Package: CNLTreg (via r-universe)

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Type Package

Title Complex-Valued Wavelet Lifting for Signal Denoising

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Description Implementations of recent complex-valued wavelet shrinkage procedures for smoothing irregularly sampled signals, see Hamilton et al (2018) <doi:10.1080/00401706.2017.1281846>.

License GPL-2

Depends adlift, miscTools, nlt

Suggests MASS

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CNLTreg-package

Description

Implementations of recent complex-valued wavelet shrinkage procedures for smoothing irregularly sampled signals, see Hamilton et al (2018) <doi:10.1080/00401706.2017.1281846>.

Details

The DESCRIPTION file:

Package:	CNLTreg
Type:	Package
Title:	Complex-Valued Wavelet Lifting for Signal Denoising
Version:	0.1-2
Date:	2018-07-18
Author:	Matt Nunes [aut, cre], Marina Knight [aut], Jean Hamilton [ctb], Piotr Fryzlewicz [ctb]
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Maintainer:	Matt Nunes <nunesrpackages@gmail.com></nunesrpackages@gmail.com>
Description:	Implementations of recent complex-valued wavelet shrinkage procedures for smoothing irregularly sampled si
License:	GPL-2
Depends:	adlift, miscTools, nlt
Suggests:	MASS

Index of help topics:

CNLTreg-package	Complex-Valued Wavelet Lifting for Signal
	Denoising
cnlt.reg	Performs 'nondecimated' complex-valued wavelet
	lifting for signal denoising
denoisepermC	Denoises a signal using the complex-valued
	lifting transform and multivariate soft
	thresholding
denoisepermCh	Denoises a signal using the complex-valued
	lifting transform and multivariate soft
	thresholding and heteroscedastic variance
	computation
fwtnppermC	Forward complex wavelet lifting transform
mthreshC	Function to perform 'multiwavelet style'
	level-dependent soft thresholding for
	complex-valued wavelet coefficients
orthpredfilters	Computes orthogonal filters

The main routines of the package are denoisepermC and cnlt.reg which perform complex-valued lifting-based denoising, using a single or a multiple (chosen) number of lifting trajectories, respectively.

cnlt.reg

Author(s)

Matt Nunes [aut, cre], Marina Knight [aut], Jean Hamilton [ctb], Piotr Fryzlewicz [ctb] Maintainer: Matt Nunes <nunesrpackages@gmail.com>

References

Hamilton, J., Nunes, M. A, Knight, M. I. and Fryzlewicz, P. (2018) Complex-valued wavelet lifting and applications. *Technometrics*, **60** (1), 48-60, DOI 10.1080/00401706.2017.1281846.

For related literature on the lifting methodology adopted in the technique, see

Nunes, M. A., Knight, M. I and Nason, G. P. (2006) Adaptive lifting for nonparametric regression. *Stat. Comput.* **16** (2), 143–159.

Knight, M. I. and Nason, G. P. (2009) A 'nondecimated' wavelet transform. *Stat. Comput.* **19** (1), 1–16.

See Also

denoise denoiseperm nlt

cnlt.reg	Performs 'nondecimated' complex-valued wavelet lifting for signal de-
	noising

Description

The transform-threshold-invert procedure for signal denoising is dependent on the trajectory (lifting order) used in the forward lifting transform. This procedure uses trajectory bootstrapping and averaging of estimates to gain denoising performance

Usage

cnlt.reg(x, f, P, returnall = FALSE, nkeep = 2, ...)

Arguments

x	Vector of any length (not necessarily equally spaced) that gives the grid on which the signal is observed.
f	Vector of the same length as x that gives the signal values corresponding to the x-locations.
Р	Number of trajectories to be used by the nondecimated lifting algorithm.
returnall	Indicates whether the function returns useful variables or just the denoised dat- apoints.
nkeep	Number of scaling points we want at the end of the transform. The usual choice is nkeep=2.

... Any other arguments to be passed to denoisepermC, see the function documentation for more details.

Details

Essentially, this function applies the complex wavelet lifting denoising procedure denoisepermC P times, each with a different random lifting trajectory. This results in P estimates of the (unknown) true signal. The average of these estimators is the proposed estimator.

Value

If returnall=FALSE, the estimate of the function after denoising. If returnall=TRUE, a list with components:

vec	A matrix of dimension P x (n - nkeep), each row corresponding to a different
	lifting trajectory.
aveghat	Estimated signal after removing the noise.

Warning

Using a large number of trajectories for long datasets could take a long time!

Author(s)

Matt Nunes

References

Hamilton, J., Nunes, M. A., Knight, M. I. and Fryzlewicz, P. (2018) Complex-valued wavelet lifting and applicati\$ *Technometrics*, bold60 (1), 48-60, DOI 10.1080/00401706.2017.1281846.

For the real-valued equivalent procedure, see also Knight, M. I. and Nason, G. P. (2009) A 'nondecimated' wavelet transform. *Stat. Comput.* **19** (1), 1–16.

See Also

denoisepermCh, fwtnppermC, mthreshC, nlt

Examples

```
library(adlift)
```

```
# construct an (irregular) observation grid
x<-runif(256)
#construct the true, normally unknown, signal
g<-make.signal2("blocks",x=x)
#generate noise with mean 0 and signal-to-noise ratio 5
```

denoisepermC

```
noise<-rnorm(256,mean=0,sd=sqrt(var(g))/5)
#generate a noisy version of g
f<-g+noise
#decide on a number of random trajectories to be used (e.g. J=5 below), and apply
# the nondecimated lifting transform to the noisy signal (x,f):
## Not run:
    est<-cnlt.reg(x,f,P=50,LocalPred=AdaptPred,neighbours=1,returnall=FALSE)
## End(Not run)</pre>
```

denoisepermC Denoises a signal using the complex-valued lifting transform and multivariate soft thresholding

Description

Denoises an input signal contaminated by noise. First the signal is decomposed using the complexvalued lifting scheme (see fwtnppermC) using an order of point removal. The resulting complexvalued wavelet coefficients are then thresholded using a soft thresholding rule on the details' magnitude. The transform is inverted and an estimate of the noisy signal is obtained.

Usage

```
denoisepermC(x, f, returnall = FALSE, sdtype = "adlift", verbose = FALSE, ...)
```

Arguments

x	Vector of any length (not necessarily equally spaced) that gives the grid on which the signal is observed.
f	Vector of the same length as x that gives the signal values corresponding to the x-locations.
returnall	Indicates whether the function returns useful variables or just the denoised datapoints.
sdtype	Options are either "adlift" or "complex", indicating whether the noise vari- ance is estimated with the average of the mean absolute deviations of both real and imaginary components of the finest wavelet coefficients, or just the real component, as in denoise.
verbose	Indicates whether useful messages should be printed to the console during the procedure.
	Any other arguments to be passed to fwtnppermC, see documentation for this function for more details.

Details

After the complex lifting transform is applied, the wavelet coefficients are divided into artificial levels. The details from the lifting scheme have different variances, and will therefore be normalized to have the same variance as the noise, by using the lifting matrix. Those normalized details falling into the finest artificial level will be used for estimating the standard deviation of the noise that contaminated the signal. The variable sdtype is used for this estimate, see Appendix B of Hamilton et al. (2018) for more details. Using this estimate, the normalized details can then be thresholded and un-normalized. The transform is then inverted to give an estimate of the signal.

Value

If returnall=FALSE, the estimate of the function after denoising. If returnall=TRUE, a list with components:

fhat	Estimated signal after removing the noise.
W	This is the matrix associated to the modified lifting transform.
indsd	Vector giving the standard deviations of the detail and scaling coefficients.
al	List giving the split of points between the artificial levels.
sd	Estimated standard deviation of the noise.

Author(s)

Matt Nunes, Marina Knight

References

Hamilton, J., Nunes, M. A., Knight, M. I. and Fryzlewicz, P. (2018) Complex-valued wavelet lifting and applications. *Technometrics*, **60** (1), 48-60, DOI 10.1080/00401706.2017.1281846.

See Also

denoisepermCh, fwtnppermC, mthreshC, cnlt.reg

Examples

library(adlift)

construct an (irregular) observation grid x<-runif(256)</pre>

#construct the true, normally unknown, signal
g<-make.signal2("blocks",x=x)</pre>

#generate noise with mean 0 and signal-to-noise ratio 5
noise<-rnorm(256,mean=0,sd=sqrt(var(g))/5)</pre>

#generate a noisy version of g
f<-g+noise</pre>

```
# perform the complex-valued denoising procedure to the noisy signal (x,f):
est<-denoisepermC(x,f,LocalPred=AdaptPred,neigh=1,returnall=FALSE)</pre>
```

denoisepermCh

Denoises a signal using the complex-valued lifting transform and multivariate soft thresholding and heteroscedastic variance computation

Description

Denoises an input signal contaminated by noise. First the signal is decomposed using the complexvalued lifting scheme (see fwtnppermC) using an order of point removal. A sliding window approach is then used on these wavelet coefficients to estimate a local noise variance. The resulting complex-valued wavelet coefficients are then thresholded using a soft thresholding rule on the details' magnitude. The transform is inverted and an estimate of the noisy signal is obtained.

Usage

denoisepermCh(x, f, returnall = FALSE, verbose = FALSE, ...)

Arguments

х	Vector of any length (not necessarily equally spaced) that gives the grid on which the signal is observed.
f	Vector of the same length as x that gives the signal values corresponding to the x-locations.
returnall	Indicates whether the function returns useful variables or just the denoised dat- apoints.
verbose	Indicates whether useful messages should be printed to the console during the procedure.
	Any other arguments to be passed to fwtnpperm and fwtnppermC.

Details

After the complex lifting transform is applied, the wavelet coeficients are divided into artificial levels. The details from the lifting scheme have different variances, and will therefore be normalized to have the same variance as the noise, by using the lifting matrix. A sliding window is used to compute a local 'heteroscedastic' noise variance by taking the MAD of those normalized details falling into the window, see Nunes et al. (2006) for more details. Given the noise estimates for each observation, the normalized details can then be thresholded and un-normalized. The transform is then inverted to give an estimate of the signal.

Value

If returnall=FALSE, the estimate of the function after denoising. If returnall=TRUE, a list with components:

fhat	Estimated signal after removing the noise.
W	This is the matrix associated to the modified lifting transform.
al	List giving the split of points between the artificial levels.
sd	Estimated heteroscedastic standard deviation of the noise.

Author(s)

Matt Nunes, Marina Knight

References

Hamilton, J., Nunes, M. A, Knight, M. I. and Fryzlewicz, P. (2018) Complex-valued wavelet lifting and applications. *Technometrics*, **60** (1), 48-60, DOI 10.1080/00401706.2017.1281846.

Nunes, M. A., Knight, M. I and Nason, G. P. (2006) Adaptive lifting for nonparametric regression. *Stat. Comput.* **16** (2), 143–159.

Knight, M. I. and Nason, G. P. (2009) A 'nondecimated' wavelet transform. *Stat. Comput.* **19** (1), 1–16.

See Also

denoisepermC, fwtnppermC, fwtnpperm, heterovar, mthreshC

Examples

```
library(MASS) # where the motorcyle data lives
```

```
mcycleu<-mcycle[which(duplicated(mcycle$times)=='FALSE'),]
time<-mcycleu[,1]
accel<-mcycleu[,2]</pre>
```

set.seed(200)
est1<-denoisepermCh(time,accel)</pre>

fwtnppermC

Description

Performs the complex-valued lifting transform on a signal with grid x and corresponding function values f.

Usage

```
fwtnppermC(x, f, LocalPred = LinearPred, neighbours = 1,
intercept = TRUE, closest = FALSE, nkeep = 2,
mod = sample(1:length(x), (length(x) - nkeep), FALSE))
```

Arguments

x	A vector of grid values. Can be of any length, not necessarily equally spaced.
f	A vector of function values corresponding to x. Must be of the same length as x.
LocalPred	The type of regression to be performed in the prediction lifting step. Possible options are LinearPred, QuadPred, CubicPred, AdaptPred and AdaptNeigh.
neighbours	The number of neighbours over which the regression is performed at each step. If closest is FALSE, then this in fact denotes the number of neighbours on each side of the removed point.
intercept	Indicates whether or not the regression prediction includes an intercept.
closest	Refers to the configuration of the chosen neighbours. If closest is FALSE, the neighbours will be chosen symmetrically around the removed point. Otherwise, the closest neighbours (in distance) will be chosen.
nkeep	The number of scaling coefficients to be kept in the final representation of the initial signal. This must be at least two.
mod	Vector of length (length(x)-nkeep). This gives the trajectory for the lifting algorithm to follow, i.e. it gives the order of point removal.

Details

Given *n* points on a line, x, each with a corresponding envf value this function computes the complex-valued lifting transform of the (x,f) data. This is similar in spirit to the real-valued lifting transform in fwtnpperm, except that the algorithm constructs *two* orthogonally linked prediction filters, as in Section 2.2 of Hamilton et al. (2018). A summary of the procedure is as follows:

Step One. Compute "integrals" associated to each point, representing the intervals that each gridpoint x_i spans.

Then for each point index in the lifting trajectory mod,

Step Two(a). The neighbours of the removed point are identified using the specified neighbour configuration. The value of f at the removed point is predicted using the specified regression over

the neighbours, unless an adaptive procedure is chosen. In this case, the algorithm chooses the regression which produces the minimal detail coefficient (in magnitude) from a range of regression types (see AdaptPred or AdaptNeigh for more information). In either case, the regression specifies a local filter of the function values over the neighbourhood, L.

Step Two(b). A second filter, M, is then constructed orthogonal to L, such that it has unit norm, see Hamilton et al. (2018) for more details.

The differences between the removed point's f value and the predictions using the two filters are computed, which constitute the real and imaginary parts of the complex-valued wavelet coefficient. This coefficient is then stored

Step Three. The integrals and the scaling function values (neighbouring coeffv values) are updated according to the filter L.

The algorithm continues until all points in mod are removed.

Value

coeff	matrix of detail and scaling coefficients in the wavelet decomposition of the signal; first column: real component, second column: imaginary component.
lengthsremove	vector of interval lengths corresponding to the points removed during the transform (in removelist).
pointsin	indices into X of the scaling coefficients in the wavelet decomposition. These are the indices of the X values which remain after all points in removelist have been predicted and removed. This has length nkeep.
removelist	a vector of indices into ${\tt X}$ of the lifted coefficients during the transform (in the order of removal).
gamlist	a list of all the prediction weights used at each step of the transform; each list entry is a matrix of two rows, corresponding to the filters L and M .
alphalist	a list of the update coefficients used in the update step of the decomposition.
W	The complex-valued lifting matrix associated to the transform.
reo	An index into the observations indicating a reordering to give $1:n$. This is reported for convenience for other functions, and is not intended for use by the user.
coeffv	vector of complex-valued detail and scaling coefficients in the wavelet decomposition of the signal; contains the same information as coeff.
Ialpha	Vector of "irregularity degree" measures corresponding to each lifting step of the transform. Note that this is returned for convenience in other functions, and is not intended for use by the user.

Author(s)

Matt Nunes, Marina Knight

References

Hamilton, J., Knight, Nunes, M. A. and Fryzlewicz (2018) Complex-valued wavelet lifting and applications. *Technometrics*, **69** (1), 48-60, DOI 10.1080/00401706.2017.1281846.

mthreshC

For related literature on the lifting methodology adopted in the technique, see

Nunes, M. A., Knight, M. I and Nason, G. P. (2006) Adaptive lifting for nonparametric regression. *Stat. Comput.* **16** (2), 143–159.

Knight, M. I. and Nason, G. P. (2009) A 'nondecimated' wavelet transform. *Stat. Comput.* **19** (1), 1–16.

See Also

AdaptNeigh, AdaptPred, CubicPred, denoisepermC, denoisepermCh, LinearPred, orthpredfilters, QuadPred

Examples

library(adlift)

construct an (irregular) observation grid x<-runif(256)</pre>

#construct a signal
f<-make.signal2("blocks",x=x)</pre>

fwd<-fwtnppermC(x,f,LocalPred=AdaptPred,neigh=1,closest=FALSE)</pre>

have a look at the complex-valued coefficients and the removal trajectory:

fwd\$coeffv

fwd\$removelist

mthreshC

Function to perform 'multiwavelet style' level-dependent soft thresholding for complex-valued wavelet coefficients

Description

This function uses chi² statistics similar to Barber and Nason (2004) to threshold wavelet coefficients based on their magnitude

Usage

```
mthreshC(coeffv, Sigma, rl, po, ali, verbose = FALSE)
```

Arguments

coeffv	A matrix of complex-valued wavelet coefficients (columns are real and imagi- nary parts of the coefficients respectively).
Sigma	An array of dimension 2 x 2 x n describing the covariance between real and imaginary parts of the wavelet coefficients. In particular, Sigma[,,i] represents the covariance between real and imaginary parts of the ith lifted wavelet coefficient (see rl argument).
rl	The removelist (trajectory of lifted points) corresponding to a forward lifting transform.
ро	A vector of indices describing the unlifted scaling coefficients in a forward lift- ing transform.
ali	A list of indices of observations, each entry corresponding to an 'artificial level' (finest to coarsest), see artlev for more details.
verbose	Indicates whether helpful messages should be printed to the console during the procedure.

Details

The procedure in Downie and Silverman (1998) or Barber and Nason (2004) makes use of the magnitude of wavelet coefficients to threshold them. In particular, the covariance between the components of the wavelet coefficients (contained in Sigma is taken into account to compute a thresholding statistic, the distribution of which is chi-squared_2 distributed, see cthresh for more details. These statistics are then compared with level-dependent universal thresholds computed by counting the number of coefficients in specific artificial levels.

Value

A list with the following components:

chi	the vector of chi-squared statistics used in the thresholding procedure.
coeffvt	the matrix of thresholded coefficients, columns representing the real and imagi-
	nary components respectively.

Author(s)

Matt Nunes, Marina Knight

References

Hamilton, J., Knight, M. I., Nunes, M. A. and Fryzlewicz (2018) Complex-valued wavelet lifting and applications. *Technometrics*, **60** (1), 48-60,DOI 10.1080/00401706.2017.1281846. Barber, S. and Nason, G. P. (2004) Real nonparametric regression using complex wavelets. *J. Roy. Stat. Soc. B* **66** (4), 927–939. Downie, T. R. and Silverman, B. W. (1998) The discrete multiple wavelet tranform and thresholding methods. *IEEE Trans. Sig. Proc.* **46** 2558–2561.

See Also

cthresh, denoisepermC, denoisepermCh

mthreshC

Examples

```
library(adlift)
set.seed(100)
# construct an (irregular) sampling structure:
x<-sort(runif(200))</pre>
g<-make.signal2("bumps",x=x)
# generate IID noise with a particular sd
noise<-rnorm(200,0,sd=0.5)</pre>
f<-g+noise
# perform forward complex lifting transform
out<-fwtnppermC(x,f,LocalPred=LinearPred,neigh=1)</pre>
# have a look at some of the coefficients
out$coeffv[1:10]
# extract lifting matrix and induced lifting variances
W <- out$W
Gpre<-tcrossprod(W,Conj(W))</pre>
indsd<-sqrt(diag(Gpre))</pre>
# now estimate noise sd using the first artificial level:
al<-artlev(out$lengthsremove.out$removelist)</pre>
fine<-(out$coeffv/indsd)[al[[1]]]</pre>
varest<-mad(Re(fine))^2</pre>
# now compute coefficient covariance structure, see
# Hamilton et al. (2018), Appendix B
C = varest * tcrossprod(W)
    G = varest * Gpre
    P = Conj(G) - t(Conj(C))
    Sigma <- array(0, dim = c(2, 2, length(out$coeffv)))</pre>
    Sigma[1, 1, ] <- diag(Re(G + C)/2)
    Sigma[2, 2, ] <- diag(Re(G - C)/2)
    Sigma[1, 2, ] <- -diag(Im(G - C)/2)</pre>
    Sigma[2, 1, ] <- diag(Im(G + C)/2)
```

now threshold complex coefficients according to this structure:

coeff.thresh<-mthreshC(out\$coeffv,Sigma,out\$removelist,out\$pointsin,al)</pre>

have a look at some of these coefficients

coeff.thresh\$coeffv[1:10]

orthpredfilters Computes orthogonal filters

Description

Given a filter L, finds a second filter M, orthogonal to L and with unit norm

Usage

```
orthpredfilters(filter = c(0.5, 1, 0.5))
```

Arguments

filter An initial filter L

Details

See Hamilton et al. (2018), section 2.2.

Value

A matrix with two rows, the first row corresponding to L, the second corresponding to the orthogonal filter M.

Warning

At present only works with odd length filters

Author(s)

Marina Knight, Matt Nunes

References

Hamilton, J., Nunes, M. A., Knight, M. I. and Fryzlewicz, P. (2018) Complex-valued wavelet lifting and applications. *Technometrics*, **60** (1), 48-60, DOI 10.1080/00401706.2017.1281846.

See Also

fwtnppermC

orthpredfilters

Examples

create a vector representing a filter for one neighbour either side of a removed point
(equally weighted):

L = c(0.5, 1, 0.5)

now work out a unit-norm filter orthogonal to L

out <- orthpredfilters(L)</pre>

M should be the second row:

out[2,]

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