .

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Tsagris. M. (2024). Constrained least squares simplicial-simplicial regression. https://arxiv.org/pdf/2403.19835.pdf

See Also

```
ascls, cv.atflr
```

Examples

```
library(MASS)
y <- rdiri( 214, runif(4, 1, 3) )
x <- as.matrix( fgl[, 2:9] )
mod <- cv.ascls(y, x, nfolds = 5)</pre>
```

Cross-validation for the alpha-TFLR model ${\it Cross-validation\ for\ the\ alpha-TFLR\ model}$

Description

Cross-validation for the alpha-TFLR model.

Usage

```
cv.atflr(y, x, a = seq(0.1, 1, by = 0.1), nfolds = 10, folds = NULL, seed = NULL)
```

Arguments

у	A numerical matrix with the simplicial response data. Zero values are allowed.	
X	A matrix with the simplicial predictor variables. Zero values are allowed.	
a	A vector or a single number of values of the α -parameter. This has to be differ from zero, and it can take negative values if there are no zeros in the simplic response (y).	
nfolds	The number of folds for the K-fold cross validation, set to 10 by default.	
folds	If you have the list with the folds supply it here. You can also leave it NULL and it will create folds.	
seed	You can specify your own seed number here or leave it NULL.	

Details

The K-fold cross validation is performed in order to select the optimal value for α of the α -TFLR model.

Value

A list including:

runtime	The runtime of the cross-validation procedure.
kl	The Kullback-Leibler divergence for every value of α .
js	The Jensen-Shannon divergence for every value of α .

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Fiksel J., Zeger S. and Datta A. (2022). A transformation-free linear regression for compositional outcomes and predictors. Biometrics, 78(3): 974–987.

Tsagris. M. (2024). Constrained least squares simplicial-simplicial regression. https://arxiv.org/pdf/2403.19835.pdf

See Also

```
atflr, cv.ascls
```

Examples

```
library(MASS)
y <- rdiri( 214, runif(4, 1, 3) )
x <- as.matrix( fgl[, 2:9] )
mod <- cv.ascls(y, x, nfolds = 2, a = c(0.5, 1))</pre>
```

Cross-validation for the Dirichlet discriminant analysis $Cross\text{-}validation\ for\ the\ Dirichlet\ discriminant\ analysis$

Description

Cross-validation for the Dirichlet discriminant analysis.

Usage

```
cv.dda(x, ina, nfolds = 10, folds = NULL, stratified = TRUE, seed = NULL)
```

Arguments

X	A matrix with the available data, the predictor variables.
ina	A vector of data. The response variable, which is categorical (factor is acceptable).
folds	A list with the indices of the folds.
nfolds	The number of folds to be used. This is taken into consideration only if "folds" is NULL.
stratified	Do you want the folds to be selected using stratified random sampling? This preserves the analogy of the samples of each group. Make this TRUE if you wish.
seed	If you set this to TRUE, the same folds will be created every time.

Details

This function estimates the performance of the Dirichlet discriminant analysis via k-fold cross-validation.

Value

A list including:

percent The percentage of correct classification

runtime The duration of the cross-validation proecdure.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Friedman J., Hastie T. and Tibshirani R. (2017). The elements of statistical learning. New York: Springer.

Thomas P. Minka (2003). Estimating a Dirichlet distribution. http://research.microsoft.com/en-us/um/people/minka/papers/dirichlet/minka-dirichlet.pdf

See Also

```
dda, alfanb.tune, alfarda.tune, compknn.tune, cv.compnb
```

Examples

```
x <- as.matrix(iris[, 1:4])
x <- x / rowSums(x)
mod <- cv.dda(x, ina = iris[, 5])</pre>
```

Cross-validation for the LASSO Kullback-Leibler divergence based regression

Cross-validation for the LASSO Kullback-Leibler divergence based regression

Description

Cross-validation for the LASSO Kullback-Leibler divergence based regression.

Usage

```
cv.lasso.klcompreg(y, x, alpha = 1, type = "grouped", nfolds = 10,
folds = NULL, seed = NULL, graph = FALSE)
```

Arguments

У	A numerical matrix with compositional data with or without zeros.
x	A matrix with the predictor variables.
alpha	The elastic net mixing parameter, with $0 \le \alpha \le 1$. The penalty is defined as a weighted combination of the ridge and of the Lasso regression. When $\alpha = 1$ LASSO is applied, while $\alpha = 0$ yields the ridge regression.
type	This information is copied from the package glmnet. If "grouped" then a grouped lasso penalty is used on the multinomial coefficients for a variable. This ensures they are all in our out together. The default in our case is "grouped".
nfolds	The number of folds for the K-fold cross validation, set to 10 by default.
folds	If you have the list with the folds supply it here. You can also leave it NULL and it will create folds.
seed	You can specify your own seed number here or leave it NULL.
graph	If graph is TRUE (default value) a filled contour plot will appear.

Details

The K-fold cross validation is performed in order to select the optimal value for λ , the penalty parameter in LASSO.

Value

The outcome is the same as in the R package glmnet. The extra addition is that if "graph = TRUE", then the plot of the cross-validated object is returned. The contains the logarithm of λ and the deviance. The numbers on top of the figure show the number of set of coefficients for each component, that are not zero.

Author(s)

Michail Tsagris and Abdulaziz Alenazi.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Abdulaziz Alenazi <a.alenazi@nbu.edu.sa>.

References

Alenazi, A. A. (2022). f-divergence regression models for compositional data. Pakistan Journal of Statistics and Operation Research, 18(4): 867–882.

Friedman, J., Hastie, T. and Tibshirani, R. (2010) Regularization Paths for Generalized Linear Models via Coordinate Descent. Journal of Statistical Software, Vol. 33(1), 1-22.

See Also

lasso.klcompreg, lassocoef.plot, lasso.compreg, cv.lasso.compreg, kl.compreg

Examples

```
library(MASS)
y <- rdiri( 214, runif(4, 1, 3) )
x <- as.matrix( fgl[, 2:9] )
mod <- cv.lasso.klcompreg(y, x)</pre>
```

```
Cross-validation for the LASSO log-ratio regression with compositional response \,
```

Cross-validation for the LASSO log-ratio regression with compositional response

Description

Cross-validation for the LASSO log-ratio regression with compositional response.

Usage

```
cv.lasso.compreg(y, x, alpha = 1, nfolds = 10,
folds = NULL, seed = NULL, graph = FALSE)
```

Arguments

У	A numerical matrix with compositional data. Zero values are not allowed as the additive log-ratio transformation (alr) is applied to the compositional response prior to implementing the LASSO algorithm.
X	A matrix with the predictor variables.
alpha	The elastic net mixing parameter, with $0 \le \alpha \le 1$. The penalty is defined as a weighted combination of the ridge and of the Lasso regression. When $\alpha = 1$ LASSO is applied, while $\alpha = 0$ yields the ridge regression.
nfolds	The number of folds for the K-fold cross validation, set to 10 by default.
folds	If you have the list with the folds supply it here. You can also leave it NULL and it will create folds.
seed	You can specify your own seed number here or leave it NULL.
graph	If graph is TRUE (default value) a filled contour plot will appear.

Details

The K-fold cross validation is performed in order to select the optimal value for λ , the penalty parameter in LASSO.

Value

The outcome is the same as in the R package glmnet. The extra addition is that if "graph = TRUE", then the plot of the cross-validated object is returned. The contains the logarithm of λ and the mean squared error. The numbers on top of the figure show the number of set of coefficients for each component, that are not zero.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

Friedman, J., Hastie, T. and Tibshirani, R. (2010) Regularization Paths for Generalized Linear Models via Coordinate Descent. Journal of Statistical Software, Vol. 33(1), 1-22.

See Also

```
lasso.compreg, lasso.klcompreg, lassocoef.plot, cv.lasso.klcompreg,comp.reg
```

Examples

```
library(MASS)
y <- rdiri( 214, runif(4, 1, 3) )
x <- as.matrix( fgl[, 2:9] )
mod <- cv.lasso.compreg(y, x)</pre>
```

Cross-validation for the naive Bayes classifiers for compositional data

Cross-validation for the naive Bayes classifiers for compositional data

Description

Cross-validation for the naive Bayes classifiers for compositional data.

Usage

Arguments

Х	A matrix with the available data, the predictor variables.
ina	A vector of data. The response variable, which is categorical (factor is acceptable).
type	The type of naive Bayes, "beta", "logitnorm", "cauchy", "laplace", "gamma", "normlog" or "weibull". For the last 4 distributions, the negative of the logarithm of the compositional data is applied first.
folds	A list with the indices of the folds.
nfolds	The number of folds to be used. This is taken into consideration only if "folds" is NULL.

52Cross-validation for the naive Bayes classifiers for compositional data using the alpha-transformation

stratified Do you want the folds to be selected using stratified random sampling? This

preserves the analogy of the samples of each group. Make this TRUE if you

wish.

seed You can specify your own seed number here or leave it NULL.

pred.ret If you want the predicted values returned set this to TRUE.

Value

A list including:

preds If pred.ret is TRUE the predicted values for each fold are returned as elements

in a list.

crit A vector whose length is equal to the number of k and is the accuracy metric for

each k. For the classification case it is the percentage of correct classification.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Friedman J., Hastie T. and Tibshirani R. (2017). The elements of statistical learning. New York: Springer.

See Also

```
comp.nb
```

Examples

```
x <- as.matrix(iris[, 1:4])
x <- x / rowSums(x)
mod <- cv.compnb(x, ina = iris[, 5] )</pre>
```

Cross-validation for the naive Bayes classifiers for compositional data using the alpha-transformation

Cross-validation for the naive Bayes classifiers for compositional data using the α -transformation

Description

Cross-validation for the naive Bayes classifiers for compositional data using the α -transformation.

Cross-validation for the naive Bayes classifiers for compositional data using the alpha-transformation53

Usage

```
alfanb.tune(x, ina, a = seq(-1, 1, by = 0.1), type = "gaussian", folds = NULL, nfolds = 10, stratified = TRUE, seed = NULL)
```

Arguments

Χ	A matrix with the available data, the predictor variables.
ina	A vector of data. The response variable, which is categorical (factor is acceptable).
a	The value of α for the $\alpha\text{-transformation}.$ This can be a vector of values or a single number.
type	The type of naive Bayes, "gaussian", "cauchy" or "laplace".
folds	A list with the indices of the folds.
nfolds	The number of folds to be used. This is taken into consideration only if "folds" is NULL.
stratified	Do you want the folds to be selected using stratified random sampling? This preserves the analogy of the samples of each group. Make this TRUE if you wish.
seed	You can specify your own seed number here or leave it NULL.

Details

This function estimates the performance of the naive Bayes classifier for each value of α of the α -transformation.

Value

A list including:

crit A vector whose length is equal to the number of k and is the accuracy metric for

each k. For the classification case it is the percentage of correct classification.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Friedman J., Hastie T. and Tibshirani R. (2017). The elements of statistical learning. New York: Springer.

See Also

```
alfa.nb, alfarda.tune, compknn.tune, cv.dda, cv.compnb
```

Examples

```
x <- as.matrix(iris[, 1:4])
x <- x / rowSums(x)
mod <- alfanb.tune(x, ina = iris[, 5], a = c(0, 0.1, 0.2) )</pre>
```

Cross-validation for the SCLS model

Cross-validation for the SCLS model

Description

Cross-validation for the SCLS model.

Usage

```
cv.scls(y, x, nfolds = 10, folds = NULL, seed = NULL)
```

Arguments

У	A matrix with compositional response data. Zero values are allowed.
X	A matrix with compositional predictors. Zero values are allowed.
nfolds	The number of folds to be used. This is taken into consideration only if the folds argument is not supplied.
folds	If you have the list with the folds supply it here. You can also leave it NULL and it will create folds.
seed	You can specify your own seed number here or leave it NULL.

Details

The function performs k-fold cross-validation for the least squares regression where the beta coefficients are constained to be positive and sum to 1.

Value

A list including:

runtime The runtime of the cross-validation procedure.
kl The Kullback-Leibler divergences for all runs.
js The Jensen-Shannon divergences for all runs.

perf The average Kullback-Leibler divergence and average Jensen-Shannon diver-

gence.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Tsagris. M. (2024). Constrained least squares simplicial-simplicial regression. https://arxiv.org/pdf/2403.19835.pdf

See Also

```
scls, cv.tflr, klalfapcr.tune
```

Examples

```
library(MASS)
set.seed(1234)
y <- rdiri(214, runif(3, 1, 3))
x <- as.matrix(fgl[, 2:9])
x <- x / rowSums(x)
mod <- cv.scls(y, x, nfolds = 5, seed = 12345)
mod</pre>
```

Cross-validation for the SCRQ model

Cross-validation for the SCRQ model

Description

Cross-validation for the SCRQ model.

Usage

```
cv.scrq(y, x, nfolds = 10, folds = NULL, seed = NULL)
```

Arguments

У	A matrix with compositional response data. Zero values are allowed.
x	A matrix with compositional predictors. Zero values are allowed.
nfolds	The number of folds to be used. This is taken into consideration only if the folds argument is not supplied.
folds	If you have the list with the folds supply it here. You can also leave it NULL and it will create folds.
seed	You can specify your own seed number here or leave it NULL.

Details

The function performs k-fold cross-validation for the absolute regression where the beta coefficients are constained to be positive and sum to 1.

Value

A list including:

runtime The runtime of the cross-validation procedure.
kl The Kullback-Leibler divergences for all runs.
js The Jensen-Shannon divergences for all runs.

perf The average Kullback-Leibler divergence and average Jensen-Shannon diver-

gence.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Tsagris. M. (2024). Constrained least squares simplicial-simplicial regression. https://arxiv.org/pdf/2403.19835.pdf

See Also

```
scrq, cv.scls, cv.tflr
```

Examples

```
library(MASS)
set.seed(1234)
y <- rdiri(214, runif(3, 1, 3))
x <- as.matrix(fgl[, 2:9])
x <- x / rowSums(x)
mod <- cv.scrq(y, x, nfolds = 5, seed = 12345)
mod</pre>
```

Density of compositional data from Gaussian mixture models

Simulation of compositional data from Gaussian mixture models

Description

Simulation of compositional data from Gaussian mixture models.

Usage

```
dmix.compnorm(x, mu, sigma, prob, type = "alr", logged = TRUE)
```

Arguments

X	A vector or a matrix with compositional data.
prob	A vector with mixing probabilities. Its length is equal to the number of clusters.
mu	A matrix where each row corresponds to the mean vector of each cluster.
sigma	An array consisting of the covariance matrix of each cluster.
type	The type of trasformation used, either the additive log-ratio ("alr"), the isometric log-ratio ("ilr") or the pivot coordinate ("pivot") transformation.
logged	A boolean variable specifying whether the logarithm of the density values to be returned. It is set to TRUE by default.

Details

A sample from a multivariate Gaussian mixture model is generated.

Value

A vector with the density values.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Ryan P. Browne, Aisha ElSherbiny and Paul D. McNicholas (2015). R package mixture: Mixture Models for Clustering and Classification.

See Also

```
mix.compnorm, bic.mixcompnorm
```

Examples

```
p <- c(1/3, 1/3, 1/3)
mu <- matrix(nrow = 3, ncol = 4)
s <- array( dim = c(4, 4, 3) )
x <- as.matrix(iris[, 1:4])
ina <- as.numeric(iris[, 5])
mu <- rowsum(x, ina) / 50
s[, , 1] <- cov(x[ina == 1, ])
s[, , 2] <- cov(x[ina == 2, ])
s[, , 3] <- cov(x[ina == 3, ])
y <- rmixcomp(100, p, mu, s, type = "alr")$x
mod <- dmix.compnorm(y, mu, s, p)</pre>
```

Density of the Flexible Dirichlet distribution

Density of the Flexible Dirichlet distribution

Description

Density of the Flexible Dirichlet distribution

Usage

```
dfd(x, alpha, prob, tau)
```

Arguments

x A vector or a matrix with compositional data. alpha A vector of the non-negative α parameters.

prob A vector of the clusters' probabilities. It must sum to one.

tau The non-negative scalar tau parameter.

Details

For more information see the references and the package FlxeDir.

Value

The density value(s).

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Ongaro A. and Migliorati S. (2013). A generalization of the Dirichlet distribution. Journal of Multivariate Analysis, 114, 412–426.

Migliorati S., Ongaro A. and Monti G. S. (2017). A structured Dirichlet mixture model for compositional data: inferential and applicative issues. Statistics and Computing, 27, 963–983.

See Also

rfd

Examples

```
alpha <- c(12, 11, 10)
prob <- c(0.25, 0.25, 0.5)
tau <- 8
x <- rfd(20, alpha, prob, tau)
dfd(x, alpha, prob, tau)</pre>
```

Density of the folded normal distribution

Density of the folded model normal distribution

Description

Density of the folded model normal distribution.

Usage

```
dfolded(x, a, p, mu, su, logged = TRUE)
```

Arguments

x A vector or a matrix with compositional data. No ze	eros are allowed.
---	-------------------

a The value of α .

p The probability inside the simplex of the folded model.

mu The mean vector.

su The covariance matrix.

logged A boolean variable specifying whether the logarithm of the density values to be

returned. It is set to TRUE by default.

Details

Density values of the folded model.

Value

The density value(s).

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Tsagris M. and Stewart C. (2020). A folded model for compositional data analysis. Australian and New Zealand Journal of Statistics, 62(2): 249-277. https://arxiv.org/pdf/1802.07330.pdf

See Also

```
rfolded, a.est, folded.contour
```

Examples

Density values of a Dirichlet distribution

Density values of a Dirichlet distribution

Description

Density values of a Dirichlet distribution.

Usage

```
ddiri(x, a, logged = TRUE)
```

Arguments

X	A matrix containing compositional data. This can be a vector or a matrix with the data.
a	A vector of parameters. Its length must be equal to the number of components, or columns of the matrix with the compositional data and all values must be greater than zero.
logged	A boolean variable specifying whether the logarithm of the density values to be returned. It is set to TRUE by default.

Details

The density of the Dirichlet distribution for a vector or a matrix of compositional data is returned.

Value

A vector with the density values.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Ng Kai Wang, Guo-Liang Tian and Man-Lai Tang (2011). Dirichlet and related distributions: Theory, methods and applications. John Wiley & Sons.

See Also

```
dgendiri, diri.nr, diri.est, diri.contour, rdiri, dda
```

Examples

```
x <- rdiri( 100, c(5, 7, 4, 8, 10, 6, 4) )
a <- diri.est(x)
f <- ddiri(x, a$param)
sum(f)
a</pre>
```

Density values of a generalised Dirichlet distribution $Density \ values \ of \ a \ generalised \ Dirichlet \ distribution$

Description

Density values of a generalised Dirichlet distribution.

Usage

```
dgendiri(x, a, b, logged = TRUE)
```

Arguments

X	A matrix containing compositional data. This can be a vector or a matrix with the data.
a	A numerical vector with the shape parameter values of the Gamma distribution.
b	A numerical vector with the scale parameter values of the Gamma distribution.
logged	A boolean variable specifying whether the logarithm of the density values to be returned. It is set to TRUE by default.

Details

The density of the Dirichlet distribution for a vector or a matrix of compositional data is returned.

Value

A vector with the density values.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Ng Kai Wang, Guo-Liang Tian and Man-Lai Tang (2011). Dirichlet and related distributions: Theory, methods and applications. John Wiley & Sons.

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
ddiri, rgendiri, diri.est, diri.contour, rdiri, dda
```

Examples

```
a <- c(1, 2, 3)
b <- c(2, 3, 4)
x <- rgendiri(100, a, b)
y <- dgendiri(x, a, b)</pre>
```

Density values of a mixture of Dirichlet distributions $Density \ values \ of \ a \ mixture \ of \ Dirichlet \ distributions$

Description

Density values of a mixture of Dirichlet distributions.

Usage

```
dmixdiri(x, a, prob, logged = TRUE)
```

Arguments

X	A vector or a matrix	with compositional	data. Zeros are not allowed.

a A matrix where each row contains the parameters of each Dirichlet component.

prob A vector with the mixing probabilities.

logged A boolean variable specifying whether the logarithm of the density values to be

returned. It is set to TRUE by default.

Details

The density of the mixture of Dirichlet distribution for a vector or a matrix of compositional data is returned.

Value

A vector with the density values.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Ye X., Yu Y. K. and Altschul S. F. (2011). On the inference of Dirichlet mixture priors for protein sequence comparison. Journal of Computational Biology, 18(8), 941-954.

See Also

```
rmixdiri, mixdiri.contour
```

Examples

```
a <- matrix( c(12, 30, 45, 32, 50, 16), byrow = TRUE, ncol = 3) prob <- c(0.5, 0.5) x <- rmixdiri(100, a, prob)x f <- dmixdiri(x, a, prob)
```

Dirichlet discriminant analysis

Dirichlet discriminant analysis

Description

Dirichlet discriminant analysis.

Usage

```
dda(xnew, x, ina)
```

Arguments

xnew	A matrix with the new compositional predictor data whose class you want to
	predict. Zeros are allowed.
X	A matrix with the available compositional predictor data. Zeros are allowed.
ina	A vector of data. The response variable, which is categorical (factor is acceptable).

Details

The funcitons performs maximum likelihood discriminant analysis using the Dirichlet distribution.

Value

A vector with the estimated group.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Friedman J., Hastie T. and Tibshirani R. (2017). The elements of statistical learning. New York: Springer.

Thomas P. Minka (2003). Estimating a Dirichlet distribution. http://research.microsoft.com/en-us/um/people/minka/papers/dirichlet/minka-dirichlet.pdf

Ng Kai Wang, Guo-Liang Tian and Man-Lai Tang (2011). Dirichlet and related distributions: Theory, methods and applications. John Wiley & Sons.

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
cv.dda, comp.nb, alfa.rda, alfa.knn,comp.knn, mix.compnorm, diri.reg, zadr
```

Examples

```
x \leftarrow Compositional::rdiri(100, runif(5))
ina <- rbinom(100, 1, 0.5) + 1
mod <- dda(x, x, ina)
```

Dirichlet random values simulation

Dirichlet random values simulation

Description

Dirichlet random values simulation.

Usage

```
rdiri(n, a)
```

Dirichlet regression 65

Arguments

- n The sample size, a numerical value.
- a A numerical vector with the parameter values.

Details

The algorithm is straightforward, for each vector, independent gamma values are generated and then divided by their total sum.

Value

A matrix with the simulated data.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris mtsagris@uoc.gr> and Giorgos Athineou gioathineou@gmail.com>.

References

Ng Kai Wang, Guo-Liang Tian and Man-Lai Tang (2011). Dirichlet and related distributions: Theory, methods and applications. John Wiley & Sons.

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
diri.est, diri.nr, diri.contour, rgendiri
```

Examples

```
x <- rdiri( 100, c(5, 7, 1, 3, 10, 2, 4) )
diri.est(x)
```

Dirichlet regression Dirichlet regression

Description

Dirichlet regression.

Usage

```
diri.reg(y, x, plot = FALSE, xnew = NULL)
diri.reg2(y, x, xnew = NULL)
diri.reg3(y, x, xnew = NULL)
```

Dirichlet regression

Arguments

У	A matrix with the compositional data (dependent variable). Zero values are not allowed.
x	The predictor variable(s), they can be either continuous or categorical or both.
plot	A boolean variable specifying whether to plot the leverage values of the observations or not. This is taken into account only when xnew = NULL.
xnew	If you have new data use it, otherwise leave it NULL.

Details

A Dirichlet distribution is assumed for the regression. This involves numerical optimization. The function "diri.reg2()" allows for the covariates to be linked with the precision parameter ϕ via the exponential link function $\phi = e^{x*b}$. The function "diri.reg3()" links the covariates to the alpha parameters of the Dirichlet distribution, i.e. it uses the classical parametrization of the distribution. This means, that there is a set of regression parameters for each component.

Value

A list including:

runtime	The time required by the regression.
loglik	The value of the log-likelihood.
phi	The precision parameter. If covariates are linked with it (function "diri.reg2()"), this will be a vector.
phipar	The coefficients of the phi parameter if it is linked to the covariates.
std.phi	The standard errors of the coefficients of the phi parameter is it linked to the covariates.
log.phi	The logarithm of the precision parameter.
std.logphi	The standard error of the logarithm of the precision parameter.
be	The beta coefficients.
seb	The standard error of the beta coefficients.
sigma	Th covariance matrix of the regression parameters (for the mean vector and the phi parameter)".
lev	The leverage values.
est	For the "diri.reg" this contains the fitted or the predicted values (if xnew is not NULL). For the "diri.reg2" if xnew is NULL, this is also NULL.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Giorgos Athineou <gioathineou@gmail.com>.

References

Maier, Marco J. (2014) DirichletReg: Dirichlet Regression for Compositional Data in R. Research Report Series/Department of Statistics and Mathematics, 125. WU Vienna University of Economics and Business, Vienna. http://epub.wu.ac.at/4077/1/Report125.pdf

Gueorguieva, Ralitza, Robert Rosenheck, and Daniel Zelterman (2008). Dirichlet component regression and its applications to psychiatric data. Computational statistics & data analysis 52(12): 5344-5355.

Ng Kai Wang, Guo-Liang Tian and Man-Lai Tang (2011). Dirichlet and related distributions: Theory, methods and applications. John Wiley & Sons.

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
js.compreg, kl.compreg, ols.compreg, comp.reg, alfa.reg, diri.nr, dda
```

Examples

```
x <- as.vector(iris[, 4])
y <- as.matrix(iris[, 1:3])
y <- y / rowSums(y)
mod1 <- diri.reg(y, x)
mod2 <- diri.reg2(y, x)
mod3 <- comp.reg(y, x)</pre>
```

Distance based regression models for proportions

Distance based regression models for proportions

Description

Distance based regression models for proportions.

Usage

```
ols.prop.reg(y, x, cov = FALSE, tol = 1e-07, maxiters = 100)
helling.prop.reg(y, x, tol = 1e-07, maxiters = 100)
```

Arguments

У	A numerical vector proportions. 0s and 1s are allowed.
X	A matrix or a data frame with the predictor variables.
cov	Should the covariance matrix be returned? TRUE or FALSE.
tol	The tolerance value to terminate the Newton-Raphson algorithm. This is set to 10^{-9} by default.
maxiters	The maximum number of iterations before the Newton-Raphson is terminated automatically.

Details

We are using the Newton-Raphson, but unlike R's built-in function "glm" we do no checks and no extra calculations, or whatever. Simply the model. The functions accept binary responses as well (0 or 1).

Value

A list including:

sse	The sum of squres of errors for the "ols.prop.reg" function.
be	The estimated regression coefficients.
seb	The standard error of the regression coefficients if "cov" is TRUE.
covb	The covariance matrix of the regression coefficients in "ols.prop.reg" if "cov" is TRUE.
Н	The Hellinger distance between the true and the obseervd proportions in "helling.prop.reg".
iters	The number of iterations required by the Newton-Raphson.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Papke L. E. & Wooldridge J. (1996). Econometric methods for fractional response variables with an application to 401(K) plan participation rates. Journal of Applied Econometrics, 11(6): 619–632.

McCullagh, Peter, and John A. Nelder. Generalized linear models. CRC press, USA, 2nd edition, 1989.

See Also

```
propreg, beta.reg
```

Examples

```
y <- rbeta(100, 1, 4)
x <- matrix(rnorm(100 * 2), ncol = 2)
a1 <- ols.prop.reg(y, x)
a2 <- helling.prop.reg(y, x)</pre>
```

Divergence based regression for compositional data

Divergence based regression for compositional data

Description

Regression for compositional data based on the Kullback-Leibler the Jensen-Shannon divergence and the symmetric Kullback-Leibler divergence.

Usage

```
kl.compreg(y, x, con = TRUE, B = 1, ncores = 1, xnew = NULL, tol = 1e-07, maxiters = 50)
js.compreg(y, x, con = TRUE, B = 1, ncores = 1, xnew = NULL)
tv.compreg(y, x, con = TRUE, B = 1, ncores = 1, xnew = NULL)
symkl.compreg(y, x, con = TRUE, B = 1, ncores = 1, xnew = NULL)
```

Arguments

У	A matrix with the compositional data (dependent variable). Zero values are allowed.
X	The predictor variable(s), they can be either continuous or categorical or both.
con	If this is TRUE (default) then the constant term is estimated, otherwise the model includes no constant term.
В	If B is greater than 1 bootstrap estimates of the standard error are returned. If B=1, no standard errors are returned.
ncores	If ncores is 2 or more parallel computing is performed. This is to be used for the case of bootstrap. If B=1, this is not taken into consideration.
xnew	If you have new data use it, otherwise leave it NULL.
tol	The tolerance value to terminate the Newton-Raphson procedure.
maxiters	The maximum number of Newton-Raphson iterations.

Details

In the kl.compreg() the Kullback-Leibler divergence is adopted as the objective function. In case of problematic convergence the "multinom" function by the "nnet" package is employed. This will obviously be slower. The js.compreg() uses the Jensen-Shannon divergence and the symkl.compreg() uses the symmetric Kullback-Leibler divergence. The tv.compreg() uses the Total Variation divergence. There is no actual log-likelihood for the last three regression models.

Value

A list including:

runtime The time required by the regression.

iters	The number of iterations required by the Newton-Raphson in the kl.compreg function.
loglik	The log-likelihood. This is actually a quasi multinomial regression. This is bascially half the negative deviance, or $-\sum_{i=1}^n y_i \log y_i/\hat{y}_i$.
be	The beta coefficients.
covbe	The covariance matrix of the beta coefficients, if bootstrap is chosen, i.e. if $B > 1$.
est	The fitted values of xnew if xnew is not NULL.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Giorgos Athineou <gioathineou@gmail.com>.

References

Murteira, Jose MR, and Joaquim JS Ramalho 2016. Regression analysis of multivariate fractional data. Econometric Reviews 35(4): 515-552.

Tsagris, Michail (2015). A novel, divergence based, regression for compositional data. Proceedings of the 28th Panhellenic Statistics Conference, 15-18/4/2015, Athens, Greece. https://arxiv.org/pdf/1511.07600.pdf

Endres, D. M. and Schindelin, J. E. (2003). A new metric for probability distributions. Information Theory, IEEE Transactions on 49, 1858-1860.

Osterreicher, F. and Vajda, I. (2003). A new class of metric divergences on probability spaces and its applicability in statistics. Annals of the Institute of Statistical Mathematics 55, 639-653.

See Also

```
diri.reg, ols.compreg, comp.reg
```

Examples

```
library(MASS)
x <- as.vector(fgl[, 1])
y <- as.matrix(fgl[, 2:9])
y <- y / rowSums(y)
mod1<- kl.compreg(y, x, B = 1, ncores = 1)
mod2 <- js.compreg(y, x, B = 1, ncores = 1)</pre>
```

```
Divergence
                                   for
                                                                 with
             based
                     regression
                                         compositional
                                                          data
                                                         using
compositional
                data
                        in
                              the
                                    covariates
                                                  side
                                                                  the
alpha-transformation
```

Divergence based regression for compositional data with compositional data in the covariates side using the α -transformation

Description

Divergence based regression for compositional data with compositional data in the covariates side using the α -transformation.

Usage

```
kl.alfapcr(y, x, covar = NULL, a, k, xnew = NULL, B = 1, ncores = 1, tol = 1e-07, maxiters = 50)
```

Arguments

У	A numerical matrixc with compositional data with or without zeros.
х	A matrix with the predictor variables, the compositional data. Zero values are allowed.
covar	If you have other covariates as well put themn here.
a	The value of the power transformation, it has to be between -1 and 1. If zero values are present it has to be greater than 0. If $\alpha=0$ the isometric log-ratio transformation is applied.
k	A number at least equal to 1. How many principal components to use.
xnew	A matrix containing the new compositional data whose response is to be predicted. If you have no new data, leave this NULL as is by default.
В	If B is greater than 1 bootstrap estimates of the standard error are returned. If $B=1$, no standard errors are returned.
ncores	If ncores is 2 or more parallel computing is performed. This is to be used for the case of bootstrap. If B=1, this is not taken into consideration.
tol	The tolerance value to terminate the Newton-Raphson procedure.
maxiters	The maximum number of Newton-Raphson iterations.

Details

The α -transformation is applied to the compositional data first, the first k principal component scores are calcualted and used as predictor variables for the Kullback-Leibler divergence based regression model.

72Divergence based regression for compositional data with compositional data in the covariates side using the alpha-transformatio

Value

A list including:

runtime	The time required by the regression.
iters	The number of iterations required by the Newton-Raphson in the kl.compreg function.
loglik	The log-likelihood. This is actually a quasi multinomial regression. This is bascially minus the half deviance, or $-sum_{i=1}^n y_i \log y_i/\hat{y}_i$.
be	The beta coefficients.
seb	The standard error of the beta coefficients, if bootstrap is chosen, i.e. if $B > 1$.
est	The fitted values of xnew if xnew is not NULL.

Author(s)

Initial code by Abdulaziz Alenazi. Modifications by Michail Tsagris.

R implementation and documentation: Abdulaziz Alenazi <a.alenazi@nbu.edu.sa> and Michail Tsagris <mtsagris@uoc.gr>.

References

Alenazi A. (2019). Regression for compositional data with compositional data as predictor variables with or without zero values. Journal of Data Science, 17(1): 219-238. https://jds-online.org/journal/JDS/article/136/file/pdf

Tsagris M. (2015). Regression analysis with compositional data containing zero values. Chilean Journal of Statistics, 6(2): 47-57. http://arxiv.org/pdf/1508.01913v1.pdf

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. http://arxiv.org/pdf/1106.1451.pdf

See Also

```
klalfapcr.tune, tflr, glm.pcr, alfapcr.tune
```

Examples

```
library(MASS)
y <- rdiri(214, runif(4, 1, 3))
x <- as.matrix(fgl[, 2:9])
x <- x / rowSums(x)
mod <- alfa.pcr(y = y, x = x, a = 0.7, k = 1)
mod</pre>
```

Divergence matrix of compositional data

Divergence matrix of compositional data

Description

Divergence matrix of compositional data.

Usage

```
divergence(x, type = "kullback_leibler", vector = FALSE)
```

Arguments

x A matrix with the compositional data.

type This is either "kullback_leibler" (Kullback-Leibler, which computes the sym-

metric Kullback-Leibler divergence) or "jensen_shannon" (Jensen-Shannon) di-

vergence.

vector For return a vector instead a matrix.

Details

The function produces the distance matrix either using the Kullback-Leibler (distance) or the Jensen-Shannon (metric) divergence. The Kullback-Leibler refers to the symmetric Kullback-Leibler divergence.

Value

if the vector argument is FALSE a symmetric matrix with the divergences, otherwise a vector with the divergences.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Endres, D. M. and Schindelin, J. E. (2003). A new metric for probability distributions. Information Theory, IEEE Transactions on 49, 1858-1860.

Osterreicher, F. and Vajda, I. (2003). A new class of metric divergences on probability spaces and its applicability in statistics. Annals of the Institute of Statistical Mathematics 55, 639-653.

See Also

```
comp.knn, js.compreg
```

Examples

```
x <- as.matrix(iris[1:20, 1:4])
x <- x / rowSums(x)
divergence(x)</pre>
```

```
Energy test of equality of distributions using the alpha-transformation
```

Energy test of equality of distributions using the α -transformation

Description

Energy test of equality of distributions using the α -transformation.

Usage

```
aeqdist.etest(x, sizes, a = 1, R = 999)
```

Arguments

X	A matrix with the compositional data with all groups stacked one under the other.
sizes	A numeric vector matrix with the sample sizes.
a	The value of the power transformation, it has to be between -1 and 1. If zero values are present it has to be greater than 0. If $\alpha=0$ the isometric log-ratio transformation is applied. If more than one values are supplied the energy distance of equality of distributions is applied for each value of α .
R	The number of permutations to apply in order to compute the approximate p-value.

Details

The α -transformation is applied to each composition and then the energy distance of equality of distributions is applied for each value of α or for the single value of α .

Value

A numerical value or a numerical vector, depending on the length of the values of α , with the approximate p-value(s) of the energy test.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Szekely, G. J. and Rizzo, M. L. (2004) Testing for Equal Distributions in High Dimension. InterStat, November (5).

Szekely, G. J. (2000) Technical Report 03-05: E-statistics: Energy of Statistical Samples. Department of Mathematics and Statistics, Bowling Green State University.

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. https://arxiv.org/pdf/1106.1451.pdf

See Also

```
acor, acor.tune, alfa, alfa.profile
```

Examples

```
y \leftarrow rdiri(50, c(3, 4, 5))

x \leftarrow rdiri(60, c(3, 4, 5))

aeqdist.etest( rbind(x, y), c(dim(x)[1], dim(y)[1]), a = c(-1, 0, 1))
```

Estimating location and scatter parameters for compositional data

Estimating location and scatter parameters for compositional data

Description

Estimating location and scatter parameters for compositional data in a robust and non robust way.

Usage

```
comp.den(x, type = "alr", dist = "normal", tol = 1e-07)
```

Arguments

X	A matrix containing compositional data. No zero values are allowed.
type	A boolean variable indicating the transformation to be used. Either "alr" or "ilr" corresponding to the additive or the isometric log-ratio transformation respectively.
dist	Takes values "normal", "t", "skewnorm", "rob" and "spatial". They first three options correspond to the parameters of the normal, t and skew normal distribution respectively. If it set to "rob" the MCD estimates are computed and if set to "spatial" the spatial median and spatial sign covariance matrix are computed.
tol	A tolerance level to terminate the process of finding the spatial median when dist = "spatial". This is set to 1e-09 by default.

Details

This function calculates robust and non robust estimates of location and scatter.

Value

A list including: The mean vector and covariance matrix mainly. Other parameters are also returned depending on the value of the argument "dist".

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

P. J. Rousseeuw and K. van Driessen (1999) A fast algorithm for the minimum covariance determinant estimator. Technometrics 41, 212-223.

Mardia K.V., Kent J.T., and Bibby J.M. (1979). Multivariate analysis. Academic press.

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

T. Karkkaminen and S. Ayramo (2005). On computation of spatial median for robust data mining. Evolutionary and Deterministic Methods for Design, Optimization and Control with Applications to Industrial and Societal Problems EUROGEN 2005.

A Durre, D Vogel, DE Tyler (2014). The spatial sign covariance matrix with unknown location. Journal of Multivariate Analysis, 130: 107-117.

J. T. Kent, D. E. Tyler and Y. Vardi (1994) A curious likelihood identity for the multivariate t-distribution. Communications in Statistics-Simulation and Computation 23, 441-453.

Azzalini A. and Dalla Valle A. (1996). The multivariate skew-normal distribution. Biometrika 83(4): 715-726.

See Also

```
spatmed.reg, multivt
```

```
library(MASS)
x <- as.matrix(iris[, 1:4])
x <- x / rowSums(x)
comp.den(x)
comp.den(x, type = "alr", dist = "t")
comp.den(x, type = "alr", dist = "spatial")</pre>
```

Estimation of the probability left outside the simplex when using the alpha-transformation

Estimation of the probability left outside the simplex when using the alpha-transformation

Description

Estimation of the probability left outside the simplex when using the alpha-transformationn.

Usage

```
probout(mu, su, a)
```

Arguments

mu	The mean vector.
su	The covariance matrix.
а	The value of α .

Details

When applying the α -transformation based on a multivariate normal there might be probability left outside the simplex as the space of this transformation is a subspace of the Euclidean space. The function estimates the missing probability via Monte Carlo simulation using 40 million generated vectors.

Value

The estimated probability left outside the simplex.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Tsagris M. and Stewart C. (2020). A folded model for compositional data analysis. Australian and New Zealand Journal of Statistics, 62(2): 249-277. https://arxiv.org/pdf/1802.07330.pdf

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. https://arxiv.org/pdf/1106.1451.pdf

See Also

```
alfa, alpha.mle, a.est, rfolded
```

Examples

Estimation of the value of alpha in the folded model Estimation of the value of α in the folded model

Description

Estimation of the value of α in the folded model.

Usage

a.est(x)

Arguments

X

A matrix with the compositional data. No zero vaues are allowed.

Details

This is a function for choosing or estimating the value of α in the folded model (Tsagris and Stewart, 2020).

Value

A list including:

runtime The runtime of the algorithm.

best The estimated optimal α of the folded model.

loglik The maximimised log-likelihood of the folded model.

p The estimated probability inside the simplex of the folded model.

mu The estimated mean vector of the folded model.

su The estimated covariance matrix of the folded model.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Tsagris M. and Stewart C. (2022). A Review of Flexible Transformations for Modeling Compositional Data. In Advances and Innovations in Statistics and Data Science, pp. 225–234. https://link.springer.com/chapter/10.103-031-08329-7_10

Tsagris M. and Stewart C. (2020). A folded model for compositional data analysis. Australian and New Zealand Journal of Statistics, 62(2): 249-277. https://arxiv.org/pdf/1802.07330.pdf

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. https://arxiv.org/pdf/1106.1451.pdf

See Also

```
alfa.profile, alfa, alfainv, alpha.mle
```

Examples

```
x <- as.matrix(iris[, 1:4])
x <- x / rowSums(x)
alfa.tune(x)
a.est(x)</pre>
```

Estimation of the value of alpha via the profile log-likelihood Estimation of the value of α via the alfa profile log-likelihood

Description

Estimation of the value of α via the alfa profile log-likelihood.

Usage

```
alfa.profile(x, a = seq(-1, 1, by = 0.01))
```

Arguments

- x A matrix with the compositional data. Zero values are not allowed.
- a A grid of values of α .

Details

For every value of α the normal likelihood (see the reference) is computed. At the end, the plot of the values is constructed.

Value

A list including:

res The chosen value of α , the corresponding log-likelihood value and the log-

likelihood when $\alpha = 0$.

ci An asympotic 95% confidence interval computed from the log-likelihood ratio

test.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Giorgos Athineou <gioathineou@gmail.com>.

References

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. https://arxiv.org/pdf/1106.1451.pdf

See Also

```
alfa.tune, alfa, alfainv
```

Examples

```
x <- as.matrix(iris[, 1:4])
x <- x / rowSums(x)
alfa.tune(x)
alfa.profile(x)</pre>
```

Fast estimation of the value of alpha ${\it Fast\ estimation\ of\ the\ value\ of\ }\alpha$

Description

Fast estimation of the value of α .

Usage

```
alfa.tune(x, B = 1, ncores = 1)
```

Arguments

x A matrix with the compositional data. No zero vaues are allo	wed.
--	------

B If no (bootstrap based) confidence intervals should be returned this should be 1

and more than 1 otherwise.

ncores If ncores is greater than 1 parallel computing is performed. It is advisable to use

it if you have many observations and or many variables, otherwise it will slow

down th process.

Details

This is a faster function than alfa.profile for choosing the value of α .

Value

A vector with the best alpha, the maximised log-likelihood and the log-likelihood at $\alpha = 0$, when B = 1 (no bootstrap). If B>1 a list including:

param The best alpha and the value of the log-likelihod, along with the 95% bootstrap

based confidence intervals.

message A message with some information about the histogram.

runtime The time (in seconds) of the process.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Giorgos Athineou <gioathineou@gmail.com>.

References

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. https://arxiv.org/pdf/1106.1451.pdf

See Also

```
alfa.profile, alfa, alfainv
```

```
library(MASS)
x <- as.matrix(iris[, 1:4])
x <- x / rowSums(x)
alfa.tune(x)
alfa.profile(x)</pre>
```

Gaussian mixture models for compositional data

Gaussian mixture models for compositional data

Description

Gaussian mixture models for compositional data.

Usage

```
mix.compnorm(x, g, model, type = "alr", veo = FALSE)
```

Arguments

x A matrix with the compositional data.

g How many clusters to create.

model The type of model to be used.

- 1. "EII": All groups have the same diagonal covariance matrix, with the same variance for all variables.
- 2. "VII": Different diagonal covariance matrices, with the same variance for all variables within each group.
- 3. "EEI": All groups have the same diagonal covariance matrix.
- 4. "VEI": Different diagonal covariance matrices. If we make all covariance matrices have determinant 1, (divide the matrix with the \$p\$-th root of its determinant) then all covariance matrices will be the same.
- 5. "EVI": Different diagonal covariance matrices with the same determinant.
- 6. "VVI": Different diagonal covariance matrices, with nothing in common.
- 7. "EEE": All covariance matrices are the same.
- 8. "EEV": Different covariance matrices, but with the same determinant and in addition, if we make them have determinant 1, they will have the same trace.
- 9. "VEV": Different covariance matrices but if we make the matrices have determinant 1, then they will have the same trace.
- 10. "VVV": Different covariance matrices with nothing in common.
- 11. "EVE": Different covariance matrices, but with the same determinant. In addition, calculate the eigenvectors for each covariance matrix and you will see the extra similarities.
- 12. "VVE": Different covariance matrices, but they have something in common with their directions. Calculate the eigenvectors of each covariance matrix and you will see the similarities.
- 13. "VEE": Different covariance matrices, but if we make the matrices have determinant 1, then they will have the same trace. In addition, calculate the eigenvectors for each covariance matrix and you will see the extra similarities.

14. "EVV": Different covariance matrices, but with the same determinant.

type The type of trasformation to be used, either the additive log-ratio ("alr"), the

isometric log-ratio ("ilr") or the pivot coordinate ("pivot") transformation.

veo Stands for "Variables exceed observations". If TRUE then if the number vari-

ablesin the model exceeds the number of observations, but the model is still

fitted.

Details

A log-ratio transformation is applied and then a Gaussian mixture model is constructed.

Value

A list including:

mu A matrix where each row corresponds to the mean vector of each cluster.

su An array containing the covariance matrix of each cluster.

prob The estimated mixing probabilities.

est The estimated cluster membership values.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Ryan P. Browne, Aisha ElSherbiny and Paul D. McNicholas (2015). R package mixture: Mixture Models for Clustering and Classification.

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
bic.mixcompnorm, rmixcomp, mix.compnorm.contour, alfa.mix.norm,alfa.knn,alfa.rda,
comp.nb
```

```
x <- as.matrix(iris[, 1:4])
x <- x/ rowSums(x)
mod1 <- mix.compnorm(x, 3, model = "EII" )
mod2 <- mix.compnorm(x, 4, model = "VII")</pre>
```

Gaussian mixture models for compositional data using the alpha-transformation

Gaussian mixture models for compositional data using the α -transformation

Description

Gaussian mixture models for compositional data using the α -transformation.

Usage

```
alfa.mix.norm(x, g, a, model, veo = FALSE)
```

Arguments

- x A matrix with the compositional data.
- g How many clusters to create.
- The value of the power transformation, it has to be between -1 and 1. If zero values are present it has to be greater than 0. If $\alpha=0$ the isometric log-ratio transformation is applied.

model

The type of model to be used.

- 1. "EII": All groups have the same diagonal covariance matrix, with the same variance for all variables.
- 2. "VII": Different diagonal covariance matrices, with the same variance for all variables within each group.
- 3. "EEI": All groups have the same diagonal covariance matrix.
- 4. "VEI": Different diagonal covariance matrices. If we make all covariance matrices have determinant 1, (divide the matrix with the \$p\$-th root of its determinant) then all covariance matrices will be the same.
- 5. "EVI": Different diagonal covariance matrices with the same determinant.
- 6. "VVI": Different diagonal covariance matrices, with nothing in common.
- 7. "EEE": All covariance matrices are the same.
- 8. "EEV": Different covariance matrices, but with the same determinant and in addition, if we make them have determinant 1, they will have the same trace.
- 9. "VEV": Different covariance matrices but if we make the matrices have determinant 1, then they will have the same trace.
- 10. "VVV": Different covariance matrices with nothing in common.
- 11. "EVE": Different covariance matrices, but with the same determinant. In addition, calculate the eigenvectors for each covariance matrix and you will see the extra similarities.
- 12. "VVE": Different covariance matrices, but they have something in common with their directions. Calculate the eigenvectors of each covariance matrix and you will see the similarities.

- 13. "VEE": Different covariance matrices, but if we make the matrices have determinant 1, then they will have the same trace. In addition, calculate the eigenvectors for each covariance matrix and you will see the extra similarities.
- 14. "EVV": Different covariance matrices, but with the same determinant.

veo

Stands for "Variables exceed observations". If TRUE then if the number variablesin the model exceeds the number of observations, but the model is still fitted.

Details

A log-ratio transformation is applied and then a Gaussian mixture model is constructed.

Value

A list including:

mu A matrix where each row corresponds to the mean vector of each cluster.

su An array containing the covariance matrix of each cluster.

prob The estimated mixing probabilities.

est The estimated cluster membership values.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Ryan P. Browne, Aisha ElSherbiny and Paul D. McNicholas (2015). R package mixture: Mixture Models for Clustering and Classification.

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. https://arxiv.org/pdf/1106.1451.pdf

See Also

```
bic.alfamixnorm, bic.mixcompnorm, rmixcomp, mix.compnorm.contour, mix.compnorm, alfa, alfa.knn, alfa.rda, comp.nb
```

```
x <- as.matrix(iris[, 1:4])
x <- x/ rowSums(x)
mod1 <- alfa.mix.norm(x, 3, 0.4, model = "EII" )
mod2 <- alfa.mix.norm(x, 4, 0.7, model = "VII")</pre>
```

Generalised Dirichlet random values simulation

Generalised Dirichlet random values simulation

Description

Generalised Dirichlet random values simulation.

Usage

```
rgendiri(n, a, b)
```

Arguments

- n The sample size, a numerical value.
- a A numerical vector with the shape parameter values of the Gamma distribution.
- b A numerical vector with the scale parameter values of the Gamma distribution.

Details

The algorithm is straightforward, for each vector, independent gamma values are generated and then divided by their total sum. The difference with rdiri is that here the Gamma distributed variables are not equally scaled.

Value

A matrix with the simulated data.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Ng Kai Wang, Guo-Liang Tian and Man-Lai Tang (2011). Dirichlet and related distributions: Theory, methods and applications. John Wiley & Sons.

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
rdiri, diri.est, diri.nr, diri.contour
```

```
a <- c(1, 2, 3)
b <- c(2, 3, 4)
x <- rgendiri(100, a, b)
```

Generate random folds for cross-validation

Generate random folds for cross-validation

Description

Random folds for use in a cross validation are generated. There is the option for stratified splitting as well.

Usage

```
makefolds(ina, nfolds = 10, stratified = TRUE, seed = NULL)
```

Arguments

ina A variable indicating the groupings.nfolds The number of folds to produce.

stratified A boolean variable specifying whether stratified random (TRUE) or simple ran-

dom (FALSE) sampling is to be used when producing the folds.

seed You can specify your own seed number here or leave it NULL.

Details

I was inspired by the command in the package TunePareto in order to do the stratified version.

Value

A list with nfolds elements where each elements is a fold containing the indices of the data.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

See Also

```
compknn.tune
```

```
a <- makefolds(iris[, 5], nfolds = 5, stratified = TRUE)
table(iris[a[[1]], 5]) ## 10 values from each group</pre>
```

```
Greenacre's power transformation
```

Greenacre's power transformation

Description

Greenacre's power transformation.

Usage

```
green(x, theta)
```

Arguments

x A matrix with the compositional data.

theta The value of the power transformation, it has to be between -1 and 1. If zero

values are present it has to be greater than 0. If $\theta = 0$ the log transformation is

applied.

Details

Greenacre's transformation is applied to the compositional data.

Value

A matrix with the power transformed data.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Greenacre, M. (2009). Power transformations in correspondence analysis. Computational Statistics & Data Analysis, 53(8): 3107-3116. http://www.econ.upf.edu/~michael/work/PowerCA.pdf

See Also

alfa

```
library(MASS)
x <- as.matrix(fgl[, 2:9])
x <- x / rowSums(x)
y1 <- green(x, 0.1)
y2 <- green(x, 0.2)
rbind( colMeans(y1), colMeans(y2) )</pre>
```

Helper Frechet mean for compositional data Helper Frechet mean for compositional data

Description

Helper Frechet mean for compositional data.

Usage

```
frechet2(x, di, a, k)
```

Arguments

Х	A matrix with the compositional data.
di	A matrix with indices as produced by the function "dista" of the package "Rfast"" or the function "nn" of the package "Rnanoflann". Better see the details section.
a	The value of the power transformation, it has to be between -1 and 1. If zero values are present it has to be greater than 0. If $\alpha=0$ the isometric log-ratio transformation is applied and the closed geometric mean is calculated.
k	The number of nearest neighbours used for the computation of the Frechet means.

Details

The power transformation is applied to the compositional data and the mean vector is calculated. Then the inverse of it is calculated and the inverse of the power transformation applied to the last vector is the Frechet mean.

What this helper function do is to speed up the Frechet mean when used in the α -k-NN regression. The α -k-NN regression computes the Frechet mean of the k nearest neighbours for a value of α and this function does exactly that. Suppose you want to predict the compositional value of some new predictors. For each predictor value you must use the Frechet mean computed at various nearest neighbours. This function performs these computations in a fast way. It is not the fastest way, yet it is a pretty fast way. This function is being called inside the function aknn.reg.

Value

A list where eqch element contains a matrix. Each matrix contains the Frechet means computed at various nearest neighbours.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. https://arxiv.org/pdf/1106.1451.pdf

See Also

```
alfa, alfainv, profile
```

Examples

```
library(MASS)
library(Rfast)
x <- as.matrix(fgl[, 2:9])
x <- x / rowSums(x)
xnew <- x[1:10, ]
x <- x[-c(1:10), ]
k <- 2:5
di <- Rfast::dista( xnew, x, k = max(k), index = TRUE, square = TRUE )
est <- frechet2(x, di, 0.2, k)</pre>
```

Helper functions for the Kullback-Leibler regression $Helper\ functions\ for\ the\ Kullback-Leibler\ regression$

Description

Helper functions for the Kullback-Leibler regression.

Usage

```
kl.compreg2(y, x, con = TRUE, xnew = NULL, tol = 1e-07, maxiters = 50)
klcompreg.boot(y, x, der, der2, id, b1, n, p, d, tol = 1e-07, maxiters = 50)
```

Arguments

У	A matrix with the compositional data (dependent variable). Zero values are allowed. For the klcompreg.boot the first column is removed.
x	The predictor variable(s), they can be either continuous or categorical or both. In the klcompreg.boot this is the design matrix.
con	If this is TRUE (default) then the constant term is estimated, otherwise the model includes no constant term.
xnew	If you have new data use it, otherwise leave it NULL.
tol	The tolerance value to terminate the Newton-Raphson procedure.
maxiters	The maximum number of Newton-Raphson iterations.

der	An vector to put the first derivative there.
der2	An empty matrix to put the second derivatives there, the Hessian matrix will be put here.
id	A help vector with indices.
b1	The matrix with the initial estimated coefficients.
n	The sample size
р	The number of columns of the design matrix.
d	The dimensionality of the simplex, that is the number of columns of the compositional data minus 1.

Details

These are help functions for the kl.compreg function. They are not to be called directly by the user.

Value

For kl.compreg2 a list including:

iters The nubmer of iterations required by the Newton-Raphson.

loglik The loglikelihood.
be The beta coefficients.

est The fitted or the predicted values (if xnew is not NULL).

For klcompreg.boot a list including:

loglik The loglikelihood.
be The beta coefficients.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Murteira, Jose MR, and Joaquim JS Ramalho 2016. Regression analysis of multivariate fractional data. Econometric Reviews 35(4): 515-552.

See Also

```
diri.reg, js.compreg, ols.compreg, comp.reg
```

Examples

```
library(MASS)
x <- as.vector(fgl[, 1])
y <- as.matrix(fgl[, 2:9])
y <- y / rowSums(y)
mod1<- kl.compreg(y, x, B = 1, ncores = 1)
mod2 <- js.compreg(y, x, B = 1, ncores = 1)</pre>
```

Hypothesis testing for two or more compositional mean vectors

Hypothesis testing for two or more compositional mean vectors

Description

Hypothesis testing for two or more compositional mean vectors.

Usage

```
comp.test(x, ina, test = "james", R = 0, ncores = 1, graph = FALSE)
```

Arguments

guinents	
Х	A matrix containing compositional data.
ina	A numerical or factor variable indicating the groups of the data.
test	This can take the values of "james" for James' test, "hotel" for Hotelling's test, "maov" for multivariate analysis of variance assuming equality of the covariance matrices, "maovjames" for multivariate analysis of variance without assuming equality of the covariance matrices. "el" for empirical likelihood or "eel" for exponential empirical likelihood.
R	This depends upon the value of the argument "test". If the test is "maov" or "maovjames", R is not taken into consideration. If test is "hotel", then R denotes the number of bootstrap resamples. If test is "james", then R can be 1 (chi-square distribution), 2 (F distribution), or more for bootstrap calibration. If test is "el", then R can be 0 (chi-square), 1 (corrected chi-square), 2 (F distribution) or more for bootstrap calibration. See the help page of each test for more information.
ncores	How many to cores to use. This is taken into consideration only if test is "el" and R is more than 2.
graph	A boolean variable which is taken into consideration only when bootstrap calibration is performed. IF TRUE the histogram of the bootstrap test statistic values

Details

The idea is to apply the α -transformation, with $\alpha=1$, to the compositional data and then use a test to compare their mean vectors. See the help page of each test for more information. The function is visible so you can see exactly what is going on.

is plotted. This is taken into account only when R is greater than 2.

Value

A list including:

result

The outcome of each test.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Giorgos Athineou <gioathineou@gmail.com>.

References

Tsagris M., Preston S. and Wood A.T.A. (2017). Nonparametric hypothesis testing for equality of means on the simplex. Journal of Statistical Computation and Simulation, 87(2): 406-422.

G.S. James (1954). Tests of Linear Hypothese in Univariate and Multivariate Analysis when the Ratios of the Population Variances are Unknown. Biometrika, 41(1/2): 19-43

Krishnamoorthy K. and Yanping Xia (2006). On Selecting Tests for Equality of Two Normal Mean Vectors. Multivariate Behavioral Research 41(4): 533-548.

Owen A. B. (2001). Empirical likelihood. Chapman and Hall/CRC Press.

Owen A.B. (1988). Empirical likelihood ratio confidence intervals for a single functional. Biometrika 75(2): 237-249.

Amaral G.J.A., Dryden I.L. and Wood A.T.A. (2007). Pivotal bootstrap methods for k-sample problems in directional statistics and shape analysis. Journal of the American Statistical Association 102(478): 695-707.

Preston S.P. and Wood A.T.A. (2010). Two-Sample Bootstrap Hypothesis Tests for Three-Dimensional Labelled Landmark Data. Scandinavian Journal of Statistics 37(4): 568-587.

Jing Bing-Yi and Andrew TA Wood (1996). Exponential empirical likelihood is not Bartlett correctable. Annals of Statistics 24(1): 365-369.

See Also

hd.meantest2, dptest

```
ina <- rep(1:2, each = 50)
x <- as.matrix(iris[1:100, 1:4])
x <- x/ rowSums(x)
comp.test( x, ina, test = "james" )
comp.test( x, ina, test = "hotel" )
comp.test( x, ina, test = "el" )
comp.test( x, ina, test = "eel" )</pre>
```

ICE plot for projection pursuit regression with compositional predictor variables

ICE plot for projection pursuit regression with compositional predictor variables

Description

ICE plot for projection pursuit regression with compositional predictor variables.

Usage

```
ice.pprcomp(model, x, k = 1, frac = 0.1, type = "log")
```

Arguments

 $\begin{tabular}{ll} model & The ppr model, the outcome of the $pprcomp$ function. \\ \end{tabular}$

x A matrix with the compositional data. No zero values are allowed.

k Which variable to select?.

frac Fraction of observations to use. The default value is 0.1.

type Either "alr" or "log" corresponding to the additive log-ratio transformation or

the simple logarithm applied to the compositional data.

Details

This function implements the Individual Conditional Expectaion plots of Goldstein et al. (2015). See the references for more details.

Value

A graph with several curves. The horizontal axis contains the selected variable, whereas the vertical axis contains the centered predicted values. The black curves are the effects for each observation and the blue line is their average effect.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

https://christophm.github.io/interpretable-ml-book/ice.html

Goldstein, A., Kapelner, A., Bleich, J. and Pitkin, E. (2015). Peeking inside the black box: Visualizing statistical learning with plots of individual conditional expectation. Journal of Computational and Graphical Statistics 24(1): 44-65.

Friedman, J. H. and Stuetzle, W. (1981). Projection pursuit regression. Journal of the American Statistical Association, 76, 817-823. doi: 10.2307/2287576.

See Also

```
pprcomp, pprcomp.tune, ice.kernreg, alfa.pcr, lc.reg, comp.ppr
```

Examples

```
x <- as.matrix( iris[, 2:4] )
x <- x/ rowSums(x)
y <- iris[, 1]
model <- pprcomp(y, x)
ice <- ice.pprcomp(model, x, k = 1)</pre>
```

```
ICE plot for the alpha-k-NN regression {\it ICE\ plot\ for\ the\ } \alpha-k-NN\ {\it regression}
```

Description

ICE plot for the $\alpha - k - NN$ regression.

Usage

```
ice.aknnreg(y, x, a, k, apostasi = "euclidean", rann = FALSE,
ind = 1, frac = 0.2, qpos = 0.9)
```

Arguments

у	A numerical vector with the response values.
x	A numerical matrix with the predictor variables.
a	The value α to consider.
k	The number of nearest neighbours to consider.
apostasi	The type of distance to use, either "euclidean" or "manhattan".
rann	If you have large scale datasets and want a faster k-NN search, you can use kd- trees implemented in the R package "Rnanoflann". In this case you must set this argument equal to TRUE. Note however, that in this case, the only available distance is by default "euclidean".
ind	Which variable to select?.
frac	Fraction of observations to use. The default value is 0.1.
qpos	A number between 0.8 and 1. This is used to place the legend of the figure better. You can play with it. In the worst case scenario the code is open and you tweak this argument as you prefer.

Details

This function implements the Individual Conditional Expectaion plots of Goldstein et al. (2015). See the references for more details.

Value

A graph with several curves, one for each component. The horizontal axis contains the selected variable, whereas the vertical axis contains the locally smoothed predicted compositional lines.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

https://christophm.github.io/interpretable-ml-book/ice.html

Goldstein, A., Kapelner, A., Bleich, J. and Pitkin, E. (2015). Peeking inside the black box: Visualizing statistical learning with plots of individual conditional expectation. Journal of Computational and Graphical Statistics 24(1): 44-65.

See Also

```
ice.akernreg, ice.pprcomp
```

Examples

```
y <- as.matrix( iris[, 2:4] )</pre>
x <- iris[, 1]
ice \leftarrow ice.aknnreg(y, x, a = 0.6, k = 5, ind = 1)
```

```
ICE plot for the alpha-kernel regression
                          ICE plot for the \alpha-kernel regression
```

Description

ICE plot for the α -kernel regression.

Usage

```
ice.akernreg(y, x, a, h, type = "gauss", ind = 1, frac = 0.1, qpos = 0.9)
```

Arguments

У	A numerical vector with the response values.
X	A numerical matrix with the predictor variables.
а	The value α to consider.

The bandwidth value to consider.

The type of kernel to use, "gauss" or "laplace". type

• 1	***** 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
ind	Which variable to select?.

frac Fraction of observations to use. The default value is 0.1.

qpos A number between 0.8 and 1. This is used to place the legend of the figure better.

You can play with it. In the worst case scenario the code is open and you tweak

this argument as you prefer.

Details

This function implements the Individual Conditional Expectaion plots of Goldstein et al. (2015). See the references for more details.

Value

A graph with several curves, one for each component. The horizontal axis contains the selected variable, whereas the vertical axis contains the locally smoothed predicted compositional lines.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

https://christophm.github.io/interpretable-ml-book/ice.html

Goldstein, A., Kapelner, A., Bleich, J. and Pitkin, E. (2015). Peeking inside the black box: Visualizing statistical learning with plots of individual conditional expectation. Journal of Computational and Graphical Statistics 24(1): 44-65.

See Also

```
ice.aknnreg, ice.pprcomp
```

Examples

```
y <- as.matrix( iris[, 2:4] )
x <- iris[, 1]
ice <- ice.akernreg(y, x, a = 0.6, h = 0.1, ind = 1)</pre>
```

ICE plot for univariate kernel regression

ICE plot for univariate kernel regression

Description

ICE plot for univariate kernel regression.

Usage

```
ice.kernreg(y, x, h, type = "gauss", k = 1, frac = 0.1)
```

Arguments

у	A numerical vector with the response values.
х	A numerical matrix with the predictor variables.
h	The bandwidth value to consider.
type	The type of kernel to use, "gauss" or "laplace".
k	Which variable to select?.
frac	Fraction of observations to use. The default value is 0.1.

Details

This function implements the Individual Conditional Expectaion plots of Goldstein et al. (2015). See the references for more details.

Value

A graph with several curves. The horizontal axis contains the selected variable, whereas the vertical axis contains the centered predicted values. The black curves are the effects for each observation and the blue line is their average effect.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

https://christophm.github.io/interpretable-ml-book/ice.html

Goldstein, A., Kapelner, A., Bleich, J. and Pitkin, E. (2015). Peeking inside the black box: Visualizing statistical learning with plots of individual conditional expectation. Journal of Computational and Graphical Statistics 24(1): 44-65.

See Also

```
ice.pprcomp, kernreg.tune, alfa.pcr, lc.reg
```

```
x <- as.matrix( iris[, 2:4] )
y <- iris[, 1]
ice <- ice.kernreg(y, x, h = 0.1, k = 1)</pre>
```

Inverse of the alpha-transformation

Inverse of the α *-transformation*

Description

The inverse of the α -transformation.

Usage

```
alfainv(x, a, h = TRUE)
```

Arguments

X	A matrix with Euclidean data. However, they must lie within the feasible, acceptable space. See references for more information.
a	The value of the power transformation, it has to be between -1 and 1. If zero values are present it has to be greater than 0. If $\alpha=0$, the inverse of the isometric log-ratio transformation is applied.
h	If h = TRUE this means that the multiplication with the Helmer sub-matrix will take place. It is set to TRUe by default.

Details

The inverse of the α -transformation is applied to the data. If the data lie outside the α -space, NAs will be returned for some values.

Value

A matrix with the pairwise distances.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Giorgos Athineou <gioathineou@gmail.com>.

References

Tsagris M. and Stewart C. (2022). A Review of Flexible Transformations for Modeling Compositional Data. In Advances and Innovations in Statistics and Data Science, pp. 225–234. https://link.springer.com/chapter/10.103-031-08329-7_10

Tsagris M.T., Preston S. and Wood A.T.A. (2016). Improved classification for compositional data using the α -transformation. Journal of Classification 33(2): 243–261. https://arxiv.org/pdf/1506.04976v2.pdf

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. https://arxiv.org/pdf/1106.1451.pdf

See Also

```
alfa, alfadist
```

Examples

```
library(MASS)
x <- as.matrix(fgl[1:10, 2:9])
x <- x / rowSums(x)
y <- alfa(x, 0.5)$aff
alfainv(y, 0.5)</pre>
```

Kernel regression with a numerical response vector or matrix

*Kernel regression with a numerical response vector or matrix

Description

Kernel regression (Nadaraya-Watson estimator) with a numerical response vector or matrix.

Usage

```
kern.reg(xnew, y, x, h = seq(0.1, 1, length = 10), type = "gauss")
```

Arguments

xnew	A matrix with the new predictor variables whose compositions are to be predicted.
у	A numerical vector or a matrix with the response value.
Х	A matrix with the available predictor variables.
h	The bandwidth value(s) to consider.
type	The type of kernel to use, "gauss" or "laplace".

Details

The Nadaraya-Watson estimator regression is applied.

Value

The fitted values. If a single bandwidth is considered then this is a vector or a matrix, depeding on the nature of the response. If multiple bandwidth values are considered then this is a matrix, if the response is a vector, or a list, if the response is a matrix.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Wand M. P. and Jones M. C. (1994). Kernel smoothing. CRC press.

See Also

```
kernreg.tune, ice.kernreg, akern.reg, aknn.reg
```

Examples

```
y <- iris[, 1]
x <- iris[, 2:4]
est <- kern.reg(x, y, x, h = c(0.1, 0.2) )</pre>
```

Kullback-Leibler divergence and Bhattacharyya distance between two Dirichlet distributions

Kullback-Leibler divergence and Bhattacharyya distance between two Dirichlet distributions

Description

Kullback-Leibler divergence and Bhattacharyya distance between two Dirichlet distributions.

Usage

```
kl.diri(a, b, type = "KL")
```

Arguments

a A vector with the parameters of the first Dirichlet distribution.

b A vector with the parameters of the second Dirichlet distribution.

type A variable indicating whether the Kullback-Leibler divergence ("KL") or the Bhattacharyya distance ("bhatt") is to be computed.

Details

Note that the order is important in the Kullback-Leibler divergence, since this is asymmetric, but not in the Bhattacharyya distance, since it is a metric.

Value

The value of the Kullback-Leibler divergence or the Bhattacharyya distance.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Ng Kai Wang, Guo-Liang Tian and Man-Lai Tang (2011). Dirichlet and related distributions: Theory, methods and applications. John Wiley & Sons.

See Also

```
diri.est, diri.nr
```

Examples

```
library(MASS)
a <- runif(10, 0, 20)
b <- runif(10, 1, 10)
kl.diri(a, b)
kl.diri(b, a)
kl.diri(a, b, type = "bhatt")
kl.diri(b, a, type = "bhatt")</pre>
```

LASSO Kullback-Leibler divergence based regression

LASSO Kullback-Leibler divergence based regression

Description

LASSO Kullback-Leibler divergence based regression.

Usage

```
lasso.klcompreg(y, x, alpha = 1, lambda = NULL,
nlambda = 100, type = "grouped", xnew = NULL)
```

Arguments

y A numerical matrix with compositional data. Zero values are allowed.

x A numerical matrix containing the predictor variables.

alpha The elastic net mixing parameter, with $0 \le \alpha \le 1$. The penalty is defined as

a weighted combination of the ridge and of the Lasso regression. When $\alpha=1$

LASSO is applied, while $\alpha = 0$ yields the ridge regression.

lambda This information is copied from the package glmnet. A user supplied lambda

sequence. Typical usage is to have the program compute its own lambda sequence based on nlambda and lambda.min.ratio. Supplying a value of lambda overrides this. WARNING: use with care. Avoid supplying a single value for lambda (for predictions after CV use predict() instead). Supply instead a decreasing sequence of lambda values. glmnet relies on its warms starts for speed,

and its often faster to fit a whole path than compute a single fit.

nlambda This information is copied from the package glmnet. The number of lambda

values, default is 100.

type	This information is copied from the package glmnet.	If "grouped" then a
------	---	---------------------

grouped lasso penalty is used on the multinomial coefficients for a variable. This ensures they are all in our out together. The default in our case is "grouped".

xnew If you have new data use it, otherwise leave it NULL.

Details

The function uses the glmnet package to perform LASSO penalised regression. For more details see the function in that package.

Value

A list including:

mod We decided to keep the same list that is returned by glmnet. So, see the function

in that package for more information.

est If you supply a matrix in the "xnew" argument this will return an array of many

matrices with the fitted values, where each matrix corresponds to each value of

 λ .

Author(s)

Michail Tsagris and Abdulaziz Alenazi.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Abdulaziz Alenazi <a.alenazi@nbu.edu.sa>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

Alenazi, A. A. (2022). f-divergence regression models for compositional data. Pakistan Journal of Statistics and Operation Research, 18(4): 867–882.

Friedman, J., Hastie, T. and Tibshirani, R. (2010) Regularization Paths for Generalized Linear Models via Coordinate Descent. Journal of Statistical Software, Vol. 33(1), 1–22.

See Also

```
lassocoef.plot, cv.lasso.klcompreg, kl.compreg, lasso.compreg, ols.compreg, alfa.pcr,
alfa.knn.reg
```

```
y <- as.matrix(iris[, 1:4])
y <- y / rowSums(y)
x <- matrix( rnorm(150 * 30), ncol = 30 )
a <- lasso.klcompreg(y, x)</pre>
```

LASSO log-ratio regression with compositional response $LASSO\ log-ratio\ regression\ with\ compositional\ response$

Description

LASSO log-ratio regression with compositional response.

Usage

```
lasso.compreg(y, x, alpha = 1, lambda = NULL,
nlambda = 100, xnew = NULL)
```

Arguments

lambda

У	A numerical matrix with compositional data. Zero values are not allowed as the
	additive log-ratio transformation (alr) is applied to the compositional response
	prior to implementing the LASSO algortihm.
Х	A numerical matrix containing the predictor variables.

alpha The elastic net mixing parameter, with $0 \le \alpha \le 1$. The penalty is defined as a weighted combination of the ridge and of the Lasso regression. When $\alpha = 1$ LASSO is applied, while $\alpha = 0$ yields the ridge regression.

This information is copied from the package glmnet. A user supplied lambda

sequence. Typical usage is to have the program compute its own lambda sequence based on nlambda and lambda.min.ratio. Supplying a value of lambda overrides this. WARNING: use with care. Avoid supplying a single value for lambda (for predictions after CV use predict() instead). Supply instead a decreasing sequence of lambda values. glmnet relies on its warms starts for speed, and its after features for a whole path then compute a single fit.

and its often faster to fit a whole path than compute a single fit.

nlambda This information is copied from the package glmnet. The number of lambda

values, default is 100.

xnew If you have new data use it, otherwise leave it NULL.

Details

The function uses the glmnet package to perform LASSO penalised regression. For more details see the function in that package.

Value

A list including:

mod We decided to keep the same list that is returned by glmnet. So, see the function

in that package for more information.

est If you supply a matrix in the "xnew" argument this will return an array of many

matrices with the fitted values, where each matrix corresponds to each value of

 λ .

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

Friedman, J., Hastie, T. and Tibshirani, R. (2010) Regularization Paths for Generalized Linear Models via Coordinate Descent. Journal of Statistical Software, Vol. 33(1), 1-22.

See Also

```
cv.lasso.compreg, lassocoef.plot, lasso.klcompreg, cv.lasso.klcompreg,comp.reg
```

Examples

```
y <- as.matrix(iris[, 1:4])
y <- y / rowSums(y)
x <- matrix( rnorm(150 * 30), ncol = 30 )
a <- lasso.compreg(y, x)</pre>
```

LASSO with compositional predictors using the alpha-transformation $LASSO\ with\ compositional\ predictors\ using\ the\ alpha-transformation$

Description

LASSO with compositional predictors using the *alpha*-transformation.

Usage

```
alfa.lasso(y, x, a = seq(-1, 1, by = 0.1), model = "gaussian", lambda = NULL, xnew = NULL)
```

Arguments

У	A numerical vector or a matrix for multinomial logistic regression.
X	A numerical matrix containing the predictor variables, compositional data, where zero values are allowed
a	A vector with a grid of values of the power transformation, it has to be between -1 and 1. If zero values are present it has to be greater than 0. If $\alpha=0$ the isometric log-ratio transformation is applied.
model	The type of the regression model, "gaussian", "binomial", "poisson", "multinomial", or "mgaussian".

1 This information is copied from the package glmnet. A user supplied lambda

sequence. Typical usage is to have the program compute its own lambda sequence based on nlambda and lambda.min.ratio. Supplying a value of lambda overrides this. WARNING: use with care. Avoid supplying a single value for lambda (for predictions after CV use predict() instead). Supply instead a decreasing sequence of lambda values. glmnet relies on its warms starts for speed,

and its often faster to fit a whole path than compute a single fit.

xnew If you have new data use it, otherwise leave it NULL.

Details

The function uses the glmnet package to perform LASSO penalised regression. For more details see the function in that package.

Value

A list including sublists for each value of α :

mod We decided to keep the same list that is returned by glmnet. So, see the function

in that package for more information.

est If you supply a matrix in the "xnew" argument this will return an array of many

matrices with the fitted values, where each matrix corresponds to each value of

 λ .

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

Friedman, J., Hastie, T. and Tibshirani, R. (2010) Regularization Paths for Generalized Linear Models via Coordinate Descent. Journal of Statistical Software, Vol. 33(1), 1–22.

See Also

```
alfalasso.tune, cv.lasso.klcompreg, lasso.compreg, alfa.knn.reg
```

```
y <- as.matrix(iris[, 1])
x <- rdiri(150, runif(20, 2, 5) )
mod <- alfa.lasso(y, x, a = c(0, 0.5, 1))</pre>
```

Log-contrast GLMs with compositional predictor variables $Log-contrast\ GLMS\ with\ compositional\ predictor\ variables$

Description

Log-contrast GLMs with compositional predictor variables.

Usage

```
lc.glm(y, x, z = NULL, model = "logistic", xnew = NULL, znew = NULL)
```

Arguments

у	A numerical vector containing the response variable values. This is either a binary variable or a vector with counts.
x	A matrix with the predictor variables, the compositional data. No zero values are allowed.
Z	A matrix, data.frame, factor or a vector with some other covariate(s).
model	For the ulc.glm(), this can be either "logistic" or "poisson".
xnew	A matrix containing the new compositional data whose response is to be predicted. If you have no new data, leave this NULL as is by default.
znew	A matrix, data.frame, factor or a vector with the values of some other covariate(s). If you have no new data, leave this NULL as is by default.

Details

The function performs the log-contrast logistic or Poisson regression model. The logarithm of the compositional predictor variables is used (hence no zero values are allowed). The response variable is linked to the log-transformed data with the constraint that the sum of the regression coefficients equals 0. If you want the regression without the zum-to-zero contraints see ulc.glm. Extra predictors variables are allowed as well, for instance categorical or continuous.

Value

A list including:

devi The residual deviance of the logistic or Poisson regression model.

The constrained regression coefficients. Their sum (excluding the constant) equals 0.

If the arguments "xnew" and znew were given these are the predicted or estimated values, otherwise it is NULL.

Author(s)

est

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

Lu J., Shi P. and Li H. (2019). Generalized linear models with linear constraints for microbiome compositional data. Biometrics, 75(1): 235–244.

See Also

```
ulc.glm, lc.glm2, ulc.glm2, lcglm.aov
```

Examples

```
y <- rbinom(150, 1, 0.5)
x <- rdiri(150, runif(3, 1, 4) )
mod1 <- lc.glm(y, x)
```

 $\label{log-contrast} \mbox{ logistic or Poisson regression with with multiple compositional predictors}$

Log-contrast logistic or Poisson regression with with multiple compositional predictors

Description

Log-contrast logistic or Poisson regression with with multiple compositional predictors.

Usage

```
lc.glm2(y, x, z = NULL, model = "logistic", xnew = NULL, znew = NULL)
```

Arguments

У	A numerical vector containing the response variable values. This is either a binary variable or a vector with counts.
х	A matrix with the predictor variables, the compositional data. No zero values are allowed.
z	A matrix, data.frame, factor or a vector with some other covariate(s).
model	This can be either "logistic" or "poisson".
xnew	A matrix containing the new compositional data whose response is to be predicted. If you have no new data, leave this NULL as is by default.
znew	A matrix, data.frame, factor or a vector with the values of some other covariate(s). If you have no new data, leave this NULL as is by default.

Details

The function performs the log-contrast logistic or Poisson regression model. The logarithm of the compositional predictor variables is used (hence no zero values are allowed). The response variable is linked to the log-transformed data with the constraint that the sum of the regression coefficients equals 0. If you want the regression without the zum-to-zero contraints see ulc.glm2. Extra predictors variables are allowed as well, for instance categorical or continuous.

Value

A list including:

devi	The residual deviance of the logistic or Poisson regression model.		
be	The constrained regression coefficients. Their sum (excluding the constant) equals $\boldsymbol{\theta}$.		
est	If the arguments "xnew" and znew were given these are the predicted or estimated values, otherwise it is NULL.		

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

Lu J., Shi P. and Li H. (2019). Generalized linear models with linear constraints for microbiome compositional data. Biometrics, 75(1): 235–244.

See Also

```
ulc.glm2, ulc.glm, lc.glm
```

Examples

```
y <- rbinom(150, 1, 0.5)
x <- list()
x1 <- as.matrix(iris[, 2:4])
x1 <- x1 / rowSums(x1)
x[[ 1 ]] <- x1
x[[ 2 ]] <- rdiri(150, runif(4) )
x[[ 3 ]] <- rdiri(150, runif(5) )
mod <- lc.glm2(y, x)</pre>
```

 $\label{log-contrast} \mbox{ quantile regression with compositional predictor } \mbox{ variables}$

Log-contrast quantile regression with compositional predictor variables

Description

Log-contrast quantile regression with compositional predictor variables.

Usage

```
lc.rq(y, x, z = NULL, tau, xnew = NULL, znew = NULL)
```

Arguments

у	A numerical vector containing the response variable values.
x	A matrix with the predictor variables, the compositional data. No zero values are allowed.
Z	A matrix, data.frame, factor or a vector with some other covariate(s).
tau	The quantile to be estimated, a number between 0 and 1.
xnew	A matrix containing the new compositional data whose response is to be predicted. If you have no new data, leave this NULL as is by default.
znew	A matrix, data.frame, factor or a vector with the values of some other covariate(s). If you have no new data, leave this NULL as is by default.

Details

The function performs the quantile regression model. The logarithm of the compositional predictor variables is used (hence no zero values are allowed). The response variable is linked to the log-transformed data with the constraint that the sum of the regression coefficients equals 0. If you want the regression without the zum-to-zero contraints see ulc.rq. Extra predictor variables are allowed as well, for instance categorical or continuous.

Value

A list including:

mod	The object as returned by the function quantreg::rq(). This is useful for hypothesis testing purposes.		
be	The constrained regression coefficients. Their sum (excluding the constant) equals $\boldsymbol{0}$.		
est	If the arguments "xnew" and znew were given these are the predicted or estimated values, otherwise it is NULL.		

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

Koenker R. W. and Bassett G. W. (1978). Regression Quantiles, Econometrica, 46(1): 33-50.

Koenker R. W. and d'Orey V. (1987). Algorithm AS 229: Computing Regression Quantiles. Applied Statistics, 36(3): 383–393.

See Also

```
lc.rq2, ulc.rq
```

Examples

```
y <- rnorm(150)
x <- rdiri(150, runif(3, 1, 4) )
mod1 <- lc.rq(y, x)</pre>
```

 $\label{log-contrast} \mbox{ Log-contrast quantile regression with with multiple compositional predictors} \\$

Log-contrast quantile regression with with multiple compositional predictors

Description

Log-contrast quantile regression with with multiple compositional predictors.

Usage

```
1c.rq2(y, x, z = NULL, tau = 0.5, xnew = NULL, znew = NULL)
```

Arguments

У	A numerical vector containing the response variable values.
X	A matrix with the predictor variables, the compositional data. No zero values are allowed.
Z	A matrix, data.frame, factor or a vector with some other covariate(s).
tau	The quantile to be estimated, a number between 0 and 1.
xnew	A matrix containing the new compositional data whose response is to be predicted. If you have no new data, leave this NULL as is by default.
znew	A matrix, data frame, factor or a vector with the values of some other covariate(s). If you have no new data, leave this NULL as is by default.

Details

The function performs the log-contrast quantile regression model. The logarithm of the compositional predictor variables is used (hence no zero values are allowed). The response variable is linked to the log-transformed data with the constraint that the sum of the regression coefficients equals 0. If you want the regression without the zum-to-zero contraints see ulc.rq2. Extra predictor variables are allowed as well, for instance categorical or continuous.

Value

A list including:

mod	The object as returned by the function quantreg::rq(). This is useful for hypothesis testing purposes.		
be	The constrained regression coefficients. Their sum (excluding the constant) equals $\boldsymbol{\theta}.$		
est	If the arguments "xnew" and znew were given these are the predicted or estimated values, otherwise it is NULL.		

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

Koenker R. W. and Bassett G. W. (1978). Regression Quantiles, Econometrica, 46(1): 33-50.

Koenker R. W. and d'Orey V. (1987). Algorithm AS 229: Computing Regression Quantiles. Applied Statistics, 36(3): 383–393.

See Also

```
lc.rq, ulc.rq
```

Examples

```
y <- rnorm(150)
x <- list()
x1 <- as.matrix(iris[, 2:4])
x1 <- x1 / rowSums(x1)
x[[ 1 ]] <- x1
x[[ 2 ]] <- rdiri(150, runif(4) )
x[[ 3 ]] <- rdiri(150, runif(5) )
mod <- lc.rq2(y, x)</pre>
```

Log-contrast regression with compositional predictor variables

Log-contrast regression with compositional predictor variables

Description

Log-contrast regression with compositional predictor variables.

Usage

```
lc.reg(y, x, z = NULL, xnew = NULL, znew = NULL)
```

Arguments

У	A numerical vector containing the response variable values. This must be a continuous variable.
X	A matrix with the predictor variables, the compositional data. No zero values are allowed.
Z	A matrix, data.frame, factor or a vector with some other covariate(s).
xnew	A matrix containing the new compositional data whose response is to be predicted. If you have no new data, leave this NULL as is by default.
znew	A matrix, data.frame, factor or a vector with the values of some other covariate(s). If you have no new data, leave this NULL as is by default.

Details

The function performs the log-contrast regression model as described in Aitchison (2003), pg. 84-85. The logarithm of the compositional predictor variables is used (hence no zero values are allowed). The response variable is linked to the log-transformed data with the constraint that the sum of the regression coefficients equals 0. Hence, we apply constrained least squares, which has a closed form solution. The constrained least squares is described in Chapter 8.2 of Hansen (2019). The idea is to minimise the sum of squares of the residuals under the constraint $R^T\beta = c$, where c = 0 in our case. If you want the regression without the zum-to-zero contraints see ulc.reg. Extra predictors variables are allowed as well, for instance categorical or continuous.

Value

A list including:

be The constrained regression coefficients. Their sum (excluding the constant)

equals 0.

covbe The covariance matrix of the constrained regression coefficients.

va The estimated regression variance.

residuals The vector of residuals.

est If the arguments "xnew" and znew were given these are the predicted or esti-

mated values, otherwise it is NULL.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

```
Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall. Hansen, B. E. (2022). Econometrics. Princeton University Press.
```

See Also

```
ulc.reg, lcreg.aov, lc.reg2, alfa.pcr, alfa.knn.reg
```

Examples

```
y <- iris[, 1]
x <- as.matrix(iris[, 2:4])
x <- x / rowSums(x)
mod1 <- lc.reg(y, x)
mod2 <- lc.reg(y, x, z = iris[, 5])</pre>
```

 ${\it Log-contrast \ regression \ with \ multiple \ compositional \ predictors} \\ {\it Log-contrast \ regression \ with \ multiple \ compositional \ predictors}}$

Description

Log-contrast regression with multiple compositional predictors.

Usage

```
lc.reg2(y, x, z = NULL, xnew = NULL, znew = NULL)
```

Arguments

У	A numerical vector containing the response variable values. This must be a continuous variable.
X	A list with multiple matrices with the predictor variables, the compositional data. No zero values are allowed.
Z	A matrix, data.frame, factor or a vector with some other covariate(s).
xnew	A matrix containing a list with multiple matrices with compositional data whose response is to be predicted. If you have no new data, leave this NULL as is by default.
znew	A matrix, data.frame, factor or a vector with the values of some other covariate(s). If you have no new data, leave this NULL as is by default.

Details

The function performs the log-contrast regression model as described in Aitchison (2003), pg. 84-85. The logarithm of the compositional predictor variables is used (hence no zero values are allowed). The response variable is linked to the log-transformed data with the constraint that the sum of the regression coefficients for each composition equals 0. Hence, we apply constrained least squares, which has a closed form solution. The constrained least squares is described in Chapter 8.2 of Hansen (2019). The idea is to minimise the sum of squares of the residuals under the constraint $R^T\beta=c$, where c=0 in our case. If you want the regression without the zum-to-zero contraints see ulc.reg2. Extra predictors variables are allowed as well, for instance categorical or continuous. The difference with lc.reg is that instead of one, there are multiple compositions treated as predictor variables.

Value

A list including:

be The constrained regression coefficients. The sum of the sets of coefficients (ex-

cluding the constant) corresponding to each predictor composition sums to 0.

covbe If covariance matrix of the constrained regression coefficients.

va The variance of the estimated regression coefficients.

residuals The vector of residuals.

est If the arguments "xnew" and "znew" were given these are the predicted or esti-

mated values, otherwise it is NULL.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

Hansen, B. E. (2022). Econometrics. Princeton University Press.

Xiaokang Liu, Xiaomei Cong, Gen Li, Kendra Maas and Kun Chen (2020). Multivariate Log-Contrast Regression with Sub-Compositional Predictors: Testing the Association Between Preterm Infants' Gut Microbiome and Neurobehavioral Outcome.

See Also

```
ulc.reg2, lc.reg, ulc.reg, lcreg.aov, alfa.pcr, alfa.knn.reg
```

Examples

```
y <- iris[, 1]
x <- list()
x1 <- as.matrix(iris[, 2:4])
x1 <- x1 / rowSums(x1)
x[[ 1 ]] <- x1</pre>
```

```
x[[ 2 ]] <- rdiri(150, runif(4) )
x[[ 3 ]] <- rdiri(150, runif(5) )
mod <- lc.reg2(y, x)
be <- mod$be
sum(be[2:4])
sum(be[5:8])
sum(be[9:13])</pre>
```

Log-likelihood ratio test for a Dirichlet mean vector

Log-likelihood ratio test for a Dirichlet mean vector

Description

Log-likelihood ratio test for a Dirichlet mean vector.

Usage

```
dirimean.test(x, a)
```

Arguments

а

x A matrix with the compositional data. No zero values are allowed.

A compositional mean vector. The concentration parameter is estimated at first. If the elements do not sum to 1, it is assumed that the Dirichlet parameters are supplied.

Details

Log-likelihood ratio test is performed for the hypothesis the given vector of parameters "a" describes the compositional data well.

Value

If there are no zeros in the data, a list including:

param A matrix with the estimated parameters under the null and the alternative hy-

pothesis.

loglik The log-likelihood under the alternative and the null hypothesis.

info The value of the test statistic and its relevant p-value.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Giorgos Athineou <gioathineou@gmail.com>.

References

Ng Kai Wang, Guo-Liang Tian and Man-Lai Tang (2011). Dirichlet and related distributions: Theory, methods and applications. John Wiley & Sons.

See Also

```
sym.test, diri.nr, diri.est, rdiri, ddiri
```

Examples

```
x <- rdiri( 100, c(1, 2, 3) )
dirimean.test(x, c(1, 2, 3) )
dirimean.test( x, c(1, 2, 3)/6 )</pre>
```

Log-likelihood ratio test for a symmetric Dirichlet distribution

Log-likelihood ratio test for a symmetric Dirichlet distribution

Description

Log-likelihood ratio test for a symmetric Dirichlet distribution.

Usage

```
sym.test(x)
```

Arguments

Х

A matrix with the compositional data. No zero values are allowed.

Details

Log-likelihood ratio test is performed for the hypothesis that all Dirichelt parameters are equal.

Value

res

A list including:

est.par The estimated parameters under the alternative hypothesis.

one.par The value of the estimated parameter under the null hypothesis.

The loglikelihood under the alternative and the null hypothesis, the value of the test statistic, its relevant p-value and the associated degrees of freedom, which are actually the dimensionality of the simplex, D-1, where D is the number of

components.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Ng Kai Wang, Guo-Liang Tian and Man-Lai Tang (2011). Dirichlet and related distributions: Theory, methods and applications. John Wiley & Sons.

See Also

```
diri.nr, diri.est, rdiri, dirimean.test
```

Examples

```
x <- rdiri( 100, c(5, 7, 1, 3, 10, 2, 4) )
sym.test(x)
x <- rdiri( 100, c(5, 5, 5, 5, 5) )
sym.test(x)</pre>
```

Minimized Kullback-Leibler divergence between Dirichlet and logistic normal

Minimized Kullback-Leibler divergence between Dirichlet and logistic normal

Description

Minimized Kullback-Leibler divergence between Dirichlet and logistic normal distributions.

Usage

```
kl.diri.normal(a)
```

Arguments

a A vector with the parameters of the Dirichlet parameters.

Details

The function computes the minimized Kullback-Leibler divergence from the Dirichlet distribution to the logistic normal distribution.

Value

The minimized Kullback-Leibler divergence from the Dirichlet distribution to the logistic normal distribution.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison J. (1986). The statistical analysis of compositional data, p. 127. Chapman & Hall.

See Also

```
diri.nr, diri.contour, rdiri, ddiri, dda, diri.reg
```

Examples

```
a <- runif(5, 1, 5)
kl.diri.normal(a)</pre>
```

Mixture model selection via BIC

Mixture model selection via BIC

Description

Mixture model selection via BIC.

Usage

```
bic.mixcompnorm(x, G, type = "alr", veo = FALSE, graph = TRUE)
```

Arguments

x	A matrix with compositional data.
G	A numeric vector with the number of components, clusters, to be considered, e.g. 1:3.
type	The type of trasformation to be used, either the additive log-ratio ("alr"), the isometric log-ratio ("ilr") or the pivot coordinate ("pivot") transformation.
veo	Stands for "Variables exceed observations". If TRUE then if the number variablesin the model exceeds the number of observations, but the model is still fitted.
graph	A boolean variable, TRUE or FALSE specifying whether a graph should be drawn or not.

Details

The alr or the ilr-transformation is applied to the compositional data first and then mixtures of multivariate Gaussian distributions are fitted. BIC is used to decide on the optimal model and number of components.

Value

A plot with the BIC of the best model for each number of components versus the number of components. A list including:

A message informing the user about the best model.

BIC The BIC values for every possible model and number of components.

optG The number of components with the highest BIC.

optmodel The type of model corresponding to the highest BIC.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Ryan P. Browne, Aisha ElSherbiny and Paul D. McNicholas (2018). mixture: Mixture Models for Clustering and Classification. R package version 1.5.

Ryan P. Browne and Paul D. McNicholas (2014). Estimating Common Principal Components in High Dimensions. Advances in Data Analysis and Classification, 8(2), 217-226.

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
mix.compnorm, mix.compnorm.contour, rmixcomp, bic.alfamixnorm
```

Examples

```
x <- as.matrix( iris[, 1:4] )
x <- x/ rowSums(x)
bic.mixcompnorm(x, 1:3, type = "alr", graph = FALSE)
bic.mixcompnorm(x, 1:3, type = "ilr", graph = FALSE)</pre>
```

Mixture model selection with the alpha-transformation using BIC ${\it Mixture\ model\ selection\ with\ the\ }\alpha\hbox{-}{\it transformation\ using\ BIC}$

Description

Mixture model selection with the α -transformation using BIC.

Usage

```
bic.alfamixnorm(x, G, a = seq(-1, 1, by = 0.1), veo = FALSE, graph = TRUE)
```

Arguments

X	A matrix with compositional data.
G	A numeric vector with the number of components, clusters, to be considered, e.g. 1:3.
a	A vector with a grid of values of the power transformation, it has to be between -1 and 1. If zero values are present it has to be greater than 0. If $\alpha=0$ the isometric log-ratio transformation is applied.
veo	Stands for "Variables exceed observations". If TRUE then if the number variablesin the model exceeds the number of observations, but the model is still fitted.
graph	A boolean variable, TRUE or FALSE specifying whether a graph should be drawn or not.

Details

The α -transformation is applied to the compositional data first and then mixtures of multivariate Gaussian distributions are fitted. BIC is used to decide on the optimal model and number of components.

Value

A list including:

abic A list that contains the matrices of all BIC values for all values of α .

optalpha The value of α that leads to the highest BIC. optG The number of components with the highest BIC. optmodel The type of model corresponding to the highest BIC.

If graph is set equal to TRUE a plot with the BIC of the best model for each number of components versus the number of components and a list with the results of the Gaussian mixture model for each value of α .

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Ryan P. Browne, Aisha ElSherbiny and Paul D. McNicholas (2018). mixture: Mixture Models for Clustering and Classification. R package version 1.5.

Ryan P. Browne and Paul D. McNicholas (2014). Estimating Common Principal Components in High Dimensions. Advances in Data Analysis and Classification, 8(2), 217-226.

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. https://arxiv.org/pdf/1106.1451.pdf

See Also

```
alfa.mix.norm, mix.compnorm, mix.compnorm.contour, rmixcomp, alfa, alfa.knn,alfa.rda, comp.nb
```

Examples

```
x <- as.matrix( iris[, 1:4] )
x <- x/ rowSums(x)
bic.alfamixnorm(x, 1:3, a = c(0.4, 0.5, 0.6), graph = FALSE)</pre>
```

MLE for the multivariate t distribution $MLE\ for\ the\ multivariate\ t\ distribution$

Description

MLE of the parameters of a multivariate t distribution.

Usage

```
multivt(y, plot = FALSE)
```

Arguments

y A matrix with continuous data.

plot If plot is TRUE the value of the maximum log-likelihood as a function of the

degres of freedom is presented.

Details

The parameters of a multivariate t distribution are estimated. This is used by the functions comp. den and bivt.contour.

Value

A list including:

center The location estimate.

scatter The scatter matrix estimate.

df The estimated degrees of freedom.

loglik The log-likelihood value.
mesos The classical mean vector.

covariance The classical covariance matrix.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Giorgos Athineou <gioathineou@gmail.com>.

References

Nadarajah, S. and Kotz, S. (2008). Estimation methods for the multivariate t distribution. Acta Applicandae Mathematicae, 102(1):99-118.

See Also

```
bivt.contour, comp.den
```

Examples

```
x <- as.matrix(iris[, 1:4])
multivt(x)</pre>
```

```
MLE of distributions defined in the (0, 1) interval 
MLE of distributions defined in the (0, 1) interval
```

Description

MLE of distributions defined in the (0, 1) interval.

Usage

```
beta.est(x, tol = 1e-07)
logitnorm.est(x)
hsecant01.est(x, tol = 1e-07)
kumar.est(x, tol = 1e-07)
unitweibull.est(x, tol = 1e-07, maxiters = 100)
ibeta.est(x, tol = 1e-07)
zilogitnorm.est(x)
```

Arguments

X	A numerical vector with proportions, i.e. numbers in (0, 1) (zeros and ones are not allowed).
tol	The tolerance level up to which the maximisation stops.
maxiters	The maximum number of iterations the Newton-Raphson algorithm will perform.

Details

Maximum likelihood estimation of the parameters of some distributions are performed, some of which use the Newton-Raphson. Some distributions and hence the functions do not accept zeros. "logitnorm.mle" fits the logistic normal, hence no Newton-Raphson is required and the "hypersecant01.mle" use the golden ratio search as is it faster than the Newton-Raphson (less computations). The "zilogitnorm.est" stands for the zero inflated logistic normal distribution. The "ibeta.est" fits the zero or the one inflated beta distribution.

Value

A list including:

iters The number of iterations required by the Newton-Raphson.

loglik The value of the log-likelihood.

param The estimated parameters. In the case of "hypersecant01.est" this is called

"theta" as there is only one parameter.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Kumaraswamy, P. (1980). A generalized probability density function for double-bounded random processes. Journal of Hydrology. 46(1-2): 79-88.

Jones, M.C. (2009). Kumaraswamy's distribution: A beta-type distribution with some tractability advantages. Statistical Methodology. 6(1): 70-81.

You can also check the relevant wikipedia pages.

See Also

```
diri.est
```

Examples

```
x <- rbeta(1000, 1, 4)
beta.est(x)
ibeta.est(x)

x <- runif(1000)
hsecant01.est(x)
logitnorm.est(x)
ibeta.est(x)

x <- rbeta(1000, 2, 5)
x[sample(1:1000, 50)] <- 0
ibeta.est(x)</pre>
```

MLE of the Dirichlet distribution

MLE of the a Dirichlet distribution

Description

MLE of the parameters of a Dirichlet distribution.

Usage

```
diri.est(x, type = "mle")
```

Arguments

x A matrix containing compositional data.

type If you want to estimate the parameters use type="mle". If you want to estimate

the mean vector along with the precision parameter, the second parametrisation

of the Dirichlet, use type="prec".

Details

Maximum likelihood estimation of the parameters of a Dirichlet distribution is performed.

Value

A list including:

loglik The value of the log-likelihood.

param The estimated parameters.

phi The estimated precision parameter, if type = "prec".

mu The estimated mean vector, if type = "prec".

runtime The run time of the maximisation procedure.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Giorgos Athineou <gioathineou@gmail.com>.

References

Ng Kai Wang, Guo-Liang Tian and Man-Lai Tang (2011). Dirichlet and related distributions: Theory, methods and applications. John Wiley & Sons.

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
diri.nr, diri.contour, rdiri, ddiri, dda, diri.reg
```

Examples

```
x <- rdiri( 100, c(5, 7, 1, 3, 10, 2, 4) )
diri.est(x)
diri.est(x, type = "prec")</pre>
```

MLE of the Dirichlet distribution via Newton-Rapshon

MLE of the Dirichlet distribution via Newton-Rapshon

Description

MLE of the Dirichlet distribution via Newton-Rapshon.

Usage

```
diri.nr(x, type = 1, tol = 1e-07)
```

Arguments

x A matrix containing compositional data. Zeros are not allowed.

type Type can either be 1, so that the Newton-Rapshon is used for the maximisation

of the log-likelihood, as Minka (2012) suggested or it can be 1. In the latter case the Newton-Raphson algorithm is implemented involving matrix inversions. In addition an even faster implementation has been implemented (in C++) in the

package **Rfast** and is used here.

tol The tolerance level indicating no further increase in the log-likelihood.

Details

Maximum likelihood estimation of the parameters of a Dirichlet distribution is performed via Newton-Raphson. Initial values suggested by Minka (2003) are used. The estimation is super faster than "diri.est" and the difference becomes really apparent when the sample size and or the dimensions increase. In fact this will work with millions of observations. So in general, I trust this one more than "diri.est".

The only problem I have seen with this method is that if the data are concentrated around a point, say the center of the simplex, it will be hard for this and the previous methods to give estimates of the parameters. In this extremely difficult scenario I would suggest the use of the previous function with the precision parametrization "diri.est(x, type = "prec")". It will be extremely fast and accurate.

Value

A list including:

iter The number of iterations required. If the argument "type" is set to 2 this is not

returned.

loglik The value of the log-likelihood.

param The estimated parameters.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Thomas P. Minka (2003). Estimating a Dirichlet distribution. http://research.microsoft.com/en-us/um/people/minka/papers/dirichlet/minka-dirichlet.pdf

See Also

```
diri.est, diri.contour rdiri, ddiri, dda
```

Examples

```
x <- rdiri( 100, c(5, 7, 5, 8, 10, 6, 4) )
diri.nr(x)
diri.nr(x, type = 2)
diri.est(x)</pre>
```

MLE of the folded model for a given value of alpha $\it MLE$ of the folded model for a given value of α

Description

MLE of the folded model for a given value of α .

Usage

```
alpha.mle(x, a)
a.mle(a, x)
```

Arguments

- x A matrix with the compositional data. No zero vaues are allowed.
- a A value of α .

Details

This is a function for choosing or estimating the value of α in the α -folded model (Tsagris and Stewart, 2020). It is called by a.est.

Value

If "alpha.mle" is called, a list including:

iters The number of iterations the EM algorithm required.loglik The maximimized log-likelihood of the folded model.

p The estimated probability inside the simplex of the α -folded model.

mu The estimated mean vector of the α -folded model.

su The estimated covariance matrix of the α -folded model.

If "a.mle" is called, the log-likelihood is returned only.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Tsagris M. and Stewart C. (2022). A Review of Flexible Transformations for Modeling Compositional Data. In Advances and Innovations in Statistics and Data Science, pp. 225–234. https://link.springer.com/chapter/10.103-031-08329-7_10

Tsagris M. and Stewart C. (2020). A folded model for compositional data analysis. Australian and New Zealand Journal of Statistics, 62(2): 249-277. https://arxiv.org/pdf/1802.07330.pdf

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. https://arxiv.org/pdf/1106.1451.pdf

See Also

```
alfa.profile, alfa, alfainv, a.est
```

Examples

```
x <- as.matrix(iris[, 1:4])
x <- x / rowSums(x)
mod <- alfa.tune(x)
mod
alpha.mle(x, mod[1])</pre>
```

MLE of the zero adjusted Dirichlet distribution $MLE \ of \ the \ zero \ adjusted \ Dirichlet \ distribution$

Description

MLE of the zero adjusted Dirichlet distribution.

Usage

zad.est(y)

Arguments

y A matrix with the compositional data.

Details

A zero adjusted Dirichlet distribution is being fitted and its parameters are estimated.

Value

A list including:

loglik The value of the log-likelihood.

phi The precision parameter. If covariates are linked with it (function "diri.reg2"),

this will be a vector.

mu The mean vector of the distribution.
runtime The time required by the model..

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Tsagris M. and Stewart C. (2018). A Dirichlet regression model for compositional data with zeros. Lobachevskii Journal of Mathematics, 39(3): 398–412.

Preprint available from https://arxiv.org/pdf/1410.5011.pdf

See Also

```
zadr, diri.nr, zilogitnorm.est, zeroreplace
```

Examples

```
y <- as.matrix(iris[, 1:3])
y <- y / rowSums(y)
mod1 <- diri.nr(y)
y[sample(1:450, 15)] <- 0
mod2 <- zad.est(y)</pre>
```

Multivariate kernel density estimation

Multivariate kernel density estimation

Description

Multivariate kernel density estimation.

Usage

```
mkde(x, h = NULL, thumb = "silverman")
```

Arguments

x A matrix with Euclidean (continuous) data.

h The bandwidh value. It can be a single value, which is turned into a vector and

then into a diagonal matrix, or a vector which is turned into a diagonal matrix. If you put this NULL then you need to specify the "thumb" argument below.

thumb Do you want to use a rule of thumb for the bandwidth parameter? If no, set

h equal to NULL and put "estim" for maximum likelihood cross-validation, "scott" or "silverman" for Scott's and Silverman's rules of thumb respectively.

Details

The multivariate kernel density estimate is calculated with a (not necssarily given) bandwidth value.

Value

A vector with the density estimates calculated for every vector.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris mtsagris@uoc.gr and Giorgos Athineou gioathineou@gmail.com.

References

Arsalane Chouaib Guidoum (2015). Kernel Estimator and Bandwidth Selection for Density and its Derivatives. The kedd R package.

M.P. Wand and M.C. Jones (1995). Kernel smoothing, pages 91-92.

B.W. Silverman (1986). Density estimation for statistics and data analysis, pages 76-78.

See Also

```
mkde.tune, comp.kerncontour
```

Examples

```
mkde( as.matrix(iris[, 1:4]), thumb = "scott" )
mkde( as.matrix(iris[, 1:4]), thumb = "silverman" )
```

Multivariate kernel density estimation for compositional data

Multivariate kernel density estimation for compositional data

Description

Multivariate kernel density estimation for compositional data.

Usage

```
comp.kern(x, type= "alr", h = NULL, thumb = "silverman")
```

Arguments

Х	A matrix with Euclidean (continuous) data.
type	The type of trasformation used, either the additive log-ratio ("alr"), the isometric log-ratio ("ilr") or the pivot coordinate ("pivot") transformation.
h	The bandwidh value. It can be a single value, which is turned into a vector and then into a diagonal matrix, or a vector which is turned into a diagonal matrix. If it is NULL, then you need to specify the "thumb" argument below.
thumb	Do you want to use a rule of thumb for the bandwidth parameter? If no, leave the "h" NULL and put "estim" for maximum likelihood cross-validation, "scott" or "silverman" for Scott's and Silverman's rules of thumb respectively.

Details

The multivariate kernel density estimate is calculated with a (not necssarily given) bandwidth value.

Value

A vector with the density estimates calculated for every vector.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Arsalane Chouaib Guidoum (2015). Kernel Estimator and Bandwidth Selection for Density and its Derivatives.

The kedd R package.

M.P. Wand and M.C. Jones (1995). Kernel smoothing, pages 91-92.

B.W. Silverman (1986). Density estimation for statistics and data analysis, pages 76-78.

See Also

```
comp.kerncontour, mkde
```

Examples

```
x <- as.matrix(iris[, 1:3])
x <- x / rowSums(x)
f <- comp.kern(x)</pre>
```

Multivariate linear regression

Multivariate linear regression

Description

Multivariate linear regression.

Usage

```
multivreg(y, x, plot = TRUE, xnew = NULL)
```

Arguments

y A matrix with the Eucldidean (continuous) data.

x A matrix with the predictor variable(s), they have to be continuous.

plot Should a plot appear or not?

xnew If you have new data use it, otherwise leave it NULL.

Details

The classical multivariate linear regression model is obtained.

Value

	1.		1 11	
А	list	1nc	luding	٠,
	1100	1110		٠.

suma	A summary as produced by ${\tt lm}$, which includes the coefficients, their standard error, t-values, p-values.
r.squared	The value of the \mathbb{R}^2 for each univariate regression.
resid.out	A vector with number indicating which vectors are potential residual outliers.
x.leverage	A vector with number indicating which vectors are potential outliers in the predictor variables space.
out	A vector with number indicating which vectors are potential outliers in the residuals and in the predictor variables space.
est	The predicted values if xnew is not NULL.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Giorgos Athineou <gioathineou@gmail.com>.

References

K.V. Mardia, J.T. Kent and J.M. Bibby (1979). Multivariate Analysis. Academic Press.

See Also

```
diri.reg, js.compreg, kl.compreg, ols.compreg, comp.reg
```

Examples

```
library(MASS)
x <- as.matrix(iris[, 1:2])
y <- as.matrix(iris[, 3:4])
multivreg(y, x, plot = TRUE)</pre>
```

Multivariate normal random values simulation on the simplex ${\it Multivariate~normal~random~values~simulation~on~the~simplex}$

Description

Multivariate normal random values simulation on the simplex.

Usage

```
rcompnorm(n, m, s, type = "alr")
```

Arguments

n	The sample size, a numerical value.
m	The mean vector in \mathbb{R}^d .
S	The covariance matrix in \mathbb{R}^d .
type	The alr (type = "alr") or the ilr (type = "ilr") is to be used for closing the Euclidean data onto the simplex.

Details

The algorithm is straightforward, generate random values from a multivariate normal distribution in \mathbb{R}^d and brings the values to the simplex \mathbb{S}^d using the inverse of a log-ratio transformation.

Value

A matrix with the simulated data.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
comp.den, rdiri, rcompt, rcompsn
```

Examples

```
x <- as.matrix(iris[, 1:2])
m <- colMeans(x)
s <- var(x)
y <- rcompnorm(100, m, s)
comp.den(y)
ternary(y)</pre>
```

Multivariate or univariate regression with compositional data in the covariates side using the alpha-transformation

Multivariate or univariate regression with compositional data in the covariates side using the α -transformation

Description

Multivariate or univariate regression with compositional data in the covariates side using the α -transformation.

Usage

```
alfa.pcr(y, x, a, k, model = "gaussian", xnew = NULL)
```

Arguments

У	A numerical vector containing the response variable values. They can be continuous, binary, discrete (counts). This can also be a vector with discrete values or a factor for the multinomial regression (model = "multinomial").
x	A matrix with the predictor variables, the compositional data.
a	The value of the power transformation, it has to be between -1 and 1. If zero values are present it has to be greater than 0. If $\alpha=0$ the isometric log-ratio transformation is applied.
k	How many principal components to use. You may also specify a vector and in this case the results produced will refer to each number of principal components.
model	The type of regression model to fit. The possible values are "gaussian", "multinomial", "binomial" and "poisson".
xnew	A matrix containing the new compositional data whose response is to be predicted. If you have no new data, leave this NULL as is by default.

Details

The α -transformation is applied to the compositional data first ,the first k principal component scores are calcualted and used as predictor variables for a regression model. The family of distributions can be either, "normal" for continuous response and hence normal distribution, "binomial" corresponding to binary response and hence logistic regression or "poisson" for count response and poisson regression.

Value

A list tincluding:

be If linear regression was fitted, the regression coefficients of the k principal component scores on the response variable y.

mod	If another regression model was fitted its outcome as produced in the package Rfast .
per	The percentage of variance explained by the first k principal components.
vec	The first k principal components, loadings or eigenvectors. These are useful for future prediction in the sense that one needs not fit the whole model again.
est	If the argument "xnew" was given these are the predicted or estimated values (if xnew is not NULL). If the argument k is a vector then this is a matrix with the estimated values for each number of components.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Tsagris M. (2015). Regression analysis with compositional data containing zero values. Chilean Journal of Statistics, 6(2): 47-57. https://arxiv.org/pdf/1508.01913v1.pdf

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. https://arxiv.org/pdf/1106.1451.pdf

See Also

```
glm.pcr, alfapcr.tune
```

Examples

```
library(MASS)
y <- as.vector(fgl[, 1])
x <- as.matrix(fgl[, 2:9])
x <- x / rowSums(x)
mod <- alfa.pcr(y = y, x = x, 0.7, 1)
mod</pre>
```

Multivariate regression with compositional data ${\it Multivariate \ regression \ with \ compositional \ data}$

Description

Multivariate regression with compositional data.

Usage

```
comp.reg(y, x, type = "classical", xnew = NULL, yb = NULL)
```

Arguments

١	ı A	A matrix	with com	psitional	data.	Zero	values	are not allowed.

The predictor variable(s), they have to be continuous.

type The type of regression to be used, "classical" for standard multivariate regres-

sion, or "spatial" for the robust spatial median regression. Alternatively you can type "lmfit" for the fast classical multivariate regression that does not return

standard errors whatsoever.

xnew This is by default set to NULL. If you have new data whose compositional data

values you want to predict, put them here.

yb If you have already transformed the data using the additive log-ratio transforma-

tion, plut it here. Othewrise leave it NULL. This is intended to be used in the

function alfareg. tune in order to speed up the process.

Details

The additive log-ratio transformation is applied and then the chosen multivariate regression is implemented. The alr is easier to explain than the ilr and that is why the latter is avoided here.

Value

A list including:

runtime The time required by the regression.

be The beta coefficients.

seb The standard error of the beta coefficients.

est The fitted values of xnew if xnew is not NULL.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Giorgos Athineou <gioathineou@gmail.com>.

References

Mardia K.V., Kent J.T., and Bibby J.M. (1979). Multivariate analysis. Academic press.

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
multivreg, spatmed.reg, js.compreg, diri.reg
```

Examples

```
library(MASS)
y <- as.matrix(iris[, 1:3])
y <- y / rowSums(y)
x <- as.vector(iris[, 4])
mod1 <- comp.reg(y, x)
mod2 <- comp.reg(y, x, type = "spatial")</pre>
```

Multivariate skew normal random values simulation on the simplex

Multivariate skew normal random values simulation on the simplex

Description

Multivariate skew normal random values simulation on the simplex.

Usage

```
rcompsn(n, xi, Omega, alpha, dp = NULL, type = "alr")
```

Arguments

n	The sample size, a numerical value.
xi	A numeric vector of length \boldsymbol{d} representing the location parameter of the distribution.
Omega	A $d \times d$ symmetric positive-definite matrix of dimension.
alpha	A numeric vector which regulates the slant of the density.
dp	A list with three elements, corresponding to xi, Omega and alpha described above. The default value is FALSE. If dp is assigned, individual parameters must not be specified.
type	The alr (type = "alr") or the ilr (type = "ilr") is to be used for closing the Euclidean data onto the simplex.

Details

The algorithm is straightforward, generate random values from a multivariate t distribution in \mathbb{R}^d and brings the values to the simplex \mathbb{S}^d using the inverse of a log-ratio transformation.

Value

A matrix with the simulated data.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Azzalini, A. and Dalla Valle, A. (1996). The multivariate skew-normal distribution. Biometrika, 83(4): 715-726.

Azzalini, A. and Capitanio, A. (1999). Statistical applications of the multivariate skew normal distribution. Journal of the Royal Statistical Society Series B, 61(3):579-602. Full-length version available from http://arXiv.org/abs/0911.2093

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
comp.den, rdiri, rcompnorm
```

Examples

```
x <- as.matrix(iris[, 1:2])
par <- sn::msn.mle(y = x)$dp
y <- rcompsn(100, dp = par)
comp.den(y, dist = "skewnorm")
ternary(y)</pre>
```

Multivariate t random values simulation on the simplex

Multivariate t random values simulation on the simplex

Description

Multivariate t random values simulation on the simplex.

Usage

```
rcompt(n, m, s, dof, type = "alr")
```

Arguments

n	The sample size, a numerical value.
m	The mean vector in \mathbb{R}^d .
S	The covariance matrix in \mathbb{R}^d .
dof	The degrees of freedom.
type	The alr (type = "alr") or the ilr (type = "ilr") is to be used for closing the Euclidean data onto the simplex.

Details

The algorithm is straightforward, generate random values from a multivariate t distribution in \mathbb{R}^d and brings the values to the simplex \mathbb{S}^d using the inverse of a log-ratio transformation.

Value

A matrix with the simulated data.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
comp.den, rdiri, rcompnorm
```

Examples

```
x <- as.matrix(iris[, 1:2])
m <- Rfast::colmeans(x)
s <- var(x)
y <- rcompt(100, m, s, 10)
comp.den(y, dist = "t")
ternary(y)</pre>
```

Naive Bayes classifiers for compositional data $Naive\ Bayes\ classifiers\ for\ compositional\ data$

Description

Naive Bayes classifiers for compositional data.

Usage

```
comp.nb(xnew = NULL, x, ina, type = "beta")
```

Arguments

xnew	A matrix with the new compositional predictor data whose class you want to predict. Zeros are not allowed
Χ	A matrix with the available compositional predictor data. Zeros are not allowed
ina	A vector of data. The response variable, which is categorical (factor is acceptable).
type	The type of naive Bayes, "beta", "logitnorm", "cauchy", "laplace", "gamma", "normlog" or "weibull". For the last 4 distributions, the negative of the logarithm of the compositional data is applied first.

Value

Depending on the classifier a list including (the ni and est are common for all classifiers):

A matrix with the shape parameters. shape A matrix with the scale parameters. scale A matrix with the mean parameters. expmu A matrix with the (MLE, hence biased) variance parameters. sigma location A matrix with the location parameters (medians). scale A matrix with the scale parameters. mean A matrix with the scale parameters. var A matrix with the variance parameters. A matrix with the "alpha" parameters. b A matrix with the "beta" parameters. The sample size of each group in the dataset. ni est

The estimated group of the xnew observations. It returns a numerical value back regardless of the target variable being numerical as well or factor. Hence, it is suggested that you do \"as.numeric(ina)\" in order to see what is the predicted

class of the new data.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Friedman J., Hastie T. and Tibshirani R. (2017). The elements of statistical learning. New York: Springer.

See Also

```
cv.compnb, alfa.rda, alfa.knn, comp.knn, mix.compnorm, dda
```

Examples

```
x \leftarrow Compositional::rdiri(100, runif(5))
ina \leftarrow rbinom(100, 1, 0.5) + 1
a \leftarrow comp.nb(x, x, ina, type = "beta")
```

Naive Bayes classifiers for compositional data using the alpha-transformation $% \left(1\right) =\left(1\right) \left(1\right) \left($

Naive Bayes classifiers for compositional data using the α -transformation

Description

Naive Bayes classifiers for compositional data using the α -transformation.

Usage

```
alfa.nb(xnew, x, ina, a, type = "gaussian")
```

Arguments

xnew	A matrix with the new compositional predictor data whose class you want to predict. Zeros are allowed.
x	A matrix with the available compositional predictor data. Zeros are allowed.
ina	A vector of data. The response variable, which is categorical (factor is acceptable).
a	This can be a vector of values or a single number.
type	The type of naive Bayes, "gaussian", "cauchy" or "laplace".

Details

The α -transformation is applied to the compositional and a naive Bayes classifier is employed.

Value

A matrix with the estimated groups. One column for each value of α .

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. https://arxiv.org/pdf/1106.1451.pdf

Friedman J., Hastie T. and Tibshirani R. (2017). The elements of statistical learning. New York: Springer.

See Also

```
comp.nb, alfa.rda, alfa.knn, comp.knn, mix.compnorm
```

Examples

```
x <- Compositional::rdiri(100, runif(5) )
ina <- rbinom(100, 1, 0.5) + 1
mod <- alfa.nb(x, x, a = c(0, 0.1, 0.2), ina )</pre>
```

Non linear least squares regression for compositional data Non linear least squares regression for compositional data

Description

Non linear least squares regression for compositional data.

Usage

```
ols.compreg(y, x, con = TRUE, B = 1, ncores = 1, xnew = NULL)
```

Arguments

у	A matrix with the compositional data (dependent variable). Zero values are allowed.
x	A matrix or a data frame with the predictor variable(s).
con	If this is TRUE (default) then the constant term is estimated, otherwise the model includes no constant term.
В	If B is greater than 1 bootstrap estimates of the standard error are returned. If B=1, no standard errors are returned.
ncores	If ncores is 2 or more parallel computing is performed. This is to be used for the case of bootstrap. If B=1, this is not taken into consideration.
xnew	If you have new data use it, otherwise leave it NULL.

Details

The ordinary least squares between the observed and the fitted compositional data is adopted as the objective function. This involves numerical optimization since the relationship is non linear. There is no log-likelihood.

Value

A list including:

runtime The time required by the regression.

beta The beta coefficients.

covbe The covariance matrix of the beta coefficients. If B=1, this is based on the

observed information (Hessian matrix), otherwise if B> this is the bootstrap

estimate.

est The fitted of xnew if xnew is not NULL.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Murteira, Jose MR, and Joaquim JS Ramalho 2016. Regression analysis of multivariate fractional data. Econometric Reviews 35(4): 515-552.

See Also

```
diri.reg, js.compreg, kl.compreg, comp.reg, comp.reg, alfa.reg
```

Examples

```
library(MASS)
x <- as.vector(fgl[, 1])
y <- as.matrix(fgl[, 2:9])
y <- y / rowSums(y)
mod1 <- ols.compreg(y, x, B = 1, ncores = 1)
mod2 <- js.compreg(y, x, B = 1, ncores = 1)</pre>
```

Non-parametric zero replacement strategies

Non-parametric zero replacement strategies

Description

Non-parametric zero replacement strategies.

Usage

```
zeroreplace(x, a = 0.65, delta = NULL, type = "multiplicative")
```

X	A matrix with the compositional data.
a	The replacement value (δ) will be "a" times the minimum value observed in the compositional data.
delta	Unless you specify the replacement value δ here.
type	This can be any of "multiplicative", "additive" or "simple". See the references for more details.

Details

The "additive" is the zero replacement strategy suggested in Aitchison (1986, pg. 269). All of the three strategies can be found in Martin-Fernandez et al. (2003).

Value

A matrix with the zero replaced compositional data.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Martin-Fernandez J. A., Barcelo-Vidal C. & Pawlowsky-Glahn, V. (2003). Dealing with zeros and missing values in compositional data sets using nonparametric imputation. Mathematical Geology, 35(3): 253-278.

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
perturbation, alfa
```

Examples

```
x <- as.matrix(iris[1:20, 1:4])
x <- x/ rowSums(x)
x[ sample(1:20, 4), sample(1:4, 1) ] <- 0
x <- x / rowSums(x)
zeroreplace(x)</pre>
```

Permutation linear independence test in the SCLS model

Permutation linear independence test in the SCLS model

Description

Permutation linear independence test in the SCLS model.

Usage

```
scls.indeptest(y, x, R = 999)
```

Arguments

- y A matrix with the compositional data (dependent variable). Zero values are
- x A matrix with the compositional predictors. Zero values are allowed.
- R The number of permutations to perform.

Details

Permutation independence test in the constrained linear least squares for compositional responses and predictors is performed. The observed test statistic is the MSE computed by scls. Then, the rows of X are permuted B times and each time the constrained OLS is performed and the MSE is computed. The p-value is then computed in the usual way.

Value

The p-value for the test of independence between Y and X.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Tsagris. M. (2024). Constrained least squares simplicial-simplicial regression. https://arxiv.org/pdf/2403.19835.pdf

See Also

```
scls, scls2, tflr, scls.betest
```

Examples

```
library(MASS)
set.seed(1234)
y <- rdiri(214, runif(4, 1, 3))
x <- as.matrix(fgl[, 2:9])
x <- x / rowSums(x)
scls.indeptest(y, x, R = 99)</pre>
```

Permutation linear independence test in the TFLR model

Permutation linear independence test in the TFLR model

Description

Permutation linear independence test in the TFLR model.

Usage

```
tflr.indeptest(y, x, R = 999, ncores = 1)
```

Arguments

у	A matrix with the compositional data (dependent variable). Zero values are allowed.
х	A matrix with the compositional predictors. Zero values are in general allowed, but there can be cases when these are problematic.
R	The number of permutations to perform.
ncores	The number of cores to use in case you are interested for parallel computations.

Details

Permutation independence test in the constrained linear least squares for compositional responses and predictors is performed. The observed test statistic is the Kullback-Leibler divergence computed by tflr. Then, the rows of X are permuted B times and each time the TFLR is performed and the Kullback-Leibler is computed. The p-value is then computed in the usual way.

Value

The p-value for the test of linear independence between the simplicial response Y and the simplicial predictor X.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Fiksel J., Zeger S. and Datta A. (2022). A transformation-free linear regression for compositional outcomes and predictors. Biometrics, 78(3): 974–987.

Tsagris. M. (2024). Constrained least squares simplicial-simplicial regression. https://arxiv.org/pdf/2403.19835.pdf

See Also

```
tflr, scls, tflr.betest
```

Examples

```
library(MASS)
set.seed(1234)
y <- rdiri(214, runif(4, 1, 3))
x <- as.matrix(fgl[, 2:9])
x <- x / rowSums(x)
tflr.indeptest(y, x, R = 10)</pre>
```

Permutation test for the matrix of coefficients in the SCLS model

Permutation test for the matrix of coefficients in the SCLS model

Description

Permutation test for the matrix of coefficients in the SCLS model.

Usage

```
scls.betest(y, x, B, R = 999)
```

Arguments

У	A matrix with the compositional data (dependent variable). Zero values are allowed.
х	A matrix with the compositional predictors. Zero values are allowed.
В	A specific matrix of coefficients to test. Under the null hypothesis, the matrix of coefficients is equal to this matrix.
R	The number of permutations to perform.

Details

Permutation independence test in the constrained linear least squares for compositional responses and predictors is performed. The observed test statistic is the MSE computed by scls. Then, the rows of X are permuted B times and each time the constrained OLS is performed and the MSE is computed. The p-value is then computed in the usual way.

Value

The p-value for the test of independence between Y and X.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Tsagris. M. (2024). Constrained least squares simplicial-simplicial regression. https://arxiv.org/pdf/2403.19835.pdf

See Also

```
scls, scls2, tflr, scls.indeptest,tflr.indeptest
```

Examples

```
y <- rdiri(100, runif(3, 1, 3) )
x <- rdiri(100, runif(3, 1, 3) )
B <- diag(3)
scls.betest(y, x, B = B, R = 99)</pre>
```

Permutation test for the matrix of coefficients in the TFLR model

Permutation test for the matrix of coefficients in the TFLR model

Description

Permutation test for the matrix of coefficients in the TFLR model.

Usage

```
tflr.betest(y, x, B, R = 999, ncores = 1)
```

Arguments

У	A matrix with the compositional data (dependent variable). Zero values are allowed.
x	A matrix with the compositional predictors. Zero values are in general allowed, but there can be cases when these are problematic.
В	A specific matrix of coefficients to test. Under the null hypothesis, the matrix of coefficients is equal to this matrix.
R	The number of permutations to perform.
ncores	The number of cores to use in case you are interested for parallel computations.

Perturbation operation

Details

Permutation independence test in the constrained linear least squares for compositional responses and predictors is performed. The observed test statistic is the Kullback-Leibler divergence computed by tflr. Then, the rows of X are permuted B times and each time the TFLR is performed and the Kullback-Leibler is computed. The p-value is then computed in the usual way.

Value

The p-value for the test of linear independence between the simplicial response Y and the simplicial predictor X.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Fiksel J., Zeger S. and Datta A. (2022). A transformation-free linear regression for compositional outcomes and predictors. Biometrics, 78(3): 974–987.

Tsagris. M. (2024). Constrained least squares simplicial-simplicial regression. https://arxiv.org/pdf/2403.19835.pdf

See Also

```
tflr, tflr.indeptest, scls, scls.indeptest
```

Examples

```
y <- rdiri(100, runif(3, 1, 3) )
x <- rdiri(100, runif(3, 1, 3) )
B <- diag(3)
tflr.betest(y, x, B = B, R = 99)</pre>
```

Perturbation operation

Perturbation operation

Description

Perturbation operation.

```
perturbation(x, y, oper = "+")
```

X	A matrix with the compositional data.
у	Either a matrix with compositional data or a vector with compositional data. In either case, the data may not be compositional data, as long as they non negative.
oper	For the summation this must be "*" and for the negation it must be "/". Accord-

ing to Aitchison (1986), multiplication is equal to summation in the log-space,

and division is equal to negation.

Details

This is the perturbation operation defined by Aitchison (1986).

Value

A matrix with the perturbed compositional data.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

power

Examples

```
x <- as.matrix(iris[1:15, 1:4])
y <- as.matrix(iris[21:35, 1:4])
perturbation(x, y)
perturbation(x, y[1, ])</pre>
```

Plot of the LASSO coefficients

Plot of the LASSO coefficients

Description

Plot of the LASSO coefficients.

```
lassocoef.plot(lasso, lambda = TRUE)
```

lasso An object where you have saved the result of the LASSO regression. See the

examples for more details.

lambda If you want the x-axis to contain the logarithm of the penalty parameter $log(\lambda)$

set this to TRUE. Otherwise the x-axis will contain the L_1 -norm of the coeffi-

cients.

Details

This function plots the L_2 -norm of the coefficients of each predictor variable versus the $\log(\lambda)$ or the L_1 -norm of the coefficients. This is the same plot as the one produced by the glmnet package with type.coef = "2norm".

Value

A plot of the L_2 -norm of the coefficients of each predictor variable (y-axis) versus the L_1 -norm of all the coefficients (x-axis).

Author(s)

Michail Tsagris and Abdulaziz Alenazi.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Abdulaziz Alenazi <a.alenazi@nbu.edu.sa>. <a.alenazi@nbu.edu.sa>.

References

Alenazi, A. A. (2022). f-divergence regression models for compositional data. Pakistan Journal of Statistics and Operation Research, 18(4): 867–882.

Friedman, J., Hastie, T. and Tibshirani, R. (2010) Regularization Paths for Generalized Linear Models via Coordinate Descent. Journal of Statistical Software, Vol. 33(1), 1–22.

See Also

```
lasso.klcompreg, cv.lasso.klcompreg, lasso.compreg, cv.lasso.compreg, kl.compreg, comp.reg
```

Examples

```
y <- as.matrix(iris[, 1:4])
y <- y / rowSums(y)
x <- matrix( rnorm(150 * 30), ncol = 30 )
a <- lasso.klcompreg(y, x)
lassocoef.plot(a)
b <- lasso.compreg(y, x)
lassocoef.plot(b)</pre>
```

Power operation 153

Power operation

Power operation

Description

Power operation.

Usage

```
pow(x, a)
```

Arguments

x A matrix with the compositional data.

a Either a vector with numbers of a single number.

Details

This is the power operation defined by Aitchison (1986). It is also the starting point of the α -transformation.

Value

A matrix with the power transformed compositional data.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. http://arxiv.org/pdf/1106.1451.pdf

See Also

```
perturbation, alfa
```

Examples

```
x <- as.matrix(iris[1:15, 1:4])
a <- runif(1)
pow(x, a)</pre>
```

Principal component analysis

Principal component analysis

Description

Principal component analysis.

Usage

```
logpca(x, center = TRUE, scale = TRUE, k = NULL, vectors = FALSE)
```

Arguments

A matrix with the compositional data. Zero values are not allowed.
A matrix with the compositional data. Zero values are not allowed.

center Do you want your data centered? TRUE or FALSE.

scale Do you want each of your variables scaled, i.e. to have unit variance? TRUE or

FALSE.

k If you want a specific number of eigenvalues and eigenvectors set it here, other-

wise all eigenvalues (and eigenvectors if requested) will be returned.

vectors Do you want the eigenvectors be returned? By dafault this is FALSE.

Details

The logarithm is applied to the compositional data and PCA is performed.

Value

A list including:

values The eigenvalues. vectors The eigenvectors.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
alfa.pca, alfa.pcr, kl.alfapcr
```

Examples

```
x <- as.matrix(iris[, 1:4])
x <- x/ rowSums(x)
a <- logpca(x)</pre>
```

Principal component analysis using the alpha-transformation Principal component analysis using the α -transformation

Description

Principal component analysis using the α -transformation.

Usage

```
alfa.pca(x, a, center = TRUE, scale = TRUE, k = NULL, vectors = FALSE)
```

Arguments

x	A matrix with the compositional data. Zero values are allowed. In that case "a" should be positive.
a	The value of α to use in the α -transformation.
center	Do you want your data centered? TRUE or FALSE.
scale	Do you want each of your variables scaled, i.e. to have unit variance? TRUE or FALSE.
k	If you want a specific number of eigenvalues and eigenvectors set it here, otherwise all eigenvalues (and eigenvectors if requested) will be returned.
vectors	Do you want the eigenvectors be returned? By dafault this is FALSE.

Details

The α -transformation is applied to the compositional data and then PCA is performed. Note however, that the right multiplication by the Helmert sub-matrix is not applied in order to be in accordance with Aitchison (1983). When $\alpha = 0$, this results to the PCA proposed by Aitchison (1983).

Value

A list including:

values The eigenvalues. vectors The eigenvectors.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

Aitchison, J. (1983). Principal component analysis of compositional data. Biometrika, 70(1), 57-65.

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. http://arxiv.org/pdf/1106.1451.pdf

See Also

```
logpca, alfa.pcr, kl.alfapcr
```

Examples

```
x <- as.matrix(iris[, 1:4])
x <- x/ rowSums(x)
a <- alfa.pca(x, 0.5)</pre>
```

Principal component generalised linear models

Principal component generalised linear models

Description

Principal component generalised linear models.

Usage

```
glm.pcr(y, x, k = 1, xnew = NULL)
```

Arguments

У	A numerical vector with 0 and 1 (binary) or a vector with discrete (count) data.
x	A matrix with the predictor variable(s), they have to be continuous.
k	A number greater than or equal to 1. How many principal components to use. You may get results for the sequence of principal components.

xnew If you have new data use it, otherwise leave it NULL.

Details

Principal component regression is performed with binary logistic or Poisson regression, depending on the nature of the response variable. The principal components of the cross product of the independent variables are obtained and classical regression is performed. This is used in the function alfa.pcr.

Value

A list including:

model The summary of the logistic or Poisson regression model as returned by the

package Rfast.

per The percentage of variance of the predictor variables retained by the k principal

components.

vec The principal components, the loadings.

est The fitted or the predicted values (if xnew is not NULL). If the argument k

is a vector then this is a matrix with the estimated values for each number of

components.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aguilera A.M., Escabias M. and Valderrama M.J. (2006). Using principal components for estimating logistic regression with high-dimensional multicollinear data. Computational Statistics & Data Analysis 50(8): 1905-1924.

Jolliffe I.T. (2002). Principal Component Analysis.

See Also

```
alfa.pcr, alfapcr.tune
```

Examples

```
x <- as.matrix(iris[, 1:4])
y <- rbinom(150, 1, 0.6)
mod <- glm.pcr(y, x, k = 1)</pre>
```

Principal coordinate analysis using the alpha-distance $\textit{Principal coordinate analysis using the α-distance }$

Description

Principal coordinate analysis using the α -distance.

```
alfa.mds(x, a, k = 2, eig = TRUE)
```

X	A matrix with the compositional data. Zero values are allowed.
а	The value of a. In case of zero values in the data it has to be greater than 1.
k	The maximum dimension of the space which the data are to be represented in. This can be a number between 1 and $D-1$, where D denotes the number of dimensions.
eig	Should eigenvalues be returned? The default value is TRUE.

Details

The function computes the α -distance matrix and then plugs it into the classical multidimensional scaling function in the "cmdscale" function.

Value

A list with the results of "cmdscale" function.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

Cox, T. F. and Cox, M. A. A. (2001). Multidimensional Scaling. Second edition. Chapman and Hall.

Mardia, K. V., Kent, J. T. and Bibby, J. M. (1979). Chapter 14 of Multivariate Analysis, London: Academic Press.

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. https://arxiv.org/pdf/1106.1451.pdf

See Also

```
esov.mds, alfa.pca,
```

Examples

```
x <- as.matrix(iris[, 1:4])
x <- x/ rowSums(x)
a <- esov.mds(x)</pre>
```

Principal coordinate analysis using the Jensen-Shannon divergence

Principal coordinate analysis using the Jensen-Shannon divergence

Description

Principal coordinate analysis using the Jensen-Shannon divergence.

Usage

```
esov.mds(x, k = 2, eig = TRUE)
```

Arguments

x A matrix with the compositional data. Zero values are allowed.

k The maximum dimension of the space which the data are to be represented in.

This can be a number between 1 and D-1, where D denotes the number of

dimensions.

eig Should eigenvalues be returned? The default value is TRUE.

Details

The function computes the Jensen-Shannon divergence matrix and then plugs it into the classical multidimensional scaling function in the "cmdscale" function.

Value

A list with the results of "cmdscale" function.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

Cox, T. F. and Cox, M. A. A. (2001). Multidimensional Scaling. Second edition. Chapman and Hall.

Mardia, K. V., Kent, J. T. and Bibby, J. M. (1979). Chapter 14 of Multivariate Analysis, London: Academic Press.

Tsagris, Michail (2015). A novel, divergence based, regression for compositional data. Proceedings of the 28th Panhellenic Statistics Conference, 15-18/4/2015, Athens, Greece. https://arxiv.org/pdf/1511.07600.pdf

See Also

```
alfa.mds, alfa.pca,
```

Examples

```
x <- as.matrix(iris[, 1:4])
x <- x/ rowSums(x)
a <- esov.mds(x)</pre>
```

Projection pursuit regression for compositional data

Projection pursuit regression for compositional data

Description

Projection pursuit regression for compositional data.

Usage

```
comp.ppr(y, x, nterms = 3, type = "alr", xnew = NULL, yb = NULL )
```

Arguments

y A matrix with the compos	itional data.
----------------------------	---------------

x A matrix with the continuous predictor variables or a data frame including cate-

gorical predictor variables.

nterms The number of terms to include in the final model.

type Either "alr" or "ilr" corresponding to the additive or the isometric log-ratio trans-

formation respectively.

xnew If you have new data use it, otherwise leave it NULL.

yb If you have already transformed the data using a log-ratio transformation put it

here. Othewrise leave it NULL.

Details

This is the standard projection pursuit. See the built-in function "ppr" for more details.

Value

A list includign:

runtime The runtime of the regression.

mod The produced model as returned by the function "ppr".

est The fitted values of xnew if xnew is not NULL.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Friedman, J. H. and Stuetzle, W. (1981). Projection pursuit regression. Journal of the American Statistical Association, 76, 817-823. doi: 10.2307/2287576.

See Also

```
compppr.tune, aknn.reg, akern.reg, comp.reg, kl.compreg, alfa.reg
```

Examples

```
y <- as.matrix(iris[, 1:3])
y <- y/ rowSums(y)
x <- iris[, 4]
mod <- comp.ppr(y, x)</pre>
```

Projection pursuit regression with compositional predictor variables

Projection pursuit regression with compositional predictor variables

Description

Projection pursuit regression with compositional predictor variables.

Usage

```
pprcomp(y, x, nterms = 3, type = "log", xnew = NULL)
```

Arguments

У	A numerical vector with the continuous variable.
X	A matrix with the compositional data. No zero values are allowed.
nterms	The number of terms to include in the final model.
type	Either "alr" or "log" corresponding to the additive log-ratio transformation or the simple logarithm applied to the compositional data.
xnew	If you have new data use it, otherwise leave it NULL.

Details

This is the standard projection pursuit. See the built-in function "ppr" for more details. When the data are transformed with the additive log-ratio transformation this is close in spirit to the log-contrast regression.

162 Projection pursuit regression with compositional predictor variables using the alpha-transformation

Value

A list including:

runtime The runtime of the regression.

mod The produced model as returned by the function "ppr".

est The fitted values of xnew if xnew is not NULL.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Friedman, J. H. and Stuetzle, W. (1981). Projection pursuit regression. Journal of the American Statistical Association, 76, 817-823. doi: 10.2307/2287576.

See Also

```
pprcomp.tune, ice.pprcomp, alfa.pcr, lc.reg, comp.ppr
```

Examples

```
x <- as.matrix( iris[, 2:4] )
x <- x/ rowSums(x)
y <- iris[, 1]
pprcomp(y, x)</pre>
```

Projection pursuit regression with compositional predictor variables using the alpha-transformation

Projection pursuit regression with compositional predictor variables using the α -transformation

Description

Projection pursuit regression with compositional predictor variables using the α -transformation.

```
alfa.pprcomp(y, x, nterms = 3, a, xnew = NULL)
```

Projection pursuit regression with compositional predictor variables using the alpha-transformation 163

Arguments

y A numerical vector with the continuous variable.

x A matrix with the compositional data. Zero values are allowed.

nterms The number of terms to include in the final model.

The value of α for the α -transformation.

xnew If you have new data use it, otherwise leave it NULL.

Details

This is the standard projection pursuit. See the built-in function "ppr" for more details. The compositional data are transformed with the α -transformation

Value

A list including:

runtime The runtime of the regression.

mod The produced model as returned by the function "ppr".

est The fitted values of xnew if xnew is not NULL.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Friedman, J. H. and Stuetzle, W. (1981). Projection pursuit regression. Journal of the American Statistical Association, 76, 817-823. doi: 10.2307/2287576.

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. https://arxiv.org/pdf/1106.1451.pdf

See Also

```
alfapprcomp.tune, pprcomp, comp.ppr
```

Examples

```
x <- as.matrix( iris[, 2:4] )
x <- x / rowSums(x)
y <- iris[, 1]
alfa.pprcomp(y, x, a = 0.5)</pre>
```

Projections based test for distributional equality of two groups

Projections based test for distributional equality of two groups

Description

Projections based test for distributional equality of two groups.

Usage

```
dptest(x1, x2, B = 100)
```

Arguments

x1 A matrix containing compositional data of the first group.
 x2 A matrix containing compositional data of the second group.
 B The number of random uniform projections to use.

Details

The test compares the distributions of two compositional datasets using random projections. For more details see Cuesta-Albertos, Cuevas and Fraiman (2009).

Value

A vector including:

pvalues The p-values of the Kolmogorov-Smirnov tests.

pvalue The p-value of the test based on the Benjamini and Heller (2008) procedure.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Cuesta-Albertos J. A., Cuevas A. and Fraiman, R. (2009). On projection-based tests for directional and compositional data. Statistics and Computing, 19: 367–380.

Benjamini Y. and Heller R. (2008). Screening for partial conjunction hypotheses. Biometrics, 64(4): 1215–1222.

See Also

comp.test

Examples

```
x1 <- rdiri(50, c(3, 4, 5)) ## Fisher distribution with low concentration x2 <- rdiri(50, c(3, 4, 5)) dptest(x1, x2)
```

Proportionality correlation coefficient matrix

Proportionality correlation coefficient matrix

Description

Proportionality correlation coefficient matrix.

Usage

pcc(x)

Arguments

Χ

A numerical matrix with the compositional data. Zeros are not allowed as the logarithm is applied.

Details

The function returns the proportionality correlation coefficient matrix. See Lovell et al. (2015) for more information.

Value

A matrix with the alr transformed data (if alr is used) or with the compositional data (if the alrinv is used).

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Zheng, B. (2000). Summarizing the goodness of fit of generalized linear models for longitudinal data. Statistics in medicine, 19(10), 1265-1275.

Lovell D., Pawlowsky-Glahn V., Egozcue J. J., Marguerat S. and Bahler, J. (2015). Proportionality: a valid alternative to correlation for relative data. PLoS Computational Biology, 11(3), e1004075.

See Also

```
acor, alr
```

Examples

```
x <- Compositional::rdiri(100, runif(4) )
a <- Compositional::pcc(x)</pre>
```

Quasi binomial regression for proportions

Quasi binomial regression for proportions

Description

Quasi binomial regression for proportions.

Usage

```
propreg(y, x, varb = "quasi", tol = 1e-07, maxiters = 100)
propregs(y, x, varb = "quasi", tol = 1e-07, logged = FALSE, maxiters = 100)
```

Arguments

У	A numerical vector proportions. 0s and 1s are allowed.
x	For the "propreg" a matrix with data, the predictor variables. This can be a matrix or a data frame. For the "propregs" this must be a numerical matrix, where each columns denotes a variable.
tol	The tolerance value to terminate the Newton-Raphson algorithm. This is set to 10^{-9} by default.
varb	The type of estimate to be used in order to estimate the covariance matrix of the regression coefficients. There are two options, either "quasi" (default value) or "glm". See the references for more information.
logged	Should the p-values be returned (FALSE) or their logarithm (TRUE)?
maxiters	The maximum number of iterations before the Newton-Raphson is terminated automatically.

Details

We are using the Newton-Raphson, but unlike R's built-in function "glm" we do no checks and no extra calculations, or whatever. Simply the model. The "propregs" is to be used for very many univariate regressions. The "x" is a matrix in this case and the significance of each variable (column of the matrix) is tested. The function accepts binary responses as well (0 or 1).

Value

For the "propreg" function a list including:

iters The number of iterations required by the Newton-Raphson.

varb The covariance matrix of the regression coefficients.

phi The phi parameter is returned if the input argument "varb" was set to "glm",

othwerise this is NULL.

info A table similar to the one produced by "glm" with the estimated regression co-

efficients, their standard error, Wald test statistic and p-values.

For the "propregs" a two-column matrix with the test statistics (Wald statistic) and the associated p-values (or their loggarithm).

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Papke L. E. & Wooldridge J. (1996). Econometric methods for fractional response variables with an application to 401(K) plan participation rates. Journal of Applied Econometrics, 11(6): 619–632.

McCullagh, Peter, and John A. Nelder. Generalized linear models. CRC press, USA, 2nd edition, 1989.

See Also

```
ols.compreg beta.reg
```

Examples

```
y <- rbeta(100, 1, 4)
x <- matrix(rnorm(100 * 3), ncol = 3)
a <- propreg(y, x)
y <- rbeta(100, 1, 4)
x <- matrix(rnorm(400 * 100), ncol = 400)
b <- propregs(y, x)
mean(b[, 2] < 0.05)</pre>
```

Random values generation from some univariate distributions defined on the (0,1) interval

Random values generation from some univariate distributions defined on the (0,1) interval

Description

Random values generation from some univariate distributions defined on the (0,1) interval.

```
rbeta1(n, a)
runitweibull(n, a, b)
rlogitnorm(n, m, s, fast = FALSE)
```

n	The sample size, a numerical value.
a	The shape parameter of the beta distribution. In the case of the unit Weibull, this is the shape parameter.
b	This is the scale parameter for the unit Weibull distribution.
m	The mean of the univariate normal in R .
S	The standard deviation of the univariate normal in R .
fast	If you want a faster generation set this equal to TRUE. This will use the Rnorm() function from the Rfast package. However, the speed is only observable if you want to simulate at least 500 (this number may vary among computers) observations. The larger the sample size the higher the speed-up.

Details

The function genrates random values from the Be(a, 1), the unit Weibull or the univariate logistic normal distribution.

Value

A vector with the simulated data.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

See Also

```
beta.est, colbeta.est, rdiri
```

Examples

```
x <- rbeta1(100, 3)
```

Read a file as a Filebacked Big Matrix $Read\ a\ file\ as\ a\ Filebacked\ Big\ Matrix$

Description

Read a file as a Filebacked Big Matrix.

```
read.fbm(file, select)
```

file The File to read.

select Indices of columns to read (sorted). The length of select will be the number of

columns of the resulting FBM.

Details

The functions read a file as a Filebacked Big Matrix object. For more information see the "bigstatsr" package.

Value

A Filebacked Big Matrix object.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

See Also

scls

Examples

```
x \leftarrow matrix( runif(50 * 20, 0, 2*pi), ncol = 20 )
```

Regression with compositional data using the alpha-transformation Regression with compositional data using the α -transformation

Description

Regression with compositional data using the α -transformation.

```
alfa.reg(y, x, a, xnew = NULL, yb = NULL)
alfa.reg2(y, x, a, xnew = NULL)
alfa.reg3(y, x, a = c(-1, 1), xnew = NULL)
```

y A matrix with the compositional data.

x A matrix with the continuous predictor variables or a data frame including cate-

gorical predictor variables.

a The value of the power transformation, it has to be between -1 and 1. If zero

values are present it has to be greater than 0. If $\alpha=0$ the isometric log-ratio transformation is applied and the solution exists in a closed form, since it the classical mutivariate regression. For the alfa.reg2() this should be a vector of α values and the function call repeatedly the alfa.reg() function. For the alfa.reg3() function it should be a vector with two values, the endpoints of the interval of α . This function searches for the optimal value of α that minimizes the sum of squares of the errors. Using the optimize function it searches for the optimal value of α . Instead of choosing the value of α using alfareg. tune (that uses

cross-validation) one can select it this way.

xnew If you have new data use it, otherwise leave it NULL.

yb If you have already transformed the data using the α -transformation with the

same α as given in the argument "a", put it here. Othewrise leave it NULL.

This is intended to be used in the function alfareg. tune in order to speed up the process. The time difference in that function is small for small samples. But, if you have a few thousands and or a few more components, there will be bigger

differences.

Details

The α -transformation is applied to the compositional data first and then multivariate regression is applied. This involves numerical optimisation. The alfa.reg2() function accepts a vector with many values of α , while the the alfa.reg3() function searches for the value of α that minimizes the Kulback-Leibler divergence between the observed and the fitted compositional values. The functions are highly optimized.

Value

For the alfa.reg() function a list including:

runtime The time required by the regression.

be The beta coefficients.

The standard error of the beta coefficients.

est The fitted values for xnew if xnew is not NULL.

For the alfa.reg2() function a list with as many sublists as the number of values of α . Each element (sublist) of the list contains the above outcomes of the alfa.reg() function.

For the alfa.reg3() function a list with all previous elements plus an output "alfa", the optimal value of α .

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

Regularised and flexible discriminant analysis for compositional data using the alpha-transformation171

References

Tsagris M. (2015). Regression analysis with compositional data containing zero values. Chilean Journal of Statistics, 6(2): 47-57. https://arxiv.org/pdf/1508.01913v1.pdf

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. https://arxiv.org/pdf/1106.1451.pdf

Mardia K.V., Kent J.T., and Bibby J.M. (1979). Multivariate analysis. Academic press.

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
alfareg.tune, diri.reg, js.compreg, kl.compreg, ols.compreg, comp.reg
```

Examples

```
library(MASS)
x <- as.vector(fgl[1:40, 1])
y <- as.matrix(fgl[1:40, 2:9])
y <- y / rowSums(y)
mod <- alfa.reg(y, x, 0.2)</pre>
```

Regularised and flexible discriminant analysis for compositional data using the alpha-transformation

Regularised and flexible discriminant analysis for compositional data using the α -transformation

Description

Regularised and flexible discriminant analysis for compositional data using the α -transformation.

Usage

```
alfa.rda(xnew, x, ina, a, gam = 1, del = 0)
alfa.fda(xnew, x, ina, a)
```

Arguments

xnew	A matrix with the new compositional data whose group is to be predicted. Zeros are allowed, but you must be careful to choose strictly positive vcalues of α .
x	A matrix with the available compositional data. Zeros are allowed, but you must be careful to choose strictly positive values of α .
ina	A group indicator variable for the available data.
а	The value of α for the α -transformation.
gam	This is a number between 0 and 1. It is the weight of the pooled covariance and the diagonal matrix.
del	This is a number between 0 and 1. It is the weight of the LDA and QDA.

Details

For the alfa.rda, the covariance matrix of each group is calcualted and then the pooled covariance matrix. The spherical covariance matrix consists of the average of the pooled variances in its diagonal and zeros in the off-diagonal elements. gam is the weight of the pooled covariance matrix and 1-gam is the weight of the spherical covariance matrix, Sa = gam * Sp + (1-gam) * sp. Then it is a compromise between LDA and QDA. del is the weight of Sa and 1-del the weight of each group covariance group.

For the alfa.fda a flexible discriminant analysis is performed. See the R package **fda** for more details.

Value

For the alfa.rda a list including:

prob The estimated probabilities of the new data of belonging to each group.

The estimated socres of the new data of each group.

The estimated group membership of the new data.

For the alfa.fda a list including:

and An fda object as returned by the command fda of the R package mda.

est The estimated group membership of the new data.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Giorgos Athineou <gioathineou@gmail.com>.

References

Friedman Jerome, Trevor Hastie and Robert Tibshirani (2009). The elements of statistical learning, 2nd edition. Springer, Berlin.

Tsagris Michail, Simon Preston and Andrew T.A. Wood (2016). Improved classification for compositional data using the α -transformation. Journal of classification, 33(2): 243-261. https://arxiv.org/pdf/1106.1451.pdf

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. https://arxiv.org/pdf/1106.1451.pdf

Hastie, Tibshirani and Buja (1994). Flexible Disriminant Analysis by Optimal Scoring. Journal of the American Statistical Association, 89(428):1255-1270.

See Also

alfa, alfarda.tune, alfa.knn, alfa.nb, comp.nb, mix.compnorm

Ridge regression 173

Examples

```
x <- as.matrix(iris[, 1:4])
x <- x / rowSums(x)
ina <- iris[, 5]
mod <- alfa.rda(x, x, ina, 0)
table(ina, mod$est)
mod2 <- alfa.fda(x, x, ina, 0)
table(ina, mod2$est)</pre>
```

Ridge regression

Ridge regression

Description

Ridge regression.

Usage

```
ridge.reg(y, x, lambda, B = 1, xnew = NULL)
```

Arguments

у	A real valued vector. If it contains percentages, the logit transformation is applied.
X	A matrix with the predictor variable(s), they have to be continuous.
lambda	The value of the regularisation parameter λ .
В	If $B = 1$ (default value) no bootstrpa is performed. Otherwise bootstrap standard errors are returned.
xnew	If you have new data whose response value you want to predict put it here, otherwise leave it as is.

Details

This is used in the function alfa.ridge. There is also a built-in function available from the MASS library, called "lm.ridge".

Value

A list including:

beta	The beta coefficients.
seb	The standard error of the coefficiens. If $B > 1$ the bootstrap standard errors will be returned.
est	The fitted or the predicted values (if xnew is not NULL).

174 Ridge regression plot

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Giorgos Athineou <gioathineou@gmail.com>.

References

Hoerl A.E. and R.W. Kennard (1970). Ridge regression: Biased estimation for nonorthogonal problems. Technometrics, 12(1): 55-67.

Brown P. J. (1994). Measurement, Regression and Calibration. Oxford Science Publications.

See Also

```
ridge.tune, alfa.ridge, ridge.plot
```

Examples

```
y <- as.vector(iris[, 1])
x <- as.matrix(iris[, 2:4])
mod1 <- ridge.reg(y, x, lambda = 0.1)
mod2 <- ridge.reg(y, x, lambda = 0)</pre>
```

Ridge regression plot Ridge regression plot

Description

A plot of the regularised regression coefficients is shown.

Usage

```
ridge.plot(y, x, lambda = seq(0, 5, by = 0.1))
```

Arguments

у	A numeric vector containing the values of the target variable. If the values are proportions or percentages, i.e. strictly within 0 and 1 they are mapped into R using the logit transformation. In any case, they must be continuous only.
X	A numeric matrix containing the continuous variables. Rows are samples and columns are features.
lambda	A grid of values of the regularisation parameter λ .

Details

For every value of λ the coefficients are obtained. They are plotted versus the λ values.

Value

A plot with the values of the coefficients as a function of λ .

Author(s)

Michail Tsagris.

R implementation and documentation: Giorgos Athineou <gioathineou@gmail.com> and Michail Tsagris <mtsagris@uoc.gr>.

References

Hoerl A.E. and R.W. Kennard (1970). Ridge regression: Biased estimation for nonorthogonal problems. Technometrics, 12(1): 55-67.

Brown P. J. (1994). Measurement, Regression and Calibration. Oxford Science Publications.

See Also

```
ridge.reg, ridge.tune, alfa.ridge, alfaridge.plot
```

Examples

```
y <- as.vector(iris[, 1])
x <- as.matrix(iris[, 2:4])
ridge.plot(y, x, lambda = seq(0, 2, by = 0.1) )</pre>
```

Ridge regression with compositional data in the covariates side using the alpha-transformation

Ridge regression with compositional data in the covariates side using the α -transformation

Description

Ridge regression with compositional data in the covariates side using the α -transformation.

Usage

```
alfa.ridge(y, x, a, lambda, B = 1, xnew = NULL)
```

Arguments

- A numerical vector containing the response variable values. If they are percentages, they are mapped onto R using the logit transformation.
- A matrix with the predictor variables, the compositional data. Zero values are allowed, but you must be careful to choose strictly positive values of α .

a	The value of the power transformation, it has to be between -1 and 1. If zero
	values are present it has to be greater than 0. If $\alpha = 0$ the isometric log-ratio
	transformation is applied.

lambda The value of the regularisation parameter, λ .

B If B > 1 bootstrap estimation of the standard errors is implemented.

xnew A matrix containing the new compositional data whose response is to be pre-

dicted. If you have no new data, leave this NULL as is by default.

Details

The α -transformation is applied to the compositional data first and then ridge components regression is performed.

Value

The output of the ridge.reg.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Giorgos Athineou <gioathineou@gmail.com>.

References

Tsagris M. (2015). Regression analysis with compositional data containing zero values. Chilean Journal of Statistics, 6(2): 47-57. https://arxiv.org/pdf/1508.01913v1.pdf

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. https://arxiv.org/pdf/1106.1451.pdf

See Also

```
ridge.reg, alfaridge.tune, alfaridge.plot
```

Examples

```
library(MASS)
y <- as.vector(fgl[, 1])
x <- as.matrix(fgl[, 2:9])
x <- x/ rowSums(x)
mod1 <- alfa.ridge(y, x, a = 0.5, lambda = 0.1, B = 1, xnew = NULL)
mod2 <- alfa.ridge(y, x, a = 0.5, lambda = 1, B = 1, xnew = NULL)</pre>
```

Ridge regression with the alpha-transformation plot $Ridge\ regression\ plot$

Description

A plot of the regularised regression coefficients is shown.

Usage

```
alfaridge.plot(y, x, a, lambda = seq(0, 5, by = 0.1))
```

Arguments

У	A numeric vector containing the values of the target variable. If the values are proportions or percentages, i.e. strictly within 0 and 1 they are mapped into R using the logit transformation. In any case, they must be continuous only.
x	A numeric matrix containing the continuous variables.
a	The value of the α -transformation. It has to be between -1 and 1. If there are zero values in the data, you must use a strictly positive value.
lambda	A grid of values of the regularisation parameter λ .

Details

For every value of λ the coefficients are obtained. They are plotted versus the λ values.

Value

A plot with the values of the coefficients as a function of λ .

Author(s)

Michail Tsagris.

R implementation and documentation: Giorgos Athineou <gioathineou@gmail.com> and Michail Tsagris <mtsagris@uoc.gr>.

References

Hoerl A.E. and R.W. Kennard (1970). Ridge regression: Biased estimation for nonorthogonal problems. Technometrics, 12(1): 55-67.

Brown P. J. (1994). Measurement, Regression and Calibration. Oxford Science Publications.

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. https://arxiv.org/pdf/1106.1451.pdf

See Also

```
ridge.plot, alfa.ridge
```

Examples

```
library(MASS)
y <- as.vector(fgl[, 1])
x <- as.matrix(fgl[, 2:9])
x <- x / rowSums(x)
alfaridge.plot(y, x, a = 0.5, lambda = seq(0, 5, by = 0.1) )</pre>
```

Simplicial constrained median regression for compositional responses and predictors \mbox{model}

Simplicial constrained median regression for compositional responses and predictors

Description

Simplicial constrained median regression for compositional responses and predictors.

Usage

```
scrq(y, x, xnew = NULL)
```

Arguments

у	A matrix with the compositional data (dependent variable). Zero values are allowed.
Х	A matrix with the compositional predictors. Zero values are allowed.
xnew	If you have new data use it, otherwise leave it NULL.

Details

The function performs median regression where the beta coefficients are constained to be positive and sum to 1.

Value

A list including:

mlad The mean absolute deviation.

be The beta coefficients.

est The fitted of xnew if xnew is not NULL.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Tsagris. M. (2024). Constrained least squares simplicial-simplicial regression. https://arxiv.org/pdf/2403.19835.pdf

See Also

```
scls, tflr
```

Examples

```
library(MASS)
set.seed(1234)
y <- rdiri(214, runif(4, 1, 3))
x <- as.matrix(fgl[, 2:9])
x <- x / rowSums(x)
mod <- scrq(y, x)
mod</pre>
```

Simulation of compositional data from Gaussian mixture models

Simulation of compositional data from Gaussian mixture models

Description

Simulation of compositional data from Gaussian mixture models.

Usage

```
rmixcomp(n, prob, mu, sigma, type = "alr")
```

Arguments

n	The sample size.
prob	A vector with mixing probabilities. Its length is equal to the number of clusters.
mu	A matrix where each row corresponds to the mean vector of each cluster.
sigma	An array consisting of the covariance matrix of each cluster.
type	Should the additive ("type=alr") or the isometric (type="ilr") log-ration be used? The default value is for the additive log-ratio transformation.

Details

A sample from a multivariate Gaussian mixture model is generated.

Value

A list including:

id A numeric variable indicating the cluster of simulated vector.

x A matrix containing the simulated compositional data. The number of dimensions will be + 1.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Ryan P. Browne, Aisha ElSherbiny and Paul D. McNicholas (2015). R package mixture: Mixture Models for Clustering and Classification.

See Also

```
mix.compnorm, bic.mixcompnorm
```

Examples

```
p <- c(1/3, 1/3, 1/3)
mu <- matrix(nrow = 3, ncol = 4)
s <- array( dim = c(4, 4, 3) )
x <- as.matrix(iris[, 1:4])
ina <- as.numeric(iris[, 5])
mu <- rowsum(x, ina) / 50
s[, , 1] <- cov(x[ina == 1, ])
s[, , 2] <- cov(x[ina == 2, ])
s[, , 3] <- cov(x[ina == 3, ])
y <- rmixcomp(100, p, mu, s, type = "alr")</pre>
```

Simulation of compositional data from mixtures of Dirichlet distributions

Simulation of compositional data from mixtures of Dirichlet distributions

Description

Simulation of compositional data from mixtures of Dirichlet distributions.

```
rmixdiri(n, a, prob)
```

Arguments

n	The sample size.

a A matrix where each row contains the parameters of each Dirichlet component.

prob A vector with the mixing probabilities.

Details

A sample from a Dirichlet mixture model is generated.

Value

A list including:

id A numeric variable indicating the cluster of simulated vector.

x A matrix containing the simulated compositional data.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Ye X., Yu Y. K. and Altschul S. F. (2011). On the inference of Dirichlet mixture priors for protein sequence comparison. Journal of Computational Biology, 18(8), 941-954.

See Also

```
rmixcomp, mixdiri.contour,
```

Examples

```
a <- matrix( c(12, 30, 45, 32, 50, 16), byrow = TRUE, ncol = 3) prob <- c(0.5, 0.5) x <- rmixdiri(100, a, prob)
```

Simulation of compositional data from the Flexible Dirichlet distribution

Simulation of compositional data from the Flexible Dirichlet distribution

Description

Simulation of compositional data from the Flexible Dirichlet distribution.

Usage

```
rfd(n, alpha, prob, tau)
```

Arguments

n The sample size.

alpha A vector of the non-negative α parameters.

prob A vector of the clusters' probabilities that must sum to one.

tau The positive scalar tau parameter.

Details

For more information see the references and the package FlxeDir.

Value

A matrix with compositional data.

Author(s)

Michail Tsagris ported from the R package FlexDir. <mtsagris@uoc.gr>.

References

Ongaro A. and Migliorati S. (2013). A generalization of the Dirichlet distribution. Journal of Multivariate Analysis, 114, 412–426.

Migliorati S., Ongaro A. and Monti G. S. (2017). A structured Dirichlet mixture model for compositional data: inferential and applicative issues. Statistics and Computing, 27, 963–983.

See Also

dfd

```
alpha <- c(12, 11, 10)
prob <- c(0.25, 0.25, 0.5)
x <- rfd(100, alpha, prob, 7)
```

Simulation of compositional data from the folded normal distribution $Simulation\ of\ compositional\ data\ from\ the\ folded\ model\ normal\ distribution$

Description

Simulation of compositional data from the folded model normal distribution.

Usage

```
rfolded(n, mu, su, a)
```

Arguments

n	The sample size.
mu	The mean vector.
su	The covariance matrix.
а	The value of α .

Details

A sample from the folded model is generated.

Value

A matrix with compositional data.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Tsagris M. and Stewart C. (2020). A folded model for compositional data analysis. Australian and New Zealand Journal of Statistics, 62(2): 249-277. https://arxiv.org/pdf/1802.07330.pdf

See Also

```
alfa, alpha.mle, a.est
```

Examples

Spatial median regression

Spatial median regression

Description

Spatial median regression with Euclidean data.

Usage

```
spatmed.reg(y, x, xnew = NULL, tol = 1e-07, ses = FALSE)
```

Arguments

y A matrix with the compositional data. Zero values are not allowed.

x The predictor variable(s), they have to be continuous.

xnew If you have new data use it, otherwise leave it NULL.

tol The threshold upon which to stop the iterations of the Newton-Rapshon algo-

The direction upon which to stop the iterations of the rewton Rapshon a

rithm.

ses If you want to extract the standard errors of the parameters, set this to TRUE.

Be careful though as this can slow down the algorithm dramatically. In a run example with 10,000 observations and 10 variables for y and 30 for x, when ses = FALSE the algorithm can take 0.20 seconds, but when ses = TRUE it can go

up to 140 seconds.

Details

The objective function is the minimization of the sum of the absolute residuals. It is the multivariate generalization of the median regression. This function is used by comp.reg.

Value

A list including:

iter The number of iterations that were required.

runtime The time required by the regression.

Ternary diagram 185

be	The beta	coefficients.
שט	THE DETA	cocincicitis.

seb The standard error of the beta coefficients is returned if ses=TRUE and NULL

otherwise.

est The fitted of xnew if xnew is not NULL.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Biman Chakraborty (2003). On multivariate quantile regression. Journal of Statistical Planning and Inference, 110(1-2), 109-132. http://www.stat.nus.edu.sg/export/sites/dsap/research/documents/tr01_2000.pdf

See Also

```
multivreg, comp.reg, alfa.reg, js.compreg, diri.reg
```

Examples

```
library(MASS)
x <- as.matrix(iris[, 3:4])
y <- as.matrix(iris[, 1:2])
mod1 <- spatmed.reg(y, x)
mod2 <- multivreg(y, x, plot = FALSE)</pre>
```

Ternary diagram

Ternary diagram

Description

Ternary diagram.

Usage

```
ternary(x, dg = FALSE, hg = FALSE, means = TRUE, pca = FALSE, colour = NULL)
```

Arguments

X	A matrix with the compositional data.
dg	Do you want diagonal grid lines to appear? If yes, set this TRUE.
hg	Do you want horizontal grid lines to appear? If yes, set this TRUE.
means	A boolean variable. Should the closed geometric mean and the arithmetic mean appear (TRUE) or not (FALSE)?.
pca	Should the first PCA calculated Aitchison (1983) described appear? If yes, then this should be TRUE, or FALSE otherwise.
colour	If you want the points to appear in different colour put a vector with the colour numbers or colours.

Details

There are two ways to create a ternary graph. We used here that one where each edge is equal to 1 and it is what Aitchison (1986) uses. For every given point, the sum of the distances from the edges is equal to 1. Horizontal and or diagonal grid lines can appear, so as the closed geometric and the simple arithmetic mean. The first PCA is calculated using the centred log-ratio transformation as Aitchison (1983, 1986) suggested. If the data contain zero values, the first PCA will not be plotted. Zeros in the data appear with green circles in the triangle and you will also see NaN in the closed geometric mean.

Value

The ternary plot and a 2-row matrix with the means. The closed geometric and the simple arithmetic mean vector and or the first principal component will appear as well if the user has asked for them. Additionally, horizontal or diagonal grid lines can appear as well.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Giorgos Athineou <gioathineou@gmail.com>.

References

Aitchison, J. (1983). Principal component analysis of compositional data. Biometrika 70(1):57-65. Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
ternary.mcr, ternary.reg, diri.contour
```

Examples

```
x <- as.matrix(iris[, 1:3])
x <- x / rowSums(x)
ternary(x, means = TRUE, pca = TRUE)</pre>
```

Ternary diagram of regression models

Ternary diagram of regression models

Description

Ternary diagram of regression models.

Usage

```
ternary.reg(y, est, id, labs)
```

Arguments

У	A matrix with the compositional data.
est	A matrix with all fitted compositional data for all regression models, one under the other.
id	A vector indicating the regression model of each fitted compositional data set.
labs	The names of the regression models to appea in the legend.

Details

The points first appear on the ternary plot. Then, the fitted compositional data appear with different lines for each regression model.

Value

The ternary plot and lines for the fitted values of each regression model.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
ternary, ternary.mcr, diri.contour
```

```
x <- cbind(1, rnorm(50) )
a <- exp( x %*% matrix( rnorm(6,0, 0.4), ncol = 3) )
y <- matrix(NA, 50, 3)
for (i in 1:50) y[i, ] <- rdiri(1, a[i, ])
est <- comp.reg(y, x[, -1], xnew = x[, -1])$est
ternary.reg(y, est, id = rep(1, 50), labs = "ALR regression")</pre>
```

Ternary diagram with confidence region for the matrix of coefficients of the SCLS or the TFLR model

Description

Ternary diagram with confidence region for the matrix of coefficients of the SCLS or the TFLR model.

Usage

```
ternary.coefcr(y, x, type = "scls", conf = 0.95, R = 1000, dg = FALSE, hg = FALSE)
```

Arguments

A matrix with the response compositional data.
A matrix with the predictor compositional data.
The type of model to use, "scls" or "tflr". Depending on the model selected, the function will construct the confidence regions of the estimated matrix of coefficients of that model.
The confidence level, by default this is set to 0.95.
Number of bootstrap replicates to run.
Do you want diagonal grid lines to appear? If yes, set this TRUE.
Do you want horizontal grid lines to appear? If yes, set this TRUE.

Details

This function runs the SCLS or the TFLR model and constructs confidence regions for the estimated matrix of regression coefficients using non-parametric bootstrap.

Value

A ternary plot of the estimated matrix of coefficients of the SCLS or of the TFLR model, and their associated confidence regions.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Fiksel J., Zeger S. and Datta A. (2022). A transformation-free linear regression for compositional outcomes and predictors. Biometrics, 78(3): 974–987.

Tsagris. M. (2024). Constrained least squares simplicial-simplicial regression. https://arxiv.org/pdf/2403.19835.pdf

See Also

```
ternary, scls, tflr, ternary.mcr
```

Examples

```
y <- rdiri(50, runif(3))
x <- rdiri(50, runif(4))
ternary.coefcr(y, x, R = 500, dg = TRUE, hg = TRUE)</pre>
```

Ternary diagram with confidence region for the mean

Ternary diagram with confidence region for the mean

Description

Ternary diagram with confidence region for the mean.

Usage

```
ternary.mcr(x, type = "alr", conf = 0.95, dg = FALSE, hg = FALSE, colour = NULL)
```

Arguments

X	A matrix with the compositional data.
dg	Do you want diagonal grid lines to appear? If yes, set this TRUE.
type	The type of log-ratio transformation to aply, the "alr" or the "ilr".
conf	The confidence level, by default this is set to 0.95.
hg	Do you want horizontal grid lines to appear? If yes, set this TRUE.
colour	If you want the points to appear in different colour put a vector with the colour numbers or colours.

Details

Ternary plot of compositional data including the log-ratio mean and its confidence region. The confidence region is based on the Hotelling T^2 test statistic of the log-ratio transformed data.

Value

A ternary plot of compositional data including the log-ratio mean and its confidence region.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison, J. (1983). Principal component analysis of compositional data. Biometrika 70(1):57-65. Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
ternary, ternary.reg, diri.contour
```

Examples

```
x <- as.matrix(iris[, 1:3])
x <- x / rowSums(x)
ternary.mcr(x, type = "alr", dg = TRUE, hg = TRUE)</pre>
```

Ternary diagram with the coefficients of the simplicial-simplicial regression models

Ternary diagram with the coefficients of the simplicial-simplicial regression models

Description

Ternary diagram with the coefficients of the simplicial-simplicial regression models.

Usage

```
ternary.coef(B, dg = FALSE, hg = FALSE, colour = NULL)
```

Arguments

В	A matrix with the coefficients of the tflr or the scls functions. See examples for this.
dg	Do you want diagonal grid lines to appear? If yes, set this TRUE.
hg	Do you want horizontal grid lines to appear? If yes, set this TRUE.
colour	If you want the points to appear in different colour put a vector with the colour numbers or colours.

Details

Ternary plot of the coefficients of the tflr or the scls functions.

Value

A ternary plot of the coefficients of the tflr or the scls functions.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison, J. (1983). Principal component analysis of compositional data. Biometrika 70(1):57-65. Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
ternary, ternary.reg, scls
```

Examples

```
y <- as.matrix(iris[, 1:3])
y <- y / rowSums(y)
x <- rdiri(150, runif(5, 1,4) )
mod <- scls(y, x)
ternary.coef(mod$be)</pre>
```

The additive log-ratio transformation and its inverse

The additive log-ratio transformation and its inverse

Description

The additive log-ratio transformation and its inverse.

Usage

```
alr(x)
alrinv(y)
```

Arguments

x A numerical matrix with the compositional data.

y A numerical matrix with data to be closed into the simplex.

Details

The additive log-ratio transformation with the first component being the common divisor is applied. The inverse of this transformation is also available. This means that no zeros are allowed.

Value

A matrix with the alr transformed data (if alr is used) or with the compositional data (if the alrinv is used).

The alpha-distance

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
bc, pivot, fp, green, alfa, alfainv
```

Examples

```
library(MASS)
x <- as.matrix(fgl[, 2:9])
x <- x / rowSums(x)
y <- alr(x)
x1 <- alrinv(y)</pre>
```

The alpha-distance

The α *-distance*

Description

This is the Euclidean (or Manhattan) distance after the α -transformation has been applied.

Usage

```
alfadist(x, a, type = "euclidean", square = FALSE)
alfadista(xnew, x, a, type = "euclidean", square = FALSE)
```

Arguments

xnew	A matrix or a vector with new compositional data.
Х	A matrix with the compositional data.
a	The value of the power transformation, it has to be between -1 and 1. If zero values are present it has to be greater than 0. If $\alpha=0$, the isometric log-ratio transformation is applied.
type	Which type distance do you want to calculate after the α -transformation, "euclidean", or "manhattan".
square	In the case of the Euclidean distance, you can choose to return the squared distance by setting this TRUE.

Details

The α -transformation is applied to the compositional data first and then the Euclidean or the Manhattan distance is calculated.

Value

For "alfadist" a matrix including the pairwise distances of all observations or the distances between xnew and x. For "alfadista" a matrix including the pairwise distances of all observations or the distances between xnew and x.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Tsagris M.T., Preston S. and Wood A.T.A. (2016). Improved classification for compositional data using the α -transformation. Journal of Classification. 33(2): 243–261. https://arxiv.org/pdf/1506.04976v2.pdf

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. https://arxiv.org/pdf/1106.1451.pdf

See Also

```
alfa, alfainv, alfa.reg, esov
```

Examples

```
library(MASS)
x <- as.matrix(fgl[1:20, 2:9])
x <- x / rowSums(x)
alfadist(x, 0.1)
alfadist(x, 1)</pre>
```

The alpha-IT transformation

The α -IT transformation

Description

The α -IT transformation.

Usage

```
ait(x, a, h = TRUE)
```

Arguments

а

h

x A matrix with the compositional data.

The value of the power transformation, it has to be between -1 and 1. If zero values are present it has to be greater than 0. If $\alpha=0$ the isometric log-ratio

transformation is applied.

A boolean variable. If is TRUE (default value) the multiplication with the Helmert sub-matrix will take place. When $\alpha=0$ and h=FALSE, the result is the centred log-ratio transformation (Aitchison, 1986). In general, when h=FALSE the resulting transformation maps the data onto a singualr space. The sum of the vectors is equal to 0. Hence, from the simplex constraint the data go

to another constraint.

Details

The α -IT transformation is applied to the compositional data.

Value

A matrix with the α -IT transformed data.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Clarotto L., Allard D. and Menafoglio A. (2022). A new class of α -transformations for the spatial analysis of Compositional Data. Spatial Statistics, 47.

See Also

```
aitdist, ait.knn, alfa, green, alr
```

```
library(MASS)
x <- as.matrix(fgl[, 2:9])
x <- x / rowSums(x)
y1 <- ait(x, 0.2)
y2 <- ait(x, 1)
rbind( colMeans(y1), colMeans(y2) )</pre>
```

The alpha-IT-distance 195

The alpha-IT-distance $\mathit{The}\ \alpha\text{-}\mathit{IT-distance}$

Description

This is the Euclidean (or Manhattan) distance after the α -IT-transformation has been applied.

Usage

```
aitdist(x, a, type = "euclidean", square = FALSE)
aitdista(xnew, x, a, type = "euclidean", square = FALSE)
```

Arguments

xnew	A matrix or a vector with new compositional data.
x	A matrix with the compositional data.
a	The value of the power transformation, it has to be between -1 and 1. If zero values are present it has to be greater than 0. If $\alpha=0$, the isometric log-ratio transformation is applied.
type	Which type distance do you want to calculate after the α -transformation, "euclidean", or "manhattan".
square	In the case of the Euclidean distance, you can choose to return the squared distance by setting this TRUE.

Details

The α -IT-transformation is applied to the compositional data first and then the Euclidean or the Manhattan distance is calculated.

Value

For "alfadist" a matrix including the pairwise distances of all observations or the distances between xnew and x. For "alfadista" a matrix including the pairwise distances of all observations or the distances between xnew and x.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Clarotto L., Allard D. and Menafoglio A. (2021). A new class of α -transformations for the spatial analysis of Compositional Data. https://arxiv.org/abs/2110.07967

See Also

```
ait, alfadist, alfa
```

Examples

```
library(MASS)
x <- as.matrix(fgl[1:20, 2:9])
x <- x / rowSums(x)
aitdist(x, 0.1)
aitdist(x, 1)</pre>
```

The alpha-k-NN regression for compositional response data $\textit{The α-k-NN regression for compositional response data}$

Description

The α -k-NN regression for compositional response data.

Usage

```
aknn.reg(xnew, y, x, a = seq(0.1, 1, by = 0.1), k = 2:10, apostasi = "euclidean", rann = FALSE)
```

Arguments

xnew	A matrix with the new predictor variables whose compositions are to be predicted.
у	A matrix with the compositional response data. Zeros are allowed.
X	A matrix with the available predictor variables.
a	The value(s) of α . Either a single value or a vector of values. As zero values in the compositional data are allowed, you must be careful to choose strictly positive values of α . However, if negative values are passed, the positive ones are used only.
k	The number of nearest neighbours to consider. It can be a single number or a vector.
apostasi	The type of distance to use, either "euclidean" or "manhattan".
rann	If you have large scale datasets and want a faster k-NN search, you can use kd-trees implemented in the R package "Rnanoflann". In this case you must set this argument equal to TRUE. Note however, that in this case, the only available distance is by default "euclidean".

Details

The α -k-NN regression for compositional response variables is applied.

Value

A list with the estimated compositional response data for each value of α and k.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Tsagris M., Alenazi A. and Stewart C. (2023). Flexible non-parametric regression models for compositional response data with zeros. Statistics and Computing, 33(106).

https://link.springer.com/article/10.1007/s11222-023-10277-5

See Also

```
aknnreg.tune, akern.reg, alfa.reg, comp.ppr, comp.reg, kl.compreg
```

Examples

```
y <- as.matrix( iris[, 1:3] )
y <- y / rowSums(y)
x <- iris[, 4]
mod <- aknn.reg(x, y, x, a = c(0.4, 0.5), k = 2:3, apostasi = "euclidean")</pre>
```

The alpha-k-NN regression with compositional predictor variables ${\it The} \,\, \alpha\text{-}k\text{-}NN \,\, regression \,\, with \,\, compositional \,\, predictor \,\, variables$

Description

The α -k-NN regression with compositional predictor variables.

Usage

```
alfa.knn.reg(xnew, y, x, a = 1, k = 2:10, apostasi = "euclidean", method = "average")
```

Arguments

xnew	A matrix with the new compositional predictor variables whose response is to be predicted. Zeros are allowed.
у	The response variable, a numerical vector.
X	A matrix with the available compositional predictor variables. Zeros are allowed.

а	A single value of α . As zero values in the compositional data are allowed,
	you must be careful to choose strictly positive values of α . If negative val-
	ues are passed, the positive ones are used only. If the data are already alpha-
	transformed, you can make this NULL.

The number of nearest neighbours to consider. It can be a single number or a vector.

apostasi The type of distance to use, either "euclidean" or "manhattan".

method If you want to take the average of the reponses of the k closest observations,

type "average". For the median, type "median" and for the harmonic mean, type

"harmonic".

Details

k

The α -k-NN regression with compositional predictor variables is applied.

Value

A matrix with the estimated response data for each value of k.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Tsagris M., Alenazi A. and Stewart C. (2023). Flexible non-parametric regression models for compositional response data with zeros. Statistics and Computing, 33(106).

https://link.springer.com/article/10.1007/s11222-023-10277-5

See Also

```
aknn.reg, alfa.knn, alfa.pcr, alfa.ridge
```

```
library(MASS)
x <- as.matrix(fgl[, 2:9])
x <- x / rowSums(x)
y <- fgl[, 1]
mod <- alfa.knn.reg(x, y, x, a = 0.5, k = 2:4)</pre>
```

The alpha-kernel regression with compositional response data ${\it The} \; \alpha \hbox{-}{\it kernel} \; {\it regression} \; {\it with} \; {\it compositional} \; {\it response} \; {\it data}$

Description

The α -kernel regression with compositional response data.

Usage

```
akern.reg( xnew, y, x, a = seq(0.1, 1, by = 0.1),
h = seq(0.1, 1, length = 10), type = "gauss")
```

Arguments

xnew	A matrix with the new predictor variables whose compositions are to be predicted.
У	A matrix with the compositional response data. Zeros are allowed.
Х	A matrix with the available predictor variables.
a	The value(s) of α . Either a single value or a vector of values. As zero values in the compositional data are allowed, you must be careful to choose strictly positive values of α . However, if negative values are passed, the positive ones are used only.
h	The bandwidth value(s) to consider.
type	The type of kernel to use, "gauss" or "laplace".

Details

The α -kernel regression for compositional response variables is applied.

Value

A list with the estimated compositional response data for each value of α and h.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Tsagris M., Alenazi A. and Stewart C. (2023). Flexible non-parametric regression models for compositional response data with zeros. Statistics and Computing, 33(106).

https://link.springer.com/article/10.1007/s11222-023-10277-5

See Also

```
akernreg.tune, aknn.reg, aknnreg.tune, alfa.reg, comp.ppr, comp.reg, kl.compreg
```

Examples

```
y <- as.matrix( iris[, 1:3] )
y <- y / rowSums(y)
x <- iris[, 4]
mod <- akern.reg( x, y, x, a = c(0.4, 0.5), h = c(0.1, 0.2) )</pre>
```

The alpha-SCLS model $\,$ The lpha-SCLS model for compositional responses and predictors

Description

The α -SCLS model for compositional responses and predictors.

Usage

```
ascls(y, x, a = seq(0.1, 1, by = 0.1), xnew)
```

Arguments

у	A matrix with the compositional data (dependent variable). Zero values are allowed.
x	A matrix with the compositional predictors. Zero values are allowed.
a	A vector or a single number of values of the α -parameter. This has to be different from zero, and it can take negative values if there are no zeros in the simplicial response (y).
xnew	The new data for which predictions will be made.

Details

This is an extension of the SCLS model that includes the α -transformation and is intended solely for prediction purposes.

Value

A list with matrices containing the predicted simplicial response values, one matrix for each value of α .

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Tsagris. M. (2024). Constrained least squares simplicial-simplicial regression. https://arxiv.org/pdf/2403.19835.pdf

See Also

```
scls, cv.ascls, atflr
```

Examples

```
library(MASS)
set.seed(1234)
y <- rdiri(214, runif(4, 1, 3))
x <- as.matrix(fgl[, 2:9])
x <- x / rowSums(x)
mod <- ascls(y, x, xnew = x)
mod</pre>
```

The alpha-TFLR model $The \alpha$ -TFLR model for compositional responses and predictors

Description

The α -TFLR model for compositional responses and predictors.

Usage

```
atflr(y, x, a = seq(0.1, 1, by = 0.1), xnew)
```

Arguments

У	A matrix with the compositional data (dependent variable). Zero values are allowed.
x	A matrix with the compositional predictors. Zero values are allowed.
a	A vector or a single number of values of the α -parameter. This has to be different from zero, and it can take negative values if there are no zeros in the simplicial response (y).
xnew	The new data for which predictions will be made.

Details

This is an extension of the TFLR model that includes the α -transformation and is intended solely for prediction purposes.

Value

A list with matrices containing the predicted simplicial response values, one matrix for each value of α .

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Fiksel J., Zeger S. and Datta A. (2022). A transformation-free linear regression for compositional outcomes and predictors. Biometrics, 78(3): 974–987.

Tsagris. M. (2024). Constrained least squares simplicial-simplicial regression. https://arxiv.org/pdf/2403.19835.pdf

See Also

```
tflr, cv.atflr, ascls
```

Examples

```
library(MASS)
set.seed(1234)
y <- rdiri(214, runif(4, 1, 3))
x <- as.matrix(fgl[, 2:9])
x <- x / rowSums(x)
mod <- ascls(y, x, a = c(0.5, 1), xnew = x)
mod</pre>
```

The alpha-transformation

The α -transformation

Description

The α -transformation.

Usage

```
alfa(x, a, h = TRUE)
alef(x, a)
```

Arguments

а

x A matrix with the compositional data.

The value of the power transformation, it has to be between -1 and 1. If zero values are present it has to be greater than 0. If $\alpha = 0$ the isometric log-ratio transformation is applied.

h

A boolean variable. If is TRUE (default value) the multiplication with the Helmert sub-matrix will take place. When $\alpha=0$ and h = FALSE, the result is the centred log-ratio transformation (Aitchison, 1986). In general, when h = FALSE the resulting transformation maps the data onto a singualr space. The sum of the vectors is equal to 0. Hence, from the simplex constraint the data go to another constraint.

Details

The α -transformation is applied to the compositional data. The command "alef" is the same as "alfa(x, a, h = FALSE)", but reurns a different element as well and is necessary for the functions a.est, a.mle and alpha.mle.

Value

A list including:

sa	The logarithm of the Jacobian determinant of the α -transformation. This is used in the "profile" function to speed up the computations.
sk	If the "alef" was called, this will return the sum of the α -power transformed data, prior to being normalised to sum to 1. If $\alpha=0$, this will not be returned.
aff	The α -transformed data.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Giorgos Athineou <gioathineou@gmail.com>.

References

Tsagris M. and Stewart C. (2022). A Review of Flexible Transformations for Modeling Compositional Data. In Advances and Innovations in Statistics and Data Science, pp. 225–234. https://link.springer.com/chapter/10.103-031-08329-7_10

Tsagris Michail and Stewart Connie (2020). A folded model for compositional data analysis. Australian and New Zealand Journal of Statistics, 62(2): 249-277. https://arxiv.org/pdf/1802.07330.pdf

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. https://arxiv.org/pdf/1106.1451.pdf

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
alfainv, pivot, alfa.profile, alfa.tune a.est, alpha.mle, alr, bc, fp, green
```

Examples

```
library(MASS)
x <- as.matrix(fg1[, 2:9])
x <- x / rowSums(x)
y1 <- alfa(x, 0.2)$aff
y2 <- alfa(x, 1)$aff
rbind( colMeans(y1), colMeans(y2) )
y3 <- alfa(x, 0.2)$aff
dim(y1) ; dim(y3)
rowSums(y1)
rowSums(y3)</pre>
```

The Box-Cox transformation applied to ratios of components

The Box-Cox transformation applied to ratios of components

Description

The Box-Cox transformation applied to ratios of components.

Usage

```
bc(x, lambda)
```

Arguments

x A matrix with the compositional data. The first component must be zero values

free.

1 ambda The value of the power transformation, it has to be between -1 and 1. If zero

values are present it has to be greater than 0. If $\lambda=0$ the additive log-ratio

transformation (alr) is applied.

Details

The Box-Cox transformation applied to ratios of components, as described in Aitchison (1986) is applied.

Value

A matrix with the transformed data.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

The ESOV-distance 205

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
alr, fp, green, alfa
```

Examples

```
library(MASS)
x <- as.matrix(fg1[, 2:9])
x <- x / rowSums(x)
y1 <- bc(x, 0.2)
y2 <- bc(x, 0)
rbind( colMeans(y1), colMeans(y2) )
rowSums(y1)
rowSums(y2)</pre>
```

The ESOV-distance

The ESOV-distance

Description

The ESOV-distance.

Usage

```
esov(x)
esova(xnew, x)
es(x1, x2)
```

Arguments

x A matrix with compositional data.

xnew A matrix or a vector with new compositional data.x1 A vector with compositional data.

x2 A vector with compositional data.

Details

The ESOV distance is calculated.

Value

For "esov()" a matrix including the pairwise distances of all observations or the distances between xnew and x.

For "esova()" a matrix including the pairwise distances of all observations or the distances between xnew and x.

For "es()" a number, the ESOV distance between x1 and x2.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Tsagris, Michail (2014). The k-NN algorithm for compositional data: a revised approach with and without zero values present. Journal of Data Science, 12(3): 519-534.

Endres, D. M. and Schindelin, J. E. (2003). A new metric for probability distributions. Information Theory, IEEE Transactions on 49, 1858-1860.

Osterreicher, F. and Vajda, I. (2003). A new class of metric divergences on probability spaces and its applicability in statistics. Annals of the Institute of Statistical Mathematics 55, 639-653.

See Also

```
alfadist, comp.knn, js.compreg
```

Examples

```
library(MASS)
x <- as.matrix(fgl[1:20, 2:9])
x <- x / rowSums(x)
esov(x)</pre>
```

The folded power transformation

The folded power transformation

Description

The folded power transformation.

Usage

```
fp(x, lambda)
```

Arguments

Х

A matrix with the compositional data. Zero values are allowed.

lambda

The value of the power transformation, it has to be between -1 and 1. If zero values are present it has to be greater than 0. If $\lambda=0$ the additive log-ratio transformation (alr) is applied. If zero values are present λ must be strictly positive.

Details

The folded power transformation is applied to the compositional data.

Value

A matrix with the transformed data.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Atkinson, A. C. (1985). Plots, transformations and regression; an introduction to graphical methods of diagnostic regression analysis Oxford University Press.

See Also

```
alr, bc, green, alfa
```

Examples

```
library(MASS)
x <- as.matrix(fg1[, 2:9])
x <- x / rowSums(x)
y1 <- fp(x, 0.2)
y2 <- fp(x, 0)
rbind( colMeans(y1), colMeans(y2) )
rowSums(y1)
rowSums(y2)</pre>
```

The Frechet mean for compositional data

The Frechet mean for compositional data

Description

Mean vector or matrix with mean vectors of compositional data using the α -transformation.

Usage

```
frechet(x, a)
```

Arguments

а

x A matrix with the compositional data.

The value of the power transformation, it has to be between -1 and 1. If zero values are present it has to be greater than 0. If $\alpha=0$ the isometric log-ratio transformation is applied and the closed geometric mean is calculated. You can also provide a sequence of values of alpha and in this case a matrix of Frechet means will be returned.

208 The Helmert sub-matrix

Details

The power transformation is applied to the compositional data and the mean vector is calculated. Then the inverse of it is calculated and the inverse of the power transformation applied to the last vector is the Frechet mean.

Value

If α is a single value, the function will return a vector with the Frechet mean for the given value of α . Otherwise the function will return a matrix with the Frechet means for each value of α .

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Giorgos Athineou <gioathineou@gmail.com>.

References

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. https://arxiv.org/pdf/1106.1451.pdf

See Also

```
alfa, alfainv, profile
```

Examples

```
library(MASS)
x <- as.matrix(fgl[, 2:9])
x <- x / rowSums(x)
frechet(x, 0.2)
frechet(x, 1)</pre>
```

The Helmert sub-matrix

The Helmert sub-matrix

Description

The Helmert sub-matrix.

Usage

helm(n)

Arguments

n

A number grater than or equal to 2.

Details

The Helmert sub-matrix is returned. It is an orthogonal matrix without the first row.

Value

```
A (n-1) \times n matrix.
```

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Giorgos Athineou <gioathineou@gmail.com>.

References

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. https://arxiv.org/pdf/1106.1451.pdf

John Aitchison (2003). The Statistical Analysis of Compositional Data, p. 99. Blackburn Press.

Lancaster H. O. (1965). The Helmert matrices. The American Mathematical Monthly 72(1): 4-12.

See Also

```
alfa, alfainv
```

Examples

helm(3)

helm(5)

The k-nearest neighbours using the alpha-distance ${\it The~k-nearest~neighbours~using~the~\alpha-distance}$

Description

The k-nearest neighbours using the α -distance.

Usage

```
alfann(xnew, x, a, k = 10, rann = FALSE)
```

Arguments

xnew	A matrix or a vector with new compositional data.
X	A matrix with the compositional data.
a	The value of the power transformation, it has to be between -1 and 1. If zero values are present it has to be greater than 0. If $\alpha=0$, the isometric log-ratio transformation is applied.
k	The number of nearest neighbours to search for.
rann	If you have large scale datasets and want a faster k-NN search, you can use kd-trees implemented in the R package "Rnanoflann". In this case you must set this argument equal to TRUE. Note however, that in this case, the only available distance is by default "euclidean".

Details

The α -transformation is applied to the compositional data first and the indices of the k-nearest neighbours using the Euclidean distance are returned.

Value

A matrix including the indices of the nearest neighbours of each xnew from x.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

MTsagris M., Alenazi A. and Stewart C. (2023). Flexible non-parametric regression models for compositional response data with zeros. Statistics and Computing, 33(106).

https://link.springer.com/article/10.1007/s11222-023-10277-5

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain.

https://arxiv.org/pdf/1106.1451.pdf

See Also

```
alfa.knn, comp.nb, alfa.rda, alfa.nb, link{aknn.reg}, alfa, alfainv
```

```
library(MASS)
xnew <- as.matrix(fgl[1:20, 2:9])
xnew <- xnew / rowSums(xnew)
x <- as.matrix(fgl[-c(1:20), 2:9])
x <- x / rowSums(x)
b <- alfann(xnew, x, a = 0.1, k = 10)</pre>
```

```
The k-NN algorithm for compositional data {\it The~k-NN~algorithm~for~compositional~data}
```

Description

The k-NN algorithm for compositional data with and without using the power transformation.

Usage

```
comp.knn(xnew, x, ina, a = 1, k = 5, apostasi = "ESOV", mesos = TRUE)
alfa.knn(xnew, x, ina, a = 1, k = 5, mesos = TRUE,
apostasi = "euclidean", rann = FALSE)
ait.knn(xnew, x, ina, a = 1, k = 5, mesos = TRUE,
apostasi = "euclidean", rann = FALSE)
```

Arguments

xnew	A matrix with the new compositional data whose group is to be predicted. Zeros are allowed, but you must be careful to choose strictly positive values of α or not to set apostasi= "Ait".
х	A matrix with the available compositional data. Zeros are allowed, but you must be careful to choose strictly positive values of α or not to set apostasi= "Ait".
ina	A group indicator variable for the available data.
a	The value of α . As zero values in the compositional data are allowed, you must be careful to choose strictly positive vcalues of α . You have the option to put a = NULL. In this case, the xnew and x are assumed to be the already α -transformed data.
k	The number of nearest neighbours to consider. It can be a single number or a vector.
apostasi	The type of distance to use. For the compk.knn this can be one of the following: "ESOV", "taxicab", "Ait", "Hellinger", "angular" or "CS". See the references for them. For the alfa.knn this can be either "euclidean" or "manhattan".
mesos	This is used in the non standard algorithm. If TRUE, the arithmetic mean of the distances is calulated, otherwise the harmonic mean is used (see details).
rann	If you have large scale datasets and want a faster k-NN search, you can use kd-trees implemented in the R package "Rnanoflann". In this case you must set this argument equal to TRUE. Note however, that in this case, the only available distance is by default "euclidean".

Details

The k-NN algorithm is applied for the compositional data. There are many metrics and possibilities to choose from. The algorithm finds the k nearest observations to a new observation and allocates it to the class which appears most times in the neighbours. It then computes the arithmetic or the harmonic mean of the distances. The new point is allocated to the class with the minimum distance.

Value

A vector with the estimated groups.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Giorgos Athineou <gioathineou@gmail.com>.

References

Tsagris, Michail (2014). The k-NN algorithm for compositional data: a revised approach with and without zero values present. Journal of Data Science, 12(3): 519–534.

Friedman Jerome, Trevor Hastie and Robert Tibshirani (2009). The elements of statistical learning, 2nd edition. Springer, Berlin

Tsagris Michail, Simon Preston and Andrew T.A. Wood (2016). Improved classification for compositional data using the α -transformation. Journal of Classification 33(2): 243–261.

Connie Stewart (2017). An approach to measure distance between compositional diet estimates containing essential zeros. Journal of Applied Statistics 44(7): 1137–1152.

Clarotto L., Allard D. and Menafoglio A. (2022). A new class of α -transformations for the spatial analysis of Compositional Data. Spatial Statistics, 47.

Endres, D. M. and Schindelin, J. E. (2003). A new metric for probability distributions. Information Theory, IEEE Transactions on 49, 1858–1860.

Osterreicher, F. and Vajda, I. (2003). A new class of metric divergences on probability spaces and its applicability in statistics. Annals of the Institute of Statistical Mathematics 55, 639–653.

See Also

```
compknn.tune, alfa.rda, comp.nb, alfa.nb, alfa,esov, mix.compnorm
```

```
x <- as.matrix( iris[, 1:4] )
x <- x/ rowSums(x)
ina <- iris[, 5]
mod <- comp.knn(x, x, ina, a = 1, k = 5)
table(ina, mod)
mod2 <- alfa.knn(x, x, ina, a = 1, k = 5)
table(ina, mod2)</pre>
```

The multiplicative log-ratio transformation and its inverse

The multiplicative log-ratio transformation and its inverse

Description

The multiplicative log-ratio transformation and its inverse.

Usage

```
mlr(x)
mlrinv(y)
```

Arguments

- x A numerical matrix with the compositional data.
- y A numerical matrix with data to be closed into the simplex.

Details

The multiplicative log-ratio transformation and its inverse are applied here. This means that no zeros are allowed.

Value

A matrix with the mlr transformed data (if mlr is used) or with the compositional data (if the mlrinv is used).

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
alr, pivot, green, alfa
```

```
library(MASS)
x <- as.matrix(fgl[, 2:9])
x <- x / rowSums(x)
y <- mlr(x)
x1 <- mlrinv(y)</pre>
```

The pivot coordinate transformation and its inverse

The pivot coordinate transformation and its inverse

Description

The pivot coordinate transformation and its inverse.

Usage

```
pivot(x)
pivotinv(y)
```

Arguments

- x A numerical matrix with the compositional data.
- y A numerical matrix with data to be closed into the simplex.

Details

The pivot coordinate transformation and its inverse are computed. This means that no zeros are allowed.

Value

A matrix with the alr transformed data (if pivot is used) or with the compositional data (if the pivotinv is used).

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Peter Filzmoser, Karel Hron and Matthias Templ (2018). Applied Compositional Data Analysis With Worked Examples in R (pages 49 and 51). Springer.

See Also

```
alfa, alfainv, alr, green
```

```
library(MASS)
x <- as.matrix(fgl[, 2:9])
x <- x / rowSums(x)
y <- pivot(x)
x1 <- alrinv(y)</pre>
```

The SCLS model 215

The SCLS model	Simplicial constrained linear least squares (SCLS) for compositional responses and predictors

Description

Simplicial constrained linear least squares (SCLS) for compositional responses and predictors.

Usage

```
scls(y, x, xnew = NULL, nbcores = 4)
```

Arguments

_	•		
	У	A matrix with the compositional data (dependent variable). Zero values are allowed. It may also by a big matrix of the FBM class.	
	х	A matrix with the compositional predictors. Zero values are allowed. It may also by a big matrix of the FBM class.	
	xnew	If you have new data use it, otherwise leave it NULL.	
	nbcores	The number of cores to use in the case of an FBM class (big) matrix. If you do not know how many to cores to use, you may try the command nb_cores () from the bigparallelr package.	

Details

The function performs least squares regression where the beta coefficients are constained to be positive and sum to 1. We were inspired by the transformation-free linear regression for compositional responses and predictors of Fiksel, Zeger and Datta (2022). Our implementation now uses quadratic programming instead of the function optim, and the solution is more accurate and extremely fast.

Big matrices, of FBM class, are now accepted.

Value

A list including:

mse The mean squared error.
be The beta coefficients.

est The fitted of xnew if xnew is not NULL.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Tsagris. M. (2024). Constrained least squares simplicial-simplicial regression. https://arxiv.org/pdf/2403.19835.pdf Fiksel J., Zeger S. and Datta A. (2022). A transformation-free linear regression for compositional outcomes and predictors. Biometrics, 78(3): 974–987.

See Also

```
cv.scls, tflr, scls.indeptest, scrq
```

Examples

```
library(MASS)
set.seed(1234)
y <- rdiri(214, runif(4, 1, 3))
x <- as.matrix(fgl[, 2:9])
x <- x / rowSums(x)
mod <- scls(y, x)
mod</pre>
```

The SCLS model with multiple compositional predictors $The \ SCLS \ model \ with \ multiple \ compositional \ predictors$

Description

The SCLS model with multiple compositional predictors.

Usage

```
scls2(y, x, wei = FALSE, xnew = NULL)
```

Arguments

У	A matrix with the compositional data (dependent variable). Zero values are allowed.
X	A list of matrices with the compositional predictors. Zero values are allowed.
wei	Do you want weights among the different simplicial predictors? The default is FALSE.
xnew	If you have new data use it, otherwise leave it NULL.

Details

The function performs least squares regression where the beta coefficients are constained to be positive and sum to 1. We were inspired by the transformation-free linear regression for compositional responses and predictors of Fiksel, Zeger and Datta (2020). Our implementation now uses quadratic programming instead of the function optim, and the solution is more accurate and extremely fast. This function allows for more than one simplicial predictors and offers the possibility of assigning weights to each simplicial predictor.

Value

A list including:

ini.mse	The mean squared error when all simplicial predictors carry equal weight.
ini.be	The beta coefficients when all simplicial predictors carry equal weight.
mse	The mean squared error when the simplicial predictors carry unequal weights.
weights	The weights in a vector form. A vector of length equal to the number of rows of the matrix of coefficients.
am	The vector of weights, one for each simplicia predictor. The length of the vector is equal to the number of simplicial predictors.
est	The fitted of xnew if xnew is not NULL.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Tsagris. M. (2024). Constrained least squares simplicial-simplicial regression. https://arxiv.org/pdf/2403.19835.pdf

See Also

```
cv.scls, tflr, scls.indeptest
```

Examples

```
library(MASS)
set.seed(1234)
y <- rdiri(214, runif(4, 1, 3))
x1 <- as.matrix(fgl[, 2:9])
x <- list()
x[[ 1 ]] <- x1 / rowSums(x1)
x[[ 2 ]] <- Compositional::rdiri(214, runif(4))
mod <- scls2(y, x)
mod</pre>
```

The TFLR model with multiple compositional predictors $The \ TFLR \ model \ with \ multiple \ compositional \ predictors$

Description

The TFLR model with multiple compositional predictors

Usage

```
tflr2(y, x, wei = FALSE, xnew = NULL)
```

Arguments

У	A matrix with the compositional data (dependent variable). Zero values are allowed.
x	A list of matrices with the compositional predictors. Zero values are allowed.
wei	Do you want weights among the different simplicial predictors? The default is FALSE.
xnew	If you have new data use it, otherwise leave it NULL.

Details

The transformation-free linear regression for compositional responses and predictors is implemented. The function to be minized is $-\sum_{i=1}^n y_i \log y_i/(X_iB)$. This is a self implementation of the function that can be found in the package codalm. This function allows for more than one simplicial predictors and offers the possibility of assigning weights to each simplicial predictor.

Value

A list including:

ini.mse	The mean squared error when all simplicial predictors carry equal weight.
ini.be	The beta coefficients when all simplicial predictors carry equal weight.
mse	The mean squared error when the simplicial predictors carry unequal weights.
weights	The weights in a vector form. A vector of length equal to the number of rows of the matrix of coefficients.
am	The vector of weights, one for each simplicia predictor. The length of the vector is equal to the number of simplicial predictors.
est	The fitted of xnew if xnew is not NULL.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Fiksel J., Zeger S. and Datta A. (2022). A transformation-free linear regression for compositional outcomes and predictors. Biometrics, 78(3): 974–987.

Tsagris. M. (2024). Constrained least squares simplicial-simplicial regression. https://arxiv.org/pdf/2403.19835.pdf

See Also

```
cv.scls, tflr, scls.indeptest
```

Examples

```
library(MASS)
set.seed(1234)
y <- rdiri(214, runif(4, 1, 3))
x1 <- as.matrix(fgl[, 2:9])
x <- list()
x[[ 1 ]] <- x1 / rowSums(x1)
x[[ 2 ]] <- Compositional::rdiri(214, runif(4))
mod <- tflr2(y, x)
mod</pre>
```

The transformation-free linear regression (TFLR) for compositional responses and predictors

Transformation-free linear regression (TFLR) for compositional responses and predictors

Description

Transformation-free linear regression (TFLR) for compositional responses and predictors.

Usage

```
tflr(y, x, xnew = NULL)
```

Arguments

y A matrix with the compositional response. Zero values are allowed.

x A matrix with the compositional predictors. Zero values are in general allowed,

but there can be cases when these are problematic.

xnew If you have new data use it, otherwise leave it NULL.

Details

The transformation-free linear regression for compositional responses and predictors is implemented. The function to be minized is $-\sum_{i=1}^{n} y_i \log y_i/(X_iB)$. This is an efficient self implementation.

Value

A list including:

kl The Kullback-Leibler divergence between the observed and the fitted response

compositional data.

be The beta coefficients.

est The fitted values of xnew if xnew is not NULL.

220 Total variability

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Fiksel J., Zeger S. and Datta A. (2022). A transformation-free linear regression for compositional outcomes and predictors. Biometrics, 78(3): 974–987.

Tsagris. M. (2024). Constrained least squares simplicial-simplicial regression. https://arxiv.org/pdf/2403.19835.pdf

See Also

```
cv.tflr, sclskl.alfapcr
```

Examples

```
library(MASS)
y <- rdiri(214, runif(3, 1, 3))
x <- as.matrix(fgl[, 2:9])
x <- x / rowSums(x)
mod <- tflr(y, x, x)
mod</pre>
```

Total variability

Total variability

Description

Total variability.

Usage

```
totvar(x, a = 0)
```

Arguments

x A numerical matrix with the compositional data.

The value of the power transformation, it has to be between -1 and 1. If zero values are present it has to be greater than 0. If $\alpha=0$ the centred log-ratio transformation is used.

Details

The α -transformation is applied and the sum of the variances of the transformed variables is calculated. This is the total variability. Aitchison (1986) used the centred log-ratio transformation, but we have extended it to cover more geometries, via the α -transformation.

Value

The total variability of the data in a given geometry as dictated by the value of α .

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
alfa, \ link{alfainv,} alfa.profile, alfa.tune
```

Examples

```
x <- as.matrix(iris[, 1:4])
x <- x / rowSums(x)
totvar(x)</pre>
```

```
Tuning of the alpha-generalised correlations between two compositional datasets
```

Tuning of the α -generalised correlations between two compositional datasets

Description

Tuning of the *alpha*-generalised correlations between two compositional datasets.

Usage

```
acor.tune(y, x, a, type = "dcor")
```

Arguments

У	A matrix with the compositional data.
Х	A matrix with the compositional data.
а	The range of values of the power transformation to search for the optimal one. If zero values are present it has to be greater than 0.
type	the type of correlation to compute, the distance correlation ("edist"), the canonical correlation type 1 ("cancor1") or the canonical correlation type 2 ("cancor2"). See details for more information.

Details

The α -transformation is applied to each composition and then, if type="dcor" the distance correlation or the canonical correlation is computed. If type = "cancor1" the function returns the value of α that maximizes the product of the eigenvalues. If type = "cancor2" the function returns the value of α that maximizes the the largest eigenvalue.

Value

A list including:

alfa The optimal value of α .

acor The maximum value of the acor. runtime The runtime of the optimization

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. https://arxiv.org/pdf/1106.1451.pdf

See Also

```
acor, alfa.profile, alfa, alfainv
```

Examples

```
y <- rdiri(30, runif(3) )
x <- rdiri(30, runif(4) )
acor(y, x, a = 0.4)</pre>
```

Tuning of the bandwidth h of the kernel using the maximum likelihood cross validation

Tuning of the bandwidth h of the kernel using the maximum likelihood cross validation

Description

Tuning of the bandwidth h of the kernel using the maximum likelihood cross validation.

Usage

```
mkde.tune( x, low = 0.1, up = 3, s = cov(x) )
```

Arguments

X	A matrix with Euclidean (continuous) data.
low	The minimum value to search for the optimal bandwidth value.
up	The maximum value to search for the optimal bandwidth value.
S	A covariance matrix. By default it is equal to the covariance matrix of the data, but can change to a robust covariance matrix, MCD for example.

Details

Maximum likelihood cross validation is applied in order to choose the optimal value of the bandwidth parameter. No plot is produced.

Value

A list including:

hopt The optimal bandwidth value.

maximum The value of the pseudo-log-likelihood at that given bandwidth value.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Giorgos Athineou <gioathineou@gmail.com>.

References

Arsalane Chouaib Guidoum (2015). Kernel Estimator and Bandwidth Selection for Density and its Derivatives. The kedd R package. http://cran.r-project.org/web/packages/kedd/vignettes/kedd.pdf

M.P. Wand and M.C. Jones (1995). Kernel smoothing, pages 91-92.

See Also

```
mkde, comp.kerncontour
```

Examples

```
library(MASS)
mkde.tune(as.matrix(iris[, 1:4]), c(0.1, 3) )
```

Tuning of the divergence based regression for compositional data with compositional data in the covariates side using the alpha-transformation

Tuning of the divergence based regression for compositional data with compositional data in the covariates side using the α -transformation

Description

Tuning of the divergence based regression for compositional data with compositional data in the covariates side using the α -transformation.

Usage

```
klalfapcr.tune(y, x, covar = NULL, nfolds = 10, maxk = 50, a = seq(-1, 1, by = 0.1), folds = NULL, graph = FALSE, tol = 1e-07, maxiters = 50, seed = NULL)
```

Arguments

у	A numerical matrix with compositional data with or without zeros.
X	A matrix with the predictor variables, the compositional data. Zero values are allowed.
covar	If you have other continuous covariates put themn here.
nfolds	The number of folds for the K-fold cross validation, set to 10 by default.
maxk	The maximum number of principal components to check.
a	The value of the power transformation, it has to be between -1 and 1. If zero values are present it has to be greater than 0. If $\alpha=0$ the isometric log-ratio transformation is applied.
folds	If you have the list with the folds supply it here. You can also leave it NULL and it will create folds.
graph	If graph is TRUE (default value) a plot will appear.
tol	The tolerance value to terminate the Newton-Raphson procedure.
maxiters	The maximum number of Newton-Raphson iterations.
seed	You can specify your own seed number here or leave it NULL.

Details

The M-fold cross validation is performed in order to select the optimal values for α and k, the number of principal components. The α -transformation is applied to the compositional data first, the first k principal component scores are calcualted and used as predictor variables for the Kullback-Leibler divergence based regression model. This procedure is performed M times during the M-fold cross validation.

Value

A list including:

mspe A list with the KL divergence for each value of α and k in every fold.

performance A matrix with the KL divergence for each value of α averaged over all folds. If

graph is set to TRUE this matrix is plotted.

best.perf The minimum KL divergence.

params The values of α and k corresponding to the minimum KL divergence.

Author(s)

Initial code by Abdulaziz Alenazi. Modifications by Michail Tsagris.

R implementation and documentation: Abdulaziz Alenazi <a.alenazi@nbu.edu.sa> and Michail Tsagris <mtsagris@uoc.gr>.

References

Alenazi A. (2019). Regression for compositional data with compositional data as predictor variables with or without zero values. Journal of Data Science, 17(1): 219–238. https://jds-online.org/journal/JDS/article/136/file/pdf

Tsagris M. (2015). Regression analysis with compositional data containing zero values. Chilean Journal of Statistics, 6(2): 47–57. http://arxiv.org/pdf/1508.01913v1.pdf

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. http://arxiv.org/pdf/1106.1451.pdf

See Also

```
kl.alfapcr, cv.tflr, glm.pcr, alfapcr.tune
```

Examples

```
library(MASS)
y <- rdiri( 214, runif(4, 1, 3) )
x <- as.matrix( fgl[, 2:9] )
x <- x / rowSums(x)
mod <- klalfapcr.tune(y = y, x = x, a = c(0.7, 0.8) )
mod</pre>
```

Tuning of the k-NN algorithm for compositional data

Tuning of the k-NN algorithm for compositional data

Description

Tuning of the k-NN algorithm for compositional data with and without using the power or the α -transformation. In addition, estimation of the rate of correct classification via K-fold cross-validation.

Usage

```
compknn.tune(x, ina, nfolds = 10, k = 2:5, mesos = TRUE,
a = seq(-1, 1, by = 0.1), apostasi = "ESOV", folds = NULL,
stratified = TRUE, seed = NULL, graph = FALSE)

alfaknn.tune(x, ina, nfolds = 10, k = 2:5, mesos = TRUE,
a = seq(-1, 1, by = 0.1), apostasi = "euclidean", rann = FALSE,
folds = NULL, stratified = TRUE, seed = NULL, graph = FALSE)

aitknn.tune(x, ina, nfolds = 10, k = 2:5, mesos = TRUE,
a = seq(-1, 1, by = 0.1), apostasi = "euclidean", rann = FALSE,
folds = NULL, stratified = TRUE, seed = NULL, graph = FALSE)
```

Arguments

X	A matrix with the available compositional data. Zeros are allowed, but you must be careful to choose strictly positive values of α or not to set apostasi= "Ait".
ina	A group indicator variable for the available data.
nfolds	The number of folds to be used. This is taken into consideration only if the folds argument is not supplied.
k	A vector with the nearest neighbours to consider.
mesos	This is used in the non standard algorithm. If TRUE, the arithmetic mean of the distances is calculated, otherwise the harmonic mean is used (see details).
a	A grid of values of α to be used only if the distance chosen allows for it.
apostasi	The type of distance to use. For the compk.knn this can be one of the following: "ESOV", "taxicab", "Ait", "Hellinger", "angular" or "CS". See the references for them. For the alfa.knn this can be either "euclidean" or "manhattan".
rann	If you have large scale datasets and want a faster k-NN search, you can use kd-trees implemented in the R package "Rnanoflann". In this case you must set this argument equal to TRUE. Note however, that in this case, the only available distance is by default "euclidean".
folds	If you have the list with the folds supply it here. You can also leave it NULL and it will create folds.
stratified	Do you want the folds to be created in a stratified way? TRUE or FALSE.
seed	You can specify your own seed number here or leave it NULL.
graph	If set to TRUE a graph with the results will appear.

Details

The k-NN algorithm is applied for the compositional data. There are many metrics and possibilities to choose from. The algorithm finds the k nearest observations to a new observation and allocates it to the class which appears most times in the neighbours.

Value

A list including:

per A matrix or a vector (depending on the distance chosen) with the averaged over

all folds rates of correct classification for all hyper-parameters (α and k).

performance The estimated rate of correct classification.

best_a The best value of α . This is returned for "ESOV" and "taxicab" only.

best_k The best number of nearest neighbours.

runtime The run time of the cross-validation procedure.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Giorgos Athineou <gioathineou@gmail.com>.

References

Tsagris, Michail (2014). The k-NN algorithm for compositional data: a revised approach with and without zero values present. Journal of Data Science, 12(3): 519–534. https://arxiv.org/pdf/1506.05216.pdf

Friedman Jerome, Trevor Hastie and Robert Tibshirani (2009). The elements of statistical learning, 2nd edition. Springer, Berlin

Tsagris M., Preston S. and Wood A.T.A. (2016). Improved classification for compositional data using the α -transformation. Journal of Classification, 33(2): 243–261. http://arxiv.org/pdf/1106.1451.pdf

Connie Stewart (2017). An approach to measure distance between compositional diet estimates containing essential zeros. Journal of Applied Statistics 44(7): 1137–1152.

Clarotto L., Allard D. and Menafoglio A. (2022). A new class of α -transformations for the spatial analysis of Compositional Data. Spatial Statistics, 47.

Endres, D. M. and Schindelin, J. E. (2003). A new metric for probability distributions. Information Theory, IEEE Transactions on 49, 1858–1860.

Osterreicher, F. and Vajda, I. (2003). A new class of metric divergences on probability spaces and its applicability in statistics. Annals of the Institute of Statistical Mathematics 55, 639–653.

See Also

```
comp.knn, alfarda.tune, cv.dda, cv.compnb
```

Examples

```
x <- as.matrix(iris[, 1:4])
x <- x/ rowSums(x)
ina <- iris[, 5]
mod1 <- compknn.tune(x, ina, a = seq(1, 1, by = 0.1) )
mod2 <- alfaknn.tune(x, ina, a = seq(-1, 1, by = 0.1) )</pre>
```

Tuning of the projection pursuit regression for compositional data

Tuning of the projection pursuit regression for compositional data

Description

Tuning of the projection pursuit regression for compositional data.

Usage

```
compppr.tune(y, x, nfolds = 10, folds = NULL, seed = NULL,
nterms = 1:10, type = "alr", yb = NULL )
```

Arguments

у	A matrix with the available compositional data, but zeros are not allowed.
X	A matrix with the continuous predictor variables.
nfolds	The number of folds to use.
folds	If you have the list with the folds supply it here.
seed	You can specify your own seed number here or leave it NULL.
nterms	The number of terms to try in the projection pursuit regression.
type	Either "alr" or "ilr" corresponding to the additive or the isometric log-ratio transformation respectively.
yb	If you have already transformed the data using a log-ratio transformation put it

Details

The function performs tuning of the projection pursuit regression algorithm.

here. Othewrise leave it NULL.

Value

A list including:

kl The average Kullback-Leibler divergence.

perf The average Kullback-Leibler divergence.

runtime The run time of the cross-validation procedure.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Friedman, J. H. and Stuetzle, W. (1981). Projection pursuit regression. Journal of the American Statistical Association, 76, 817-823. doi: 10.2307/2287576.

See Also

```
comp.ppr, aknnreg.tune, akernreg.tune
```

Examples

```
y <- as.matrix(iris[, 1:3])
y <- y/ rowSums(y)
x <- iris[, 4]
mod <- compppr.tune(y, x)</pre>
```

Tuning of the projection pursuit regression with compositional predictor variables

Tuning of the projection pursuit regression with compositional predictor variables

Description

Tuning of the projection pursuit regression with compositional predictor variables.

Usage

```
pprcomp.tune(y, x, nfolds = 10, folds = NULL, seed = NULL,
nterms = 1:10, type = "log", graph = FALSE)
```

Arguments

у	A numerical vector with the continuous variable.
X	A matrix with the available compositional data, but zeros are not allowed.
nfolds	The number of folds to use.
folds	If you have the list with the folds supply it here.
seed	You can specify your own seed number here or leave it NULL.
nterms	The number of terms to try in the projection pursuit regression.
type	Either "alr" or "log" corresponding to the additive log-ratio transformation or the logarithm applied to the compositional predictor variables.
graph	If graph is TRUE (default value) a filled contour plot will appear.

Details

The function performs tuning of the projection pursuit regression algorithm with compositional predictor variables.

230 Tuning of the projection pursuit regression with compositional predictor variables using the alpha-transformation

Value

A list including:

runtime The run time of the cross-validation procedure.

mse The mean squared error of prediction for each number of terms.

opt.nterms The number of terms corresponding to the minimum mean squared error of pre-

diction.

opt.alpha The value of α corresponding to the minimum mean squared error of prediction.

performance The minimum mean squared error of prediction.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Friedman, J. H. and Stuetzle, W. (1981). Projection pursuit regression. Journal of the American Statistical Association, 76, 817-823. doi: 10.2307/2287576.

See Also

```
pprcomp, ice.pprcomp, alfapcr.tune, compppr.tune
```

Examples

```
x <- as.matrix(iris[, 2:4])
x <- x/ rowSums(x)
y <- iris[, 1]
mod <- pprcomp.tune(y, x)</pre>
```

Tuning of the projection pursuit regression with compositional predictor variables using the alpha-transformation

Tuning of the projection pursuit regression with compositional predictor variables using the α -transformation

Description

Tuning of the projection pursuit regression with compositional predictor variables using the α -transformation.

Usage

```
alfapprcomp.tune(y, x, nfolds = 10, folds = NULL, seed = NULL, nterms = 1:10, a = seq(-1, 1, by = 0.1), graph = FALSE)
```

Tuning of the projection pursuit regression with compositional predictor variables using the alpha-transformation 231

Arguments

y A numerical vector with the continuous variable.

x A matrix with the available compositional data. Zeros are allowed.

nfolds The number of folds to use.

folds If you have the list with the folds supply it here.

seed You can specify your own seed number here or leave it NULL.

nterms The number of terms to try in the projection pursuit regression.

a A vector with the values of α for the α -transformation.

graph If graph is TRUE (default value) a filled contour plot will appear.

Details

The function performs tuning of the projection pursuit regression algorithm with compositional predictor variables using the α -transformation.

Value

A list including:

runtime The run time of the cross-validation procedure.

mse The mean squared error of prediction for each number of terms.

opt.nterms The number of terms corresponding to the minimum mean squared error of pre-

diction.

performance The minimum mean squared error of prediction.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Friedman, J. H. and Stuetzle, W. (1981). Projection pursuit regression. Journal of the American Statistical Association, 76, 817-823. doi: 10.2307/2287576.

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. https://arxiv.org/pdf/1106.1451.pdf

See Also

alfa.pprcomp, pprcomp.tune, compppr.tune

Examples

```
x <- as.matrix(iris[, 2:4])
x <- x / rowSums(x)
y <- iris[, 1]
mod <- alfapprcomp.tune( y, x, a = c(0, 0.5, 1) )</pre>
```

Tuning the number of PCs in the PCR with compositional data using the alpha-transformation

Tuning the number of PCs in the PCR with compositional data using the α -transformation

Description

This is a cross-validation procedure to decide on the number of principal components when using regression with compositional data (as predictor variables) using the α -transformation.

Usage

```
alfapcr.tune(y, x, model = "gaussian", nfolds = 10, maxk = 50, a = seq(-1, 1, by = 0.1), folds = NULL, ncores = 1, graph = TRUE, col.nu = 15, seed = NULL)
```

Arguments

у	A vector with either continuous, binary or count data.
X	A matrix with the predictor variables, the compositional data. Zero values are allowed.
model	The type of regression model to fit. The possible values are "gaussian", "binomial" and "poisson".
nfolds	The number of folds for the K-fold cross validation, set to 10 by default.
maxk	The maximum number of principal components to check.
a	A vector with a grid of values of the power transformation, it has to be between -1 and 1. If zero values are present it has to be greater than 0. If $\alpha=0$ the isometric log-ratio transformation is applied.
folds	If you have the list with the folds supply it here. You can also leave it NULL and it will create folds.
ncores	How many cores to use. If you have heavy computations or do not want to wait for long time more than 1 core (if available) is suggested. It is advisable to use it if you have many observations and or many variables, otherwise it will slow down th process.
graph	If graph is TRUE (default value) a filled contour plot will appear.
col.nu	A number parameter for the filled contour plot, taken into account only if graph is TRUE.
seed	You can specify your own seed number here or leave it NULL.

Details

The α -transformation is applied to the compositional data first and the function "pcr.tune" or "glm-pcr.tune" is called.

Value

If graph is TRUE a filled contour will appear. A list including:

mspe The MSPE where rows correspond to the α values and the columns to the num-

ber of principal components.

best.par The best pair of α and number of principal components.

performance The minimum mean squared error of prediction.

runtime The time required by the cross-validation procedure.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Tsagris M. (2015). Regression analysis with compositional data containing zero values. Chilean Journal of Statistics, 6(2): 47-57. https://arxiv.org/pdf/1508.01913v1.pdf

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. https://arxiv.org/pdf/1106.1451.pdf

Jolliffe I.T. (2002). Principal Component Analysis.

See Also

```
alfa, profile, alfa.pcr, pcr.tune, glmpcr.tune, glm
```

Examples

```
library(MASS)
y <- as.vector(fgl[, 1])
x <- as.matrix(fgl[, 2:9])
x <- x/ rowSums(x)
mod <- alfaper.tune(y, x, nfolds = 10, maxk = 50, a = seq(-1, 1, by = 0.1) )</pre>
```

Tuning the principal components with GLMs

Tuning the principal components with GLMs

Description

Tuning the number of principal components in the generalised linear models.

Usage

```
pcr.tune(y, x, nfolds = 10, maxk = 50, folds = NULL, ncores = 1,
seed = NULL, graph = TRUE)

glmpcr.tune(y, x, nfolds = 10, maxk = 10, folds = NULL, ncores = 1,
seed = NULL, graph = TRUE)

multinompcr.tune(y, x, nfolds = 10, maxk = 10, folds = NULL, ncores = 1,
seed = NULL, graph = TRUE)
```

Arguments

у	A real valued vector for "pcr.tune". A real valued vector for the "glmpcr.tune" with either two numbers, 0 and 1 for example, for the binomial regression or with positive discrete numbers for the poisson. For the "multinompcr.tune" a vector or a factor with more than just two values. This is a multinomial regression.
X	A matrix with the predictor variables, they have to be continuous.
nfolds	The number of folds in the cross validation.
maxk	The maximum number of principal components to check.
folds	If you have the list with the folds supply it here. You can also leave it NULL and it will create folds.
ncores	The number of cores to use. If more than 1, parallel computing will take place. It is advisable to use it if you have many observations and or many variables, otherwise it will slow down th process.
seed	You can specify your own seed number here or leave it NULL.
graph	If graph is TRUE a plot of the performance for each fold along the values of α will appear.

Details

Cross validation is performed to select the optimal number of principal components in the GLMs or the multinomial regression. This is used by alfaper. tune.

Value

If graph is TRUE a plot of the performance versus the number of principal components will appear. A list including:

A matrix with the mean deviance of prediction or mean accuracy for every fold. msp A vector with the mean deviance of prediction or mean accuracy, each value mpd corresponds to a number of principal components. k The number of principal components which minimizes the deviance or maximises the accuracy. The optimal performance, MSE for the linea regression, minimum deviance for performance the GLMs and maximum accuracy for the multinomial regression.

runtime The time required by the cross-validation procedure.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aguilera A.M., Escabias M. and Valderrama M.J. (2006). Using principal components for estimating logistic regression with high-dimensional multicollinear data. Computational Statistics & Data Analysis 50(8): 1905-1924.

Jolliffe I.T. (2002). Principal Component Analysis.

See Also

```
pcr.tune, glm.pcr, alfa.pcr, alfapcr.tune
```

Examples

```
library(MASS)
x <- as.matrix(fgl[, 2:9])</pre>
y <- rpois(214, 10)
glmpcr.tune(y, x, nfolds = 10, maxk = 20, folds = NULL, ncores = 1)
```

Tuning the value of alpha in the alpha-regression Tuning the value of α in the α -regression

Description

Tuning the value of α in the α -regression.

Usage

```
alfareg.tune(y, x, a = seq(0.1, 1, by = 0.1), nfolds = 10, folds = NULL, nc = 1, seed = NULL, graph = FALSE)
```

Arguments

у	A matrix with compositional data. zero values are allowed.
X	A matrix with the continuous predictor variables or a data frame including categorical predictor variables.
a	The value of the power transformation, it has to be between -1 and 1. If zero values are present it has to be greater than 0. If $\alpha=0$ the isometric log-ratio transformation is applied.
nfolds	The number of folds to split the data.
folds	If you have the list with the folds supply it here. You can also leave it NULL and it will create folds.
nc	The number of cores to use. IF you have a multicore computer it is advisable to use more than 1. It makes the procedure faster. It is advisable to use it if you have many observations and or many variables, otherwise it will slow down th process.
seed	You can specify your own seed number here or leave it NULL.
graph	If graph is TRUE a plot of the performance for each fold along the values of α will appear.

Details

The α -transformation is applied to the compositional data and the numerical optimisation is performed for the regression, unless $\alpha = 0$, where the coefficients are available in closed form.

Value

A plot of the estimated Kullback-Leibler divergences (multiplied by 2) along the values of α (if graph is set to TRUE). A list including:

runtime	The runtime required by the cross-validation.
kula	A matrix with twice the Kullback-Leibler divergence of the observed from the fitted values. Each row corresponds to a fold and each column to a value of α . The average over the columns equal the next argument, "kl".
kl	A vector with twice the Kullback-Leibler divergence of the observed from the fitted values. Every value corresponds to a value of α .
opt	The optimal value of α .
value	The minimum value of twice the Kullback-Leibler.

Author(s)

Michail Tsagris

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr> and Giorgos Athineou <gioathineou@gmail.com>.

References

Tsagris M. (2015). Regression analysis with compositional data containing zero values. Chilean Journal of Statistics, 6(2): 47-57. https://arxiv.org/pdf/1508.01913v1.pdf

Tsagris M.T., Preston S. and Wood A.T.A. (2011). A data-based power transformation for compositional data. In Proceedings of the 4th Compositional Data Analysis Workshop, Girona, Spain. https://arxiv.org/pdf/1106.1451.pdf

See Also

```
alfa.reg, alfa
```

Examples

```
library(MASS)
y <- as.matrix(fgl[1:40, 2:4])
y <- y /rowSums(y)
x <- as.vector(fgl[1:40, 1])
mod <- alfareg.tune(y, x, a = seq(0, 1, by = 0.1), nfolds = 5)</pre>
```

Two-sample test of high-dimensional means for compositional data

Two-sample test of high-dimensional means for compositional data

Description

Two-sample test of high-dimensional means for compositional data.

Usage

```
hd.meantest2(y1, y2, R = 1)
```

Arguments

y1	A matrix containing the compositional data of the first group.
y2	A matrix containing the compositional data of the second group.
R	If R is 1 no bootstrap calibration is performed and the asymptotic p-value is
	returned. If R is greater than 1, the bootstrap p-value is returned.

Details

A two sample for high dimensional mean vectors of compositional data is implemented. See references for more details.

Value

A vector with the test statistic value and its associated (bootstrap) p-value.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Cao Y., Lin W. and Li H. (2018). Two-sample tests of high-dimensional means for compositional data. Biometrika, 105(1): 115-132.

See Also

```
comp.test
```

Examples

```
m <- runif(200, 10, 15)
x1 <- rdiri(100, m)
x2 <- rdiri(100, m)
hd.meantest2(x1, x2)</pre>
```

Unconstrained GLMs with compositional predictor variables $Unconstrained \; GLMs \; with \; compositional \; predictor \; variables$

Description

Unconstrained GLMs with compositional predictor variables.

Usage

```
ulc.glm(y, x, z = NULL, model = "logistic", xnew = NULL, znew = NULL)
```

Arguments

У	A numerical vector containing the response variable values. This is either a binary variable or a vector with counts.
X	A matrix with the predictor variables, the compositional data. No zero values are allowed.
z	A matrix, data.frame, factor or a vector with some other covariate(s).
model	For the ulc.glm(), this can be either "logistic" or "poisson".
xnew	A matrix containing the new compositional data whose response is to be predicted. If you have no new data, leave this NULL as is by default.
znew	A matrix, data.frame, factor or a vector with the values of some other covariate(s). If you have no new data, leave this NULL as is by default.

Details

The function performs the unconstrained log-contrast logistic or Poisson regression model. The logarithm of the compositional predictor variables is used (hence no zero values are allowed). The response variable is linked to the log-transformed data **without** the constraint that the sum of the regression coefficients equals 0. If you want the regression without the zum-to-zero contraints see lc.glm. Extra predictors variables are allowed as well, for instance categorical or continuous.

Value

A list including:

devi The residual deviance of the logistic or Poisson regression model.

be The unconstrained regression coefficients. Their sum does not equal 0.

est If the arguments "xnew" and znew were given these are the predicted or esti-

mated values, otherwise it is NULL.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

Lu J., Shi P., and Li H. (2019). Generalized linear models with linear constraints for microbiome compositional data. Biometrics, 75(1): 235–244.

See Also

```
lc.glm, lc.glm2, ulc.glm2, lcglm.aov
```

Examples

```
y <- rbinom(150, 1, 0.5)
x <- rdiri(150, runif(3, 1,3))
mod <- ulc.glm(y, x)</pre>
```

```
Unconstrained linear regression with compositional predictor variables
```

Unconstrained linear regression with compositional predictor variables

Description

Unconstrained linear regression with compositional predictor variables.

Usage

```
ulc.reg(y, x, z = NULL, xnew = NULL, znew = NULL)
```

Arguments

у	A numerical vector containing the response variable values. This must be a continuous variable.
X	A matrix with the predictor variables, the compositional data. No zero values are allowed.
Z	A matrix, data.frame, factor or a vector with some other covariate(s).
xnew	A matrix containing the new compositional data whose response is to be predicted. If you have no new data, leave this NULL as is by default.
znew	A matrix, data.frame, factor or a vector with the values of some other covariate(s). If you have no new data, leave this NULL as is by default.

Details

The function performs the unconstrained log-contrast regression model as opposed to the log-contrast regression described in Aitchison (2003), pg. 84-85. The logarithm of the compositional predictor variables is used (hence no zero values are allowed). The response variable is linked to the log-transformed data **without** the constraint that the sum of the regression coefficients equals 0. If you want the regression model with the zum-to-zero contraints see lc.reg. Extra predictors variables are allowed as well, for instance categorical or continuous.

Value

A list including:

be The unconstrained regression coefficients. Their sum does not equal 0.

covbe If covariance matrix of the constrained regression coefficients.

va The estimated regression variance.

residuals The vector of residuals.

est If the arguments "xnew" and "znew" were given these are the predicted or esti-

mated values, otherwise it is NULL.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

See Also

```
lc.reg, lcreg.aov, lc.reg2, ulc.reg2, alfa.pcr, alfa.knn.reg
```

Examples

```
y <- iris[, 1]
x <- as.matrix(iris[, 2:4])
x <- x / rowSums(x)
mod1 <- ulc.reg(y, x)
mod2 <- ulc.reg(y, x, z = iris[, 5])</pre>
```

```
Unconstrained linear regression with multiple compositional predictors Unconstrained\ linear\ regression\ with\ multiple\ compositional\ predictors
```

Description

Unconstrained linear regression with multiple compositional predictors.

Usage

```
ulc.reg2(y, x, z = NULL, xnew = NULL, znew = NULL)
```

Arguments

У	A numerical vector containing the response variable values. This must be a continuous variable.
X	A list with multiple matrices with the predictor variables, the compositional data. No zero values are allowed.
z	A matrix, data.frame, factor or a vector with some other covariate(s).
xnew	A matrix containing a list with multiple matrices with compositional data whose response is to be predicted. If you have no new data, leave this NULL as is by default.
znew	A matrix, data.frame, factor or a vector with the values of some other covariate(s). If you have no new data, leave this NULL as is by default.

Details

The function performs the unconstrained log-contrast regression model as opposed to the log-contrast regression described in Aitchison (2003), pg. 84-85. The logarithm of the compositional predictor variables is used (hence no zero values are allowed). The response variable is linked to the log-transformed data **without** the constraint that the sum of the regression coefficients equals 0. If you want the regression model with the zum-to-zero contraints see lc.reg2. Extra predictors variables are allowed as well, for instance categorical or continuous. Similarly to lc.reg2 there are multiple compositions treated as predictor variables.

Value

A list including:

be The unconstrained regression coefficients. Their sum for each composition does

not equal 0.

covbe If covariance matrix of the constrained regression coefficients.

va The estimated regression variance.

residuals The vector of residuals.

est If the arguments "xnew" and "znew" were given these are the predicted or esti-

mated values, otherwise it is NULL.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

Xiaokang Liu, Xiaomei Cong, Gen Li, Kendra Maas and Kun Chen (2020). Multivariate Log-Contrast Regression with Sub-Compositional Predictors: Testing the Association Between Preterm Infants' Gut Microbiome and Neurobehavioral Outcome.

See Also

```
lc.reg2, ulc.reg, lc.reg, alfa.pcr, alfa.knn.reg
```

Examples

```
y <- iris[, 1]
x <- list()
x1 <- as.matrix(iris[, 2:4])
x1 <- x1 / rowSums(x1)
x[[ 1 ]] <- x1
x[[ 2 ]] <- rdiri(150, runif(4) )
x[[ 3 ]] <- rdiri(150, runif(5) )
mod <- lc.reg2(y, x)</pre>
```

Unconstrained logistic or Poisson regression with multiple compositional predictors

Unconstrained logistic or Poisson regression with multiple compositional predictors

Description

Unconstrained logistic or Poisson regression with multiple compositional predictors.

Usage

```
ulc.glm2(y, x, z = NULL, model = "logistic", xnew = NULL, znew = NULL)
```

Arguments

У	A numerical vector containing the response variable values. This is either a binary variable or a vector with counts.
X	A list with multiple matrices with the predictor variables, the compositional data. No zero values are allowed.
Z	A matrix, data.frame, factor or a vector with some other covariate(s).
model	This can be either "logistic" or "poisson".
xnew	A matrix containing a list with multiple matrices with compositional data whose response is to be predicted. If you have no new data, leave this NULL as is by default.
znew	A matrix, data.frame, factor or a vector with the values of some other covariate(s). If you have no new data, leave this NULL as is by default.

Details

The function performs the unconstrained log-contrast logistic or Poisson regression model. The logarithm of the compositional predictor variables is used (hence no zero values are allowed). The response variable is linked to the log-transformed data **without** the constraint that the sum of the regression coefficients equals 0. If you want the regression without the zum-to-zero contraints see lc.glm2. Extra predictors variables are allowed as well, for instance categorical or continuous.

Value

A list including:

devi	The residual deviance of the logistic or Poisson regression model.
be	The unconstrained regression coefficients. Their sum does not equal 0.
est	If the arguments "xnew" and znew were given these are the predicted or esti-
	mated values, otherwise it is NULL.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

Lu J., Shi P., and Li H. (2019). Generalized linear models with linear constraints for microbiome compositional data. Biometrics, 75(1): 235–244.

See Also

```
lc.glm2, ulc.glm, lc.glm
```

Examples

```
y <- rbinom(150, 1, 0.5)
x <- list()
x1 <- as.matrix(iris[, 2:4])
x1 <- x1 / rowSums(x1)
x[[ 1 ]] <- x1
x[[ 2 ]] <- rdiri(150, runif(4) )
x[[ 3 ]] <- rdiri(150, runif(5) )
mod <- ulc.glm2(y, x)</pre>
```

Unconstrained quantile regression with compositional predictor variables

Unconstrained quantile regression with compositional predictor variables

Description

Unconstrained quantile regression with compositional predictor variables.

Usage

```
ulc.rq(y, x, z = NULL, tau = 0.5, xnew = NULL, znew = NULL)
```

Arguments

У	A numerical vector containing the response variable values.
x	A matrix with the predictor variables, the compositional data. No zero values are allowed.
z	A matrix, data.frame, factor or a vector with some other covariate(s).
tau	The quantile to be estimated, a number between 0 and 1.
xnew	A matrix containing the new compositional data whose response is to be predicted. If you have no new data, leave this NULL as is by default.
znew	A matrix, data.frame, factor or a vector with the values of some other covariate(s). If you have no new data, leave this NULL as is by default.

Details

The function performs the unconstrained log-contrast quantile regression model. The logarithm of the compositional predictor variables is used (hence no zero values are allowed). The response variable is linked to the log-transformed data **without** the constraint that the sum of the regression coefficients equals 0. If you want the regression without the zum-to-zero contraints see lc.rq. Extra predictors variables are allowed as well, for instance categorical or continuous.

Value

A list including:

mod The object as returned by the function quantreg::rq(). This is useful for hypoth-

esis testing purposes.

be The unconstrained regression coefficients. Their sum does not equal 0.

est If the arguments "xnew" and znew were given these are the predicted or esti-

mated values, otherwise it is NULL.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

Koenker R. W. and Bassett G. W. (1978). Regression Quantiles, Econometrica, 46(1): 33-50.

Koenker R. W. and d'Orey V. (1987). Algorithm AS 229: Computing Regression Quantiles. Applied Statistics, 36(3): 383–393.

See Also

```
lc.glm, lc.glm2, ulc.glm2, lcglm.aov
```

Examples

```
y <- rnorm(150)
x <- rdiri(150, runif(3, 1,3))
mod <- ulc.rq(y, x)</pre>
```

Unconstrained quantile regression with multiple compositional predictors

Unconstrained quantile regression with multiple compositional predictors

Description

Unconstrained quantile regression with multiple compositional predictors.

Usage

```
ulc.rq2(y, x, z = NULL, tau = 0.5, xnew = NULL, znew = NULL)
```

Arguments

У	A numerical vector containing the response variable values.	
x	A list with multiple matrices with the predictor variables, the compositional data. No zero values are allowed.	
z	A matrix, data.frame, factor or a vector with some other covariate(s).	
tau	The quantile to be estimated, a number between 0 and 1.	
xnew	A matrix containing a list with multiple matrices with compositional data whose response is to be predicted. If you have no new data, leave this NULL as is by default.	
znew	A matrix, data.frame, factor or a vector with the values of some other covariate(s). If you have no new data, leave this NULL as is by default.	

Details

The function performs the unconstrained log-contrast quantile regression model. The logarithm of the compositional predictor variables is used (hence no zero values are allowed). The response variable is linked to the log-transformed data **without** the constraint that the sum of the regression coefficients equals 0. If you want the regression without the zum-to-zero contraints see lc.rq2. Extra predictors variables are allowed as well, for instance categorical or continuous.

Value

A list including:

mod	The object as returned by the function quantreg::rq(). This is useful for hypothesis testing purposes.
be	The unconstrained regression coefficients. Their sum does not equal 0.
est	If the arguments "xnew" and znew were given these are the predicted or estimated values, otherwise it is NULL.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Aitchison J. (1986). The statistical analysis of compositional data. Chapman & Hall.

Koenker R. W. and Bassett G. W. (1978). Regression Quantiles, Econometrica, 46(1): 33-50.

Koenker R. W. and d'Orey V. (1987). Algorithm AS 229: Computing Regression Quantiles. Applied Statistics, 36(3): 383–393.

See Also

```
ulc.rq, lc.rq
```

Examples

```
y <- rnorm(150)
x <- list()
x1 <- as.matrix(iris[, 2:4])
x1 <- x1 / rowSums(x1)
x[[ 1 ]] <- x1
x[[ 2 ]] <- rdiri(150, runif(4) )
x[[ 3 ]] <- rdiri(150, runif(5) )
mod <- ulc.rq2(y, x)</pre>
```

Unit-Weibull regression models for proportions

Unit-Weibull regression models for proportions

Description

Unit-Weibull regression models for proportions.

Usage

```
unitweib.reg(y, x, tau = 0.5)
```

Arguments

y A numerical vector proportions. 0s and 1s are allowed.x A matrix or a data frame with the predictor variables.

tau The quantile to be used for estimation. The default value is 0.5 yielding the

median.

Details

See the reference paper.

Value

A list including:

loglik The loglikelihood of the regression model.

info A matrix with all estimated parameters, their standard error, their Wald-statistic

and its associated p-value.

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Mazucheli J., Menezes A. F. B., Fernandes L. B., de Oliveira R. P. and Ghitany M. E. (2020). The unit-Weibull distribution as an alternative to the Kumaraswamy distribution for the modeling of quantiles conditional on covariates. Journal of Applied Statistics, 47(6): 954–974.

See Also

```
propreg, beta.reg
```

Examples

```
y <- exp( - rweibull(100, 1, 1) )
x <- matrix( rnorm(100 * 2), ncol = 2 )
a <- unitweib.reg(y, x)</pre>
```

Zero adjusted Dirichlet regression

Zero adjusted Dirichlet regression

Description

Zero adjusted Dirichlet regression.

Usage

```
zadr(y, x, con = TRUE, B = 1, ncores = 2, xnew = NULL)
zadr2(y, x, con = TRUE, B = 1, ncores = 2, xnew = NULL)
```

Arguments

У	A matrix with the compositional data (dependent variable). The number of observations (vectors) with no zero values should be more than the columns of the predictor variables. Otherwise, the initial values will not be calculated.
x	The predictor variable(s), they can be either continuous or categorical or both.
con	If this is TRUE (default) then the constant term is estimated, otherwise the model includes no constant term.
В	If B is greater than 1 bootstrap estimates of the standard error are returned. If you set this greater than 1, then you must define the number of clusters in order to run in parallel.
ncores	The number of cores to use when $B>1$. This is to be used for the case of bootstrap. If $B=1$, this is not taken into consideration. If this does not work then you might need to load the doParallel yourselves.
xnew	If you have new data use it, otherwise leave it NULL.

Details

A zero adjusted Dirichlet regression is being fittd. The likelihood conists of two components. The contributions of the non zero compositional values and the contributions of the compositional vectors with at least one zero value. The second component may have many different sub-categories, one for each pattern of zeros. The function "zadr2()" links the covariates to the alpha parameters of the Dirichlet distribution, i.e. it uses the classical parametrization of the distribution. This means, that there is a set of regression parameters for each component.

Value

A list including:

runtime The time required by the regression. loglik The value of the log-likelihood.

phi The precision parameter. be The beta coefficients.

seb The standard error of the beta coefficients.

sigma Th covariance matrix of the regression parameters (for the mean vector and the

phi parameter).

est The fitted or the predicted values (if xnew is not NULL).

Author(s)

Michail Tsagris.

R implementation and documentation: Michail Tsagris <mtsagris@uoc.gr>.

References

Tsagris M. and Stewart C. (2018). A Dirichlet regression model for compositional data with zeros. Lobachevskii Journal of Mathematics, 39(3): 398–412.

Preprint available from https://arxiv.org/pdf/1410.5011.pdf

See Also

```
zad.est, diri.reg, kl.compreg, ols.compreg, alfa.reg
```

Examples

```
x <- as.vector(iris[, 4])
y <- as.matrix(iris[, 1:3])
y <- y / rowSums(y)
mod1 <- diri.reg(y, x)
y[sample(1:450, 15)] <- 0
mod2 <- zadr(y, x)</pre>
```

Index

* Additive log-ratio-transformation	125
The additive log-ratio	MLE of the Dirichlet distribution
transformation and its	via Newton-Rapshon, 126
inverse, 191	* Dirichlet regression
* Bhattacharyya distance	Dirichlet regression, 65
Kullback-Leibler divergence and	* Discriminant analysis
Bhattacharyya distance	Compositional-package, 7
between two Dirichlet	* Euclidean distance
distributions, 101	The alpha-distance, 192
* Compositional data	The alpha-IT-distance, 195
Compositional-package,7	The k-nearest neighbours using the
* Contour plots	alpha-distance, 209
Compositional-package, 7	* Frechet mean
* Dirichelt mean vector	Helper Frechet mean for
Log-likelihood ratio test for a	compositional data, 89
Dirichlet mean vector, 116	The Frechet mean for compositional
* Dirichlet distribution	data, 207
Contour plot of the Dirichlet	* GLM
distribution in S^2 , 20	Tuning the principal components
Contour plot of the Flexible	with GLMs, 234
Dirichlet distribution in S^2,	* Gaussian mixture models
21	Density of compositional data from
Contour plot of the generalised	Gaussian mixture models, 56
Dirichlet distribution in S^2,	Density of the folded normal
23	distribution, 59
Density values of a Dirichlet	Simulation of compositional data
distribution, 60	from Gaussian mixture models,
Density values of a generalised	179
Dirichlet distribution, 61	Simulation of compositional data
Dirichlet random values	from the folded normal
simulation, 64	distribution, 183
Kullback-Leibler divergence and	* Gaussianmixture model
Bhattacharyya distance	Contour plot of the Gaussian
between two Dirichlet	mixture model in S^2, 22
distributions, 101	* Generalised Dirichlet distribution
Minimized Kullback-Leibler	Generalised Dirichlet random
divergence between Dirichlet	values simulation, 86
and logistic normal, 118	* Kullback-Lebler divergence
MLE of the Dirichlet distribution,	Helper functions for the

INDEX 251

Kullback-Leibler regression,	* Ridge regression
90	Cross validation for the ridge
* Kullback-Leibler divergence	regression, 38
Kullback-Leibler divergence and	* Unequality of the covariance matrices
Bhattacharyya distance	Two-sample test of
between two Dirichlet	high-dimensional means for
distributions, 101	compositional data, 237
* Log-likelihood ratio test	* bandwidth tuning
Log-likelihood ratio test for a	Tuning of the bandwidth h of the
Dirichlet mean vector, 116	kernel using the maximum
Log-likelihood ratio test for a	likelihood cross validation,
symmetric Dirichlet	222
distribution, 117	* bivariate normal distribution
* MLE	Contour plot of the alpha
Compositional-package, 7	multivariate normal in S^2, 17
* Manhattan distance	Contour plot of the alpha-folded
The alpha-distance, 192	model in S^2,18
The alpha-IT-distance, 195	Contour plot of the normal
The k-nearest neighbours using the	distribution in S^2, 26
alpha-distance, 209	* bivariate skew skewnormal distribution
* Multiplicative log-ratio-transformation	Contour plot of the skew
The multiplicative log-ratio	skew-normal distribution in
transformation and its	S^2, 27
inverse, 213	* bivariate t distribution
* Multivariate analysis of variance	Contour plot of the t distribution
Two-sample test of	in S^2, 28
high-dimensional means for	* compositional data
compositional data, 237	Hypothesis testing for two or more
* Multivariate hypothesis testing	compositional mean vectors, 92
Hypothesis testing for two or more	* contour plot
compositional mean vectors, 92	Contour plot of the alpha
* Newton-Raphson	multivariate normal in S^2, 17
MLE of the Dirichlet distribution	Contour plot of the alpha-folded
	model in S^2, 18
via Newton-Rapshon, 126	
* Regression	Contour plot of the Dirichlet
Compositional-package, 7	distribution in S^2, 20
* Regularised discriminant analysis	Contour plot of the Flexible
Cross validation for the	Dirichlet distribution in S^2,
regularised and flexible	21
discriminant analysis with	Contour plot of the Gaussian
compositional data using the	mixture model in S^2,22
alpha-transformation, 36	Contour plot of the generalised
Regularised and flexible	Dirichlet distribution in S^2,
discriminant analysis for	23
compositional data using the	Contour plot of the kernel density
alpha-transformation, 171	estimate in S^2, 24
Tuning of the k-NN algorithm for	Contour plot of the normal
compositional data 225	distribution in SA2 26

distribution in S^2, 26

compositional data, 225

252 INDEX

Contour plot of the skew MLE of the folded model for a skew-normal distribution in given value of alpha, 127 S^2, 27 * maximum log-likelihood estimation Fast estimation of the value of Contour plot of the t distribution in S^2. 28 alpha, 80 * cross-validation * mixtures of normal distributions Mixture model selection via BIC. Cross validation for the regularised and flexible 119 discriminant analysis with * model selection compositional data using the Mixture model selection via BIC, alpha-transformation, 36 119 * density values * multivariate kernel Density values of a Dirichlet Multivariate kernel density distribution, 60 estimation, 130 Density values of a generalised * multivariate linear regression Dirichlet distribution, 61 Multivariate linear regression, 132 * inverse transformation * multivariate normal distribution Inverse of the Multivariate normal random values alpha-transformation, 99 simulation on the simplex, 133 * kernel density estimate * multivariate regression Dirichlet regression, 65 Multivariate kernel density estimation, 130 Helper functions for the * kernel density Kullback-Leibler regression, Contour plot of the kernel density 90 estimate in S^2, 24 Non linear least squares regression for compositional Tuning of the bandwidth h of the kernel using the maximum data, 143 likelihood cross validation, Spatial median regression, 184 222 * multivariate rgression * location and scatter Multivariate regression with Estimating location and scatter compositional data, 136 parameters for compositional * multivariate skew normal distribution data, 75 Multivariate skew normal random * maximum likelihood cross validation values simulation on the simplex, 138 Tuning of the bandwidth h of the kernel using the maximum * multivariate t distribution likelihood cross validation, MLE for the multivariate t 222 distribution, 122 * maximum likelihood estimation Multivariate t random values Estimation of the value of alpha simulation on the simplex, 139 in the folded model, 78 * non parametric test Minimized Kullback-Leibler Hypothesis testing for two or more divergence between Dirichlet compositional mean vectors, 92 and logistic normal, 118 * ordinary least squares MLE of the Dirichlet distribution, Non linear least squares regression for compositional MLE of the Dirichlet distribution data, 143

via Newton-Rapshon, 126

* orthogonal matrix

The Helmert sub-matrix, 208	from the folded normal
* parameters tuning	distribution, 183
Cross validation for the ridge	* ridge regression
regression with compositional	Cross validation for the ridge
data as predictor using the	regression with compositional
alpha-transformation, 40	data as predictor using the
* plot	alpha-transformation, 40
Ridge regression plot, 174	Ridge regression plot, 174
Ridge regression with the	Ridge regression with
alpha-transformation plot, 177	compositional data in the
* principal components regression	covariates side using the
Multivariate or univariate	alpha-transformation, 175
regression with compositional	Ridge regression with the
data in the covariates side	alpha-transformation plot, 177
using the	* robust estimation
alpha-transformation, 135	Estimating location and scatter
Tuning the number of PCs in the	parameters for compositional
PCR with compositional data	data, 75
using the	* spatial median regression
alpha-transformation, 232	Multivariate regression with
* principal components	compositional data, 136
Tuning the principal components	Spatial median regression, 184
with GLMs, 234	* symmetric Dirichlet distribution
* profile log-likelihood	Log-likelihood ratio test for a
Estimation of the value of alpha	symmetric Dirichlet
via the profile	distribution, 117
log-likelihood, 79	* ternary plot
* random values simulation	Ternary diagram, 185
Dirichlet random values	Ternary diagram of regression
simulation, 64	models, 186
Generalised Dirichlet random	* tuning
values simulation, 86	Tuning the number of PCs in the
Multivariate normal random values	PCR with compositional data
simulation on the simplex, 133	using the
Multivariate skew normal random	alpha-transformation, 232
values simulation on the	* visualisation
simplex, 138	Ternary diagram, 185
Multivariate t random values	Ternary diagram of regression
simulation on the simplex, 139	models, 186
* random vectors simulation	2 22+ 60 77 129 192 202
Density of compositional data from	a.est, 60, 77, 128, 183, 203 a.est (Estimation of the value of
Gaussian mixture models, 56	alpha in the folded model), 78
Density of the folded normal	· · · · · · · · · · · · · · · · · · ·
distribution, 59	a.mle, 203
Simulation of compositional data	a.mle(MLE of the folded model for a given value of alpha), 127
from Gaussian mixture models,	acor, 75, 165, 222
179	acor (Alpha-generalised correlations
Simulation of compositional data	between two compositional
Simulation of compositional data	nerween rwo combosiciolai

datasets), 10	212–214, 221, 222, 233, 237
acor. tune, <i>11</i> , <i>75</i>	alfa(The alpha-transformation), 202
acor.tune (Tuning of the	alfa.contour, 19
alpha-generalised	alfa.contour (Contour plot of the alpha
correlations between two	multivariate normal in S^2), 17
compositional datasets), 221	alfa.fda, <i>31</i> , <i>33</i> , <i>35</i>
aeqdist.etest, 11	alfa.fda(Regularised and flexible
aeqdist.etest (Energy test of equality	discriminant analysis for
of distributions using the	compositional data using the
alpha-transformation), 74	alpha-transformation), 171
ait, <i>196</i>	alfa.knn, 64, 83, 85, 122, 141, 143, 172, 198,
ait(The alpha-IT transformation), 193	210
ait.knn, <i>194</i>	alfa.knn(The k-NN algorithm for
ait.knn(The k-NN algorithm for	compositional data), 211
compositional data), 211	alfa.knn.reg, 13, 44, 103, 106, 114, 115,
ait.test(Aitchison's test for two	240, 242
mean vectors and/or covariance	alfa.knn.reg(The alpha-k-NN
matrices), 8	regression with compositional
Aitchison's test for two mean vectors	predictor variables), 197
and/or covariance matrices, 8	alfa.lasso,44
aitdist, <i>194</i>	alfa.lasso(LASSO with compositional
aitdist(The alpha-IT-distance), 195	predictors using the
aitdista(The alpha-IT-distance), 195	alpha-transformation), 105
aitknn.tune(Tuning of the k-NN	alfa.mds, <i>159</i>
algorithm for compositional	alfa.mds(Principal coordinate
data), 225	analysis using the
akern.reg, 33, 35, 101, 161, 197	alpha-distance), 157
akern.reg(The alpha-kernel regression	alfa.mix.norm, <i>83</i> , <i>122</i>
with compositional response	alfa.mix.norm(Gaussian mixture models
data), 199	for compositional data using
akernreg.tune, 33, 200, 229	the alpha-transformation), 84
akernreg.tune(Cross validation for	alfa.nb, 53, 172, 210, 212
the alpha-kernel regression	alfa.nb(Naive Bayes classifiers for
with compositional response	compositional data using the
data), 33	alpha-transformation), 142
aknn.reg, 33, 35, 36, 89, 101, 161, 198, 200	alfa.pca, 154, 158, 159
aknn.reg(The alpha-k-NN regression	alfa.pca(Principal component analysis
for compositional response	using the
data), 196	alpha-transformation), 155
aknnreg. tune, 30, 35, 36, 197, 200, 229	alfa.pcr, 13, 95, 98, 103, 114, 115, 154, 156,
aknnreg.tune (Cross validation for the	157, 162, 198, 233, 235, 240, 242
alpha-k-NN regression with	alfa.pcr(Multivariate or univariate
compositional response data),	regression with compositional
32	data in the covariates side using the
alef (The alpha-transformation), 202	alpha-transformation), 135
alfa, 10, 11, 75, 77, 79–81, 85, 88, 90, 100, 122, 128, 145, 153, 172, 183,	alfa.pprcomp, 231
192_194_196_205_207_210	alfa pprcomp (Projection pursuit

regression with compositional	allakililleg. tulle (Cross Valluation Tor
predictor variables using the	the alpha-k-NN regression with
alpha-transformation), 162	compositional predictor
alfa.profile, 11, 75, 79, 81, 128, 203, 221,	variables), 30
222	alfalasso.tune, 106
alfa.profile(Estimation of the value	alfalasso.tune(Cross-validation for
of alpha via the profile	LASSO with compositional
log-likelihood), 79	predictors using the
alfa.rda, 31, 33, 35, 38, 64, 83, 85, 122, 141,	alpha-transformation), 43
143, 210, 212	alfanb.tune, $38,48$
alfa.rda(Regularised and flexible	alfanb.tune (Cross-validation for the
discriminant analysis for	naive Bayes classifiers for
compositional data using the	compositional data using the
alpha-transformation), 171	alpha-transformation), 52
alfa.reg, 67, 144, 161, 185, 193, 197, 200,	alfann (The k-nearest neighbours using
237, 249	the alpha-distance), 209
alfa.reg(Regression with	alfapcr.tune, 72, 136, 157, 225, 230, 234,
compositional data using the	235
alpha-transformation), 169	alfapcr.tune (Tuning the number of PCs
alfa.reg2(Regression with	in the PCR with compositional
compositional data using the	data using the
alpha-transformation), 169	alpha-transformation), 232
alfa.reg3 (Regression with	alfapprcomp.tune, 163
compositional data using the	alfapprcomp.tune(Tuning of the
alpha-transformation), 169	projection pursuit regression
alfa.ridge, 41, 173-175, 178, 198	with compositional predictor
alfa.ridge(Ridge regression with	variables using the
compositional data in the	alpha-transformation), 230
covariates side using the	alfarda.tune, 48, 53, 172, 227
alpha-transformation), 175	alfarda.tune(Cross validation for the
alfa.tune, 80, 203, 221	regularised and flexible
alfa.tune(Fast estimation of the	discriminant analysis with
value of alpha), 80	compositional data using the
alfadist, 100, 196, 206	alpha-transformation), 36
alfadist (The alpha-distance), 192	alfareg.tune, <i>137</i> , <i>170</i> , <i>171</i>
alfadista (The alpha-distance), 192	alfareg.tune(Tuning the value of alpha
alfafda.tune(Cross validation for the	in the alpha-regression), 235
regularised and flexible	alfaridge.plot, <i>175</i> , <i>176</i>
discriminant analysis with	alfaridge.plot(Ridge regression with
compositional data using the	the alpha-transformation
alpha-transformation), 36	plot), 177
alfainv, 79-81, 90, 128, 192, 193, 203,	alfaridge.tune, 39, 176
208–210, 214, 222	alfaridge.tune(Cross validation for
alfainv(Inverse of the	the ridge regression with
alpha-transformation), 99	compositional data as
alfaknn.tune(Tuning of the k-NN	predictor using the
algorithm for compositional	alpha-transformation), 40
data). 225	All pairwise additive log-ratio

transformations, 9	collogitnorm.est(Column-wise MLE of
Alpha-generalised correlations between	some univariate
two compositional datasets, 10	distributions), 15
alpha.mle, 77, 79, 183, 203	Column-wise MLE of some univariate
alpha.mle(MLE of the folded model for	distributions, 15
a given value of alpha), 127	colunitweibull.est(Column-wise MLE of
alr, 10, 50, 104, 165, 194, 203–207, 213, 214	some univariate
alr (The additive log-ratio	distributions), 15
transformation and its	colzilogitnorm.est (Column-wise MLE of
inverse), 191	some univariate
alr.all(All pairwise additive	distributions), 15
log-ratio transformations), 9	comp.den, 122, 123, 134, 139, 140
alrinv (The additive log-ratio	comp.den(Estimating location and
transformation and its	scatter parameters for
inverse), 191	compositional data), 75
ANOVA for the log-contrast GLM versus	comp.kern (Multivariate kernel density
the uncostrained GLM, 12	·
ANOVA for the log-contrast regression	estimation for compositional
versus the uncostrained linear	data), 131
regression, 13	comp.kerncontour, 17, 20, 22, 24, 131, 132,
ascls, 46, 202	223
ascls (The alpha-SCLS model), 200	comp.kerncontour(Contour plot of the
atflr, 47, 201	kernel density estimate in
atflr (The alpha-TFLR model), 201	S^2), 24
attit (the alpha-filk model), 201	comp.knn, 64, 73, 141, 143, 206, 227
bc, 192, 203, 207	comp.knn(The k-NN algorithm for
	• • • • • • • • • • • • • • • • • • • •
	compositional data), 211
bc(The Box-Cox transformation applied	compositional data), 211 comp.nb, 52, 64, 83, 85, 122, 143, 172, 210,
bc (The Box-Cox transformation applied to ratios of components), 204	
bc (The Box-Cox transformation applied to ratios of components), 204 Beta regression, 14	comp.nb, 52, 64, 83, 85, 122, 143, 172, 210,
bc (The Box-Cox transformation applied to ratios of components), 204 Beta regression, 14 beta.est, <i>14</i> , <i>16</i> , <i>168</i>	comp. nb, 52, 64, 83, 85, 122, 143, 172, 210, 212
bc (The Box-Cox transformation applied to ratios of components), 204 Beta regression, 14 beta.est, 14 , 16 , 168 beta.est (MLE of distributions defined	comp.nb, 52, 64, 83, 85, 122, 143, 172, 210, 212 comp.nb (Naive Bayes classifiers for
bc (The Box-Cox transformation applied to ratios of components), 204 Beta regression, 14 beta.est, 14 , 16 , 168 beta.est (MLE of distributions defined in the $(0, 1)$ interval), 123	comp.nb, 52, 64, 83, 85, 122, 143, 172, 210, 212 comp.nb (Naive Bayes classifiers for compositional data), 140
bc (The Box-Cox transformation applied to ratios of components), 204 Beta regression, 14 beta.est, 14, 16, 168 beta.est (MLE of distributions defined in the (0, 1) interval), 123 beta.reg, 68, 167, 248	comp.nb, 52, 64, 83, 85, 122, 143, 172, 210, 212 comp.nb (Naive Bayes classifiers for compositional data), 140 comp.ppr, 95, 162, 163, 197, 200, 229
bc (The Box-Cox transformation applied to ratios of components), 204 Beta regression, 14 beta.est, 14, 16, 168 beta.est (MLE of distributions defined in the (0, 1) interval), 123 beta.reg, 68, 167, 248 beta.reg (Beta regression), 14	<pre>comp.nb, 52, 64, 83, 85, 122, 143, 172, 210,</pre>
bc (The Box-Cox transformation applied to ratios of components), 204 Beta regression, 14 beta.est, 14, 16, 168 beta.est (MLE of distributions defined in the (0, 1) interval), 123 beta.reg, 68, 167, 248 beta.reg (Beta regression), 14 bic.alfamixnorm, 85, 120	comp.nb, 52, 64, 83, 85, 122, 143, 172, 210, 212 comp.nb (Naive Bayes classifiers for compositional data), 140 comp.ppr, 95, 162, 163, 197, 200, 229 comp.ppr (Projection pursuit regression for compositional data), 160
bc (The Box-Cox transformation applied to ratios of components), 204 Beta regression, 14 beta.est, 14, 16, 168 beta.est (MLE of distributions defined in the (0, 1) interval), 123 beta.reg, 68, 167, 248 beta.reg (Beta regression), 14 bic.alfamixnorm, 85, 120 bic.alfamixnorm (Mixture model	comp.nb, 52, 64, 83, 85, 122, 143, 172, 210, 212 comp.nb (Naive Bayes classifiers for compositional data), 140 comp.ppr, 95, 162, 163, 197, 200, 229 comp.ppr (Projection pursuit regression for compositional
bc (The Box-Cox transformation applied to ratios of components), 204 Beta regression, 14 beta.est, 14, 16, 168 beta.est (MLE of distributions defined in the (0, 1) interval), 123 beta.reg, 68, 167, 248 beta.reg (Beta regression), 14 bic.alfamixnorm, 85, 120 bic.alfamixnorm (Mixture model selection with the	comp.nb, 52, 64, 83, 85, 122, 143, 172, 210, 212 comp.nb (Naive Bayes classifiers for compositional data), 140 comp.ppr, 95, 162, 163, 197, 200, 229 comp.ppr (Projection pursuit regression for compositional data), 160 comp.reg, 30, 51, 67, 70, 91, 105, 133, 144, 152, 161, 171, 184, 185, 197, 200
bc (The Box-Cox transformation applied to ratios of components), 204 Beta regression, 14 beta.est, 14, 16, 168 beta.est (MLE of distributions defined in the (0, 1) interval), 123 beta.reg, 68, 167, 248 beta.reg (Beta regression), 14 bic.alfamixnorm, 85, 120 bic.alfamixnorm (Mixture model selection with the alpha-transformation using	comp.nb, 52, 64, 83, 85, 122, 143, 172, 210, 212 comp.nb (Naive Bayes classifiers for compositional data), 140 comp.ppr, 95, 162, 163, 197, 200, 229 comp.ppr (Projection pursuit regression for compositional data), 160 comp.reg, 30, 51, 67, 70, 91, 105, 133, 144, 152, 161, 171, 184, 185, 197, 200 comp.reg (Multivariate regression with
bc (The Box-Cox transformation applied to ratios of components), 204 Beta regression, 14 beta.est, 14, 16, 168 beta.est (MLE of distributions defined in the (0, 1) interval), 123 beta.reg, 68, 167, 248 beta.reg (Beta regression), 14 bic.alfamixnorm, 85, 120 bic.alfamixnorm (Mixture model selection with the alpha-transformation using BIC), 120	comp.nb, 52, 64, 83, 85, 122, 143, 172, 210, 212 comp.nb (Naive Bayes classifiers for compositional data), 140 comp.ppr, 95, 162, 163, 197, 200, 229 comp.ppr (Projection pursuit regression for compositional data), 160 comp.reg, 30, 51, 67, 70, 91, 105, 133, 144, 152, 161, 171, 184, 185, 197, 200 comp.reg (Multivariate regression with compositional data), 136
bc (The Box-Cox transformation applied to ratios of components), 204 Beta regression, 14 beta.est, 14, 16, 168 beta.est (MLE of distributions defined in the (0, 1) interval), 123 beta.reg, 68, 167, 248 beta.reg (Beta regression), 14 bic.alfamixnorm, 85, 120 bic.alfamixnorm (Mixture model selection with the alpha-transformation using BIC), 120 bic.mixcompnorm, 23, 57, 83, 85, 180	comp.nb, 52, 64, 83, 85, 122, 143, 172, 210, 212 comp.nb (Naive Bayes classifiers for compositional data), 140 comp.ppr, 95, 162, 163, 197, 200, 229 comp.ppr (Projection pursuit regression for compositional data), 160 comp.reg, 30, 51, 67, 70, 91, 105, 133, 144, 152, 161, 171, 184, 185, 197, 200 comp.reg (Multivariate regression with compositional data), 136 comp.test, 9, 164, 238
bc (The Box-Cox transformation applied to ratios of components), 204 Beta regression, 14 beta.est, 14, 16, 168 beta.est (MLE of distributions defined in the (0, 1) interval), 123 beta.reg, 68, 167, 248 beta.reg (Beta regression), 14 bic.alfamixnorm, 85, 120 bic.alfamixnorm (Mixture model selection with the alpha-transformation using BIC), 120 bic.mixcompnorm, 23, 57, 83, 85, 180 bic.mixcompnorm (Mixture model	comp.nb, 52, 64, 83, 85, 122, 143, 172, 210, 212 comp.nb (Naive Bayes classifiers for compositional data), 140 comp.ppr, 95, 162, 163, 197, 200, 229 comp.ppr (Projection pursuit regression for compositional data), 160 comp.reg, 30, 51, 67, 70, 91, 105, 133, 144, 152, 161, 171, 184, 185, 197, 200 comp.reg (Multivariate regression with compositional data), 136 comp.test, 9, 164, 238 comp.test (Hypothesis testing for two
bc (The Box-Cox transformation applied to ratios of components), 204 Beta regression, 14 beta.est, 14, 16, 168 beta.est (MLE of distributions defined in the (0, 1) interval), 123 beta.reg, 68, 167, 248 beta.reg (Beta regression), 14 bic.alfamixnorm, 85, 120 bic.alfamixnorm (Mixture model selection with the alpha-transformation using BIC), 120 bic.mixcompnorm, 23, 57, 83, 85, 180 bic.mixcompnorm (Mixture model selection via BIC), 119	comp.nb, 52, 64, 83, 85, 122, 143, 172, 210, 212 comp.nb (Naive Bayes classifiers for compositional data), 140 comp.ppr, 95, 162, 163, 197, 200, 229 comp.ppr (Projection pursuit regression for compositional data), 160 comp.reg, 30, 51, 67, 70, 91, 105, 133, 144, 152, 161, 171, 184, 185, 197, 200 comp.reg (Multivariate regression with compositional data), 136 comp.test, 9, 164, 238 comp.test (Hypothesis testing for two or more compositional mean
bc (The Box-Cox transformation applied to ratios of components), 204 Beta regression, 14 beta.est, 14, 16, 168 beta.est (MLE of distributions defined in the (0, 1) interval), 123 beta.reg, 68, 167, 248 beta.reg (Beta regression), 14 bic.alfamixnorm, 85, 120 bic.alfamixnorm (Mixture model selection with the alpha-transformation using BIC), 120 bic.mixcompnorm, 23, 57, 83, 85, 180 bic.mixcompnorm (Mixture model selection via BIC), 119 bivt.contour, 18, 19, 22, 25, 26, 28, 122, 123	comp.nb, 52 , 64 , 83 , 85 , 122 , 143 , 172 , 210 , 212 comp.nb (Naive Bayes classifiers for compositional data), 140 comp.ppr, 95 , 162 , 163 , 197 , 200 , 229 comp.ppr (Projection pursuit regression for compositional data), 160 comp.reg, 30 , 51 , 67 , 70 , 91 , 105 , 133 , 144 , 152 , 161 , 171 , 184 , 185 , 197 , 200 comp.reg (Multivariate regression with compositional data), 136 comp.test, 9 , 164 , 238 comp.test (Hypothesis testing for two or more compositional mean vectors), 92
bc (The Box-Cox transformation applied to ratios of components), 204 Beta regression, 14 beta.est, 14, 16, 168 beta.est (MLE of distributions defined in the (0, 1) interval), 123 beta.reg, 68, 167, 248 beta.reg (Beta regression), 14 bic.alfamixnorm, 85, 120 bic.alfamixnorm (Mixture model selection with the alpha-transformation using BIC), 120 bic.mixcompnorm, 23, 57, 83, 85, 180 bic.mixcompnorm (Mixture model selection via BIC), 119 bivt.contour, 18, 19, 22, 25, 26, 28, 122, 123 bivt.contour (Contour plot of the t	comp.nb, 52 , 64 , 83 , 85 , 122 , 143 , 172 , 210 , 212 comp.nb (Naive Bayes classifiers for compositional data), 140 comp.ppr, 95 , 162 , 163 , 197 , 200 , 229 comp.ppr (Projection pursuit regression for compositional data), 160 comp.reg, 30 , 51 , 67 , 70 , 91 , 105 , 133 , 144 , 152 , 161 , 171 , 184 , 185 , 197 , 200 comp.reg (Multivariate regression with compositional data), 136 comp.test, 9 , 164 , 238 comp.test (Hypothesis testing for two or more compositional mean vectors), 92 compknn.tune, 38 , 48 , 53 , 87 , 212
bc (The Box-Cox transformation applied to ratios of components), 204 Beta regression, 14 beta.est, 14, 16, 168 beta.est (MLE of distributions defined in the (0, 1) interval), 123 beta.reg, 68, 167, 248 beta.reg (Beta regression), 14 bic.alfamixnorm, 85, 120 bic.alfamixnorm (Mixture model selection with the alpha-transformation using BIC), 120 bic.mixcompnorm, 23, 57, 83, 85, 180 bic.mixcompnorm (Mixture model selection via BIC), 119 bivt.contour, 18, 19, 22, 25, 26, 28, 122, 123	comp.nb, 52, 64, 83, 85, 122, 143, 172, 210, 212 comp.nb (Naive Bayes classifiers for compositional data), 140 comp.ppr, 95, 162, 163, 197, 200, 229 comp.ppr (Projection pursuit regression for compositional data), 160 comp.reg, 30, 51, 67, 70, 91, 105, 133, 144, 152, 161, 171, 184, 185, 197, 200 comp.reg (Multivariate regression with compositional data), 136 comp.test, 9, 164, 238 comp.test (Hypothesis testing for two or more compositional mean vectors), 92 compknn.tune, 38, 48, 53, 87, 212 compknn.tune (Tuning of the k-NN
bc (The Box-Cox transformation applied to ratios of components), 204 Beta regression, 14 beta.est, 14, 16, 168 beta.est (MLE of distributions defined in the (0, 1) interval), 123 beta.reg, 68, 167, 248 beta.reg (Beta regression), 14 bic.alfamixnorm, 85, 120 bic.alfamixnorm (Mixture model selection with the alpha-transformation using BIC), 120 bic.mixcompnorm, 23, 57, 83, 85, 180 bic.mixcompnorm (Mixture model selection via BIC), 119 bivt.contour, 18, 19, 22, 25, 26, 28, 122, 123 bivt.contour (Contour plot of the t distribution in S^2), 28	comp.nb, 52, 64, 83, 85, 122, 143, 172, 210, 212 comp.nb (Naive Bayes classifiers for compositional data), 140 comp.ppr, 95, 162, 163, 197, 200, 229 comp.ppr (Projection pursuit regression for compositional data), 160 comp.reg, 30, 51, 67, 70, 91, 105, 133, 144, 152, 161, 171, 184, 185, 197, 200 comp.reg (Multivariate regression with compositional data), 136 comp.test, 9, 164, 238 comp.test (Hypothesis testing for two or more compositional mean vectors), 92 compknn.tune, 38, 48, 53, 87, 212 compknn.tune (Tuning of the k-NN algorithm for compositional
bc (The Box-Cox transformation applied to ratios of components), 204 Beta regression, 14 beta.est, 14, 16, 168 beta.est (MLE of distributions defined in the (0, 1) interval), 123 beta.reg, 68, 167, 248 beta.reg (Beta regression), 14 bic.alfamixnorm, 85, 120 bic.alfamixnorm (Mixture model selection with the alpha-transformation using BIC), 120 bic.mixcompnorm, 23, 57, 83, 85, 180 bic.mixcompnorm (Mixture model selection via BIC), 119 bivt.contour, 18, 19, 22, 25, 26, 28, 122, 123 bivt.contour (Contour plot of the t distribution in S^2), 28 colbeta.est, 168	comp.nb, 52, 64, 83, 85, 122, 143, 172, 210, 212 comp.nb (Naive Bayes classifiers for compositional data), 140 comp.ppr, 95, 162, 163, 197, 200, 229 comp.ppr (Projection pursuit regression for compositional data), 160 comp.reg, 30, 51, 67, 70, 91, 105, 133, 144, 152, 161, 171, 184, 185, 197, 200 comp.reg (Multivariate regression with compositional data), 136 comp.test, 9, 164, 238 comp.test (Hypothesis testing for two or more compositional mean vectors), 92 compknn.tune, 38, 48, 53, 87, 212 compknn.tune (Tuning of the k-NN algorithm for compositional data), 225
bc (The Box-Cox transformation applied to ratios of components), 204 Beta regression, 14 beta.est, 14, 16, 168 beta.est (MLE of distributions defined in the (0, 1) interval), 123 beta.reg, 68, 167, 248 beta.reg (Beta regression), 14 bic.alfamixnorm, 85, 120 bic.alfamixnorm (Mixture model selection with the alpha-transformation using BIC), 120 bic.mixcompnorm, 23, 57, 83, 85, 180 bic.mixcompnorm (Mixture model selection via BIC), 119 bivt.contour, 18, 19, 22, 25, 26, 28, 122, 123 bivt.contour (Contour plot of the t distribution in S^2), 28	comp.nb, 52, 64, 83, 85, 122, 143, 172, 210, 212 comp.nb (Naive Bayes classifiers for compositional data), 140 comp.ppr, 95, 162, 163, 197, 200, 229 comp.ppr (Projection pursuit regression for compositional data), 160 comp.reg, 30, 51, 67, 70, 91, 105, 133, 144, 152, 161, 171, 184, 185, 197, 200 comp.reg (Multivariate regression with compositional data), 136 comp.test, 9, 164, 238 comp.test (Hypothesis testing for two or more compositional mean vectors), 92 compknn.tune, 38, 48, 53, 87, 212 compknn.tune (Tuning of the k-NN algorithm for compositional

normal distribution in S^2 , 26	alpha-transformation, 36
Compositional-package, 7	Cross validation for the ridge
compppr.tune, 30, 161, 230, 231	regression, 38
compppr.tune (Tuning of the projection	Cross validation for the ridge
pursuit regression for	regression with compositional
compositional data), 228	data as predictor using the
Contour plot of mixtures of Dirichlet	alpha-transformation, 40
distributions in S^2, 16	Cross validation for the TFLR model, 42
Contour plot of the alpha multivariate	Cross-validation for LASSO with
normal in S^2, 17	compositional predictors using
Contour plot of the alpha-folded model	the alpha-transformation, 43
in S^2, 18	Cross-validation for the alpha-SCLS
Contour plot of the Dirichlet	model, 45
distribution in S^2 , 20	Cross-validation for the alpha-TFLR
Contour plot of the Flexible Dirichlet	model, 46
distribution in S^2,21	Cross-validation for the Dirichlet
Contour plot of the Gaussian mixture	discriminant analysis, 47
model in S^2, 22	Cross-validation for the LASSO
Contour plot of the generalised	Kullback-Leibler divergence
Dirichlet distribution in S^2,	based regression, 48
23	Cross-validation for the LASSO
Contour plot of the kernel density	log-ratio regression with
estimate in S^2,24	compositional response, 50
Contour plot of the normal	Cross-validation for the naive Bayes
distribution in S^2 , 26	classifiers for compositional
Contour plot of the skew skew-normal	data, 51
distribution in S^2,27	Cross-validation for the naive Bayes
Contour plot of the t distribution in	classifiers for compositional
S^2, 28	data using the
Cross validation for some	alpha-transformation, 52
compositional regression	Cross-validation for the SCLS model, 54
models, 29	Cross-validation for the SCRQ model, 55
Cross validation for the alpha-k-NN	cv.ascls, 47, 201
regression with compositional	cv.ascls(Cross-validation for the
predictor variables, 30	alpha-SCLS model), 45
Cross validation for the alpha-k-NN	cv.atflr, 46, 202
regression with compositional	cv.atflr(Cross-validation for the
response data, 32	alpha-TFLR model), 46
Cross validation for the alpha-kernel	cv.comp.reg(Cross validation for some
regression with compositional	compositional regression
response data, 33	models), 29
Cross validation for the kernel	cv. compnb, 38, 48, 53, 141, 227
regression with Euclidean	cv.compnb (Cross-validation for the
response data, 35	naive Bayes classifiers for
Cross validation for the regularised	compositional data), 51
and flexible discriminant	cv.dda, 38, 53, 64, 227
analysis with compositional	cv.dda(Cross-validation for the
data using the	Dirichlet discriminant

analysis), 47	diri.contour, 17–19, 23–26, 28, 29, 61, 62,
cv.lasso.compreg, 49, 105, 152	65, 86, 119, 126, 127, 186, 187, 190
cv.lasso.compreg (Cross-validation for	diri.contour (Contour plot of the
the LASSO log-ratio regression	Dirichlet distribution in
with compositional response),	S^2), 20
50	diri.est, 8, 61, 62, 65, 86, 102, 117, 118,
cv.lasso.klcompreg, 44, 51, 103, 105, 106,	124, 127
152	diri.est (MLE of the Dirichlet
cv.lasso.klcompreg(Cross-validation	distribution), 125
for the LASSO Kullback-Leibler	diri.nr, 17, 61, 65, 67, 86, 102, 117–119,
divergence based regression),	126, 129
48	diri.nr(MLE of the Dirichlet
cv.scls, 43, 56, 216–218	distribution via
cv.scls(Cross-validation for the SCLS	Newton-Rapshon), 126
model), 54	diri.reg, 7, 8, 14, 64, 70, 91, 119, 126, 133,
cv.scrq(Cross-validation for the SCRQ	137, 144, 171, 185, 249
model), 55	diri.reg (Dirichlet regression), 65
cv.tflr, 55, 56, 220, 225	diri.reg2 (Dirichlet regression), 65
cv.tflr(Cross validation for the TFLR	diri.reg3 (Dirichlet regression), 65
model), 42	Dirichlet discriminant analysis, 63
	Dirichlet random values simulation, 64
dda, 17, 48, 61, 62, 67, 119, 126, 127, 141	Dirichlet regression, 65
dda (Dirichlet discriminant analysis),	dirimean.test, 8, 118
63	dirimean.test(Log-likelihood ratio
ddiri, 62, 117, 119, 126, 127	test for a Dirichlet mean
ddiri (Density values of a Dirichlet	vector), 116
distribution), 60	Distance based regression models for
Density of compositional data from	proportions, 67
Gaussian mixture models, 56	divergence (Divergence matrix of
Density of the Flexible Dirichlet	compositional data), 73
distribution, 58	Divergence based regression for
Density of the folded normal	compositional data, 69
distribution, 59	Divergence based regression for
Density values of a Dirichlet	compositional data with
distribution, 60	compositional data in the
Density values of a generalised	covariates side using the
Dirichlet distribution, 61	alpha-transformation, 71
Density values of a mixture of	Divergence matrix of compositional
Dirichlet distributions, 62	data, 73
dfd, 182	dmix.compnorm(Density of
dfd (Density of the Flexible Dirichlet	compositional data from
distribution), 58	Gaussian mixture models), 56
dfolded (Density of the folded normal	dmixdiri(Density values of a mixture
distribution), 59	of Dirichlet distributions), 62
dgendiri, 61	dptest, 93
dgendiri (Density values of a	dptest (Projections based test for
generalised Dirichlet	distributional equality of two
distribution), 61	groups), 164

Energy test of equality of	Generate random folds for
distributions using the	cross-validation, 87
alpha-transformation,74	glm, 233
es (The ESOV-distance), 205	glm.pcr, 72, 136, 225, 235
esov, <i>193</i> , <i>212</i>	glm.pcr(Principal component
esov (The ESOV-distance), 205	generalised linear models), 156
esov.mds, 158	glmpcr.tune, 233
esov.mds (Principal coordinate	glmpcr.tune (Tuning the principal
analysis using the	components with GLMs), 234
Jensen-Shannon divergence), 159	green, 192, 194, 203, 205, 207, 213, 214
esova (The ESOV-distance), 205	green (Greenacre's power
Estimating location and scatter	transformation), 88
parameters for compositional	
data, 75	Greenacre's power transformation, 88
Estimation of the probability left	hd.meantest2, 93
outside the simplex when using	hd.meantest2(Two-sample test of
the alpha-transformation, 77	high-dimensional means for
Estimation of the value of alpha in	compositional data), 237
the folded model, 78	helling.prop.reg(Distance based
Estimation of the value of alpha via	regression models for
the profile log-likelihood, 79	proportions), 67
	helm (The Helmert sub-matrix), 208
Fast estimation of the value of alpha,	Helper Frechet mean for compositional
80	data, 89
fd.contour (Contour plot of the	Helper functions for the
Flexible Dirichlet	Kullback-Leibler regression,
distribution in S^2), 21	90
folded.contour, <i>18</i> , <i>22</i> , <i>60</i>	
folded.contour (Contour plot of the	hsecant01.est (MLE of distributions
alpha-folded model in S^2), 18	defined in the (0, 1)
fp, 192, 203, 205	interval), 123
fp (The folded power transformation),	Hypothesis testing for two or more
206	compositional mean vectors, 92
frechet (The Frechet mean for	
compositional data), 207	<pre>ibeta.est(MLE of distributions defined</pre>
frechet2 (Helper Frechet mean for	in the (0, 1) interval), 123
compositional data), 89	ICE plot for projection pursuit
compositional data), 67	regression with compositional
Gaussian mixture models for	predictor variables, 94
compositional data, 82	ICE plot for the alpha-k-NN
Gaussian mixture models for	regression, 95
compositional data using the	ICE plot for the alpha-kernel
alpha-transformation, 84	regression, 96
·	ICE plot for univariate kernel
gendiri.contour, 17, 20	•
gendiri.contour (Contour plot of the	regression, 97
generalised Dirichlet	ice.akernreg, 96
distribution in S^2), 23	ice.akernreg(ICE plot for the
Generalised Dirichlet random values	alpha-kernel regression), 96
simulation, 86	ice.aknnreg, 97

ice.aknnreg(ICE plot for the	between Dirichlet and logistic
alpha-k-NN regression), 95	normal), 118
ice.kernreg, 95, 101	klalfapcr.tune, <i>43</i> , <i>55</i> , <i>72</i>
ice.kernreg(ICE plot for univariate	klalfapcr.tune(Tuning of the
kernel regression), 97	divergence based regression
ice.pprcomp, 96-98, 162, 230	for compositional data with
<pre>ice.pprcomp(ICE plot for projection</pre>	compositional data in the
pursuit regression with	covariates side using the
compositional predictor	alpha-transformation), 224
variables), 94	klcompreg.boot (Helper functions for
Inverse of the alpha-transformation, 99	the Kullback-Leibler
There is or the alpha transformation,	regression), 90
	Kullback-Leibler divergence and
js.compreg, 7, 67, 73, 91, 133, 137, 144, 171,	Bhattacharyya distance
185, 206	
js.compreg(Divergence based	between two Dirichlet
regression for compositional	distributions, 101
data), 69	kumar.est (MLE of distributions defined
	in the (0, 1) interval), 123
kern.reg, 36	LACCO Kullhadi Laihlan diwanana
kern.reg(Kernel regression with a	LASSO Kullback-Leibler divergence
numerical response vector or	based regression, 102
	LASSO log-ratio regression with
matrix), 100	compositional response, 104
Kernel regression with a numerical	LASSO with compositional predictors
response vector or matrix, 100	using the
kernreg. tune, $98, 101$	alpha-transformation, 105
kernreg.tune(Cross validation for the	lasso.compreg, 44, 49, 51, 103, 106, 152
kernel regression with	lasso.compreg(LASSO log-ratio
Euclidean response data), 35	regression with compositional
kl.alfapcr, 154, 156, 220, 225	response), 104
kl.alfapcr(Divergence based	lasso.klcompreg, 49, 51, 105, 152
regression for compositional	lasso.klcompreg(LASSO
data with compositional data	Kullback-Leibler divergence
in the covariates side using	based regression), 102
the alpha-transformation), 71	lassocoef.plot, 49, 51, 103, 105
kl.compreg, 7, 8, 30, 49, 67, 91, 103, 133,	lassocoef.plot (Plot of the LASSO
144, 152, 161, 171, 197, 200, 249	
kl.compreg (Divergence based	coefficients), 151
	lc.glm, 8, 12, 109, 239, 244, 245
regression for compositional	lc.glm(Log-contrast GLMs with
data), 69	compositional predictor
kl.compreg2(Helper functions for the	variables), 107
Kullback-Leibler regression),	lc.glm2, 108, 239, 243-245
90	lc.glm2(Log-contrast logistic or
kl.diri(Kullback-Leibler divergence	Poisson regression with with
and Bhattacharyya distance	multiple compositional
between two Dirichlet	predictors), 108
distributions), 101	lc.reg, 13, 95, 98, 115, 162, 240, 242
kl.diri.normal(Minimized	lc.reg(Log-contrast regression with
Kullback-Leibler divergence	compositional predictor

variables), 113	logpca(Principal component analysis),
lc.reg2, <i>114</i> , <i>240–242</i>	154
<pre>lc.reg2 (Log-contrast regression with</pre>	
multiple compositional	makefolds (Generate random folds for
predictors), 114	cross-validation), 87
lc.rq, 112, 244, 246	Minimized Kullback-Leibler divergence
<pre>lc.rq(Log-contrast quantile</pre>	between Dirichlet and logistic
regression with compositional	normal, 118
predictor variables), 110	mix.compnorm, 22, 23, 57, 64, 85, 120, 122,
lc.rq2, 111, 246	141, 143, 172, 180, 212
<pre>lc.rq2(Log-contrast quantile</pre>	mix.compnorm (Gaussian mixture models
regression with with multiple	for compositional data), 82
compositional predictors), 111	mix.compnorm.contour, 17–20, 22, 24–26,
lcglm.aov, 108, 239, 245	28, 29, 83, 85, 120, 122
lcglm.aov(ANOVA for the log-contrast	mix.compnorm.contour (Contour plot of
GLM versus the uncostrained	the Gaussian mixture model in
GLM), 12	\$^2), 22
lcreg.aov, 114, 115, 240	mixdiri.contour, 20, 24, 63, 181
lcreg.aov (ANOVA for the log-contrast	mixdiri.contour(Contour plot of
regression versus the	mixtures of Dirichlet
uncostrained linear	distributions in S^2), 16
regression), 13	Mixture model selection via BIC, 119
lm, 133	Mixture model selection with the
Log-contrast GLMs with compositional	alpha-transformation using
predictor variables, 107	BIC, 120
Log-contrast logistic or Poisson	mkde, 7, 132, 223
regression with with multiple	mkde (Multivariate kernel density
compositional predictors, 108	estimation), 130
Log-contrast quantile regression with	mkde.tune, 131
compositional predictor	mkde.tune (Tuning of the bandwidth h
variables, 110	of the kernel using the
Log-contrast quantile regression with	maximum likelihood cross
with multiple compositional	validation), 222
predictors, 111	MLE for the multivariate t
Log-contrast regression with	distribution, 122
compositional predictor	MLE of distributions defined in the
variables, 113	(0, 1) interval, 123
Log-contrast regression with multiple	MLE of the Dirichlet distribution, 125 MLE of the Dirichlet distribution via
compositional predictors, 114	Newton-Rapshon, 126
Log-likelihood ratio test for a	MLE of the folded model for a given
Dirichlet mean vector, 116	<u> </u>
Log-likelihood ratio test for a	value of alpha, 127 MLE of the zero adjusted Dirichlet
symmetric Dirichlet	
distribution, 117	distribution, 129
logitnorm.est (MLE of distributions	<pre>mlr(The multiplicative log-ratio transformation and its</pre>
defined in the (0, 1)	
interval), 123	<pre>inverse), 213 mlrinv (The multiplicative log-ratio</pre>
logpca, 156	transformation and its
Tughca, 100	transionmation and its

inverse), 213	pcr.tune, 233, 235
multinompcr.tune (Tuning the principal	pcr.tune(Tuning the principal
components with GLMs), 234	components with GLMs), 234
Multivariate kernel density	Permutation linear independence test
estimation, 130	in the SCLS model, 146
Multivariate kernel density estimation	Permutation linear independence test
for compositional data, 131	in the TFLR model, 147
Multivariate linear regression, 132	Permutation test for the matrix of
Multivariate normal random values	coefficients in the SCLS
simulation on the simplex, 133	model, 148
Multivariate or univariate regression	Permutation test for the matrix of
with compositional data in the	coefficients in the TFLR
covariates side using the	model, 149
alpha-transformation, 135	perturbation, <i>145</i> , <i>153</i>
Multivariate regression with	
compositional data, 136	perturbation (Perturbation operation),
Multivariate skew normal random values	150
simulation on the simplex, 138	Perturbation operation, 150
Multivariate t random values	pivot, 192, 203, 213
simulation on the simplex, 139	pivot (The pivot coordinate
multivreg, 137, 185	transformation and its
multivreg (Multivariate linear	inverse), 214
regression), 132	pivotinv(The pivot coordinate
multivt, 76	transformation and its
multivt(MLE for the multivariate t	inverse), 214
distribution), 122	Plot of the LASSO coefficients, 151
d15t1 1but1011), 122	pow(Power operation), 153
Naive Bayes classifiers for	power, <i>151</i>
compositional data, 140	Power operation, 153
Naive Bayes classifiers for	pprcomp, 94, 95, 163, 230
compositional data using the	pprcomp (Projection pursuit regression
alpha-transformation, 142	with compositional predictor
Non linear least squares regression	variables), 161
for compositional data, 143	pprcomp.tune, 95, 162, 231
Non-parametric zero replacement	pprcomp.tune (Tuning of the projection
strategies, 144	pursuit regression with
	compositional predictor
ols.compreg, 67, 70, 91, 103, 133, 167, 171,	variables), 229
249	Principal component analysis, 154
ols.compreg(Non linear least squares	Principal component analysis using the
regression for compositional	alpha-transformation, 155
data), 143	Principal component generalised linear
ols.prop.reg(Distance based	models, 156
regression models for	Principal coordinate analysis using
proportions), 67	
optim, 215, 216	the alpha-distance, 157
optimize, 170	Principal coordinate analysis using the Jensen-Shannon divergence,
nee (Proportionality correlation	159
pcc (Proportionality correlation	
coefficient matrix), 165	<pre>probout (Estimation of the probability</pre>

left outside the simplex when	rdiri(Dirichlet random values
using the	simulation), 64
alpha-transformation),77	Read a file as a Filebacked Big
profile, 90, 208, 233	Matrix, 168
Projection pursuit regression for	read.fbm(Read a file as a Filebacked
compositional data, 160	Big Matrix), 168
Projection pursuit regression with	Regression with compositional data
compositional predictor	using the
variables, 161	alpha-transformation, 169
Projection pursuit regression with	Regularised and flexible discriminant
compositional predictor	analysis for compositional
variables using the	data using the
alpha-transformation, 162	alpha-transformation, 171
Projections based test for	rfd, 58
distributional equality of two	rfd(Simulation of compositional data
groups, 164	from the Flexible Dirichlet
Proportionality correlation	distribution), 181
coefficient matrix, 165	rfolded, 60, 77
propreg, 14, 68, 248	rfolded(Simulation of compositional
propreg (Quasi binomial regression for	data from the folded normal
proportions), 166	distribution), 183
propregs (Quasi binomial regression	rgendiri, <i>62</i> , <i>65</i>
for proportions), 166	rgendiri (Generalised Dirichlet random
	values simulation), 86
Quasi binomial regression for	Ridge regression, 173
proportions, 166	Ridge regression plot, 174
	Ridge regression with compositional
Random values generation from some	data in the covariates side
univariate distributions	using the
defined on the $(0,1)$ interval,	alpha-transformation, 175
167	Ridge regression with the
rbeta1 (Random values generation from	alpha-transformation plot, 177
some univariate distributions	ridge.plot, 174, 178
defined on the $(0,1)$	ridge.plot (Ridge regression plot), 174
interval), 167	ridge.reg, 39, 175, 176
rcompnorm, 139, 140	ridge.reg (Ridge regression), 173
rcompnorm (Multivariate normal random	ridge.tune, 41, 174, 175
values simulation on the	ridge.tune (Cross validation for the
simplex), 133	ridge regression), 38
rcompsn, 134	rlogitnorm(Random values generation
rcompsn (Multivariate skew normal	from some univariate
random values simulation on	distributions defined on the
the simplex), 138	(0,1) interval), 167
rcompt, 134	rmixcomp, 83, 85, 120, 122, 181
rcompt (Multivariate t random values	rmixcomp (Simulation of compositional
simulation on the simplex), 139	data from Gaussian mixture
rdiri, 61, 62, 86, 117–119, 126, 127, 134,	models), 179
139, 140, 168	rmixdiri, 63

runitweibull (Random values generation from some univariate distributions defined on the (0,1) interval), 167 scls, 55, 146, 148–150, 169, 179, 189–191, 201, 220 scls (The SCLS model), 215 scls. betest, 146 scls. betest (Permutation test for the matrix of coefficients in the SCLS model), 148 scls. indeptest, 149, 150, 216–218 scls. indeptest, 149, 150, 216–218 scls.2 (146, 149 scls.2 (146, 149 scls.2 (146, 149 scls.2 (17he SCLS model with multiple compositional predictors), 216 scrq, 56, 216 scrq, 56, 216 scrq (Simplicial constrained median regression for compositional responses and predictors model), 178 Simplicial constrained median regression for compositional responses and predictors model, 178 Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet distributions, 180 sym.test, 117 sym.test, 117 sym.test (Log-likelihood ratio test for a symmetric Dirichlet distribution), 117 sym.test, 117 sym.test, (Log-likelihood ratio test for a symmetric Dirichlet distribution), 117 sym.test, 117 sym.test, (Log-likelihood ratio test for a symmetric Dirichlet distribution), 117 sym.test, 117 sym.test, (Log-likelihood ratio test for a symmetric Dirichlet distribution), 117 symkl.compreg (Divergence based regression for compositional data), 69 ternary, 187, 189–191 ternary diagram, 185 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the simplicial-simplicial regression models, 190 ternary.coef (Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models, 190 ternary.coef (Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models, 190 ternary.coef (Ternary diagram with confidence region for the matrix of coefficients of the simplicial-regression models, 186 Ternary diagram with confidence region for the mean, 189 Ternary diagram of regression for compositi	rmixdiri(Simulation of compositional	<pre>spatmed.reg(Spatial median</pre>
runitweibull (Random values generation from some univariate distributions defined on the (0,1) interval), 167 scl., 169, 148, 150, 169, 179, 189–191, 201, 220 scls (The SCLS model), 215 scls.betest, 146 scls.betest, 146 scls.model), 148 scls.indeptest, 149, 150, 216–218 scls.indeptest (Permutation linear independence test in the SCLS model), 146 scls2, 146, 149 scls2 (The SCLS model with multiple compositional predictors), 216 scrq, 56, 216 scrq (Simplicial constrained median regression for compositional responses and predictors model), 178 Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet distribution), 117 symkl.compreg (Divergence based regression for compositional data), 69 ternary, 187, 189–191 ternary diagram, 185 Ternary diagram of regression models, 186 Ternary diagram with confidence region for the mean, 189 Ternary diagram with the coefficients of the simplicial-simplicial regression models, 190 ternary.coef (Ternary diagram with confidence region for the simplicial-simplicial regression models), 190 ternary.coef (Ternary diagram with confidence region for the simplicial-simplicial regression models), 190 ternary.coef (Ternary diagram with coefficients of the simplicial-simplicial regression models), 190 ternary.coef (Ternary diagram with coefficients of the simplicial-simplicial regression models), 190 ternary.coef (Ternary diagram with coefficients of the simplicial-simplicial regression models), 190 ternary.coef (Ternary diagram with coefficients of the simplicial-simplicial regression models, 190 ternary.coef (Ternary diagram with coefficients of the simplicial-simplicial regression models, 188 ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the simplicial-simplicial regression models, 190 ternary.coef (Ternary diagram with coefficients of the simplicial-simplicial regression models, 190 ternary.coef (Ternary diagram with coefficients of the	data from mixtures of	regression), 184
from some univariate distributions defined on the (0,1) interval), 167 symkl.compreg (Divergence based regression for compositional data), 69 scls, 55, 146, 148–150, 169, 179, 189–191, 201, 220 scls (The SCLS model), 215 scls.betest, 146 scls.betest (Permutation test for the matrix of coefficients in the SCLS model), 148 scls.indeptest, 149, 150, 216–218 scls.indeptest, 149, 150, 216–218 scls.indeptest (Permutation linear independence test in the SCLS model), 146 scls2, 146, 149 scls2 (The SCLS model with multiple compositional predictors), 216 scrq, 56, 216 scrq (Simplicial constrained median regression for compositional responses and predictors model), 178 Simplicial constrained median regression for compositional responses and predictors model, 178 Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet distributions, 180 for a symmetric Dirichlet distribution,, 117 symkl.compreg (Divergence based regression for compositional data), 69 ternary, 187, 189–191 ternary (Ternary diagram), 185 Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models, 190 ternary.coef(Ternary diagram with the coefficients of the simplicial-simplicial regression models, 190 ternary.coef(Ternary diagram with the coefficients of the simplicial-simplicial regression models, 190 ternary.coef(Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models, 190 ternary.coef(Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models, 190 ternary.coef(Ternary diagram with confidence region for the matrix of coefficients of the simplicial-regression models, 190 ternary.coef(Ternary diagram with confidence region for the matrix of coefficients of the simplicial-regression models, 188 Ternary diagram with confidence region for the matrix of coefficients of the simplicial-regression models, 188 Tern	Dirichlet distributions), 180	sym.test, <i>117</i>
distributions defined on the (0,1) interval), 167 symkl.compreg (Divergence based regression for compositional data), 69 201, 220 scls (The SCLS model), 215 scls.betest, 146 scls.betest (Permutation test for the matrix of coefficients in the SCLS model), 148 scls.indeptest, 149, 150, 216–218 scls.indeptest (Permutation linear independence test in the SCLS model), 146 scls2, 146, 149 scls2 (The SCLS model with multiple compositional predictors), 216 scrq, 56, 216 scrq (Simplicial constrained median regression for compositional responses and predictors model), 178 Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet distributions, 180 distribution), 117 symkl.compreg (Divergence based regression for compositional data), 69 ternary, 187, 189–191 ternary, (Ternary diagram, 185 Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models, 190 ternary, coeff (Ternary diagram with the coefficients of the simplicial-simplicial regression models), 190 ternary.coeff (Ternary diagram with the coefficients of the simplicial-simplicial regression models), 190 ternary.coeff (Ternary diagram with confidence region for the matrix of coefficients of the SCLS or the TFLR model), 188 ternary diagram with confidence region for the simplicial-simplicial regression models, 190 ternary.coeff (Ternary diagram with the coefficients of the SCLS or the TFLR model), 188 ternary mcr, 186, 187, 189 ternary mcr, 186, 187,	runitweibull(Random values generation	<pre>sym.test(Log-likelihood ratio test</pre>
symkl.compreg (Divergence based regression for compositional data), 69 scls, 55, 146, 148–150, 169, 179, 189–191, 201, 220 scls (The SCLS model), 215 scls.betest, 146 scls.betest, Permutation test for the matrix of coefficients in the SCLS model), 148 scls.indeptest, 149, 150, 216–218 scls.indeptest (Permutation linear independence test in the SCLS model), 146 scls2, 146, 149 scls2 (The SCLS model with multiple compositional predictors), 216 scrq, 56, 216 scrq (Simplicial constrained median regression for compositional responses and predictors model), 178 Simplicial constrained median regression for compositional responses and predictors model, 178 Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet distributions, 180 symkl.compreg (Divergence based regression for compositional data), 69 ternary, 187, 189–191 ternary (Ternary diagram), 185 Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models, 190 ternary.coef(Ternary diagram with the coefficients of the simplicial-simplicial regression models), 190 ternary.coef(Ternary diagram with the coefficients of the simplicial-simplicial regression models), 190 ternary.coef(Ternary diagram with the coefficients of the simplicial-simplicial regression models), 190 ternary.coef(Ternary diagram with the coefficients of the simplicial-simplicial regression models), 190 ternary.coef(Ternary diagram with the coefficients of the simplicial-simplicial regression models, 188 ternary.mcr, 186, 187, 189 ternary.l87, 189–191 ternary (diagram, 185 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 ternary.coef(Ternary diagram with the coefficients of the simplicial regression models, 188 Ternary diagram with confidence region for the mean, 189 ternary.l86, 187, 189 ternary.l87, 189–191 ternary.l87, 189–191 ternary diagram with confidence region for the mean, 189 ternary.coef(Te	from some univariate	for a symmetric Dirichlet
regression for compositional data), 69 scls, 55, 146, 148–150, 169, 179, 189–191, 201, 220 scls (The SCLS model), 215 scls.betest, 146 scls.betest (Permutation test for the matrix of coefficients in the SCLS model), 148 scls.indeptest, 149, 150, 216–218 scls.indeptest, 149, 150, 216–218 scls.indeptest (Permutation linear independence test in the SCLS model), 146 scls2, 146, 149 scls2 (The SCLS model with multiple compositional predictors), 216 scrq, 56, 216 scrq (Simplicial constrained median regression for compositional responses and predictors model), 178 Simplicial constrained median regression for compositional aresponses and predictors model, 178 Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet distributions, 180 regression for compositional data, 69 ternary, 187, 189–191 ternary diagram, 185 Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models, 190 ternary. Coef (Ternary diagram with the coefficients of the simplicial-simplicial regression models), 190 ternary, 187, 189–191 ternary (Ternary diagram, 185 Ternary diagram, 185 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the simplicial-simplicial regression models, 190 ternary. Coef (Ternary diagram with the coefficients of the simplicial-simplicial regression models), 190 ternary. Coef (Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models), 190 ternary. 187, 189–191 ternary (Ternary diagram, 185 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with the coefficients of the simplicial-regression models, 188 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagra	distributions defined on the	distribution), 117
regression for compositional data), 69 scls, 55, 146, 148–150, 169, 179, 189–191, 201, 220 scls (The SCLS model), 215 scls.betest, 146 scls.betest (Permutation test for the matrix of coefficients in the SCLS model), 148 scls.indeptest, 149, 150, 216–218 scls.indeptest (Permutation linear independence test in the SCLS model), 146 scls2, 146, 149 scls2 (The SCLS model with multiple compositional predictors), 216 scrq, 56, 216 scrq (Simplicial constrained median regression for compositional responses and predictors model), 178 Simplicial constrained median regression for compositional responses and predictors model, 178 Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet distributions, 180 regression for compositional data, 69 ternary, 187, 189–191 ternary diagram, 185 Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models, 190 ternary. Coef (Ternary diagram with the coefficients of the simplicial-simplicial regression models), 190 ternary, 187, 189–191 ternary (Ternary diagram, 185 Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models), 190 ternary. Coef (Ternary diagram with the coefficients of the simplicial-simplicial regression models), 190 ternary, 187, 189–191 ternary, 187, 189–191 ternary diagram, 185 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 ternary. Coef (Ternary diagram with the coefficients of the simplicial regression models), 190 ternary, 187, 189–191 ternary, 187, 189–191 ternary diagram, 185 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with con	(0,1) interval), 167	symkl.compreg (Divergence based
201, 220 scls (The SCLS model), 215 scls.betest, 146 scls.betest, 146 scls.betest (Permutation test for the matrix of coefficients in the SCLS model), 148 scls.indeptest, 149, 150, 216–218 scls.indeptest (Permutation linear independence test in the SCLS model), 146 scls2, 146, 149 scls2 (The SCLS model with multiple compositional predictors), 216 scrq, 56, 216 scrq (Simplicial constrained median regression for compositional responses and predictors model), 178 Simplicial constrained median regression for compositional responses and predictors model, 178 Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet distributions, 180 ternary, 187, 189–191 ternary diagram, 185 Ternary diagram with confidence region for the matrix of coefficients of the SCLS or the TFLR model, 188 Ternary diagram with confidence region for the mean, 189 Ternary diagram with the coefficients of the simplicial-simplicial regression models, 190 ternary.coef (Ternary diagram with the coefficients of the simplicial-simplicial regression models), 190 ternary.coef (Ternary diagram with the coefficients of the simplicial-simplicial regression models), 190 ternary.coef (Ternary diagram with the coefficients of the simplicial-simplicial regression models), 190 ternary.coef (Ternary diagram with the coefficients of the simplicial-simplicial regression models), 190 ternary.coef (Ternary diagram with the coefficients of the simplicial-simplicial regression models, 190 ternary.regrical regression models, 186 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with co		regression for compositional
scls (The SCLS model), 215 scls.betest, 146 scls.betest, 146 scls.betest (Permutation test for the matrix of coefficients in the SCLS model), 148 scls.indeptest, 149, 150, 216–218 scls.indeptest (Permutation linear independence test in the SCLS model), 146 scls.2 (The SCLS model with multiple compositional predictors), 216 scrq. 56, 216 scrq. (Simplicial constrained median regression for compositional responses and predictors model), 178 Simplicial constrained median regression for compositional responses and predictors model, 178 Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet distributions, 180 ternary, 187, 189–191 ternary, (Ternary diagram), 185 Ternary diagram of regression models, 186 Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models, 190 ternary.coefc (Ternary diagram with confidence region for the matrix of coefficients of the scls or the TFLR model), 188 ternary.reg, 186, 187, 189 ternary.mcr (Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models), 190 ternary.coefc (Ternary diagram with the coefficients of the scls or the TFLR model), 188 ternary.reg, 186, 187, 189 ternary.reg, 186, 190, 191	scls 55 1/6 1/8 150 160 170 180 101	data), 69
scls (The SCLS model), 215 scls.betest, 146 scls.betest (Permutation test for the matrix of coefficients in the SCLS model), 148 scls.indeptest, 149, 150, 216–218 scls.indeptest (Permutation linear independence test in the SCLS model), 146 scls2, 146, 149 scls2 (The SCLS model with multiple compositional predictors), 216 scrq, 56, 216 scrq (Simplicial constrained median regression for compositional responses and predictors model), 178 Simplicial constrained median regression for compositional responses and predictors model, 178 Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet distributions, 180 ternary (Ternary diagram), 185 Ternary diagram with confidence region for the matrix of coefficients of the SCLS or the TFLR model, 188 Ternary diagram with confidence region for the matrix of the simplicial-simplicial regression models, 190 ternary coeff (Ternary diagram with the coefficients of the simplicial-simplicial regression models), 190 ternary coeff (Ternary diagram with the coefficients of the simplicial-simplicial regression models), 190 ternary. 186, 187, 189–191		
scls.betest, 146 scls.betest (Permutation test for the matrix of coefficients in the SCLS model), 148 scls.indeptest, 149, 150, 216–218 scls.indeptest (Permutation linear independence test in the SCLS model), 146 scls2, 146, 149 scls2 (The SCLS model with multiple compositional predictors), 216 scrq, 56, 216 scrq (Simplicial constrained median regression for compositional responses and predictors model), 178 Simplicial constrained median regression for compositional responses and predictors model, 178 Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet distributions, 180 ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the meatrix of coefficients of the simplicial-simplicial regression models, 190 ternary.coef(Ternary diagram with the coefficients of the simplicial-simplicial regression models), 190 ternary.coefcr (Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models, 188 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region fo		
scls.betest (Permutation test for the matrix of coefficients in the SCLS model), 148 scls.indeptest, 149, 150, 216–218 scls.indeptest (Permutation linear independence test in the SCLS model), 146 scls2, 146, 149 scls2 (The SCLS model with multiple compositional predictors), 216 scrq, 56, 216 scrq (Simplicial constrained median regression for compositional responses and predictors model), 178 Simplicial constrained median regression for compositional responses and predictors model, 178 Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet distributions, 180 Ternary diagram with confidence region for the matrix of coefficients of the SCLS or the TFLR model, 188 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the simplicial-simplicial regression models, 190 ternary.coef(Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models), 190 ternary diagram with confidence region for the simplicial-simplicial regression models, 190 ternary.coef(Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models, 190 ternary.coef(Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models, 190 ternary.coef(Ternary diagram with the coefficients of the simplicial-simplicial regression models), 190 ternary.coef(Ternary diagram with confidence region for the matrix of coefficients of the simplicial-regression for the matrix of coefficients of the scls 200 ternary.coef(Ternary diagram with the coefficients of the simplicial-regression models, 190 ternary.coef(Ternary diagram with the coefficients of the simplicial-regression models, 190 ternary.coef(Ternary diagram with confidence region for the matrix of coefficients of the simplicial-regression models, 190 ternary.coef(Ternary diagram, 185		ternary (Ternary diagram), 185
matrix of coefficients in the SCLS model), 148 scls.indeptest, 149, 150, 216–218 scls.indeptest (Permutation linear independence test in the SCLS model), 146 scls2, 146, 149 scls2 (The SCLS model with multiple compositional predictors), 216 scrq, 56, 216 scrq (Simplicial constrained median regression for compositional responses and predictors model), 178 Simplicial constrained median regression for compositional responses and predictors model, 178 Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet distributions, 180 matrix of coefficients of the simplicial regression models, 190 ternary.coef (Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models, 190 ternary.coef (Ternary diagram with confidence region for the matrix of coefficients of the simplicial-regression models, 190 ternary.coef (Ternary diagram with confidence region for the matrix of coefficients of the simplicial-regression models, 190 ternary.coef (Ternary diagram with confidence region for the matrix of coefficients of the scls or the TFLR model, 188 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternary diagram with confidence region for the mean, 189 Ternar	•	Ternary diagram, 185
SCLS model), 148 scls.indeptest, 149, 150, 216–218 scls.indeptest (Permutation linear independence test in the SCLS model), 146 scls2, 146, 149 scls2 (The SCLS model with multiple compositional predictors), 216 scrq, 56, 216 scrq (Simplicial constrained median regression for compositional responses and predictors model), 178 Simplicial constrained median regression for compositional responses and predictors model, 178 Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet distributions, 180 Ternary diagram with confidence region for the matrix of coefficients of the sumplicial-simplicial regression models, 190 ternary.coef (Ternary diagram with confidence region for the simplicial-simplicial regression models), 190 ternary.coef (Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models, 190 ternary.coef (Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models, 190 ternary.coef (Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models), 190 ternary.coef (Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models, 190 ternary.coef (Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models, 190 ternary.coef (Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models, 190 ternary.coef (Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models, 190 ternary.coef (Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models, 190 ternary.coef (Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models, 190 ternary.coef (Ternary d		Ternary diagram of regression models,
scls.indeptest, 149, 150, 216–218 scls.indeptest (Permutation linear independence test in the SCLS model), 146 scls2, 146, 149 scls2 (The SCLS model with multiple compositional predictors), 216 scrq, 56, 216 scrq (Simplicial constrained median regression for compositional responses and predictors model), 178 Simplicial constrained median regression for compositional responses and predictors model, 178 Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet distributions, 180 scls. indeptest, 149, 150, 216–218 for the matrix of coefficients of the SCLS or the TFLR model, 188 Ternary diagram with confidence region for the simplicial-simplicial regression models, 190 ternary.coef (Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models), 190 ternary.coef (Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models), 190 ternary.coef (Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models), 190 ternary.coef (Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models), 190 ternary.coef (Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models), 190 ternary.coef (Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models), 190 ternary.coef (Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models), 190 ternary.coef (Ternary diagram with the coefficients of the simplicial-simplicial regression models), 190 ternary.coef (Ternary diagram with confidence region for the matrix of coefficients of the simplicial-simplicial regression models), 190 ternary.coef (Ternary diagram with confidence region for the matrix of coefficients of the simplici		186
scls.indeptest (Permutation linear independence test in the SCLS model), 146 scls2, 146, 149 scls2 (The SCLS model with multiple compositional predictors), 216 scrq, 56, 216 scrq (Simplicial constrained median regression for compositional responses and predictors model), 178 Simplicial constrained median regression for compositional responses and predictors model, 178 Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet distributions, 180 scls2 (The SCLS or the TFLR model, 188 Ternary diagram with the coefficients of the simplicial-simplicial regression models, 190 ternary.coef (Ternary diagram with confidence region for the simplicial-simplicial regression models), 190 ternary.coefcr (Ternary diagram with confidence region for the mative of coefficients of the simplicial-simplicial regression models), 190 ternary.coef (Ternary diagram with confidence region for the simplicial-simplicial regression models), 190 ternary.coef(Ternary diagram with confidence region for the simplicial-simplicial regression models), 190 ternary.coef(Ternary diagram with confidence region for the simplicial-simplicial regression models), 190 ternary.coef(Ternary diagram with the coefficients of the simplicial-simplicial regression models), 190 ternary.coef(Ternary diagram with confidence region for the mative of coefficients of the simplicial-simplicial regression models, 190 ternary.coef(Ternary diagram with confidence region for the mative of the SCLS or the TFLR model, 188		Ternary diagram with confidence region
independence test in the SCLS model), 146 scls2, 146, 149 scls2 (The SCLS model with multiple compositional predictors), 216 scrq, 56, 216 scrq (Simplicial constrained median regression for compositional responses and predictors model), 178 Simplicial constrained median regression for compositional responses and predictors model, 178 Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet distributions, 180 Ternary diagram with confidence region for the simplicial-simplicial regression models, 190 ternary.coef (Ternary diagram with confidence region for the matrix of coefficients of the SCLS or the TFLR model), 188 Ternary diagram with confidence region for the simplicial regression models, 190 ternary.coefc (Ternary diagram with confidence region for the matrix of coefficients of the SCLS or the TFLR model), 188 ternary.mcr, 186, 187, 189 ternary.mcr, 186, 187, 189 ternary.mcr (Ternary diagram with confidence region for the mean), 189 ternary.reg, 186, 190, 191		for the matrix of coefficients
model), 146 scls2, 146, 149 scls2 (The SCLS model with multiple compositional predictors), 216 scrq, 56, 216 scrq (Simplicial constrained median responses and predictors model), 178 Simplicial constrained median regression for compositional responses and predictors model, 178 Simplicial constrained median regression for compositional responses and predictors model, 178 Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet distributions, 180 Ternary diagram with confidence region for the simplicial-simplicial regression models, 190 ternary.coef (Ternary diagram with confidence region for the matrix of coefficients of the SCLS or the TFLR model), 188 ternary.mcr, 186, 187, 189 ternary.mcr, 186, 187, 189 ternary.reg, 186, 190, 191	• •	of the SCLS or the TFLR model,
scls2, 146, 149 scls2 (The SCLS model with multiple compositional predictors), 216 scrq, 56, 216 scrq (Simplicial constrained median regression for compositional responses and predictors model), 178 Simplicial constrained median regression for compositional responses and predictors model, 178 Simplicial constrained median regression for compositional responses and predictors model, 178 Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet distributions, 180 Ternary diagram with the coefficients of the simplicial-simplicial regression models, 190 ternary.coef (Ternary diagram with confidence region for the matrix of coefficients of the SCLS or the TFLR model), 188 ternary.mcr, 186, 187, 189 ternary.rcr, 186, 187, 189 ternary.rcr, 186, 187, 189 ternary.reg, 186, 190, 191	·	188
scls2 (The SCLS model with multiple compositional predictors), 216 scrq, 56, 216 scrq (Simplicial constrained median regression for compositional model), 178 Simplicial constrained median regression for compositional regression models), 190 Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet mixtures of Dirichlet distributions, 180 Ternary diagram with the coefficients of the simplicial-simplicial regression models, 190 ternary.coef (Ternary diagram with the coefficients of the simplicial-simplicial regression models), 190 ternary.coefcr (Ternary diagram with confidence region for the matrix of coefficients of the simplicial-regression models), 190 ternary.coefcr (Ternary diagram with confidence region for the matrix of coefficients of the simplicial-regression models, 190 ternary.coefcr (Ternary diagram with confidence region for the matrix of coefficients of the simplicial regression models, 190 ternary.coefcr (Ternary diagram with confidence region for the matrix of coefficients of the simplicial regression models, 190 ternary.coefcr (Ternary diagram with confidence region for the matrix of coefficients of the simplicial regression models, 190 ternary.coefcr (Ternary diagram with confidence region for the matrix of coefficients of the simplicial regression models, 190 ternary.coef (Ternary diagram with the coefficients of the simplicial regression models, 190 ternary.coefcr (Ternary diagram with confidence region for the matrix of coefficients of the simplicial regression models, 190 ternary.coefcr (Ternary diagram with confidence region for the matrix of coefficients of the simplicial regression models, 190 ternary.coefcr (Ternary diagram with confidence region for the matrix of coefficients of the simplicial regression models, 190 ternary.coefcr (Te		Ternary diagram with confidence region
of the simplicial-simplicial regression models, 190 scrq (Simplicial constrained median regression for compositional model), 178 Simplicial constrained median regression for compositional responses and predictors model, 178 Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet mixtures of Dirichlet distributions, 180 of the simplicial-simplicial regression models, 190 ternary.coef(Ternary diagram with confidence region for the matrix of coefficients of the SCLS or the TFLR model), 188 ternary.mcr, 186, 187, 189 ternary.mcr (Ternary diagram with confidence region for the mean), 189 ternary.reg, 186, 190, 191		for the mean, 189
scrq, 56, 216 scrq (Simplicial constrained median regression for compositional model), 178 Simplicial constrained median regression for compositional regression for compositional regression for compositional responses and predictors model, 178 Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet mixtures of Dirichlet distributions, 180 Somution of the simplicial regression models, 190 ternary.coef (Ternary diagram with confidence region for the matrix of coefficients of the SCLS or the TFLR model), 188 ternary.mcr (Ternary diagram with confidence region for the mean), 189 ternary.reg, 186, 190, 191		Ternary diagram with the coefficients
scrq (Simplicial constrained median regression for compositional model), 178 Simplicial constrained median regression for compositional regression models), 190 Simplicial constrained median regression for compositional regression models), 190 Simplicial constrained median regression for compositional regression models), 190 Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet mixtures of Dirichlet mixtures of Dirichlet mean), 189 distributions, 180 ternary.coef (Ternary diagram with the simplicial regression models), 190 ternary.coefcr (Ternary diagram with confidence region for the mean), 189 ternary.coef (Ternary diagram with the coefficients of the simplicial regression models), 190 ternary.coefcr (Ternary diagram with confidence region for the mean), 189 ternary.coef (Ternary diagram with the coefficients of the solutions), 190		of the simplicial-simplicial
regression for compositional responses and predictors model), 178 Simplicial constrained median regression for compositional regression for compositional regression for compositional regression for compositional regression models), 190 ternary.coefcr(Ternary diagram with confidence region for the matrix of coefficients of the SCLS or the TFLR model), 188 ternary.mcr, 186, 187, 189 ternary.mcr (Ternary diagram with confidence region for the matrix of coefficients of the scls or the TFLR model), 188 ternary.mcr (Ternary diagram with confidence region for the mean), 189 ternary.reg, 186, 190, 191	•	regression models, 190
responses and predictors model), 178 Simplicial constrained median regression for compositional responses and predictors model, 178 Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet distributions, 180 simplicial-simplicial regression models), 190 ternary.coefcr (Ternary diagram with confidence region for the matrix of coefficients of the SCLS or the TFLR model), 188 ternary.mcr, 186, 187, 189 ternary.mcr (Ternary diagram with confidence region for the mean), 189 ternary.reg, 186, 190, 191		ternary.coef (Ternary diagram with the
model), 178 Simplicial constrained median regression models), 190 ternary.coefcr(Ternary diagram with confidence region for the matrix of coefficients of the SCLS or the TFLR model), 188 Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet mixtures of Dirichlet distributions, 180 Simplicial simplicial regression models), 190 ternary.coefcr(Ternary diagram with confidence region for the mean), 189 ternary.reg, 186, 190, 191		coefficients of the
model), 178 Simplicial constrained median regression for compositional responses and predictors model, 178 Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet distributions, 180 regression models), 190 ternary.coefcr (Ternary diagram with confidence region for the matrix of coefficients of the SCLS or the TFLR model), 188 ternary.mcr, 186, 187, 189 ternary.mcr (Ternary diagram with confidence region for the mean), 189 ternary.reg, 186, 190, 191		simplicial-simplicial
Simplicial constrained median regression for compositional responses and predictors model, 178 Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet distributions, 180 ternary.coefcr (Ternary diagram with confidence region for the matrix of coefficients of the SCLS or the TFLR model), 188 ternary.mcr, 186, 187, 189 ternary.mcr (Ternary diagram with confidence region for the mean), 189 ternary.reg, 186, 190, 191		regression models), 190
regression for compositional confidence region for the matrix of coefficients of the model, 178 Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet mixtures of Dirichlet distributions, 180 confidence region for the matrix of coefficients of the matrix of coefficients of the matrix of coefficients of the scale in the matrix of coefficients of the scale in the matrix of coefficients of the matrix of coefficients of the matrix of coefficients of the scale in the matrix of coefficients of the matrix of coefficients of the matrix of coefficients of the scale in the matrix of coefficients of the matrix of coefficients of the scale in the matrix of coefficients of the matrix of coefficients of the scale in the matrix of coefficients of		ternary.coefcr(Ternary diagram with
model, 178 Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet mean), 189 distributions, 180 SCLS or the TFLR model), 188 ternary.mcr, 186, 187, 189 ternary.mcr (Ternary diagram with confidence region for the mean), 189 ternary.reg, 186, 190, 191		confidence region for the
Simulation of compositional data from Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet distributions, 180 Simulation of compositional data from mixtures of Dirichlet distributions, 180 Ternary.mcr, 186, 187, 189 ternary.mcr (Ternary diagram with confidence region for the mean), 189 ternary.reg, 186, 190, 191		matrix of coefficients of the
Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet mean), 189 distributions, 180 ternary.mcr (Ternary diagram with confidence region for the mean), 189 ternary.reg, 186, 190, 191	model, 178	SCLS or the TFLR model), 188
Gaussian mixture models, 179 Simulation of compositional data from mixtures of Dirichlet mean), 189 distributions, 180 ternary.mcr (Ternary diagram with confidence region for the mean), 189 ternary.reg, 186, 190, 191	Simulation of compositional data from	ternary.mcr, 186, 187, 189
Simulation of compositional data from confidence region for the mixtures of Dirichlet mean), 189 distributions, 180 ternary.reg, 186, 190, 191	Gaussian mixture models, 179	
mixtures of Dirichlet mean), 189 distributions, 180 ternary.reg, 186, 190, 191	Simulation of compositional data from	
distributions, 180 ternary.reg, 186, 190, 191	mixtures of Dirichlet	
	distributions, 180	
	Simulation of compositional data from	
the Flexible Dirichlet regression models), 186	the Flexible Dirichlet	
distribution, 181 tflr, 43, 72, 146–150, 179, 189, 190, 202,	distribution, 181	
Simulation of compositional data from 216–218	Simulation of compositional data from	
the folded normal tflr(The transformation-free linear	the folded normal	tflr (The transformation-free linear
distribution, 183 regression (TFLR) for	distribution, 183	
skewnorm.contour, 18, 19, 26, 29 compositional responses and	skewnorm.contour, 18, 19, 26, 29	
skewnorm.contour (Contour plot of the predictors), 219		
skew skew-normal distribution tflr.betest, 148		
in S^2), 27 tflr.betest (Permutation test for the		•
Spatial median regression, 184 matrix of coefficients in the		
spatmed.reg, 76, 137 TFLR model), 149		

tflr.indeptest, <i>149</i> , <i>150</i>	Total variability, 220
tflr.indeptest (Permutation linear	totvar (Total variability), 220
independence test in the TFLR	Tuning of the alpha-generalised
model), 147	correlations between two
tflr2(The TFLR model with multiple	compositional datasets, 221
compositional predictors), 217	Tuning of the bandwidth h of the
The additive log-ratio transformation	kernel using the maximum
and its inverse, 191	likelihood cross validation,
The alpha-distance, 192	222
The alpha-IT transformation, 193	Tuning of the divergence based
The alpha-IT-distance, 195	regression for compositional
The alpha-k-NN regression for	data with compositional data
compositional response data,	in the covariates side using
196	the alpha-transformation, 224
The alpha-k-NN regression with	Tuning of the k-NN algorithm for
compositional predictor	compositional data, 225
variables, 197	Tuning of the projection pursuit
The alpha-kernel regression with	regression for compositional
compositional response data,	data, 228
199	Tuning of the projection pursuit
The alpha-SCLS model, 200	regression with compositional
The alpha-TFLR model, 201	predictor variables, 229
The alpha-transformation, 202	Tuning of the projection pursuit
The Box-Cox transformation applied to	regression with compositional
ratios of components, 204	predictor variables using the
The ESOV-distance, 205	alpha-transformation, 230
The folded power transformation, 206	Tuning the number of PCs in the PCR
The Frechet mean for compositional	with compositional data using
data, 207	the alpha-transformation, 232
The Helmert sub-matrix, 208	Tuning the principal components with
The k-nearest neighbours using the	GLMs, 234
alpha-distance, 209	Tuning the value of alpha in the
The k-NN algorithm for compositional	alpha-regression, 235
data, 211	tv.compreg (Divergence based
The multiplicative log-ratio	regression for compositional
transformation and its	data), 69
inverse, 213	Two-sample test of high-dimensional
The pivot coordinate transformation	means for compositional data, 237
and its inverse, 214	231
The SCLS model, 215	ulc.glm, 12, 107-109, 244
The SCLS model with multiple	ulc.glm(Unconstrained GLMs with
compositional predictors, 216	compositional predictor
The TFLR model with multiple	variables), 238
compositional predictors, 217	ulc.glm2, 108, 109, 239, 245
The transformation-free linear	ulc.glm2(Unconstrained logistic or
regression (TFLR) for	Poisson regression with
compositional responses and	multiple compositional
predictors, 219	predictors), 242

ulc.reg, 13, 113-115, 242
ulc.reg(Unconstrained linear
regression with compositional
predictor variables), 239
ulc.reg2, <i>115</i> , <i>240</i>
ulc.reg2(Unconstrained linear
regression with multiple
compositional predictors), 241
ulc.rq, 110-112, 246
ulc.rq(Unconstrained quantile
regression with compositional
predictor variables), 244
ulc.rq2, 112
ulc.rq2(Unconstrained quantile
regression with multiple
compositional predictors), 245
Unconstrained GLMs with compositional
predictor variables, 238
Unconstrained linear regression with
compositional predictor
variables, 239
Unconstrained linear regression with
multiple compositional
predictors, 241
Unconstrained logistic or Poisson
regression with multiple
compositional predictors, 242
Unconstrained quantile regression with
compositional predictor
variables, 244
Unconstrained quantile regression with
multiple compositional
predictors, 245
Unit-Weibull regression models for
proportions, 247
unitweib.reg (Unit-Weibull regression
models for proportions), 247
unitweibull.est (MLE of distributions
defined in the $(0, 1)$
interval), 123
111001 (41), 120
zad.est, 249
zad.est (MLE of the zero adjusted
Dirichlet distribution), 129
zadr, 8, 64, 129
zadr (Zero adjusted Dirichlet
regression), 248
zadr2 (Zero adjusted Dirichlet
regression), 248

Zero adjusted Dirichlet regression, 248 zeroreplace, 129 zeroreplace (Non-parametric zero replacement strategies), 144 zilogitnorm.est, 129 zilogitnorm.est (MLE of distributions defined in the (0, 1) interval), 123