Package: BNSP (via r-universe)

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Title Bayesian Non- And Semi-Parametric Model Fitting

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Description MCMC algorithms & processing functions for: 1. single

response multiple regression, see Papageorgiou, G. (2018) [<doi:10.32614/RJ-2018-](https://doi.org/10.32614/RJ-2018-069) [069>](https://doi.org/10.32614/RJ-2018-069), 2. multivariate response multiple regression, with nonparametric models for the means, the variances and the correlation matrix, with variable selection, see Papageorgiou, G. and Marshall, B. C. (2020) [<doi:10.1080/10618600.2020.1739534>](https://doi.org/10.1080/10618600.2020.1739534), 3. joint mean-covariance models for multivariate responses, see Papageorgiou, G. (2022) [<doi:10.1002/sim.9376>](https://doi.org/10.1002/sim.9376), and 4.Dirichlet process mixtures, see Papageorgiou, G. (2019) [<doi:10.1111/anzs.12273>](https://doi.org/10.1111/anzs.12273).

Depends $R (= 3.5.0)$

Imports coda, ggplot2, plot3D, threejs, gridExtra, cubature, Formula, plyr, mgcv, corrplot, label.switching

LinkingTo cubature

Suggests mvtnorm, np

License GPL $(>= 2)$

NeedsCompilation yes

Repository CRAN

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Contents

BNSP-package *Bayesian non- and semi-parametric model fitting*

Description

Markov chain Monte Carlo algorithms for non- and semi-parametric models: 1. spike-slab variable selection in multivariate mean/variance regression models with function mvrm, 2. joint meancovariance models for multivariate longitudinal responses with function lmrm, and 3. Dirichlet process mixture models with function dpmj.

Details

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Author(s)

Georgios Papageorgiou (2014)

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References

Papageorgiou, G. (2020). Bayesian semiparametric modelling of covariance matrices for multivariate longitudinal data. https://arxiv.org/abs/2012.09833

Papageorgiou, G. and Marshall, B.C. (2020). Bayesian semiparametric analysis of multivariate continuous responses, with variable selection. Journal of Computational and Graphical Statistics, 29:4, 896-909, DOI: 10.1080/10618600.2020.1739534

Papageorgiou, G. (2018). BNSP: an R Package for fitting Bayesian semiparametric regression models and variable selection. The R Journal, 10(2):526-548.

Papageorgiou, G. (2018). Bayesian density regression for discrete outcomes. Australian and New Zealand Journal of Statistics, arXiv:1603.09706v3 [stat.ME].

Papageorgiou, G., Richardson, S. and Best, N. (2015). Bayesian nonparametric models for spatially indexed data of mixed type. Journal of the Royal Statistical Society: Series B (Statistical Methodology), 77:973-999.

ami *Amitriptyline dataset from Johnson and Wichern*

Description

Amitriptyline is a prescription antidepressant. The dataset consists of measurements on 17 patients who had over-dosed on amitriptyline.

Usage

data(ami)

Format

A data frame containing 17 rows and 7 columns. The columns represent

- tot total blood plasma level.
- ami amount of amitriptyline found in the plasma.
- gen gender (1 for female).
- amt amount of the drug taken.
- pr PR wave measurement.
- bp diastolic blood pressure.
- qrs QRS wave measurement.

Source

Johnson, R. A., and Wichern, D. W. (2007), Applied Multivariate Statistical Analysis, Essex: Pearson, page 426.

References

Johnson, R. A., and Wichern, D. W. (2007). *Applied Multivariate Statistical Analysis*, Essex: Pearson.

chol *The Cholesky and modified Cholesky decompositions*

Description

Computes the Cholesky factorization and modified Cholesky factorizations of a real symmetric positive-definite square matrix.

Usage

chol(x, mod = TRUE, $p = 1, ...$)

Arguments

Details

The function computes the modified Cholesky decomposition of a real symmetric positive-definite square matrix Σ . This is given by

$$
L\Sigma L^{\top} = D,
$$

where L is a lower tringular matrix with ones on its main diagonal and D is a block diagonal matrix with block size determined by argument p.

Value

The function returns matrices L and D.

Author(s)

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See Also

The default function from **base**, [chol](#page-3-1)

Examples

```
Sigma <- matrix(c(1.21,0.18,0.13,0.41,0.06,0.23,
                  0.18,0.64,0.10,-0.16,0.23,0.07,
                  0.13,0.10,0.36,-0.10,0.03,0.18,
                  0.41,-0.16,-0.10,1.05,-0.29,-0.08,
                  0.06,0.23,0.03,-0.29,1.71,-0.10,
                  0.23,0.07,0.18,-0.08,-0.10,0.36),6,6)
LD <- chol(Sigma)
L <- LD$L
D <- LD$D
round(L,5)
round(D,5)
solve(L) %*% D %*% solve(t(L))
LD \leftarrow chol(Sigma, p = 2)L <- LD$L
D <- LD$D
round(L, 5)
round(D, 5)
solve(L) %*% D %*% solve(t(L))
```
clustering *Computes the similarity matrix*

Description

Computes the similarity matrix.

Usage

```
clustering(object, ...)
```
Arguments

Details

The function computes the similarity matrix for clustering based on corrrelations or variables.

Value

Similarity matrix.

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Author(s)

Georgios Papageorgiou <gpapageo@gmail.com>

See Also

[mvrm](#page-18-1)

Examples

#see \code{mvrm} example

continue *Continues the sampler from where it stopped*

Description

Allows the user to continue the sampler from the state it stopped in the previous call to mvrm.

Usage

continue(object, sweeps, burn = 0 , thin, discard = $FALSE$,...)

Arguments

Details

The function allows the sampler to continue from the state it last stopped.

Value

The function returns an object of class mvrm.

Author(s)

Georgios Papageorgiou <gpapageo@gmail.com>

See Also

[mvrm](#page-18-1)

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Examples

#see \code{mvrm} example

dpmj *Dirichlet process mixtures of joint models*

Description

Fits Dirichlet process mixtures of joint response-covariate models, where the covariates are of mixed type while the discrete responses are represented utilizing continuous latent variables. See 'Details' section for a full model description and Papageorgiou (2018) for all technical details.

Usage

dpmj(formula, Fcdf, data, offset, sampler = "truncated", Xpred, offsetPred, StorageDir, ncomp, sweeps, burn, thin = 1, seed, H, Hdf, d, D, Alpha.xi, Beta.xi, Alpha.alpha, Beta.alpha, Trunc.alpha, ...)

Arguments

- 2. If Fcdf = "negative binomial", this argument is a two-dimensional vector that includes parameters $\beta_{1\xi}$ and $\beta_{2\xi}$ of the priors: $\xi_1 \sim \text{Gamma}(\alpha_{1\xi}, \beta_{1\xi})$ and $\xi_2 \sim \text{Gamma}(\alpha_{2\xi}, \beta_{2\xi})$, where ξ_1 and ξ_2 are the two parameters of the Negative Binomial pmf.
- 3. If Fcdf = "generalized poisson", this argument is a two-dimensional vector that includes parameters $\beta_{1\xi}$ and $\beta_{2\xi}$ of the priors: $\xi_1 \sim \text{Gamma}(\alpha_{1\xi}, \beta_{1\xi})$ and $\xi_2 \sim \text{Normal}(\alpha_{2\xi}, \beta_{2\xi}) I[\xi_2 \in R_{\xi_2}]$, where ξ_1 and ξ_2 are the two parameters of the Generalized Poisson pmf. Parameter ξ_2 is restricted in the range $R_{\xi_2} = (0.05, \infty)$ as it is a dispersion parameter. Note that $\beta_{2\xi}$ is a standard deviation.
- 4. If Fcdf = "binomial", this argument is parameter β_{ξ} of the prior of the Binomial probability: $\xi \sim \text{Beta}(\alpha_{\xi}, \beta_{\xi}).$
- 5. If Fcdf = "beta binomial", this argument is a two-dimensional vector that includes parameters $\beta_{1\xi}$ and $\beta_{2\xi}$ of the priors: $\xi_1 \sim \text{Gamma}(\alpha_{1\xi}, \beta_{1\xi})$ and $\xi_2 \sim \text{Gamma}(\alpha_{2\xi}, \beta_{2\xi})$, where ξ_1 and ξ_2 are the two parameters of the Beta Binomial pmf.

See 'Details' section.

Details

Function dpmj returns samples from the posterior distributions of the parameters of the model:

$$
f(y_i, x_i) = \sum_{h=1}^{\infty} \pi_h f(y_i, x_i | \theta_h), \qquad (1)
$$

where y_i is a univariate discrete response, x_i is a p-dimensional vector of mixed type covariates, and $\pi_h, h \geq 1$, are obtained according to Sethuraman's (1994) stick-breaking construction: $\pi_1 = v_1$, and for $l \geq 2, \pi_l = v_l \prod_{j=1}^{l-1} (1 - v_j)$, where v_k are iid samples $v_k \sim$ Beta $(1, \alpha)$, $k \geq 1$.

Let Z denote a discrete variable (response or covariate). It is represented as discretized version of a continuous latent variable Z^* . Observed discrete Z and continuous latent variable Z^* are connected by:

$$
z = q \iff c_{q-1} < z^* < c_q, q = 0, 1, 2, \dots
$$

where the cut-points are obtained as: $c_{-1} = -\infty$, while for $q \ge 0$, $c_q = c_q(\lambda) = \Phi^{-1}{F(q; \lambda)}$. Here $\Phi(.)$ is the cumulative distribution function (cdf) of a standard normal variable and $F()$ denotes an appropriate cdf. Further, latent variables are assumed to independently follow a $N(0, 1)$ distribution, where the mean and variance are restricted to be zero and one as they are non-identifiable by the data. Choices for $F()$ are described next.

For counts, three options are supported. First, $F(\cdot; \lambda_i)$ can be specified as the cdf of a Poisson($H_i \xi_h$) variable. Here $\lambda_i = (\xi_h, H_i)^T, \xi_h$ denotes the Poisson rate associated with cluster h, and H_i the offset term associated with sampling unit i. Second, $F(.; \lambda_i)$ can be specified as the negative binomial cdf, where $\lambda_i = (\xi_{1h}, \xi_{2h}, H_i)^T$. This option allows for overdispersion within each cluster relative to the Poisson distribution. Third, $F(.; \lambda_i)$ can be specified as the Generalized Poisson cdf, where, again, $\lambda_i = (\xi_{1h}, \xi_{2h}, H_i)^T$. This option allows for both over- and under-dispersion within each cluster.

For Binomial data, two options are supported. First, $F(.; \lambda_i)$ may be taken to be the cdf of a Binomial (H_i, ξ_h) variable, where ξ_h denotes the success probability of cluster h and H_i the number of trials associated with sampling unit i. Second, $F(.; \lambda_i)$ may be specified to be the beta-binomial cdf, where $\lambda = (\xi_{1h}, \xi_{2h}, H_i)^T$.

The special case of Binomial data is treated as

$$
Z = 0 \iff z^* < 0, z^* \sim N(\mu_z^*, 1).
$$

Details on all kernels are provided in the two tables below. The first table provides the probability mass functions and the mean in the presence of an offset term (which may be taken to be one). The column 'Sample' indicates for which parameters the routine provides posterior samples. The second table provides information on the assumed priors along with the default values of the parameters of the prior distributions and it also indicates the function arguments that allow the user to alter these.

Let $z_i = (y_i, x_i^T)^T$ denote the joint vector of observed continuous and discrete variables and z_i^* the corresponding vector of continuous observed and latent variables. With θ_h denoting model parameters associated with the *h*th cluster, the joint density $f(z_i|\theta_h)$ takes the form

$$
f(z_i|\theta_h) = \int_{R(y)} \int_{R(x_d)} N_q(z_i^*; \mu_h^*, \Sigma_h^*) dx_d^* dy^*,
$$

where

$$
\mu_h^* = \left(\begin{array}{c} 0 \\ \mu_h \end{array}\right), \quad \Sigma_h^* = \left[\begin{array}{cc} C_h & \nu_h^T \\ \nu_h & \Sigma_h \end{array}\right] ,
$$

where C_h is the covariance matrix of the latent continuous variables and it has diagonal elements equal to one i.e. it is a correlation matrix.

In addition to the priors defined in the table above, we specify the following:

- 1. The restricted covariance matrix Σ_h^* is assigned a prior distribution that is based on the Wishart distribution with degrees of freedom set by default to dimension of matrix plus two and diagonal scale matrix, with the sub-matrix that corresponds to discrete variables taken to be the identity matrix and with sub-matrix that corresponds to continuous variables having entries equal to 1/8 of the square of the observed data range. Default values can be changed using arguments H and Hdf.
- 2. The prior on μ_h , the non-zero part of μ_h^* , is taken to be multivariate normal $\mu_h \sim N(d, D)$. The mean d is taken to be equal to the center of the dataset. The covariance matrix D is taken to be diagonal. Its elements that correspond to continuous variables are set equal to 1/8 of the square of the observed data range while the elements that correspond to binary variables are set equal to 5. Arguments Mu.mu and Sigma.mu allow the user to change the default values.
- 3. The concentration parameter α is assigned a Gamma $(\alpha_{\alpha}, \beta_{\alpha})$ prior over the range (c_{α}, ∞) , that is, $f(\alpha) \propto \alpha^{\alpha_{\alpha}-1} \exp\{-\alpha \beta_{\alpha}\} I[\alpha > c_{\alpha}]$, where I[.] is the indicator function. The default values are $\alpha_{\alpha} = 2.0$, $\beta_{\alpha} = 5.0$, and $c_{\alpha} = 0.25$. Users can alter the default using using arguments Alpha.alpha, Beta.alpha and Turnc.alpha.

Value

Function dpmj returns the following:

Further, function dpmj creates files where the posterior samples are written. These files are (with all file names preceded by 'BNSP.'):

- alpha.txt this file contains samples from the posterior of the concentration parameters α . The file is arranged in (sweeps-burn)/thin lines and one column, each line including one posterior sample.
- compAlloc.txt this file contains the allocations to clusters obtained during posterior sampling. It consists of (sweeps-burn)/thin lines, that represent the posterior samples, and n columns, that represent the sampling units. Clusters are represented by integers ranging from 0 to ncomp-1.
- MeanReg.txt this file contains the conditional means of the response y given covariates x obtained during posterior sampling. The rows represent the (sweeps-burn)/thin posterior samples. The columns represent the various covariate values x for which the means are obtained.
- MedianReg.txt this file contains the 50% conditional quantile of the response y given covariates x obtained during posterior sampling. The rows represent the (sweeps-burn)/thin posterior samples. The columns represent the various covariate values x for which the medians are obtained.
- muh. txt this file contains samples from the posteriors of the p -dimensional mean vectors μ_h , $h = 1, 2, \ldots$, ncomp. The file is arranged in ((sweeps-burn)/thin)*ncomp lines and p columns. In more detail, sweeps create ncomp lines representing samples $\mu_h^{(sw)}$ $h_h^{(sw)}$, $h = 1, \ldots$, ncomp, where superscript sw represents a particular sweep. The elements of $\mu_h^{(sw)}$ $h^{(sw)}$ are written in the columns of the file.
- nmembers.txt this file contains (sweeps-burn)/thin lines and ncomp columns, where the lines represent posterior samples while the columns represent the components or clusters. The entries represent the number of sampling units allocated to each component.
- Q05Reg.txt this file contains the 5% conditional quantile of the response y given covariates x obtained during posterior sampling. The rows represent the (sweeps-burn)/thin posterior samples. The columns represent the various covariate values x for which the quantiles are obtained.
- Q10Reg.txt as above, for the 10% conditional quantile.
- 015Reg.txt as above, for the 15% conditional quantile.
- Q20Reg.txt as above, for the 20% conditional quantile.
- Q25Reg.txt as above, for the 25% conditional quantile.
- Q75Reg.txt as above, for the 75% conditional quantile.
- Q80Reg.txt as above, for the 80% conditional quantile.
- Q85Reg.txt as above, for the 85% conditional quantile.
- Q90Reg.txt as above, for the 90% conditional quantile.
- Q95Reg.txt as above, for the 95% conditional quantile.
- Sigmah.txt this file contains samples from the posteriors of the $q \times q$ restricted covariance matrices $\Sigma_h^*,h=1,2,\ldots,$ ncomp. The file is arranged in ((sweeps-burn)/thin)*ncomp lines and q^2 columns. In more detail, sweeps create ncomp lines representing samples $\Sigma_h^{(sw)}$ $h_h^{(sw)}$, $h = 1, \ldots$, ncomp, where superscript sw represents a particular sweep. The elements of $\Sigma_h^{(sw)}$ $h_h^{(sw)}$ are written in the columns of the file.

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References

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Papaspiliopoulos, O. (2008). A note on posterior sampling from Dirichlet mixture models. Technical report, University of Warwick.

Sethuraman, J. (1994). A constructive definition of Dirichlet priors. Statistica Sinica, 4, 639-650.

Walker, S. G. (2007). Sampling the Dirichlet mixture model with slices. Communications in Statistics Simulation and Computation, 36(1), 45-54.

Examples

```
#Bayesian nonparametric joint model with binomial response Y and one predictor X
data(simD)
pred<-seq(with(simD,min(X))+0.1,with(simD,max(X))-0.1,length.out=30)
npred<-length(pred)
# fit1 and fit2 define the same model but with different numbers of
# components and posterior samples
fit1 <- dpmj(cbind(Y,(E-Y))~X, Fcdf="binomial", data=simD, ncomp=10, sweeps=20,
             burn=10, sampler="truncated", Xpred=pred, offsetPred=30)
fit2 <- dpmj(cbind(Y,(E-Y))~X, Fcdf="binomial", data=simD, ncomp=50, sweeps=5000,
              burn=1000, sampler="truncated", Xpred=pred, offsetPred=30)
plot(with(simD,X),with(simD,Y)/with(simD,E))
lines(pred,fit2$medianReg/30,col=3,lwd=2)
# with discrete covariate
simD<-data.frame(simD,Xd=sample(c(0,1),300,replace=TRUE))
pred<-c(0,1)fit3 <- dpmj(cbind(Y,(E-Y))~Xd, Fcdf="binomial", data=simD, ncomp=10, sweeps=20,
             burn=10, sampler="truncated", Xpred=pred, offsetPred=30)
```


Description

This function plots the posterior distribution of the elements of correlation matrices.

Usage

```
histCorr(x, term = "R", plotOptions = list(),...)
```
Arguments

Details

Use this function to visualize the elements of a correlation matrix.

Value

Posterior distributions of elements of correlation matrices.

Author(s)

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See Also

[mvrm](#page-18-1)

Examples

#see \code{mvrm} example

lmrm *Bayesian semiparametric modelling of covariance matrices for multivariate longitudinal data*

Description

Implements an MCMC algorithm for posterior sampling based on a semiparametric model for continuous longitudinal multivariate responses. The overall model consists of 5 regression submodels and it utilizes spike-slab priors for variable selection and function regularization. See 'Details' section for a full description of the model.

Usage

```
lmrm(formula, data = list(), centre=TRUE, id, time,
sweeps, burn = 0, thin = 1, seed, StorageDir,
c.betaPrior = "IG(0.5, 0.5*n*p)", pi.muPrior = "Beta(1,1)",
c.alphaPrior = "IG(1.1, 1.1)", pi.phiPrior = "Beta(1,1)", c.psiPrior = "HN(2)",
signaPrior = "HN(2)", pi.sigmaPrior = "Beta(1,1)",
corr.Model = c("common", nClust = 1), DP.concPrior = "Gamma(5,2)",c.etaPrior = "IG(0.5, 0.5*sampling,", pi.nuPrior = "Beta(1,1)",pi.fiPrior = "Beta(1,1)", c.omegaPrior = "IG(1.1,1.1)", sigmaCorPrior = "HN(2)",
tuneCalpha, tuneSigma2, tuneCbeta, tuneAlpha, tuneSigma2R, tuneR, tuneCpsi,
tuneCbCor, tuneOmega, tuneComega, tau, FT = 1,...)
```
Arguments

Details

Function lmrm returns samples from the posterior distributions of the parameters of a regression model with normally distributed multivariate longitudinal responses. To describe the model, let $Y_{ij} = (Y_{ij1}, \ldots, Y_{ijp})^\top$ denote the vector of p responses observed on individual $i, i = 1, \ldots, n$, at time point t_{ij} , $j = 1, \ldots, n_i$. The observational time points t_{ij} are allowed to be unequally spaced. Further, let u_{ij} denote the covariate vector that is observed along with Y_{ij} and that may include time, other time-dependent covariates and time-independent ones. In addition, let $Y_i = (Y_{i1}^\top, \dots, Y_{i n_i}^\top)^\top$ denote the *i*th response vector. With $\mu_i = E(Y_i)$ and $\Sigma_i = cov(Y_i)$, the model assumes multivariate normality, $Y_i \sim N(\mu_i, \Sigma_i), i = 1, 2, ..., n$. The means μ_i and covariance matrices Σ_i are modelled semiparametrically in terms of covariates. For the means one can specify semiparametric models,

$$
\mu_{ijk} = \beta_{k0} + \sum_{l=1}^{K_1} u_{ijl} \beta_{kl} + \sum_{l=K_1+1}^{K} f_{\mu,k,l}(u_{ijl}).
$$

This is the first of the 5 regression submodels.

To model the covariance matrix, first consider the modified Cholesky decomposition, $L_i \Sigma_i L_i^{\top} =$ D_i , where L_i is a unit block lower triangular matrix and D_i is a block diagonal matrix,

For modelling D_{ij} , $i = 1, \ldots, n, j = 1, \ldots, n_i$ in terms of covariates, first we separate the variances and the correlations $D_{ij} = S_{ij}^{1/2} R_{ij} S_{ij}^{1/2}$. It is easy to model matrix S_{ij} in terms of covariates as the only requirement on its diagonal elements is that they are nonnegative,

$$
\log \sigma_{ijk}^2 = \alpha_{k0} + \sum_{l=1}^{L_1} w_{ijl} \alpha_{kl} + \sum_{l=L_1+1}^{L} f_{\sigma,k,l}(w_{ijl})
$$

This is the second of the 5 regression submodels.

For ϕ_{ijklm} , the (l, m) element of Φ_{ijk} , $l, m = 1, \dots, p$, one can specify semiparametric models

$$
\phi_{ijklm} = \psi_{lm0} + \sum_{b=1}^{B_1} v_{ijkb} \psi_{lmb} + \sum_{b=B_1+1}^{B} f_{\phi,l,m,b}(v_{ijkb})
$$

This is the third of the 5 regression submodels.

The elements of the correlations matrices R_{ij} are modelled in terms of covariate time only, hence they are denoted by R_t . Subject to the positive definiteness constraint, the elements of R_t are modelled using a normal distribution with location and scale parameters, μ_{ct} and σ_{ct}^2 , modelled as

$$
\mu_{ct} = \eta_0 + f_{\mu}(t),
$$

$$
\log \sigma_{ct}^2 = \omega_0 + f_{\sigma}(t),
$$

and these are the last 2 of the 5 submodels.

Value

Function lmrm returns samples from the posteriors of the model parameters.

Author(s)

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References

Papageorgiou, G. (2020). Bayesian semiparametric modelling of covariance matrices for multivariate longitudinal data. arXiv:2012.09833.

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Examples

```
# Fit a joint mean-covariance model on the simulated dataset simD2
require(ggplot2)
data(simD2)
model \le Y1 | Y2 \sim time | sm(time) | sm(lag) | sm(time) | 1
# the above defines the responses and the regression models on the left and
# right of "~", respectively
# the first model, for the mean, is a linear function of time, this is sufficient as
# the 2 responses have constant mean.
# the second model, for the variances, is a smooth function of time
# the third model, for the dependence structure, is a smooth function of lag,
# that lmrm figures out and it does not need to be computed by the user
# the fourth model, for location of the correlations, is a smooth function of time
# the fifth model, for scale of the correlations, is just an intercept model
## Not run:
m1 < -1mrm(formula = model, corr.Model = c("common", nClust = 1), data = simD2,
        id = id, time = time, sweeps = 2500, burn = 500, thin = 2,
        StorageDir = getwd(), seed = 1)
plot(m1)
```
End(Not run)

mvrm *Bayesian semiparametric analysis of multivariate continuous responses, with variable selection*

Description

Implements an MCMC algorithm for posterior sampling based on a semiparametric model for continuous multivariate responses and additive models for the mean and variance functions. The model utilizes spike-slab priors for variable selection and regularization. See 'Details' section for a full description of the model.

Usage

```
mvrm(formula, distribution = "normal", data = list(), centre = TRUE, sweeps,
burn = 0, thin = 1, seed, StorageDir, c.betaPrior = "IG(0.5, 0.5 * n * p)",
pi.muPrior = "Beta(1, 1)", c.alphaPrior = "IG(1.1, 1.1)", sigmaPrior = "HN(2)",pi.sigmaPrior = "Beta(1, 1)", c.psiPrior = "HN(1)", phiPrior = "HN(2)",
pi.omegaPrior = "Beta(1, 1)", mu.RPrior = "N(0, 1)", sigma.RPrior = "HN(1)",
corr.Model = c("common", nClust = 1), DPconcPrior = "Gamma(5, 2)",breaksPrior = "SBeta(1, 2)", tuneCbeta, tuneCalpha, tuneAlpha, tuneSigma2,
tuneCpsi, tunePsi, tunePhi, tuneR, tuneSigma2R, tuneHar, tuneBreaks, tunePeriod, tau,
FT = 1, compDeviance = FALSE, ...)
```
Arguments

Details

Function mvrm returns samples from the posterior distributions of the parameters of a regression model with normally distributed multivariate responses and mean and variance functions modeled in terms of covariates. For instance, in the presence of two responses (y_1, y_2) and two covariates in the mean model (u_1, u_2) and two in the variance model (w_1, w_2) , we may choose to fit

$$
\mu_u = \beta_0 + \beta_1 u_1 + f_\mu(u_2),
$$

$$
\log(\sigma_W^2) = \alpha_0 + \alpha_1 w_1 + f_\sigma(w_2),
$$

parametrically modelling the effects of u_1 and w_1 and non-parametrically modelling the effects of u_2 and w_2 . Smooth functions, such as f_μ and f_σ , are represented by basis function expansion,

$$
f_{\mu}(u_2) = \sum_j \beta_j \phi_j(u_2),
$$

$$
f_{\sigma}(w_2) = \sum_j \alpha_j \phi_j(w_2),
$$

where ϕ are the basis functions and β and α are regression coefficients.

The variance model can equivalently be expressed as

$$
\sigma_W^2 = \exp(\alpha_0) \exp(\alpha_1 w_1 + f_\sigma(w_2)) = \sigma^2 \exp(\alpha_1 w_1 + f_\sigma(w_2)),
$$

where $\sigma^2 = \exp(\alpha_0)$. This is the parameterization that we adopt in this implementation.

Positive prior probability that the regression coefficients in the mean model are exactly zero is achieved by defining binary variables γ that take value $\gamma = 1$ if the associated coefficient $\beta \neq 0$ and $\gamma = 0$ if $\beta = 0$. Indicators δ that take value $\delta = 1$ if the associated coefficient $\alpha \neq 0$ and $\delta = 0$ if $\alpha = 0$ for the variance function are defined analogously. We note that all coefficients in the mean and variance functions are subject to selection except the intercepts, β_0 and α_0 .

Prior specification:

For the vector of non-zero regression coefficients β_{γ} we specify a g-prior

$$
\beta_{\gamma}|c_{\beta}, \sigma^2, \gamma, \alpha, \delta \sim N(0, c_{\beta}\sigma^2(\tilde{X}_{\gamma}^{\top}\tilde{X}_{\gamma})^{-1}).
$$

where \tilde{X} is a scaled version of design matrix X of the mean model.

For the vector of non-zero regression coefficients α_{δ} we specify a normal prior

$$
\alpha_{\delta}|c_{\alpha}, \delta \sim N(0, c_{\alpha}I).
$$

Independent priors are specified for the indicators variables γ and δ as $P(\gamma = 1 | \pi_\mu) = \pi_\mu$ and $P(\delta = 1 | \pi_{\sigma}) = \pi_{\sigma}$. Further, Beta priors are specified for π_{μ} and π_{σ}

$$
\pi_{\mu} \sim Beta(c_{\mu}, d_{\mu}), \pi_{\sigma} \sim Beta(c_{\sigma}, d_{\sigma}).
$$

We note that blocks of regression coefficients associated with distinct covariate effects have their own probability of selection (π_{μ} or π_{σ}) and this probability has its own prior distribution.

Further, we specify inverse Gamma priors for c_β and c_α

$$
c_{\beta} \sim IG(a_{\beta}, b_{\beta}), c_{\alpha} \sim IG(a_{\alpha}, b_{\alpha})
$$

 $mvrm$ and 23

For σ^2 we consider inverse Gamma and half-normal priors

$$
\sigma^2 \sim IG(a_{\sigma}, b_{\sigma}), |\sigma| \sim N(0, \phi_{\sigma}^2).
$$

Lastly, for the elements of the correlation matrix, we specify normal distributions with mean μ_R and variance σ_R^2 , with the priors on these two parameters being normal and half-normal, respectively. This is the common correlations model. Further, the grouped correlations model can be specified. It considers a mixture of normal distributions for the means μ_R . The grouped correlations model can also be specified. It clusters the variables instead of the correlations.

Value

Function mvrm returns the following:

Further, function mvrm creates files where the posterior samples are written. These files are (with all file names preceded by 'BNSP.'):

Author(s)

Georgios Papageorgiou <gpapageo@gmail.com>

References

Papageorgiou, G. and Marshall, B.C. (2019). Bayesian semiparametric analysis of multivariate continuous responses, with variable selection. arXiv.

Papageorgiou, G. (2018). BNSP: an R Package for fitting Bayesian semiparametric regression models and variable selection. The R Journal, 10(2):526-548.

Chan, D., Kohn, R., Nott, D., & Kirby, C. (2006). Locally adaptive semiparametric estimation of the mean and variance functions in regression models. Journal of Computational and Graphical Statistics, 15(4), 915-936.

Examples

```
# Fit a mean/variance regression model on the cps71 dataset from package np.
#This is a univariate response model
require(np)
require(ggplot2)
data(cps71)
model \leq logwage \leq sm(age, k = 30, bs = "rd") | sm(age, k = 30, bs = "rd")
DIR < - getwd()## Not run: m1 <- mvrm(formula = model, data = cps71, sweeps = 10000, burn = 5000,
                                      thin = 2, seed = 1, StorageDir = DIR)
#Print information and summarize the model
print(m1)
```
mvrm2mcmc 25

```
summary(m1)
#Summarize and plot one parameter of interest
alpha <- mvrm2mcmc(m1, "alpha")
summary(alpha)
plot(alpha)
#Obtain a plot of a term in the mean model
wagePlotOptions <- list(geom_point(data = cps71, aes(x = age, y = logwage)))
plot(x = m1, model = "mean", term = "sm(age)", plotOptions = wagePlotOptions)plot(m1)
#Obtain predictions for new values of the predictor "age"
predict(m1, data-frame(age = c(21, 65)), interval = "credible")# Fit a bivariate mean/variance model on the marks dataset from package ggm
# two responses: marks mechanics and vectors, and one covariate: marks on algebra
model2 <- mechanics | vectors ~ sm(algebra, k = 5) | sm(algebra, k = 3)
m2 < - mvrm(formula = model2, data = marks, sweeps = 100000, burn = 50000,
                       thin = 2, seed = 1, StorageDir = DIR)
plot(m2)
## End(Not run)
```
mvrm2mcmc *Convert posterior samples from function* mvrm *into an object of class 'mcmc'*

Description

Reads in files where the posterior samples were written and creates an object of class 'mcmc' so that functions like summary and plot from package coda can be used

Usage

```
mvrm2mcmc(mvrmObj, labels)
```
Arguments

Value

An object of class 'mcmc' that holds the samples from the posterior of the selected parameter.

Author(s)

Georgios Papageorgiou <gpapageo@gmail.com>

See Also

[mvrm](#page-18-1)

Examples

#see \code{mvrm} example

plot.mvrm *Creates plots of terms in the mean and/or variance models*

Description

This function plots estimated terms that appear in the mean and variance models.

Usage

```
## S3 method for class 'mvrm'
plot(x, model, term, response, response2, intercept = TRUE, grid = 30,
centre = mean, quantiles = c(0.1, 0.9), contour = TRUE, static = TRUE,
centreEffects = FALSE, plotOptions = list(), nrow, ask = FALSE,
plotEmptyCluster = FALSE, combine = FALSE, ...)
```
Arguments

plot.mvrm 27

Details

Use this function to obtain predictions.

Value

Predictions along with credible/pediction intervals

Author(s)

Georgios Papageorgiou <gpapageo@gmail.com>

See Also

[mvrm](#page-18-1)

Examples

#see \code{mvrm} example

Description

This function plots the posterior mean and credible intervals of the elements of correlation matrices.

Usage

```
plotCorr(x, term = "R", centre = mean, quantiles = c(0.1, 0.9), ...)
```
Arguments

Details

Use this function to visualize the elements of a correlation matrix.

Value

Posterior means and credible intervals of elements of correlation matrices.

Author(s)

Georgios Papageorgiou <gpapageo@gmail.com>

See Also

[mvrm](#page-18-1)

Examples

#see \code{mvrm} example

predict.mvrm *Model predictions*

Description

Provides predictions and posterior credible/prediction intervals for given feature vectors.

Usage

```
## S3 method for class 'mvrm'
predict(object, newdata, interval = c("none", "credible", "prediction"),
                       level = 0.95, ind.preds = FALSE, ...)
```
Arguments

Details

The function returns predictions of new responses or the means of the responses for given feature vectors. Predictions for new responses or the means of new responses are the same. However, the two differ in the associated level of uncertainty: response predictions are associated with wider (prediction) intervals than mean response predictions. To obtain prediction intervals (for new responses) the function samples from the normal distributions with means and variances as sampled during the MCMC run.

Value

Predictions for given covariate/feature vectors.

Author(s)

Georgios Papageorgiou <gpapageo@gmail.com>

See Also

[mvrm](#page-18-1)

Examples

```
#see \code{mvrm} example
```
print.mvrm *Prints an mvrm fit*

Description

Provides basic information from an mvrm fit.

Usage

S3 method for class 'mvrm' print(x, digits = $5, ...$)

Arguments

Details

The function prints information about mvrm fits.

Value

The function provides a matched call, the number of posterior samples obtained and marginal inclusion probabilities of the terms in the mean and variance models.

Author(s)

Georgios Papageorgiou <gpapageo@gmail.com>

See Also

[mvrm](#page-18-1)

Examples

#see \code{mvrm} example

Description

Provides interface between mgcv::s and BNSP. s(...) calls mgcv::smoothCon(mgcv::s(...),...

Usage

```
s(\ldots, data, knots = NULL, absorbcons = FALSE, scale.penalty = TRUE,n = nrow(data), dataX = NULL, null.space.penalty = FALSE, sparse.cons = 0,
diagonal.penalty = FALSE, apply.by = TRUE, modCon = \theta, k = -1, fx = FALSE,
bs = "tp", m = NA, by = NA, xt = NULL, id = NULL, sp = NULL, pc = NULL)
```
Arguments

Details

The most relevant arguments for BNSP users are the list of variables ..., knots, absorb.cons, bs, and by.

Value

A design matrix that specifies a smooth term in a model.

Author(s)

Georgios Papageorgiou <gpapageo@gmail.com>

simD *Simulated dataset*

Description

Just a simulated dataset to illustrate the DO mixture model. The success probability and the covariate have a non-linear relationship.

Usage

data(simD)

Format

A data frame with 300 independent observations. Three numerical vectors contain information on

Y number of successes.

E number of trials.

X explanatory variable.

simD2 *Simulated dataset*

Description

A simulated dataset to illustrate the multivariate longitudinal model. It consists of a bivariate vector of responses observed over 6 time points.

Usage

data(simD2)

sinusoid 33

Format

A data frame that includes observations on 50 sampling units. The data frame has 300 rows for the 50 sampling units observed over 6 time points. It has 4 columns

- Y1 first response.
- Y2 second response.

time the time of observation.

id unique sampling unit identifier.

sinusoid *Sinusoid terms in mvrm formulae*

Description

Function used to define sinusoidal curves in the mean formula of function mvrm. The function is used internally to construct design matrices.

Usage

```
sinusoid(..., harmonics = 1, amplitude = 1, period = 0, periodRange = NULL,
breaks = NULL, knots = NULL)
```
Arguments

Details

Use this function within calls to function mvrm to specify sinusoidal waves in the mean function of a regression model.

Consider the sinusoidal curve

 $y_t = \beta_0 + A(t) \sin(2\pi t/\omega + \varphi) + \epsilon_t,$

where y_t is the response at time t, β_0 is an intercept term, $A(t)$ is a time-varying amplitude, $\varphi \in$ $[0, 2\pi]$ is the phase shift parameter, ω is the period taken to be known, and ϵ_t is the error term.

The period ω is defined by the argument period.

The time-varying amplitude is represented using $A(t) = \sum_{j=1}^{K} \beta_{Aj} \phi_{Aj}(t)$, where K, the number of knots, is defined by argument amplitude. If amplitude = 1, then the amplitude is taken to be fixed: $A(t) = A$.

Further, $\sin(2\pi t/\omega + \varphi)$ is represented utilizing $\sin(2\pi t/\omega + \varphi) = \sum_{k=1}^{L} a_k \sin(2k\pi t/\omega) +$ $b_k \cos(2k\pi t/\omega)$, where L, the number of harmonics, is defined by argument harmonics.

Value

Specifies the design matrices of an mvrm call

Author(s)

Georgios Papageorgiou <gpapageo@gmail.com>

See Also

[mvrm](#page-18-1)

Examples

```
# Simulate and fit a sinusoidal curve
# First load releveant packages
require(BNSP)
require(ggplot2)
require(gridExtra)
require(Formula)
# Simulate the data
mu <- function(u) \{\cos(\theta.5 \times u) \times \sin(2 \times pi \times u + 1)\}\set.seed(1)
n < - 100u \le -\text{sort}(\text{runif}(n, \text{min} = \emptyset, \text{max} = 2 \star \text{pi}))y \le - rnorm(n, mu(u), 0.1)
data \leq data.frame(y, u)
# Define the model and call function \code{mvrm} that perfomes posterior sampling for the given
# dataset and defined model
model \leq y \leq sinusoid(u, harmonics = 2, amplitude = 20, period = 1)
## Not run:
m1 < - mvrm(formula = model, data = data, sweeps = 10000, burn = 5000, thin = 2, seed = 1,
            StorageDir = getwd())
# Plot
```


```
x1 \leq -\text{seq}(\text{min}(u), \text{max}(u), \text{length.out} = 100)plotOptionsM <- list(geom_line(aes_string(x = x1, y = mu(x1)), col = 2, alpha = 0.5, lty = 2),
                      geom\_point(data = data, aes(x = u, y = y)))plot(x = m1, term = 1, plotOptions = plotOptionsM, intercept = TRUE,quantiles = c(0.005, 0.995), grid = 100, combine = 1)
## End(Not run)
```
sm *Smooth terms in mvrm formulae*

Description

Function used to define smooth effects in the mean and variance formulae of function mvrm. The function is used internally to construct the design matrices.

Usage

 $sm(\ldots, k = 10, knots = NULL, bs = "rd")$

Arguments

Details

Use this function within calls to function mvrm to specify smooth terms in the mean and/or variance function of the regression model.

Univariate radial basis functions with q basis functions or $q - 1$ knots are defined by

$$
\mathcal{B}_1 = \left\{ \phi_1(u) = u, \phi_2(u) = ||u - \xi_1||^2 \log (||u - \xi_1||^2), \ldots, \phi_q(u) = ||u - \xi_{q-1}||^2 \log (||u - \xi_{q-1}||^2) \right\},\
$$

where ||u|| denotes the Euclidean norm of u and ξ_1, \ldots, ξ_{q-1} are the knots that are chosen as the quantiles of the observed values of explanatory variable u, with $\xi_1 = \min(u_i), \xi_{q-1} = \max(u_i)$ and the remaining knots chosen as equally spaced quantiles between ξ_1 and ξ_{q-1} .

Thin plate splines are defined by

$$
\mathcal{B}_2 = \{ \phi_1(u) = u, \phi_2(u) = (u - \xi_1)_+, \dots, \phi_q(u) = (u - \xi_q)_+ \},
$$

where $(a)_{+} = \max(a, 0)$.

Radial basis functions for bivariate smooths are defined by

$$
\mathcal{B}_3 = \left\{ u_1, u_2, \phi_3(u) = ||u - \xi_1||^2 \log \left(||u - \xi_1||^2 \right), \ldots, \phi_q(u) = ||u - \xi_{q-1}||^2 \log \left(||u - \xi_{q-1}||^2 \right) \right\}.
$$

Value

Specifies the design matrices of an mvrm call

Author(s)

Georgios Papageorgiou <gpapageo@gmail.com>

See Also

[mvrm](#page-18-1)

Examples

#see \code{mvrm} example

summary.mvrm *Summary of an mvrm fit*

Description

Provides basic information from an mvrm fit.

Usage

```
## S3 method for class 'mvrm'
summary(object, nModels = 5, digits = 5, printTuning = FALSE, ...)
```
Arguments

Details

Use this function to summarize mvrm fits.

Value

The functions provides a detailed description of the specified model and priors. In addition, the function provides information about the Markov chain ran (length, burn-in, thinning) and the folder where the files with posterior samples are stored. Lastly, the function provides the mean posterior and null deviance and the mean/variance models visited most often during posterior sampling.

Author(s)

Georgios Papageorgiou <gpapageo@gmail.com>

See Also

[mvrm](#page-18-1)

Examples

#see \code{mvrm} example

te *mgcv constructor* te

Description

Provides interface between mgcv::te and BNSP. te(...) calls mgcv::smoothCon(mgcv::te(...),...

Usage

```
te(..., data, knots = NULL, absorbcons = FALSE, scale.penalty = TRUE,n = nrow(data), dataX = NULL, null.space.penalty = FALSE, sparse.cons = 0,
diagonal.penalty = FALSE, apply.by = TRUE, modCon = 0, k = NA, bs = "cr",
m = NA, d = NA, by = NA, fx = FALSE, np = TRUE, xt = NULL, id = NULL,
sp = NULL, pc = NULL)
```
Arguments

 38 times the contract of t in \mathbf{z} is the contract of t in \mathbf{z} is the contract of t is th

diagonal.penalty

Details

The most relevant arguments for BNSP users are the list of variables ..., knots, absorb.cons, bs, and by.

Value

A design matrix that specifies a smooth term in a model.

Author(s)

Georgios Papageorgiou <gpapageo@gmail.com>

ti *mgcv constructor* ti

Description

Provides interface between mgcv::ti and BNSP. ti(...) calls mgcv::smoothCon(mgcv::ti(...),...

Usage

```
ti(..., data, knots = NULL, absorbcons = FALSE, scale.penalty = TRUE,n = nrow(data), dataX = NULL, null.\spacespace space.penalty = FALSE, sparse.cons = 0,
diagonal.penalty = FALSE, apply.by = TRUE, modCon = \theta, k = NA, bs = "cr",
m = NA, d = NA, by = NA, fx = FALSE, np = TRUE, xt = NULL, id = NULL,
sp = NULL, mc = NULL, pc = NULL)
```
Arguments

Details

The most relevant arguments for BNSP users are the list of variables ..., knots, absorb.cons, bs, and by.

Value

A design matrix that specifies a smooth term in a model.

Author(s)

Georgios Papageorgiou <gpapageo@gmail.com>

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